

- 1 Write a C Program to implement Recursive Binary search and linear search and determine the time required to search an element.

ALGORITHM

Linear Search (Array A, Value x)

Step 1: Set i to 1
Step 2: if i > n then go to step 7
Step 3: if A[i] = x then go to step 6
Step 4: Set i to i + 1
Step 5: Go to Step 2
Step 6: Print Element x Found at index i and go to step 8
Step 7: Print element not found!!
Step 8: Exit

Binary_search

A ← sorted array
n ← size of array
x ← value to be searched
Set lowerBound = 1
Set upperBound = n
while x not found
 if upperBound < lowerBound
 EXIT: x does not exists.
 set midPoint = lowerBound + (upperBound - lowerBound) / 2
 if A[midPoint] < x set lowerBound = midPoint + 1
 if A[midPoint] > x
 set upperBound = midPoint - 1
 if A[midPoint] = x
 EXIT: x found at location midPoint
end while
end procedure

Linear search

PROGRAM CODE:

```
#include<stdio.h>
#include<time.h>
#define max 20
int a[max],n,key;
int ls(int,int);
int bs(int,int,int);
void main()
{
    int i,key,ch,mid,low,high,L;
    clock_t start1,end1,start2,end2;
    printf("Enter the limit\n");
    scanf("%d",&n);
    printf("Enter the elements \n");
    for(i=1;i<=n;i++)
        scanf("%d",&a[i]);
    printf("\n LINEAR SEARCH \n");
    start1=clock();
    printf("Enter the key element to search\n");
```

```

scanf("%d",&key);
L=ls(1,key);
end1=clock();
if(L==-1)
printf("Element is not found \n");
else
printf("Element is found \n");
printf("Time=%f",((double)(end1-start1))/CLOCKS_PER_SEC);
printf("\n");
printf("\n BINARY SEARCH \n");
start2=clock();
printf("enter the key element to be searched\n");
scanf("%d",&key);
low=1;
high=n;
ch=bs(low,high,key);
end2=clock();
if(ch==-1)
printf("element is not found\n");
else
printf("element is found\n");
printf("Time=%f",((double)(end2-start2))/CLOCKS_PER_SEC);
}
int ls(int i, int key)
{
if(i>n)
return(-1);
if(a[i]==key)
return i;
else
ls(++i,key);
return;
}
int bs(int low,int high,int key)
{
int mid;
if(low>high)
return (-1);
mid=(low+high)/2;
if(a[mid]==key)
return mid;
else
{
if(key<a[mid])
bs(low,mid-1,key);
else
bs(mid+1,high,key);
}
}

/*OUTPUT:
enter the limit
3
enter the elements
10
20

```

```
30
LINEAR SEARCH
enter the key element to search
20
element is found
TIME =0.000078
BINARY SEAERCH
enter the key element to be searched
20
element is found
TIME = 0.000037 */
```

- 2 Write a C Program to sort a given set of elements using Merge sort method and determine the time required to sort the elements.

ALGORITHM

Merge sort

Step 1 - if it is only one element in the list it is already sorted, return.

Step 2 - divide the list recursively into two halves until it can no more be divided.

Step 3 - merge the smaller lists into new list in sorted order.

PROGRAM CODE:

//Merge Sort

```
#include<stdio.h>
#include<time.h>
int mergesort(int *, int , int);
int merge(int *, int, int, int);
void main ()
{
    int i,n,a[20];
    clock_t start,end;
    start = clock();
    printf("Enter the limit \n");
    scanf("%d",&n);
    printf("Enter the elements \n");
    for(i=0;i<n;i++)
        scanf("%d",&a[i]);
    mergesort(a,0,n-1);
    end = clock();
    printf("The sorted elements are\n");
    for (i=0;i<n;i++)
        printf("%d\n",a[i]);
    printf("\n Time = %f", (double) (end - start)/CLOCKS_PER_SEC);
    return;
}

int mergesort (int a[], int low, int high)
{
    int mid;
    if (low < high)
    {
        mid = (low + high)/2;
        mergesort(a,low,mid);
        mergesort(a,mid+1,high);
        merge(a,low,mid,high);
    }
}

int merge(int a[], int low,int mid, int high)
{
    int i,j,k,h,b[20];
    h=i=low;
    j=mid + 1;
```

```

        while (h <= mid && j<=high)
        if (a[h] < a[j])
        b[i++] = a[h++];
        else
        b[i++] = a[j++];
        if (h > mid)
        for(k=j; k<=high; k++)
        b[i++] = a[k];
        else
        for (k=h; k<=mid; k++)
        b[i++] = a[k];
        for(k=low; k<=high; k++)
        a[k] = b[k];
    }

