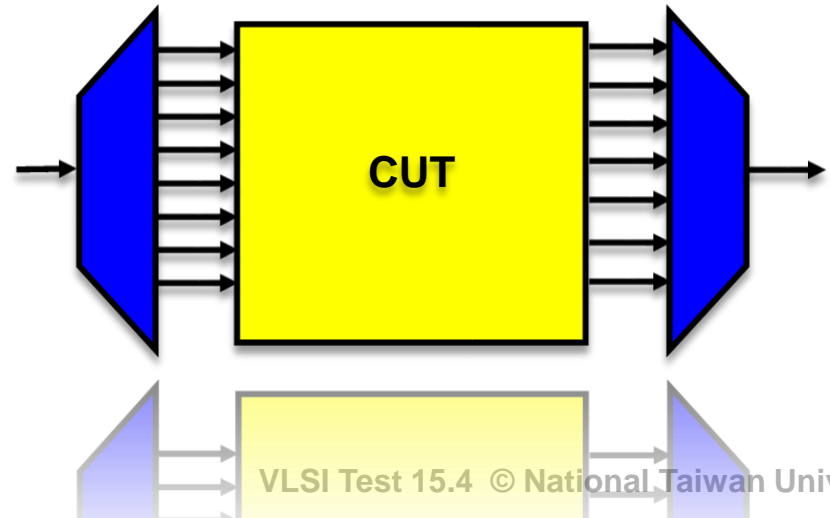


# Test Compression

- Introduction
- Software Techniques
- **Hardware Techniques**
  - ♦ Test Stimulus Compression
  - ♦ **Test Response Compaction(TRC)\***
- Industry Practices
- Conclusion

**\* NOTE**

Test stimulus **compression** is lossless  
Test response **compaction** can be lossy



# What is Good TRC?

## 1. High Compaction Ratio (CR)

$$CR = \frac{\text{Original Data Volume}}{\text{Compacted Data Volume}}$$

## 2. Low Aliasing

$$PAL = \frac{\text{number of faulty outputs that generate gold signature}}{\text{total number of faulty outputs}}$$

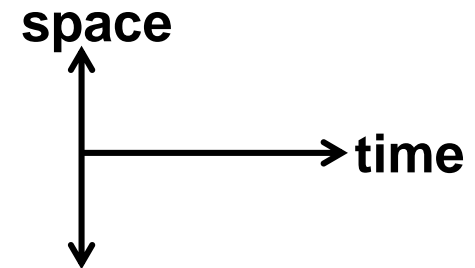
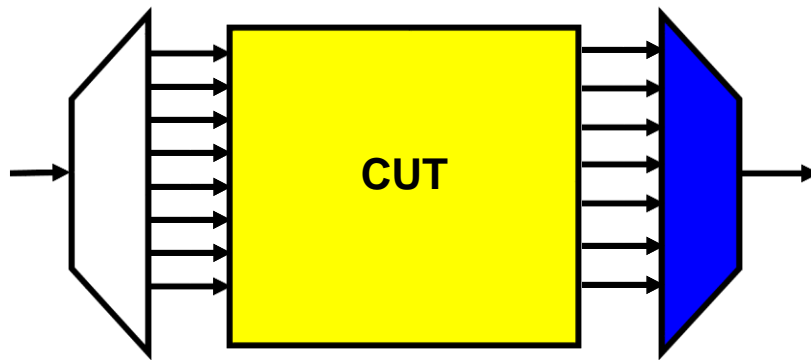
## 3. Tolerate/mask unknown (X) outputs

- ♦ Unknown outputs come from memory or non-scan flip-flop
- ♦ NOTE: this is different from *unspecified bit (X)* during ATPG

## 4. Diagnosis support (not in this lecture)

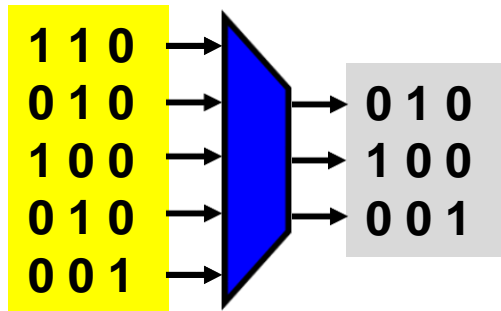
Compacted test responses of a fault is different from those of another fault

