

# Combinational ATPG

- **Deterministic Test Pattern Generation**

- ◆ Boolean difference approach\*
- ◆ Path sensitization method\*\*
- ◆ D-Algorithm [Roth 1966] \*\*
- ◆ PODEM [Goel 1981]\*\*

- \* Idea

- \* Heuristics

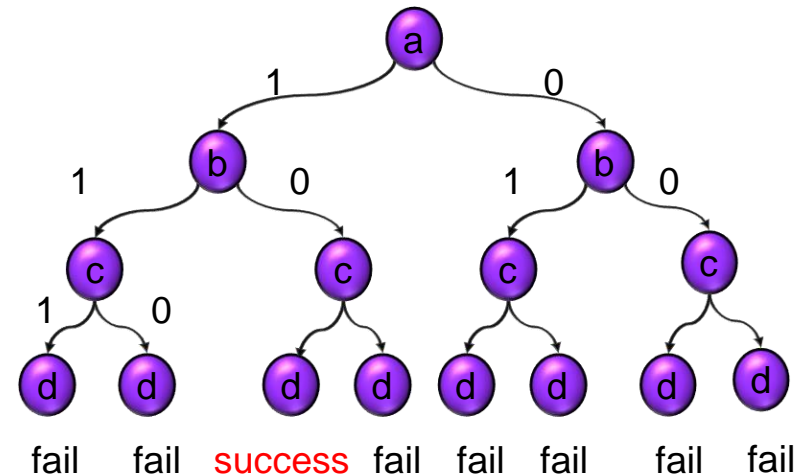
- \* Algorithms

- \* Summary

- ◆ FAN [Fujiwara 1983]\*\*
- ◆ SAT-based [Larrabee 1992]\*

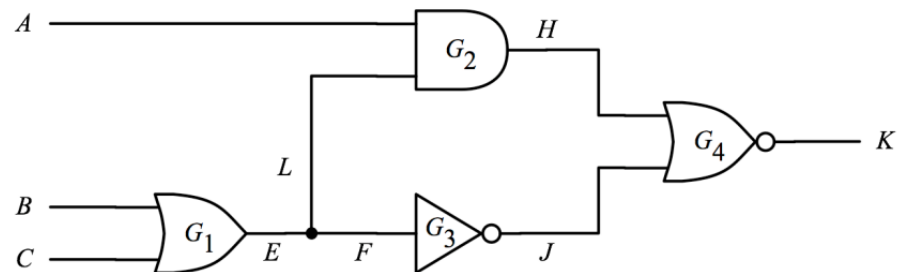
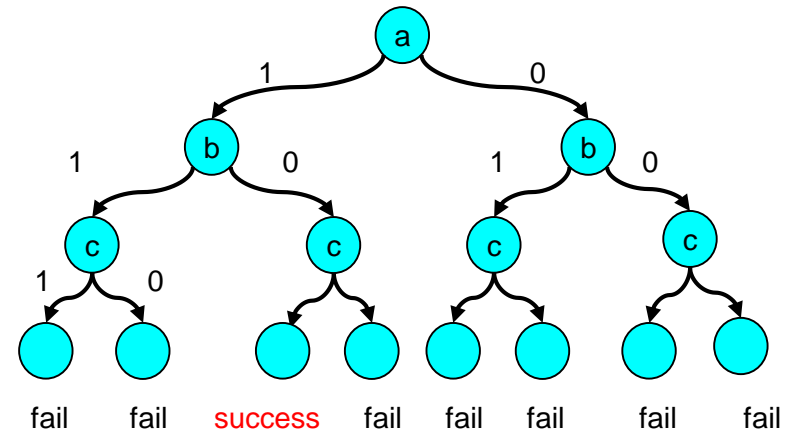
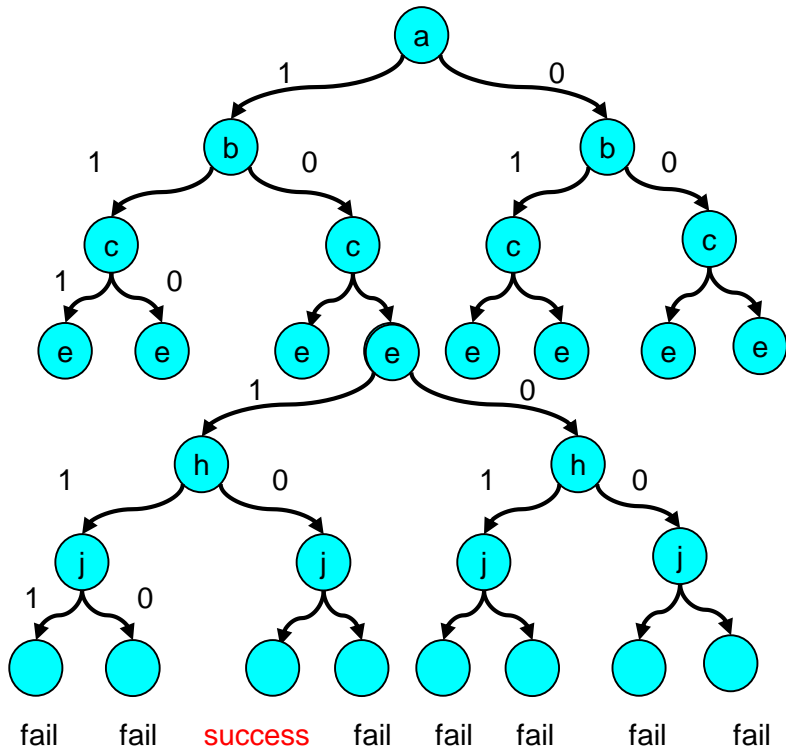
\*Boolean-based methods