```

/*

OUTPUT

RUN 1:

Enter the limit

7

Enter the elements

12

67

23

89

0

34

13

The sorted elements are

0

12

13

23

34

67

89

*/

- 3 Write a C Program to Sort a given set of elements using Selection sort and determine the time required to sort elements.

ALGORITHM

Selection Sort

- Step 1 - Set MIN to location 0
- Step 2 - Search the minimum element in the list
- Step 3 - Swap with value at location MIN
- Step 4 - Increment MIN to point to next element
- Step 5 - Repeat until list is sorted

PROGRAM CODE:

```
//SELECTION SORT
#include<stdio.h>
#include<time.h>
int selection_sort(int a[], int n);
int main()
{
    int i,n,a[20],key;
    clock_t end,start;
    printf("Enter the size of an array\n");
    scanf("%d",&n);
    printf("Enter the array elements\n");
    for (i=0;i<n;i++)
        scanf("%d",&a[i]);
    start = clock();
    selection_sort(a,n);
    end = clock();
    printf("Sorted elements are\n");
    for (i=0;i<n;i++)
        printf("\n %d",a[i]);
    printf("\nTime = %f", (double) (end - start)/CLOCKS_PER_SEC);
}

int selection_sort(int a[], int n)
{
    int i,j,pos,small,temp;
    for(i=0;i<n-1;i++)
    {
        small = a[i];
        pos = i;
        for (j=i+1;j<n;j++)
        {
            if (a[j] < small)
            {
                small = a[j];
                pos=j;
            }
        }
        temp = a[pos];
```

```
        a[pos] = a[i];  
        a[i] = temp;  
    }  
}
```

```
/*
```

OUTPUT

Enter the size of an array

7

Enter the array elements

12

67

23

0

1

45

78

Sorted elements are

0

1

12

23

45

67

78

Time = 0.000012

```
*/
```

- 4 Write a C Program to Sort a given set of elements using Insertion sort and determine the time required to sort elements.

ALGORITHM:

Step 1 - If it is the first element, it is already sorted. return 1;
Step 2 - Pick next element
Step 3 - Compare with all elements in the sorted sub-list
Step 4 - Shift all the elements in the sorted sub-list that is greater than the value to be sorted
Step 5 - Insert the value
Step 6 - Repeat until list is sorted

PROGRAM CODE:

//INSERTION SORT

```
#include<stdio.h>
#include<time.h>
void main()
{
    int a[10],v,j,n,i;
    clock_t start,end;
    printf("\n Enter the order of an array\n");
    scanf("%d",&n);
    start=clock();
    printf("Enter the elements of an array\n");
    for (i=1;i<=n;i++)
        scanf("%d",&a[i]);
    for (i=1;i<=n;i++)
    {
        v=a[i];
        j=i-1;
        while (j >= 00 && a[j] > v)
        {
            a[j+1]=a[j];
            j=j-1;
        }
        a[j+1]=v;
    }
    end = clock();
    printf("\n The Sorted array is \n");
    for (i=1;i<=n;i++)
        printf("\n %d",a[i]);
    printf("\nTime = %f", (double) (end-start)/CLOCKS_PER_SEC);
}
```



```
/*
```

OUTPUT

```
Enter the order of an array
```

```
6
```

```
Enter the elements of an array
```

```
9 4 5 2 6 1
```

```
The Sorted array is
```

```
1
```

```
2
```

```
4
```

```
5
```

```
6
```

```
9
```

```
Time = 0.000035
```

```
*/
```

- 5 Write a C Program to Sort a given set of elements using the Heap sort method and determine the time required to sort the elements.

ALGORITHM:

Heap Sort

- Step 1 - Construct a **Binary Tree** with given list of Elements.
- Step 2 - Transform the Binary Tree into **Min Heap**.
- Step 3- Delete the root element from Min Heap using **Heapify** method.
- Step 4 - Put the deleted element into the Sorted list.
- Step 5 - Repeat the same until Min Heap becomes empty.
- Step 6 - Display the sorted list.