# Test Response Compactor (TRC)



- **Space compaction**

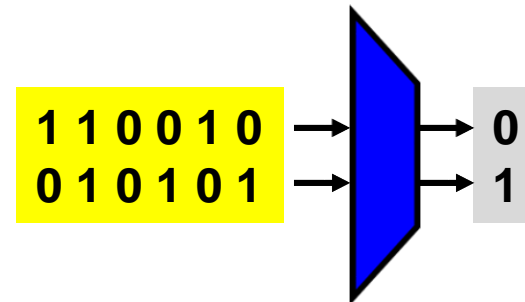
- ♦ reduces output pins



$$\text{Compaction Ratio} = \frac{5}{3}$$

- **Time compaction**

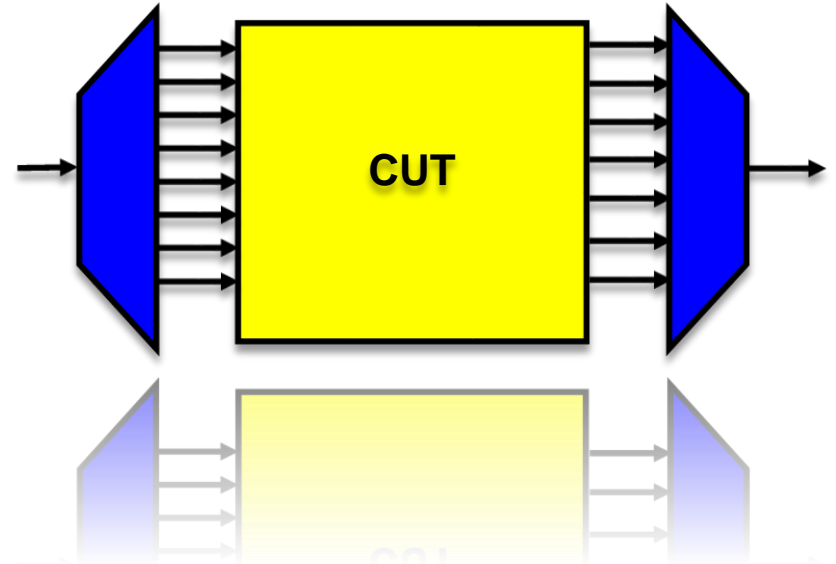
- ♦ reduces output length



$$\text{Compaction Ratio} = \frac{6}{1}$$

# Test Compression

- Introduction
- Software Techniques
- Hardware Techniques
  - ◆ Test Stimulus Compression
  - ◆ Test Response Compaction
    - \* Space Compaction
      - X-compact
    - \* Time Compaction
      - MISR
    - \* Other X-handling techniques
      - X-blocking
      - X-masking
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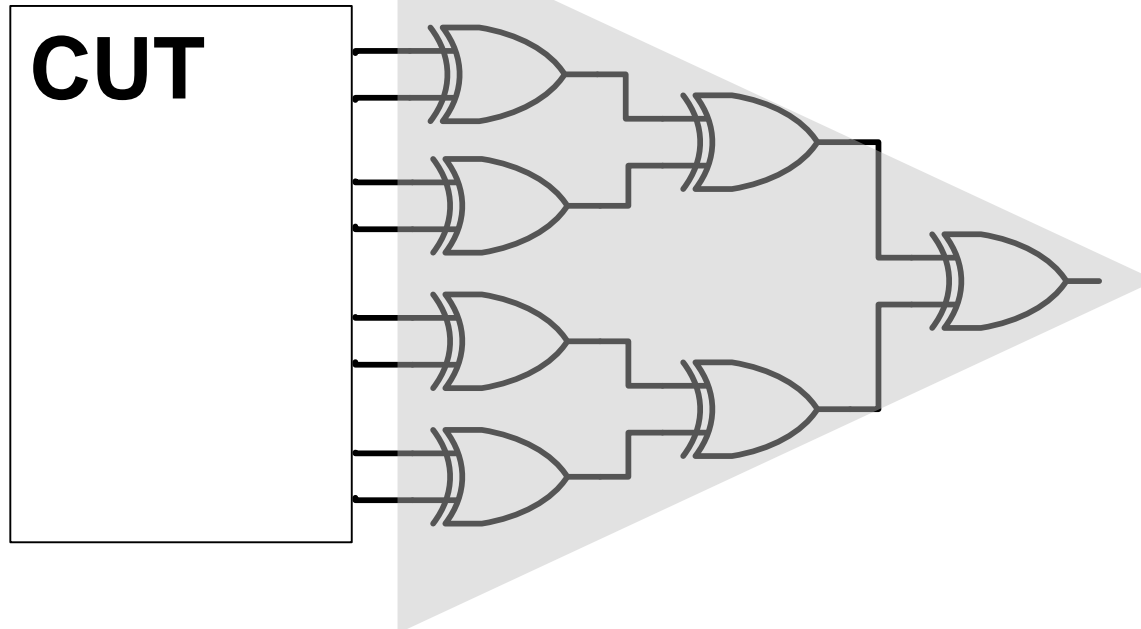


# Single XOR-Tree

- 1. High CR
- 2. Bad PAL
  - ♦ Detects **odd** number of errors, not even
- 3. What happens if X?

$$CR = \#CUT \text{ outputs}$$

$$PAL = \frac{1}{2}$$

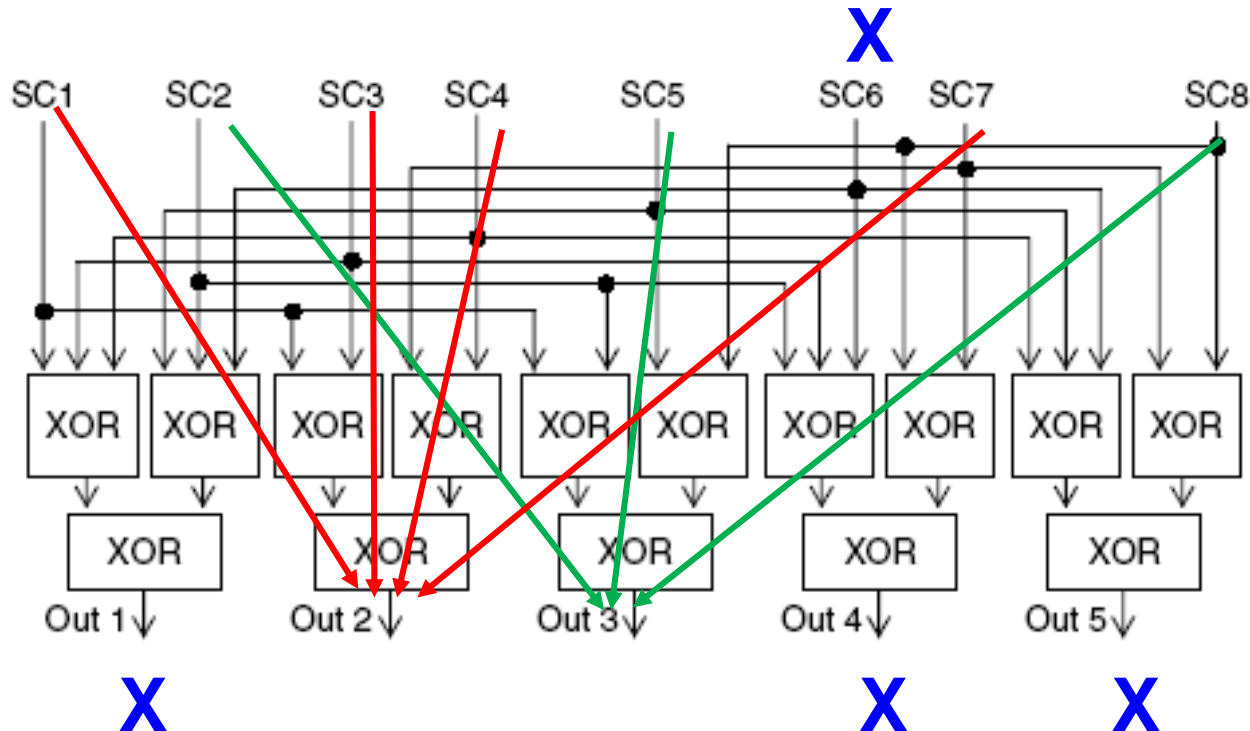


**Single XOR Tree Can NOT Tolerate X**

Idea: can we add more trees?