\*\*path-based methods



$$2^6 \rightarrow 2^3$$

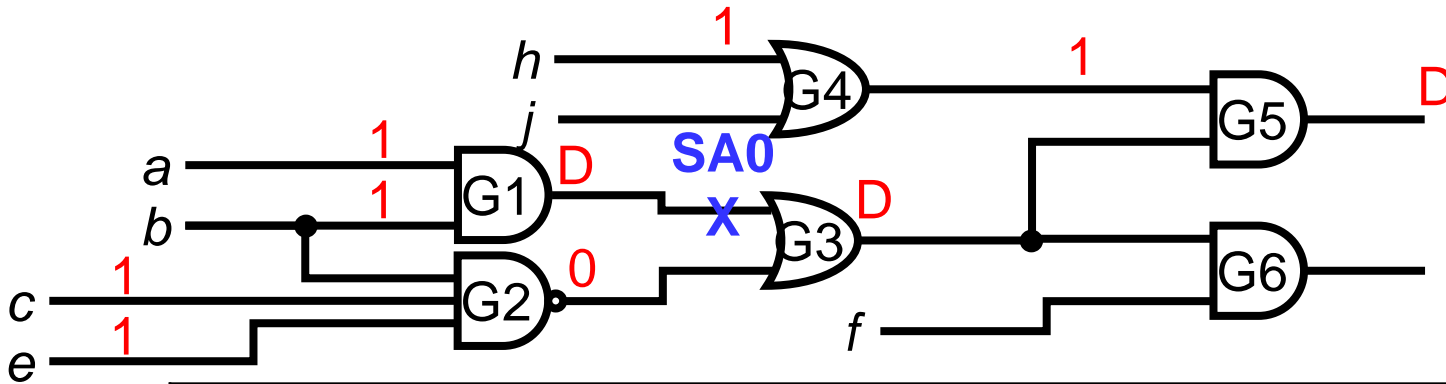
- D-alg. makes decision at **intern nodes**
  - ♦ 6 internal nodes
  - ♦  $2^6=64$  decisions! large
- PODEM makes decision at **PI**
  - ♦ 3 PI
  - ♦  $2^3=8$  decisions, smaller



# PODEM [Goel 1981]

- *Path Oriented Decision Making (PODEM)*
- IDEAS:
  1. Only allow assignments to *PI only*
    - ♦ Doesn't assign internal nodes
    - ♦ Greatly reduces search tree
  2. Assigned PI are then *forward implication*
    - ♦ No justification needed (Why ? FFT)
  3. Flip last PI assignment when two conditions:
    - ♦ A. *Fault not activated*
    - ♦ B. *No propagation path* to any output