PROGRAM CODE:

//HEAP SORT

```
#include<stdio.h>
int swap(int *x, int *y);
int heap(int n);
int heapsort (int n);
int a[10];
int main()
{
    int i,n;
    printf("Enter the limit\n");
    scanf("%d",&n);
    printf("Enter the elements \n");
    for (i=1;i<=n;i++)
        scanf("%d",&a[i]);
    heap(n);
    heapsort(n);
    printf("Sorted elements \n");
    for (i=1;i<=n;i++)
        printf("%d\t",a[i]);
}
int heap(int n)
{
    int ch, ps, temp;
    for (ch=1;ch<=n;ch++)
    {
        temp=a[ch];
        ps=ch/2;
        while (ch>1 && temp > a[ps])
        {
            a[ch] = a[ps];
            ch=ps;
            ps=ch/2;
            if (ps < 1)
                ps=1;
        }
        a[ch] = temp;
    }
}
int heapsort (int n)
{

```

```

        while (n>1)
        {
            swap(&a[1], &a[n]);
            {
                n--;
                heap(n);
            }
        }
}

```

```

int swap(int *x, int *y)
{
    int temp;
    temp=*x;
    *x = *y;
    *y = temp;
}

```

/*

OUTPUT

Enter the limit

5

Enter the elements

2 4 3 7 6

Sorted elements

2 3 4 6 7

*/

- 6 Write a C Program to Sort a given set of elements using Quick sort method and determine the time required sort the elements

ALGORITHM

Step 1 - Choose the highest index value has pivot
Step 2 - Take two variables to point left and right of the list excluding pivot
Step 3 - left points to the low index
Step 4 - right points to the high
Step 5 - while value at left is less than pivot move right
Step 6 - while value at right is greater than pivot move left
Step 7 - if both step 5 and step 6 does not match swap left and right
Step 8 - if $\text{left} \geq \text{right}$, the point where they met is new pivot

PROGRAM CODE:

//QUICK SORT

```
#include<stdio.h>
#include<time.h>
int partition(int a[],int low,int high);
void quicksort(int a[],int low,int high)
{
    int j;
    if(low < high)
    {
        j=partition(a,low,high);
        quicksort(a,low,j-1);
        quicksort(a,j+1,high);
    }
}

int partition(int a[],int low,int high)
{
    int i,j,temp,key;
    key=a[low];
    i=low+1;
    j=high;
    while (1)
    {
        while (i<high && key >= a[i])
            i++;
        while (key < a[j] )
            j--;
        if (i < j)
        {
            temp=a[i];
            a[i]=a[j];
            a[j]=temp;
        }
        else
        {
            break;
        }
    }
}
```

```
temp = a[low];
a[low]=a[j];
a[j]=temp;
return j;
}
}
}
void main ()
{
int i,n,a[20];
float f;
clock_t start,end;
printf("Enter the No of Elements\n");
scanf("%d",&n);
printf("Enter the [%d] element : \n",n);
for(i=0;i<n;i++)
scanf("%d",&a[i]);
start=clock();
quicksort(a,0,n-1);
end=clock();
printf("\n The Sorted array is : \n");
for(i=0;i<n;i++)
printf("%d\t",a[i]);
printf("\n Time Taken = %f", (double) (end-start)/CLOCKS_PER_SEC);
}
```

- 7 Write a C Program to Print all the nodes reachable from a given starting node in a digraph using BFS method.

ALGORITHM

Rule 1 - Visit the adjacent unvisited vertex. Mark it as visited. Display it. Insert it in a queue.

Rule 2 - If no adjacent vertex is found, remove the first vertex from the queue.

Rule 3 - Repeat Rule 1 and Rule 2 until the queue is empty.