# X-compact [Mitra 04]

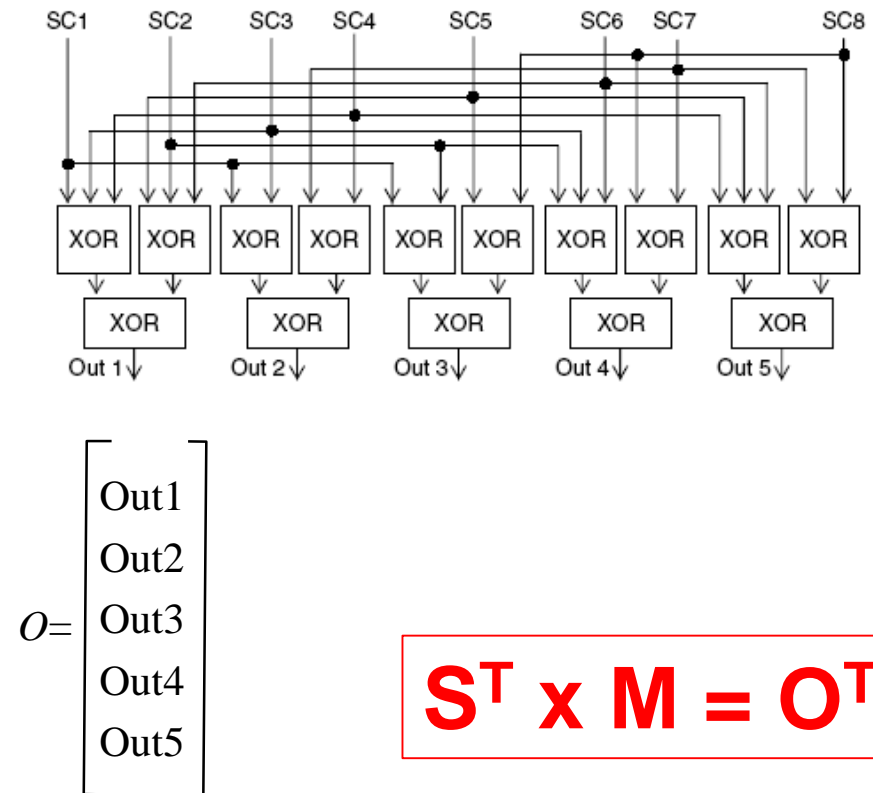
- Multiple XOR trees can detect errors in presence of X
- Example (WW. Fig. 6.24)
  - ♦ Scan chain (SC) 6 produces unknown 'X'
  - ♦ The other 7 scan chains are not contaminated



# X-compact Matrix, $M$

- Each row represents a scan chain
- Each column represents an compactor output
- $M_{i,j} = 1$  means  $j_{th}$  compactor outputs depends on  $i_{th}$  scan output

$$S = \begin{bmatrix} SC1 \\ SC2 \\ SC3 \\ SC4 \\ SC5 \\ SC6 \\ SC7 \\ SC8 \end{bmatrix} \quad M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$



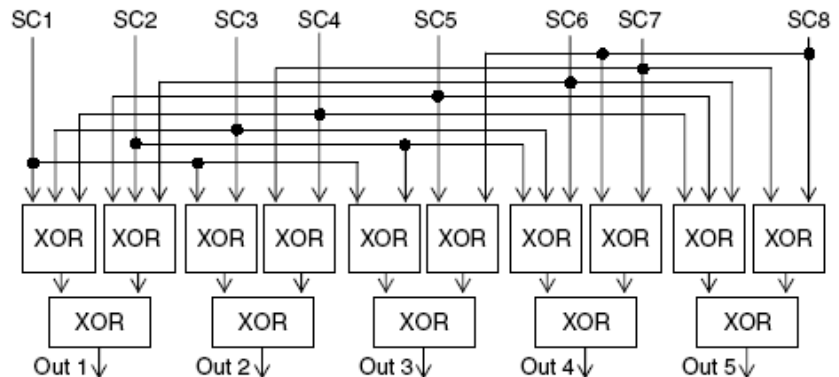
$$S^T \times M = O^T$$

# X-compact Matrix, $M$

(WWW Theorem 6.4) Any 1, 2 or odd number of errors at same cycle are detected if every row in  $M$  has *distinct odd number of 1's*.

- 1) Single error is detected because no row is all zeros
- 2) Two errors are detected because adding any two rows produces non-zero results since no two rows are the same
- 3) Odd number of errors are detected because adding odd number of rows produces non-zero results (since all rows has odd 1's)

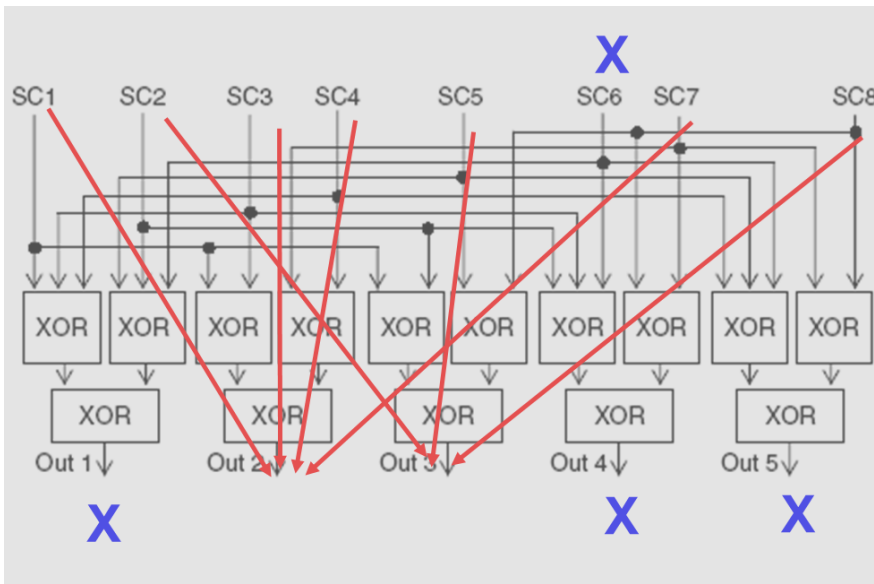
$$M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$





# Theorem for X-tolerance

- X-compact guarantees to **detect 1 error** from any scan chain with **1 unknown (X)** from any other scan chain at same cycle
  - ♦ If and only if submatrix obtained by removing that row and columns having 1's
  - ♦ does not contain **a row of all 0s**
- Example: SC 6 produces X



$$M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ \rightarrow 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