# PODEM Example



Initial objective:  $G_1 = 1$

Backtrace to PI:  $b = 1$ . simulation, objective not achieved

Backtrace to PI:  $a = 1$ . simulation, objective achieved

Objective:  $G_2 = 0$  (propagate through  $G_3$ )

Backtrace to PI:  $C = 1$ . simulation, objective not achieved

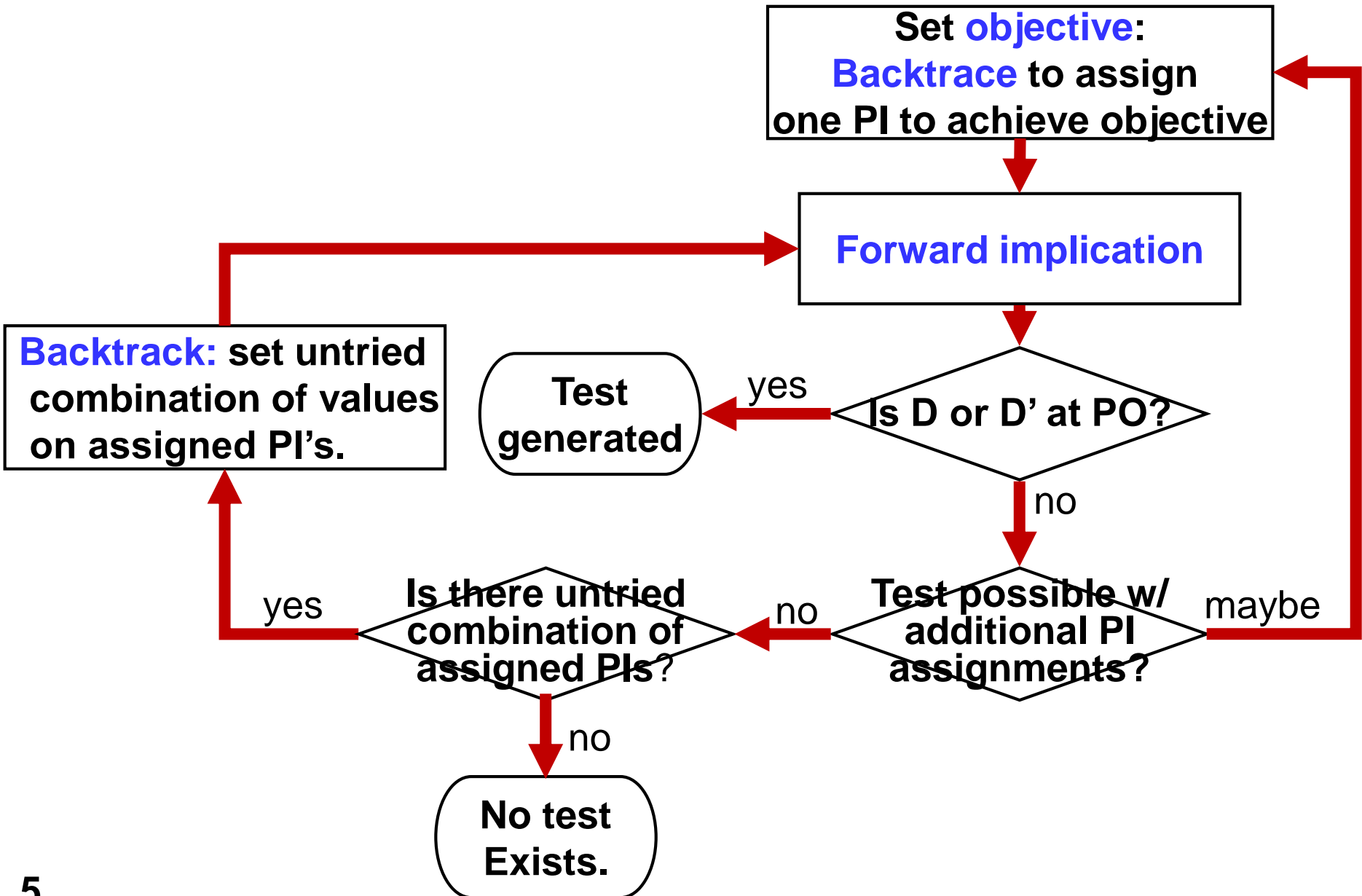
Backtrace to PI:  $e = 1$ . simulation, objective achieved

Objective:  $G_4 = 1$  (we choose to propagate through  $G_5$ )

Backtrace to PI:  $h = 1$ . objective achieved.