PROGRAM CODE:

//BFS METHOD

```
#include<stdio.h>
int i,j,n,r=-1,f,q[20],visited[20];
int a[20][20];
int bfs(int v);
void main()
{
    int v;
    printf("Enter the number of vertices....\n");
    scanf("%d",&n);
    for(i=1;i<=n;i++)
    {
        q[i]=0;
        visited[i]=0;
    }
    printf("Enter the adjacency matrix..\n");
    for(i=1;i<=n;i++)
    for(j=1;j<=n;j++)
    scanf("%d",&a[i][j]);
    printf("Enter the starting vertex...\n");
    scanf("%d",&v);
    bfs(v);
    printf("the nodes that are rachable from given node %d
are..\n",v);
    for(i=1;i<=n;i++)
    if (visited[i])
    printf("%d ",i);
}

int bfs(int v)
{
    for(i=1;i<=n;i++)
```

```

        if(a[v][i] && !visited[i])
            q[++r]=i;
        visited[i]=1;
        if (f <= r)
            {
                visited[q[f]]=1;
                bfs(q[f++]);
            }
    }
}
/*OUTPUT
Enter the number of vertices....
4
Enter the adjacency matrix..
0 1 1 1
0 0 0 1
0 0 0 0
0 0 1 0
Enter the starting vertex...
1
the nodes that are rachable from given node 1 are..
2 3 4 */

```

- 8 Write a C Program to Check whether a given graph is connected or not using DFS method.

ALGORITHM

Rule 1 - Visit the adjacent unvisited vertex. Mark it as visited. Display it. Push it in a stack.

Rule 2 - If no adjacent vertex is found, pop up a vertex from the stack. (It will pop up all the vertices from the stack, which do not have adjacent vertices.)

Rule 3 - Repeat Rule 1 and Rule 2 until the stack is empty.

PROGRAM CODE:

//DFS METHOD

```
#include<stdio.h>
int a[20][20],reach[20],n;
void dfs(int v)
{
    int i;
    reach[v]=1;
    for(i=1;i<=n;i++)
        if(a[v][i] && !reach[i])
        {
            printf("\n %d --> %d",v,i);
            dfs(i);
        }
}

void main()
{
    int i,j,count=0;
    printf("Enter the number of Vertices: ");
    scanf("%d",&n);
    for(i=1;i<=n;i++)
    {
        reach[i]=0;
        for(j=1;j<=n;j++)
            a[i][j]=0;
    }
    printf("Enter the Adacency matrix\n");
    for(i=1;i<=n;i++)
        for(j=1;j<=n;j++)
            scanf("%d",&a[i][j]);

    dfs(1);
    printf("\n");
    for(i=1;i<=n;i++)
    {
        if (reach[i])
            count++;
    }
    if (count == n)
```



```
        printf("\n Graph is connected : ");
        else
            printf("\n Graph is not connected : ");
    }
```

/*OUTPUT

RUN 1:

Enter the number of Vertices: 4

Enter the Adacency matrix

0 1 1 1

0 0 0 1

0 0 0 0

0 0 1 0

1 --> 2

2 --> 4

4 --> 3

Graph is connected

RUN 2:

Enter the number of Vertices: 4

Enter the Adacency matrix

0 1 0 0

1 0 0 0

0 0 0 1

0 0 1 0

1 --> 2

Graph is not connected

***/**

PART B

- 1 Write a C Program to Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm.

ALGORITHM

Step 1- Sort all the edges in non-decreasing order of their weight.
Step 2- Pick the smallest edge. Check if it forms a cycle with the spanning tree formed so far. If cycle is not formed, include this edge. Else, discard it.
Step 3- Repeat step#2 until there are (V-1) edges in the spanning tree.

PROGRAM CODE:

//Kruskal's algorithm

```
#include<stdio.h>
int parent[10],min,ne=1,mincost=0,cost[10][10];
int i,j,a,b,u,v,n;
int main()
{
    printf("Enter the No. of Vettices of Graph\n");
    scanf("%d",&n);
    printf("Enter the cost Adjancecy Of Matrix\n");
    for(i=1;i<=n;i++)
        for(j=1;j<=n;j++)
        {
            scanf("%d",&cost[i][j]);
            if(cost[i][j] == 0)
                cost[i][j]=999;
        }
    while (ne < n)
    {
        for(i=1,min=999;i<=n;i++)
            for(j=1;j<=n;j++)
                if(cost[i][j] < min)
                {
                    min = cost[i][j];
                    a=u=i;
                    b=v=j;
                }
        while (parent[u])
            u=parent[u];
        while (parent[v])
            v=parent[v];
        if (u != v)
        {
            ne++;
            printf("\n %d\t edge \t (%d,%d) =
%d",ne,a,b,min);
            mincost+=min;
            parent[v] = u;
        }
        cost[a][b] = cost[b][a] = 999;
    }
    printf("\n mincost = %d \n",mincost);
}
```

```
}  
/*
```