# What is CR?

- Every row in the X-compact matrix is *nonzero, distinct*
  - ♦ contains *odd number of 1's*

number of compactor outputs (#out)	max number of scan chains (#sc)	CR
5	$C_3^5=10$	2
6	$C_3^6=20$	3.3
7	$C_3^7=35$	5
8	$C_3^8=56$	7
9	$C_5^9=126$	14
10	$C_5^{10}=252$	25.2

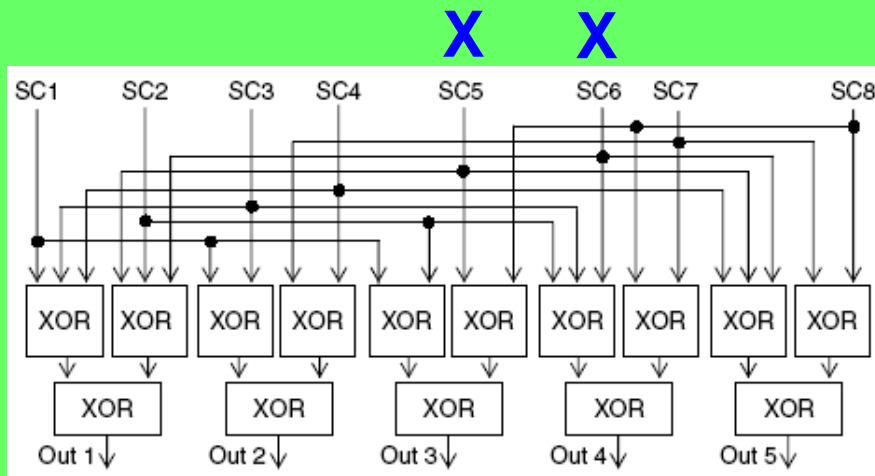
$$M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 & 1 \end{bmatrix} \left. \vphantom{\begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 & 1 \end{bmatrix}} \right\} C_3^5 = 10$$

$$CR = \frac{\text{Original Data}}{\text{Compacted Data}} = \frac{\#SC}{\#Out}$$

# QUIZ

**Q: Which scan chain error we can NOT detect, when there are 2 X's from SC5 and SC6?**

**ANS:**

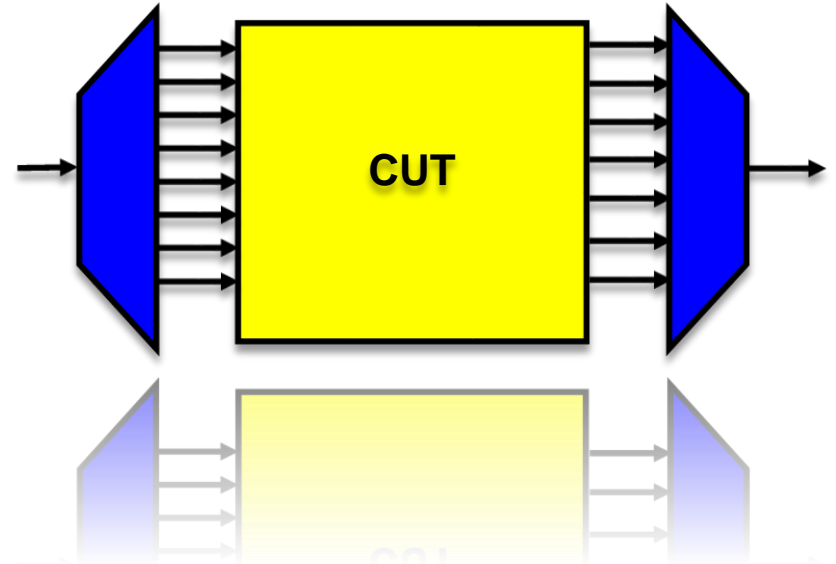


$$M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

**Cannot Tolerate Many X at Same Time**

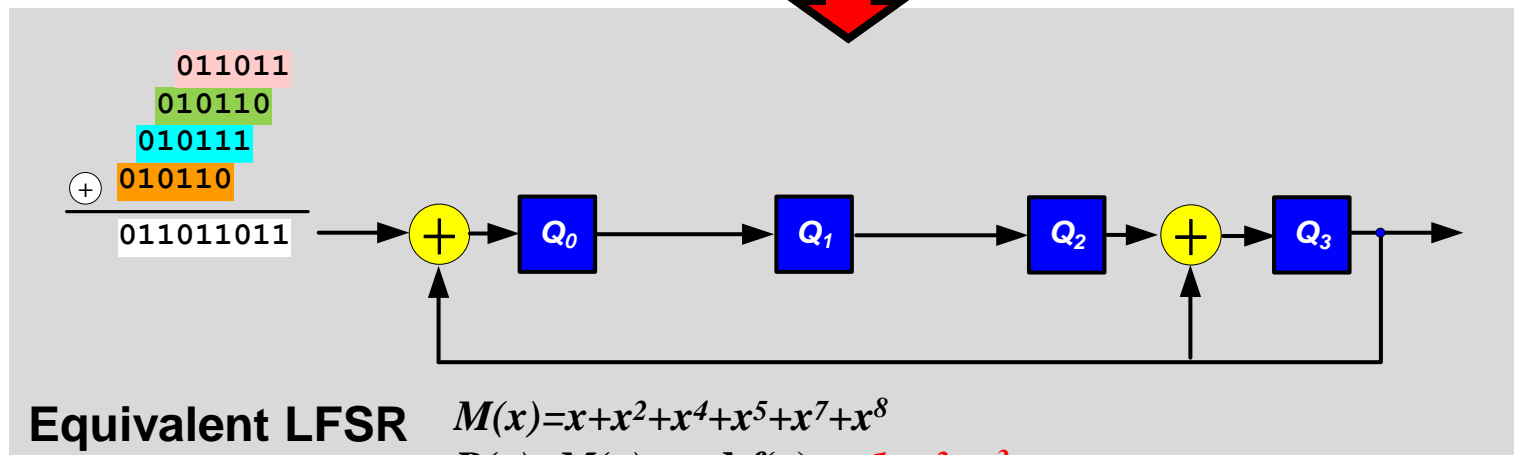
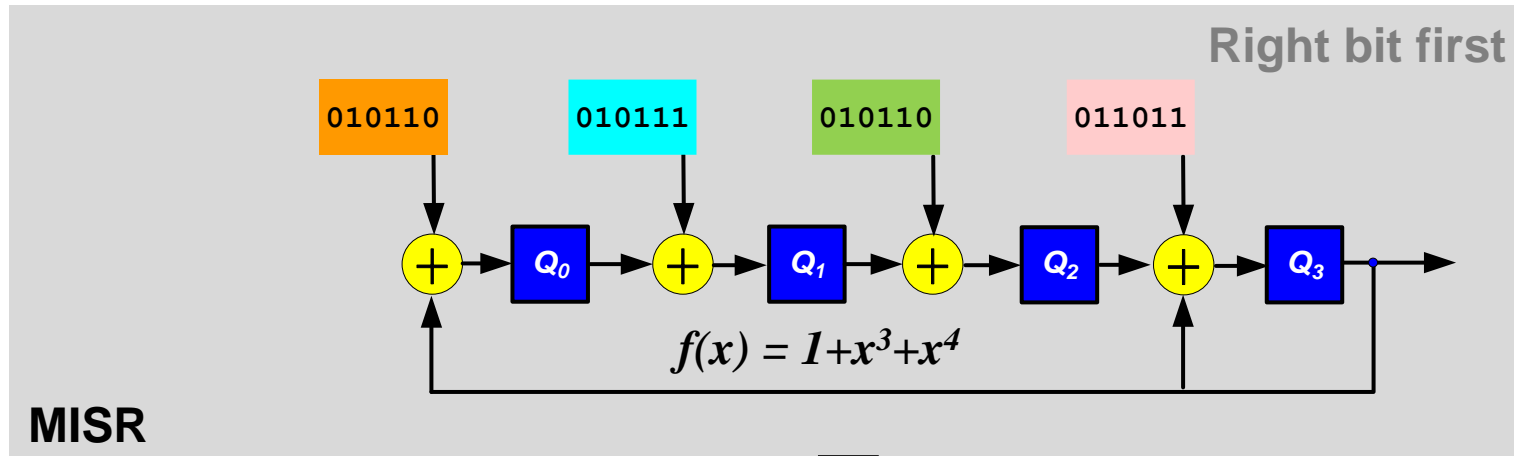
# Test Compression