Test Generated:  $abcehjf = 11111XX$

# Flowchart of PODEM

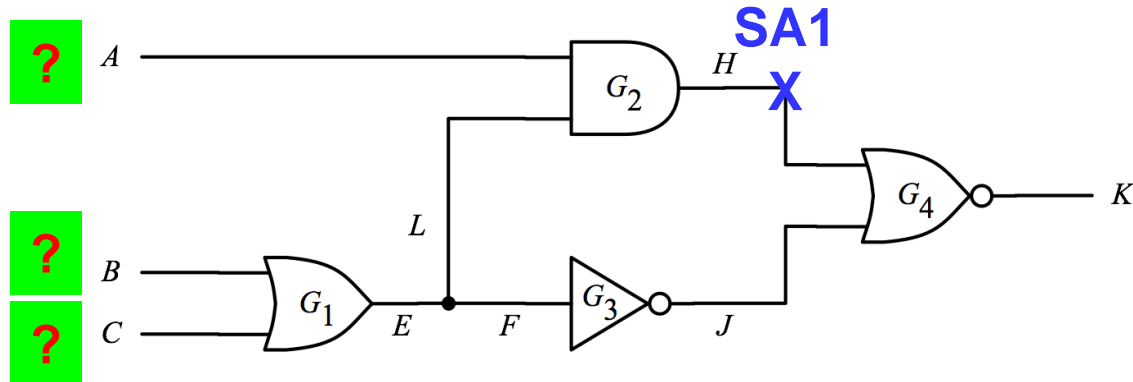


# Components of PODEM

- Determine an **objective**
  - ◆ If D/D' has not appeared at the fault site,
    - \* set objective to **activate fault**
  - ◆ If D/D' has appeared
    - \* set objective to **propagate fault effect**
- Given objective, determine PI value
  - ◆ **Backtrace to PI**
  - ◆ **Backtrack** if conflict occurs
- NOTE: **Backtrace** is different from **backtrack**
  - ◆ Backtrace goes back to primary inputs of a certain signal
    - \* In netlist
  - ◆ Backtrack goes back to last decision
    - \* in decision tree

# Quiz

**Q: Use PODEM to generate a test for H SA 1 fault  
please mark your**  
**1. objective,**  
**2. backtrace**

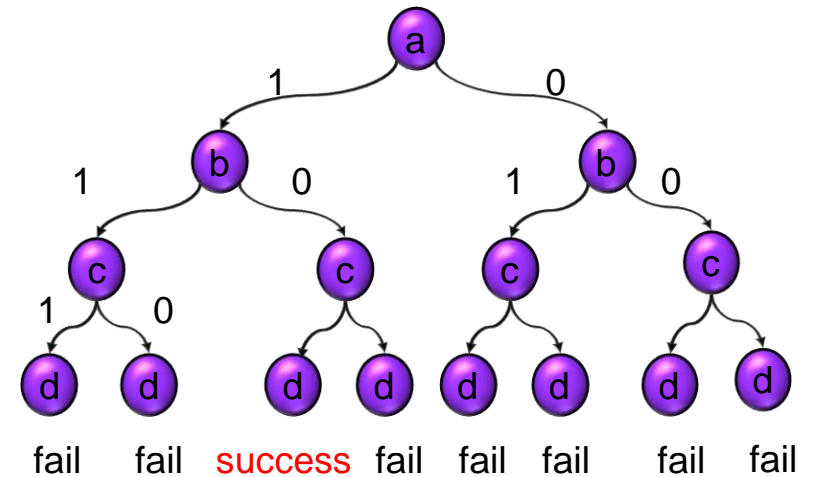


Totally 2 objectives, 2 backtraces

# PODEM

- PODEM [Goel 1981]