OUTPUT

RUN 1:

Enter the No. of Vettices of Graph

4

Enter the cost Adjancey Of Matrix

0 5 11 4

5 0 6 13

11 6 0 7

4 13 7 0

2 edge (1,4) = 4

3 edge (1,2) = 5

4 edge (2,3) = 6

mincost = 15

RUN 2:

Enter the No. of Vettices of Graph

3

Enter the cost Adjancey Of Matrix

0 1 1

1 0 0

1 0 0

2 edge (1,2) = 1

3 edge (1,3) = 1

mincost = 2

```
*/
```

- 2 Write a C Program to Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm.

ALGORITHM

Step 1- Create a set mstSet that keeps track of vertices already included in MST.

Step 2- Assign a key value to all vertices in the input graph.

Initialize all key values as INFINITE. Assign key value as 0 for the first vertex so that it is picked first.

Step 3- While mstSet doesn't include all vertices

a) Pick a vertex u which is not there in mstSet and has minimum key value.

b) Include u to mstSet.

c) Update key value of all adjacent vertices of u. To update the key values, iterate through all adjacent vertices. For every adjacent vertex v, if weight of u-v is less than the previous key value of v, edge update the
key value as weight of u-v

PROGRAM CODE

//PRIMS ALGORITHM

```
#include<stdio.h>
int a,b,u,v,i,j,n,ne=1;
int visited [10],min,mincost=0,cost[10][10];
int main()
{
    printf("Enter the No. of Vertices\n");
    scanf("%d",&n);
    printf("Enter the adjacent matrix\n");
    for(i=1;i<=n;i++)
        for(j=1;j<=n;j++)
        {
            scanf("%d",&cost[i][j]);
            if (cost[i][j] == 0)
                cost[i][j] = 999;
        }
    for (i=2;i<=n;i++)
        visited[i] = 0;
    printf("\n Edges of Spanning Tree ... \n");
    visited[1]=1;
    while (ne < n)
    {
        for(i=1,min=999;i<=n;i++)
            for (j=1;j<=n;j++)
                if (cost[i][j] < min)
                    if (visited[i] == 0)
                        continue;
                    else
                    {
                        min = cost[i][j];
                        a=u=i;
                        b=v=j;
                    }
        if (visited[u] == 0 || visited[v] == 0)
        {
```

```

        ne++;
        printf("\n %d Edge \t (%d, %d) =
%d",ne,a,b,min);
        mincost+=min;
        visited[b] = 1;
    }
    cost[a][b] = cost [b][a] = 999;
}
printf("\n Minimum cost = %d",mincost);
}

```

/* **OUTPUT**

RUN 1:

Ente the No. of Vertices

5

Enter the adjacent matrix

0 11 9 7 8

11 0 15 14 13

9 15 0 12 14

7 14 12 0 6

8 13 14 6 0

Edges of Spanning Tree ...

2 Edge (1, 4) = 7

3 Edge (4, 5) = 6

4 Edge (1, 3) = 9

5 Edge (1, 2) = 11

Minimum cost = 33

RUN 2:

Ente the No. of Vertices

3

Enter the adjacent matrix

0 1 2

1 0 3

2 3 0

Edges of Spanning Tree ...

2 Edge (1, 2) = 1

3 Edge (1, 3) = 2

Minimum cost = 3

*/

- 3 Write a C Program to From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

ALGORITHM

Step 1- Create a set *sptSet* (shortest path tree set) that keeps track of vertices included in shortest path tree, i.e., whose minimum distance from source is calculated and finalized. Initially, this set is empty.

Step 2- Assign a distance value to all vertices in the input graph. Initialize all distance values as INFINITE. Assign distance value as 0 for the source vertex so that it is picked first.

Step 3- While *sptSet* doesn't include all vertices

a) Pick a vertex *u* which is not there in *sptSet* and has minimum distance value.

b) Include *u* to *sptSet*.

c) Update distance value of all adjacent vertices of *u*. To update the distance values, iterate through all adjacent vertices. For every adjacent vertex *v*, if sum of distance value of *u* (from source) and weight of edge *u-v*, is less than the distance value of *v*, then update the distance value of *v*.