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- Software Techniques
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  - ◆ Test Response Compaction
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    - \* Time Compaction
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    - \* Other X-handling techniques
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      - X-masking
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# Review: MISR (video 14.3)

- **MISR (multiple input signature register)** is similar to LFSR
  - ♦ except parallel inputs feed XOR between stages



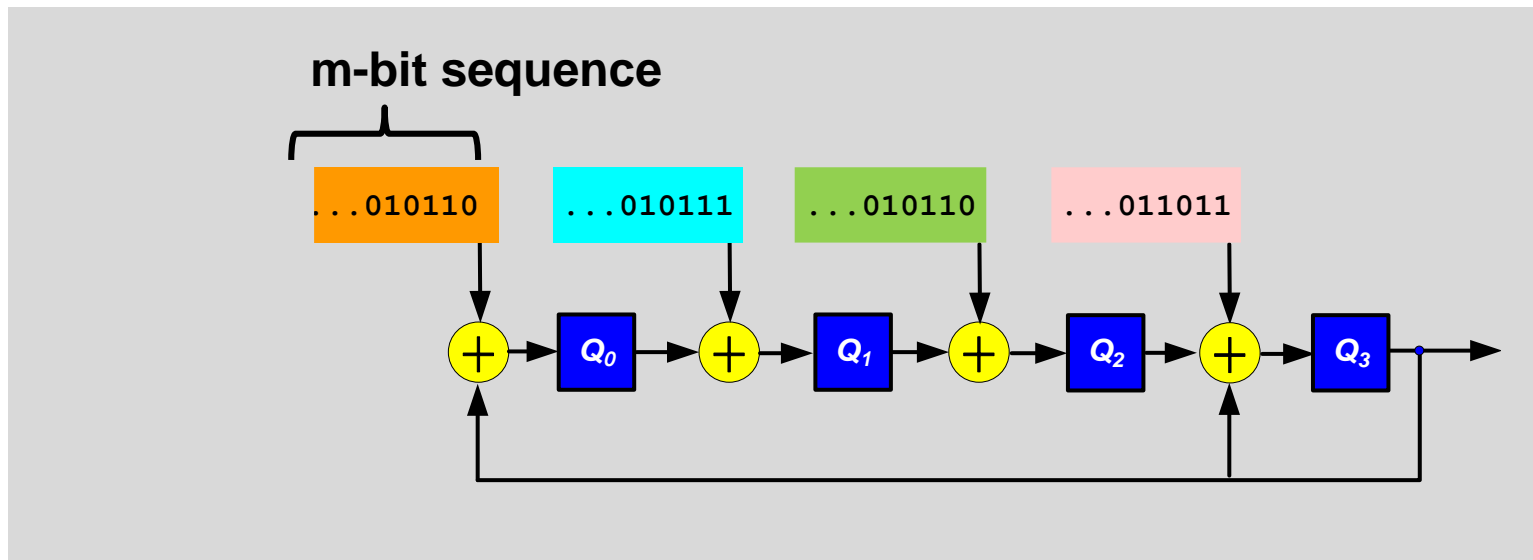
$$R(x) = M(x) \bmod f(x) = 1 + x^2 + x^3$$

# CR=? Aliasing=?

- MISR degree =  $N$ , input bit sequence length =  $m$ 
  - ♦ Signature is  $N$  bits

$$CR = \frac{\text{Original Data}}{\text{Compacted Data}} = \frac{N \times m}{N} = m$$