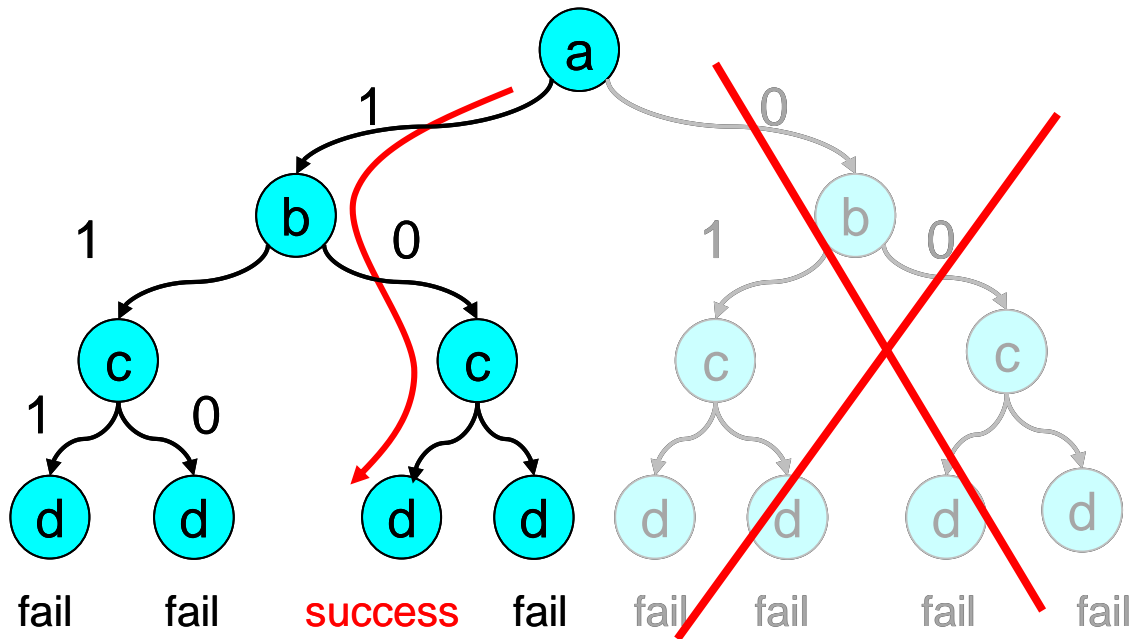
- ◆ Idea
- ◆ Heuristics
- ◆ Algorithms
- ◆ Summary





# ATPG Decision Tree

- Need smart heuristics to speed up
  - ♦ 1. Prune **impossible sub-trees** ASAP
  - ♦ 2. Find **good assignments** ASAP
- Heuristics are experience-based rules that help correct decision
  - ♦ Note: Heuristics **Do NOT** guaranteed to be correct all the time



# Questions to Be Answered

- PODEM proposed **three heuristics** to answer three questions:
  - ◆ Q1: What path to *backtrace*?
  - ◆ Q2: **What input value** to assign?
  - ◆ Q3: What path to **propagate D (D')** to PO?