PROGRAM CODE

// Dijkstra's algorithm

```
#include<stdio.h>
int dij (int n,int v, int cost[10][10], int dist[]);
int main()
{
    int n,i,j,cost[10][10],dist[10],v;
    printf("Enter the No of nodes of graph\n");
    scanf("%d",&n);
    printf("Enter the elements of the matrix\n");
    for(i=1;i<=n;i++)
        for (j=1;j<=n;j++)
        {
            scanf("%d",&cost[i][j]);
            if(cost[i][j] == 0)
                cost[i][j] = 999;
        }
    printf("Enter the source vertex\n");
    scanf("%d",&v);
    dij(n,v,cost,dist);
    printf("Shortes path from \n");
    for(j=1;j<=n;j++)
        if(j != v)
            printf("%d --> %d.....%d\n",v,j,dist[j]);
}

int dij (int n,int v, int cost[10][10], int dist[])
{
```

```

int i,u,count,w,min,flag[10];
for (i=1;i<=n;i++)
    flag[i]=0,dist[i] = cost[v][i];
flag[v] = 1, dist[v] = 1;
count = 2;
while (count <= n)
{
    min = 999;
    for (w=1;w<=n;w++)
        if (dist[w]<min && !flag[w])
            min = dist[w],u=w;

    flag[u]=1;
    count++;
    for (w=1;w<=n;w++)
        if ((dist[u] + cost[u][w] < dist[w]) &&
!flag[w])
            dist[w] = dist[u] + cost[u][w];
}
}

```

/*

OUTPUT

Enter the No of nodes of graph

4

Enter the elements of the matrix

0 5 11 4

5 0 6 13

11 6 0 7

44 13 7 0

Enter the source vertex

1

Shortest path from

1 --> 2.....5

1 --> 3.....11

1 --> 4.....4

*/

- 4 Write a C Program to implement 0/1 Knapsack problem using dynamic programming.

ALGORITHM

Optimal Substructure:

To consider all subsets of items, there can be two cases for every item: (1) the item is included in the optimal subset, (2) not included in the optimal set.

Therefore, the maximum value that can be obtained from n items is max of following two values.

- 1) Maximum value obtained by n-1 items and W weight (excluding nth item).
- 2) Value of nth item plus maximum value obtained by n-1 items and W minus weight of the nth item (including nth item).

If weight of nth item is greater than W, then the nth item cannot be included and case 1 is the only possibility.

PROGRAM CODE:

//KNAPSACK PROBLEM

```
#include<stdio.h>
int n,capacity,w[50],p[50],maxprofit,i,j;
int MAX(int x, int y)
{
    return (x>y)?x:y;
}
int sack (int i, int y)
{
    if (i == n)
        if (y < w[n])
            return 0;
        else
            return p[n];
    if (y < w[i]) return sack (i+1,y);
    return MAX (sack(i+1,y),sack(i+1,y-w[i])+p[i]);
}

int main ()
{
    printf("Enter the No of Objects\n");
    scanf("%d",&n);
    printf("Enter the weights\n");
    for(i=0;i<n;i++)
        scanf("%d",&w[i]);
    printf("Enter the profit\n");
    for (i=0;i<n;i++)
        scanf("%d",&p[i]);
    printf("Enter the capacity\n");
    scanf("%d",&capacity);
    maxprofit = sack(0,capacity);
    printf("Maximum profit = %d ",maxprofit);
}
```



```
/*
```

OUTPUT

```
Enter the No of Objects
```

```
4
```

```
Enter the weights
```

```
3 4 5 6
```

```
Enter the profit
```

```
10 20 30 40
```

```
Enter the capacity
```

```
10
```

```
Maximum profit = 60
```

```
*/
```

- 5 Write a C Program to Find a subset of a given set $S = \{s_1, s_2, \dots, s_n\}$ of n positive integers whose sum is equal to a given positive integer d . For example, if $S = \{1, 2, 5, 6, 8\}$ and $d = 9$ there are two solutions $\{1, 2, 6\}$ and $\{1, 8\}$. A suitable message is to be displayed if the given problem instance doesn't have a solution.

ALGORITHM:

SUBSET CNSTRUCTION

Find a subset of a given set $s = \{s_1, s_2, \dots, s_n\}$ of n positive integers whose sum is equal to a given positive integer d . For example, if $s = \{1, 2, 5, 6, 8\}$ and $d = 9$ there are two solutions $(1, 2, 6)$ and $(1, 8)$ a suitable message is to be displayed if the given problem instance doesn't have a solution.

