

Report

2b)

Lemma sorted2IfSorted1

If sorted1 holds for a sequence *ints*, then sorted2 will hold for *ints*

Let there be two integers *a* and *b* and let $0 \leq a < b < |ints|$, we have to show that $ints[a] \leq ints[b]$

Because we know that $a < b$, we know that there is a integer *c* for which $a + c = b$

Let's show that $ints[a] \leq ints[a+c]$ through induction on *c*

Base case: $c = 1$

When $c = 1$ we get $ints[a] \leq ints[a+1]$, which is true by the definition of sorted1 where a number *i* gives us that $ints[i] \leq ints[i+1]$

Step case: Assume that *c* will hold for any integer *n*, show that it holds for

$ints[a] \leq ints[a+c+1]$

Like for the base case, this can be proven by using sorted1, hence

$ints[a] \leq ints[a+c] \leq ints[a+c+1]$. It follows through transition that

$ints[a] \leq ints[a+c+1]$.

We have shown by induction that $ints[a] \leq ints[a+c]$, hence for any integers

$0 \leq a < b < |ints|$ we get $ints[a] \leq ints[b]$. Thus we have proven sorted2.

Lemma sorted1IfSorted2

If sorted2 holds for a sequence *ints*, then sorted1 will hold for *ints*

Let there be an integer *a*, we have to show that $ints[a] \leq ints[a+1]$.

By the definition of sorted2, we know that $\text{forall } i, j :: 0 \leq i < j < |ints| \Rightarrow ints[i] \leq ints[j]$

Particularly, $\text{forall } i :: 0 \leq i < i+1 < |ints| \Rightarrow ints[i] \leq ints[i+1]$

We see that if sorted2 holds for a sequence, then sorted1 will also hold.

3a)

A multiset counts the number of each unique element in a set. In this case two sequences *a* and *b* are compared to each other to check if they are the same via multisets.