**Good Heuristic = Simple  
and Effective** (most of the time)

# Q1: What Path to Backtrace?

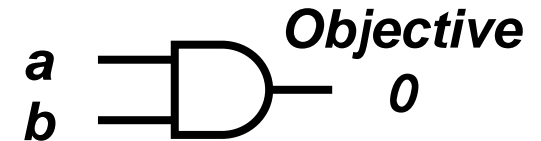
- **Decision Gate:**

- ♦ Only one input can control gate output to objective value

- \* OR/NAND with output objective =1

- \* AND/NOR with output objective =0

- ♦ choose easiest gate input



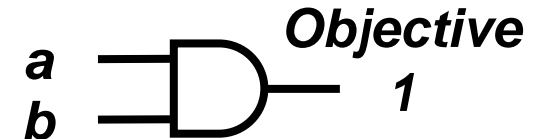
- **Implied Gate:**

- ♦ One input can't control gate output to objective value

- \* OR/NAND with output objective =0

- \* AND/NOR with output objective =1

- ♦ Choose hardest gate input

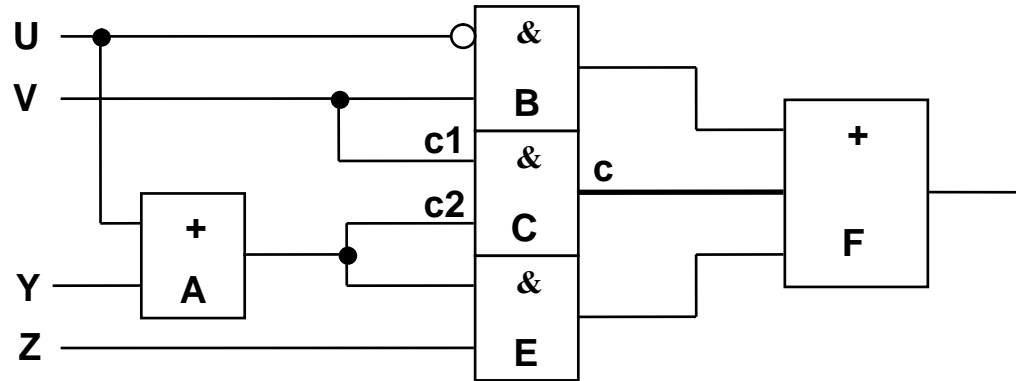


- Why? find out if test exists or not as soon as possible

**Heuristic#1: Make Correct Backtrace ASAP**

# Example

- If objective is  $c=0$ ; backtrace **c1**, then  $V=0$  (decision gate)
- If objective is  $c=1$ ; backtrace **c2**, then  $U=1$  or  $Y=1$  (imply gate)



- Q: how do you know  $c1$  is easy and  $c2$  is hard?
  - ♦ Level of  $c1$  smaller than level of  $c2$
  - ♦ (Use other controllability measure, like SCOAP, also fine)