I. Theory

To generate 2^n subsets where $n=4$ we follow the following steps.

When $n=4$, $2^n=16$ subsets are possible.

N	Subjects
0	.
1	0 (1)
2	$\emptyset \{1\} \{2\} \{1, 2\}$
3	$\{1\} \{2\} \{3\} \{1, 2\} \{1, 3\} \{2, 3\} \{1, 2, 3\}$
4	$p \{1\} \{2\} \{3\} \{4\} \{1, 2\} \{1, 3\} \{2, 3\}$ $\{1, 2, 3\} \{1, 2, 4\} \{2, 3, 4\} \{1, 3, 4\}$ $\{1, 4\}$ $\{2, 4\} \{3, 4\} \{1, 2, 3, 4\}$

Given a set $s = \{s_1, s_2, \dots, s_n\}$. If $S = \{7, 11, 13, 24\}$ and $d=31$ then desired subsets are $\{11, 13, 7\}$ and $\{7, 24\}$.

We draw a stage space tree for this problem. We start from root and generate left and right child. Then left is generated based on including the element in subset and right node without including the element it is repeated until all nodes are completed.

The number inside 0 is sum of elements already included in subset.

The equality below 0 leaf

node indicates the reason.

PROGRAM CODE:

//SUBSET

```
#include<stdio.h>
void subset (int n, int d, int w[])
{
    int s,k,i,x[10];
    for (i=1;i<=n;i++)
        x[i] = 0;
```

```

s = 0; k = 1;
x[k] = 1;
while (1)
{
    if (k <= n && x[k] == 1)
    {
        if (s+w[k] == d)
        {
            printf("Solution is \n");
            for(i=1;i<=n;i++)
            {
                if (x[i] == 1)
                    printf("%d",w[i]);
            }
            printf("\n");
            x[k] = 0;
        }
        else if (s+w[k] < d)
        {
            s+=w[k];
        }
        else
        {
            x[k]=0;
        }
    }
    else
    {
        k--;
        while(k>0 && x[k] == 0)
        {
            k--;
        }
        if (k==0)
            break;
        x[k] = 0;
        s = s-w[k];
    }
    k = k + 1;
    x[k] = 1;
}

}

void main()
{
    int n,i,d,w[10];
    printf("Enter the value of n\n");
    scanf("%d",&n);
    printf("Enter the set in increasing order\n");
    for (i=1;i<=n;i++)
        scanf("%d",&w[i]);
    printf("Enter the maximum subset value of D\n");
    scanf("%d",&d);
    subset(n,d,w);
}

```

```
/*
```

OUTPUT

```
Enter the value of n
```

```
4
```

```
Enter the set in increasing order
```

```
3 6 7 10
```

```
Enter the maximum subset value of D
```

```
10
```

```
Solution is
```

```
37
```

```
Solution is
```

```
10
```

```
*/
```

6 Write a C Program to Implement Horspool algorithm for String Matching.

ALGORITHM

Step 1- calculate the value of each letter of the substring to create the Bad Match Table, using this formula,

Value = length of substring - index of each letter in the substring - 1.

The value of the last letter and other letters that are not in the substring will be the length of the substring

Step 2- the value should be assigned to each letter in the Bad Match Table.

Step 3- compare the substring and the string. You start from the index of the end letter in the substring

A) If the letter matches, then compare with the preceding letter

B) If it doesn't match, check its value in the Bad Match Table.

C) Then, skip the number of spaces that the table value indicates.

Step 4- Repeat this steps until all the letters match.

PROGRAM CODE:

//HORSPOL

```
#include<stdio.h>
#include<string.h>
#include<stdlib.h>
#define M 256
char pattern[M],text[M],table[M];
long m,n,i,j,k;
void shifttable()
{
    int in;
    for(i=0;i<M;i++)
        table[i] = m;
    for (j=0;j<m-1;j++)
    {
        in = (int)pattern[j] - '0';
        table[in] = m-1-j;
    }
}
int horsepool()
{
    int index;
    shifttable();
    for (i=m-1;i<=n-1;)
    {
        k = 0;
        while ((k <= m-1) && (pattern[m-1-k] == text[i-k]))
            k++;
    }
}
```

```

        if (k == m)
            return i-m+1;
        else
        {
            index=(int)text[i] - '0';
            i = i + table[index];
        }
    }
    return -1;
}

int main ()
{
    int found;
    printf("Enter the text\n");
    gets(text);
    printf("\n Enter the Pattern ");
    scanf("%s",pattern);
    n = strlen(text);
    m = strlen(pattern);
    found = horsepool();
    if (found == -1)
        printf("\n Pattern not found!!!\n");
    else
        printf("\n Pattern found at position %d ",found+1);
}

