

Figure 1 shows the critical deflection as a function of diameter for these parameters:

$$D=2\text{mm}$$

$$G=82.7 \text{ Gpa}$$

$$E=203.4 \text{ Gpa}$$

$$4\text{mm} < L_f < 20\text{mm}$$

$$C1 = E / ( 2 * ( E - G ) )$$

$$C2 = ( 2 * ( \pi^2 ) * ( E - G ) ) / ( 2 * G + E )$$

$$A_{eff} = ( a \setminus D ) * L_f$$

$$Y = L_f * C1 * ( 1 - ( 1 - ( C2 / ( A_{eff} )^2 ) )^0.5 )$$

Spring supported between flat parallel surfaces (fixed ends):

$a=0.5 \rightarrow \text{Green}$

One end supported by flat surface perpendicular to spring axis (fixed);  
other end pivoted (hinged):

$a=0.707 \rightarrow \text{Blue}$

Both ends pivoted (hinged):

$a=1 \rightarrow \text{Red}$

One end clamped; other end free:

$a=2 \rightarrow \text{Black}$

## The script:

```
clear all
close all
clc
Lf=linspace(4,20,1000);
G=82.7*(10^9);
E=203.4*(10^9);
C1=E/(2*(E-G));
C2=(2*(pi^2)*(E-G))/(2*G+E);
D=2;
X=Lf/D;
a=1;
Aeff=(a\D)*Lf;
for i=1:1000;
    y(i)=Lf(i)*C1*(1-(1-(C2/(Aeff(i))^2))^0.5);
    Y(i)=y(i)/Lf(i);
end
plot(X,Y,'color','red')
hold on
a=2;
Aeff=(a\D)*Lf;
for i=1:1000;
    y(i)=Lf(i)*C1*(1-(1-(C2/(Aeff(i))^2))^0.5);
    Y(i)=y(i)/Lf(i);
end
plot(X,Y,'color','black')
hold on
a=0.5;
Aeff=(a\D)*Lf;
for i=1:1000;
    y(i)=Lf(i)*C1*(1-(1-(C2/(Aeff(i))^2))^0.5);
    Y(i)=y(i)/Lf(i);
end
plot(X,Y,'color','green')
hold on
a=0.707;
Aeff=(a\D)*Lf;
for i=1:1000;
    y(i)=Lf(i)*C1*(1-(1-(C2/(Aeff(i))^2))^0.5);
    Y(i)=y(i)/Lf(i);
end
plot(X,Y,'color','blue')
hold on
```

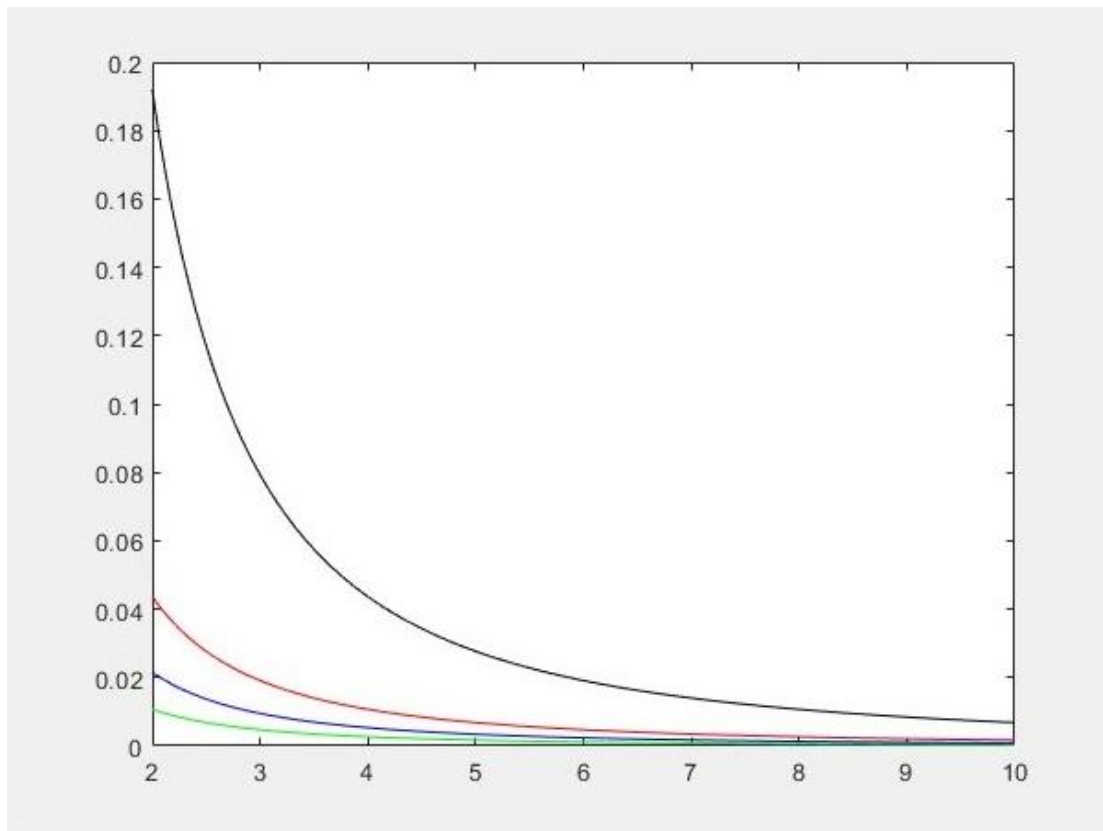


Fig 1. different end conditions - the critical deflection as a function of diameter