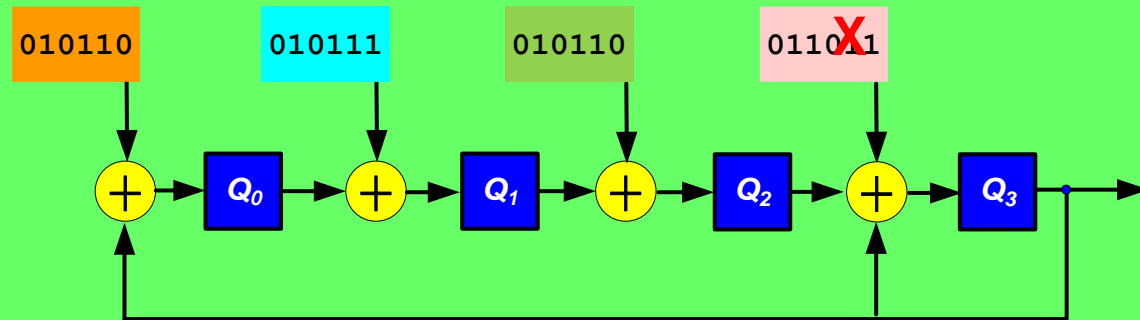
$$PAL \approx 2^{-N} \quad (\text{see 14.3})$$



**MISR has High CR and Low PAL**

# QUIZ

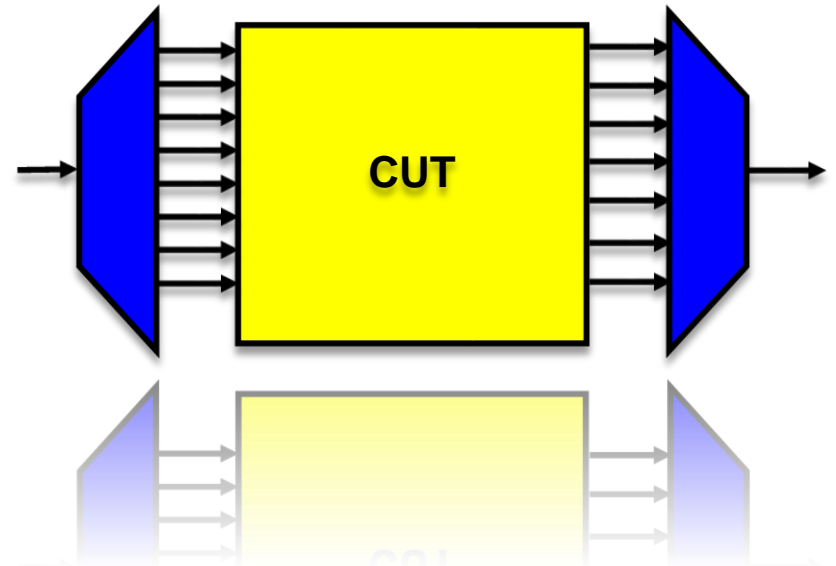
Q: What is signature if one bit is changed to X 'unknown' ?  
ANS:



**MISR is NOT X-tolerant**

# Test Compression

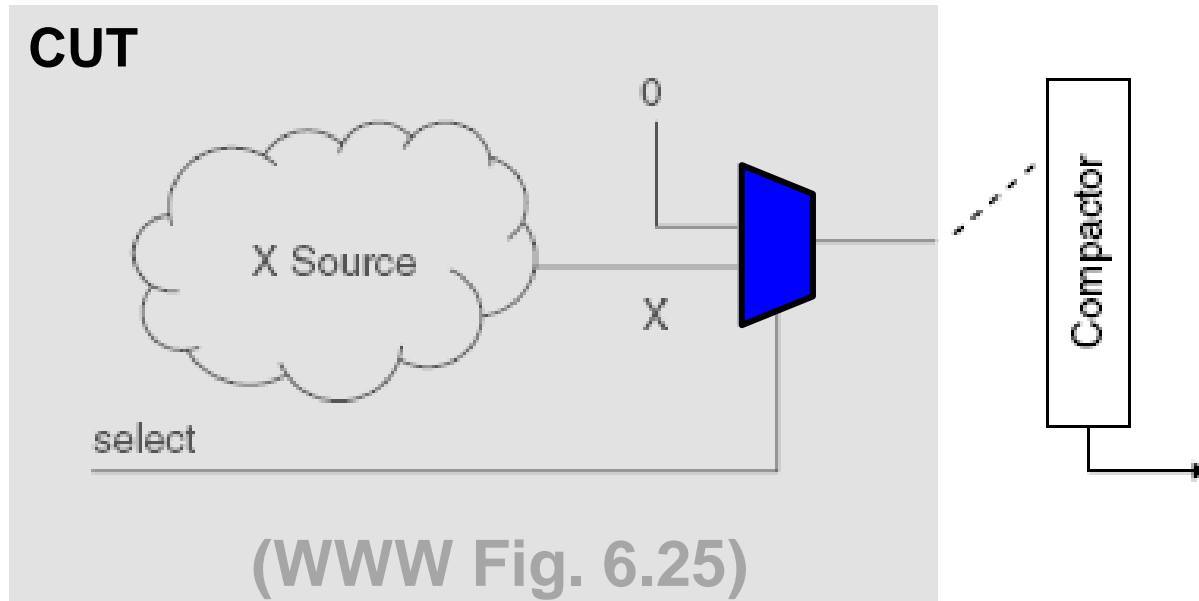
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# X-blocking (or X-bounding)

- Add extra DFT inside CUT to block X before reaching compactor
  - ♦ Area overhead and extra delay
- X source can be
  - ♦ non-scan FF, memory, multi-cycle paths, false paths\*...