```

7 Write a C Program to Find the Binomial Co-efficient using Dynamic Programming.

ALGORITHM:

Computing a Binomial Coefficient

Computing binomial coefficients is non optimization problem but can be solved using dynamic programming.

Binomial coefficients are represented by $C(n, k)$ or $\binom{n}{k}$ and can be used to represent the coefficients of a binomial:

$$(a + b)^n = C(n, 0)a^n + \dots + C(n, k)a^{n-k}b^k + \dots + C(n, n)b^n$$

The recursive relation is defined by the prior power

$$C(n, k) = C(n-1, k-1) + C(n-1, k) \text{ for } n > k > 0$$

$$IC \ C(n, 0) = C(n, n) = 1$$

Dynamic algorithm constructs a $n \times k$ table, with the first column and diagonal filled out using the IC.

Construct the table:

	0	1	2	...	k-1	k
0	1					
1	1	1				
2	1	2	1			
...						
k	1					1
...						
n-1	1				$C(n-1, k-1)$	
n	1					$C(n, k)$

The table is then filled out iteratively, row by row using the recursive relation.

Algorithm Binomial(n, k)

```

for i ← 0 to n do // fill out the table row wise
    for j = 0 to min(i, k) do
        if j==0 or j==i then C[i, j] ← 1 // IC
        else C[i, j] ← C[i-1, j-1] + C[i-1, j] // recursive
            relation
return C[n, k]
```

The cost of the algorithm is filling out the table. Addition is the basic operation. Because $k \leq n$, the sum needs to be split into two parts because only the half the table needs to be filled out

for $i < k$ and remaining part of the table is filled out across the entire row.

$$\begin{aligned}
 A(n, k) &= \text{sum for upper triangle} + \text{sum for the lower rectangle} \\
 &= \sum_{i=1}^k \sum_{j=1}^{i-1} 1 + \sum_{i=1}^n \sum_{j=1}^k 1 \\
 &= \sum_{i=1}^k (i-1) + \sum_{i=1}^n k \\
 &= (k-1)k/2 + k(n-k) \in \Theta(nk)
 \end{aligned}$$

Note we do not need to keep the whole table, only the prior row.

We'll consider more sophisticated dynamic programming problems, Warshall's and Floyd's algorithms

PROGRAM CODE:

//BINOMIAL COEFFICIENT

```

#include<stdio.h>
void main()
{
    int i,j,n,min,k,c[10][10];
    printf("Enter N & K\n");
    scanf("%d%d",&n,&k);
    for (i=0;i<n;i++)
        for(j=0;j<=k;j++)
            c[i][j]=0;
    if (n >= k)
    {
        for (i=0;i<=n;i++)
        {
            min=(i<j) ? i : j;
            for(j=0;j<=min;j++)
                if((j==0) || (i==j))
                    c[i][j] = 1;
                else
                    c[i][j] = c[i - 1][j - 1]
+ c[i-1][j];
        }
        printf("\n The Binomial Co-efficient form : ");
        for (i=0;i<=n;i++)
        {
            for(j=0;j<=k;j++)
                if(i >= j)
                    printf("%4d",c[i][j]);

            printf("\n");
        }
        if(k != 0)
            printf("\n The value if c (%d,%d) = :
%d",n,k,c[n-1][k-1] + c[n-1][k]);
        else
            printf("\n The value id c(%d,%d)= 1 \n",n,k);
    }
    else
        printf("n must be greater than k ");
}

```



```
}
```

```
/*
```

OUTPUT

RUN 1:

Enter N & K

5 2

The Binomial Co-efficient form : 1

1	1	
1	2	1
1	3	3
1	4	6
1	5	10

The value if $c(5,2) =$: 10

RUN 2:

Enter N & K

2 7

n must be greater than k

```
*/
```