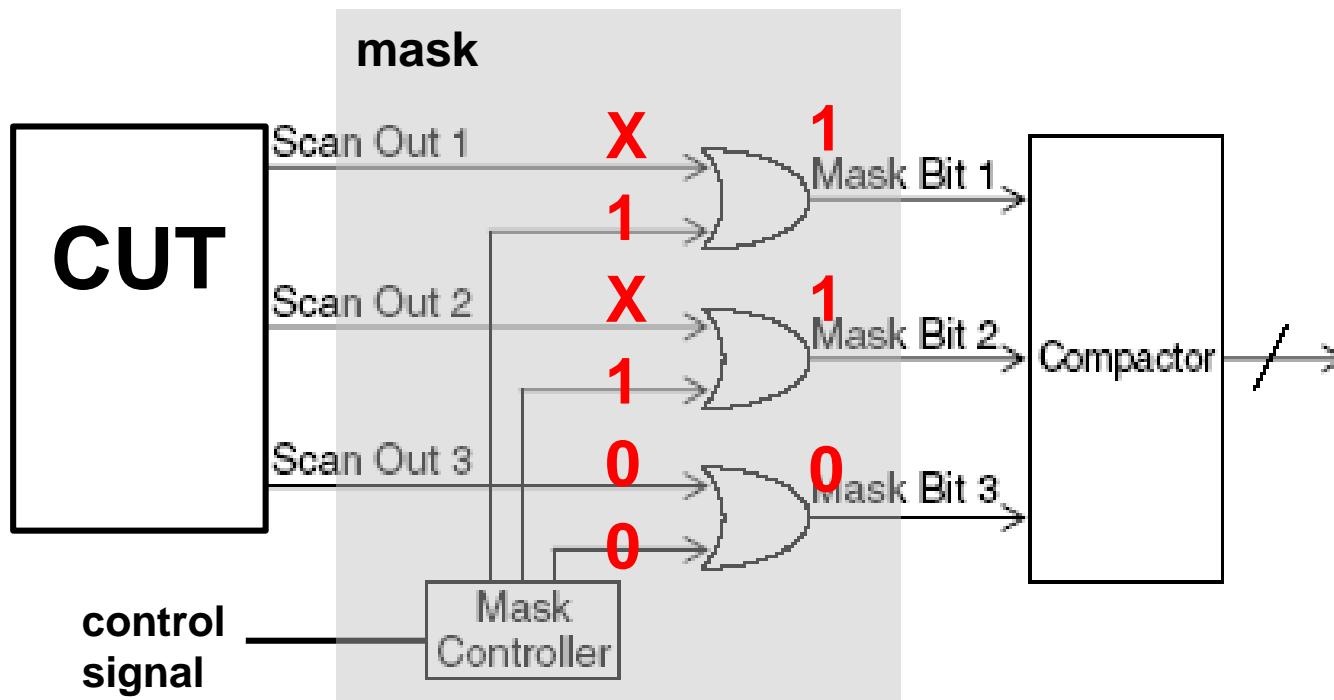


\*multi-cycle paths needs more than 1 cycle to finish computation so test responses can be X

\*false paths are not activated by normal operation so test responses can be X

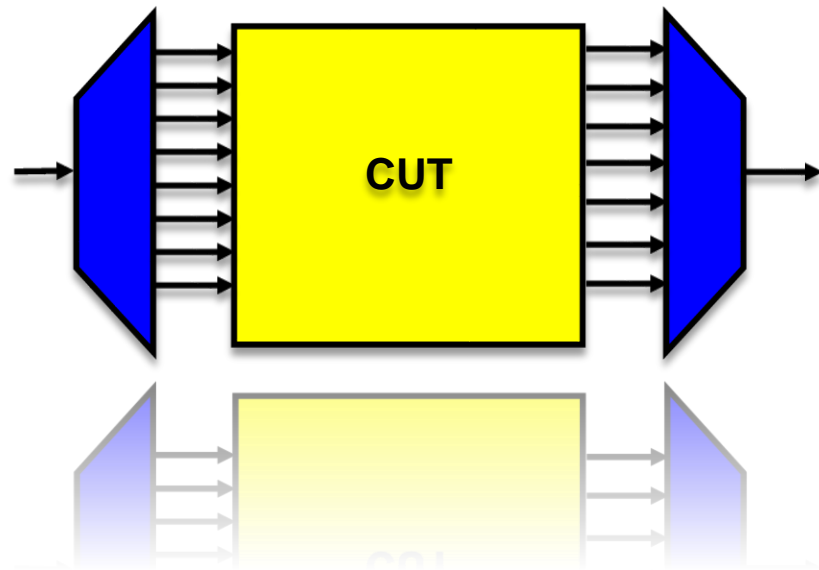
# X-masking

- Add extra mask between CUT and compactor
- Example: mask outputs by OR gates
  - ♦ 1 = mask
  - ♦ 0 = pass through



# Summary

- Test Response Compaction
  - ◆ Space Compaction
    - \* XOR-tree, X-compact
  - ◆ Time Compaction
    - \* MISR
      - High CR, Low PAL
      - Cannot tolerate X
  - ◆ X-bounding, X-masking
    - Can mask many X

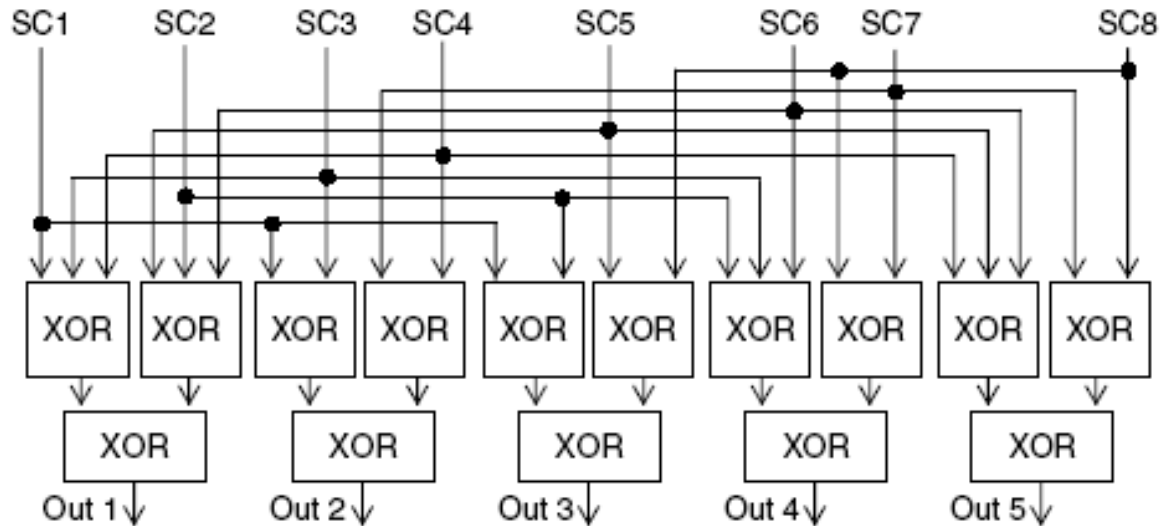


**X-Masking + MISR/XOR-tree  
is Most Popular Solution**

# FFT

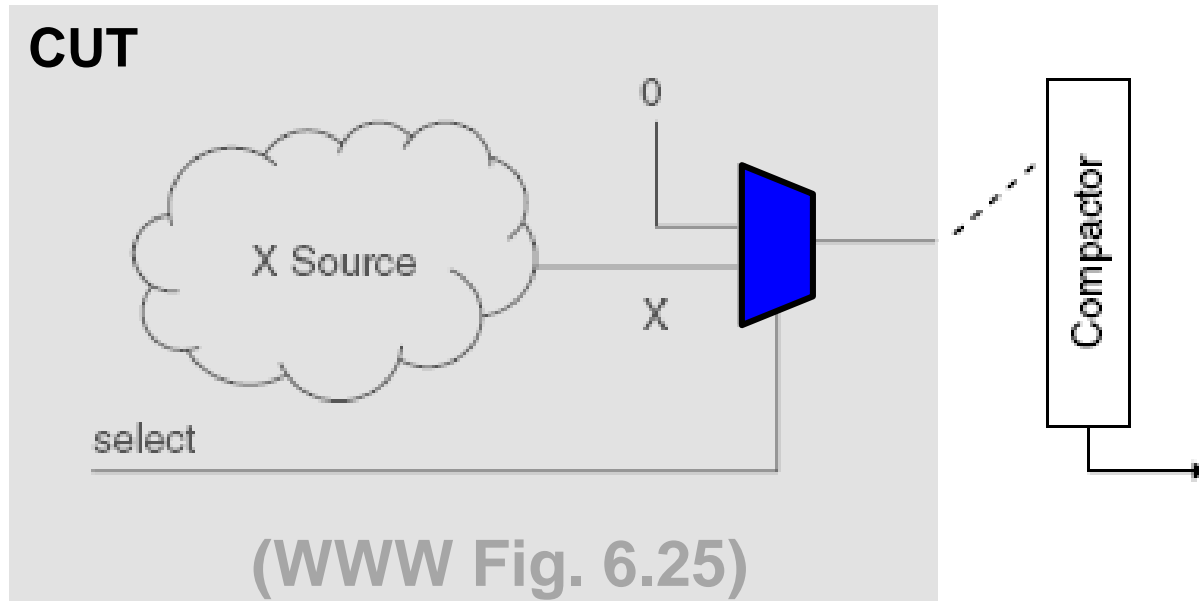
- What is Prob. of Aliasing for X-compactor?

(Theorem 6.4) Any **1, 2 or odd number** of errors at same scan-out cycle are detected if **every row in  $M$  has distinct odd number of 1's.**



# FFT

- X source can be multi-cycle paths, false paths
- Q: why multi-cycle paths generate X in test mode?
- Q: why false paths generate X in test mode?

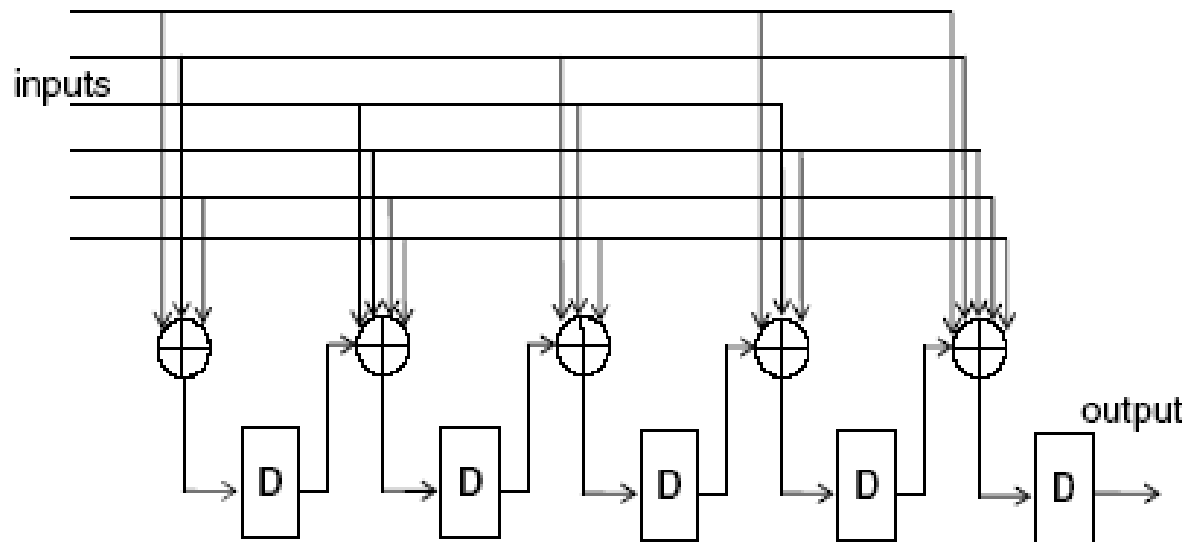


\*multi-cycle paths needs more than 1 cycle to finish computation so test responses can be X

\*false paths are not activated by normal operation so test responses can be X

# FFT

- This is a **hybrid space-time compactor**
- Q: What are advantages and disadvantages ?



# FFT

- Q: In X-compact matrix, why cannot we have **even number of 1's** in each row?

$$\begin{bmatrix} 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

# Theorems for Error Detection

- (WWW Theorem 6.3)
  - ◆ If only a single scan chain produces an error at any scan-out cycle (scan slice), the X-compactor is guaranteed to produce errors if and only if *no row of the X-compact matrix contains all 0's.*
- (WWW Theorem 6.4)
  - ◆ Errors from any **one , two or an odd number** of scan chains at the same scan-out cycle are guaranteed to be detected
    - \* if **every row in the X-compact matrix is *nonzero, distinct and contains an odd number of 1's.***



# How to Design X-compactor?

- (WWW Theorem 6.4)
  - ♦ Errors from any **one , two or an odd number** of scan chains at the same scan-out cycle are guaranteed to be detected
  - ♦ if **every row in the X-compact matrix is *nonzero, distinct and contains an odd number of 1's***.

max number of scan chains (#sc)	number of compactor outputs (#out)
$C^5_3=10$	5
$C^6_3=20$	6
$C^7_3=35$	7
$C^8_3=56$	8
$C^9_5=126$	9
$C^{10}_5=252$	10

$$M = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

$$CR = \frac{\text{Original Data}}{\text{Compressed Data}} = \frac{\#SC}{\#Out}$$

# Time v.s. Space Compaction

- **D**: original test responses
- **C**: compacted test responses
- Compactor converts **D** matrix ( $m \times n$ ) to **C** matrix ( $p \times q$ )
  - ♦ Column index referred to as time dimension
  - ♦ Row index referred to as space dimension
- Space compression:  $p < m, q = n$
- Time compression:  $q < n$

$$C = \Phi(D)$$