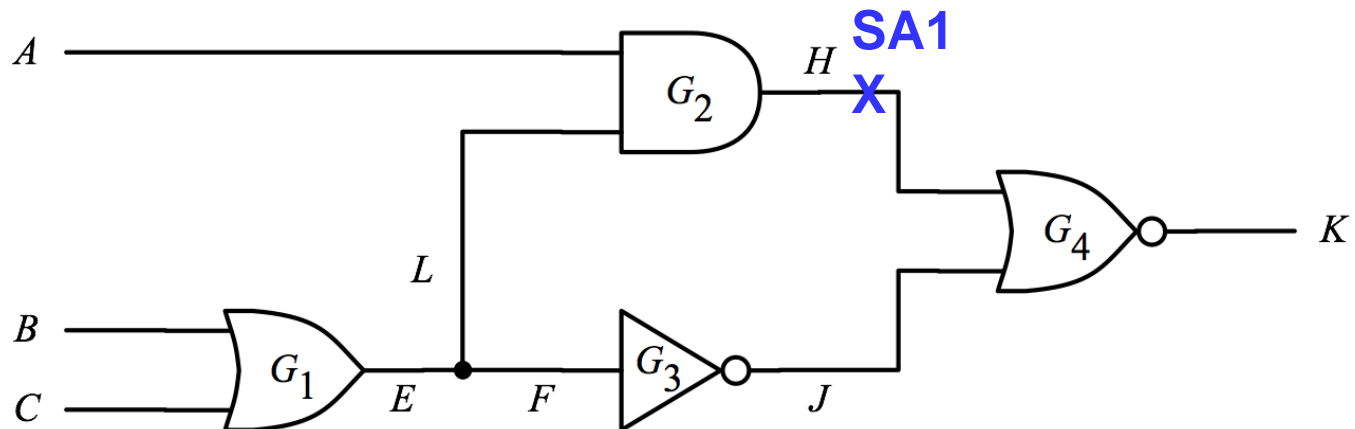
# Quiz

**Q: Given SCOAP, generate a test for H SA1 fault.**

**A1: Follow heuristic**

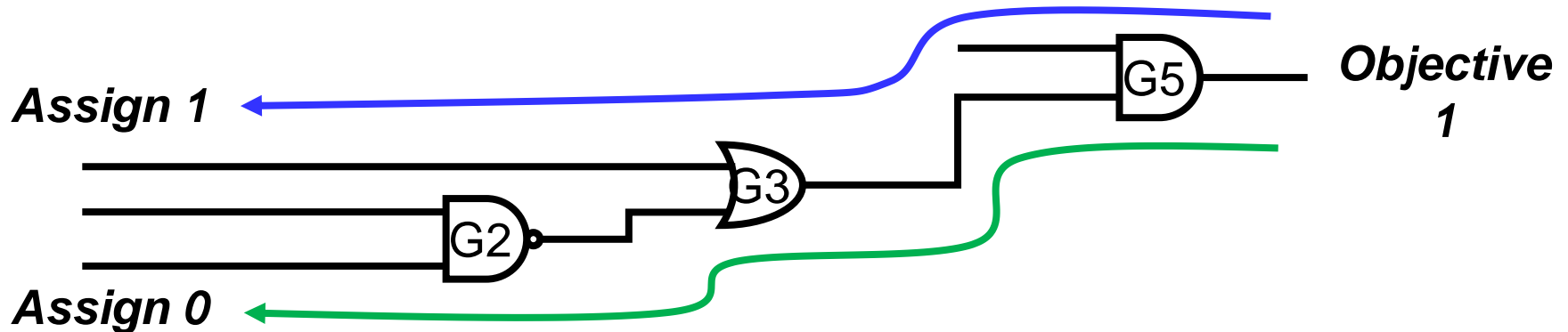
**A2: Do not follow heuristic**

	A	B	C	E	F	L	H	J	K
CC <sup>0</sup>	1	1	1	3	3	3	2	3	5
CC <sup>1</sup>	1	1	1	2	2	2	4	4	6
CO	7	6	6	4	4	6	4	3	0



## Q2: What Input Values to Assign?

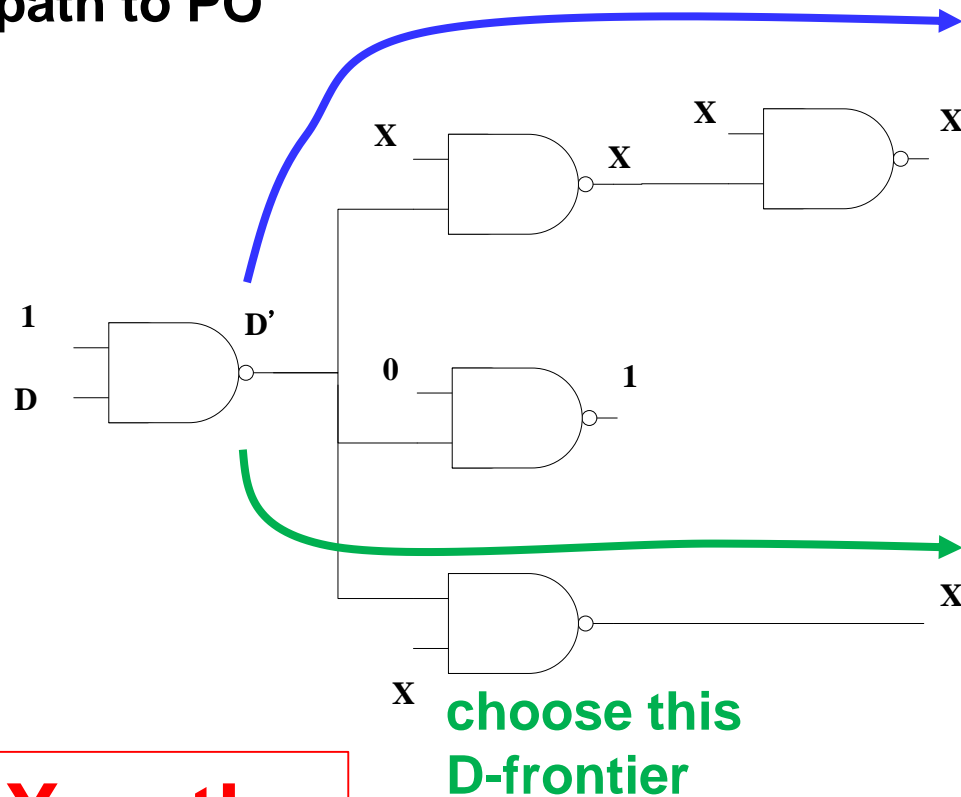
- If **even inversion parity** path
  - ♦ Assign same value as objective
- If **odd inversion parity** path
  - ♦ Assign opposite value to objective
- Why? This assignment is most likely to be correct



**Heuristic#2: Inversion Parity for Assignment**

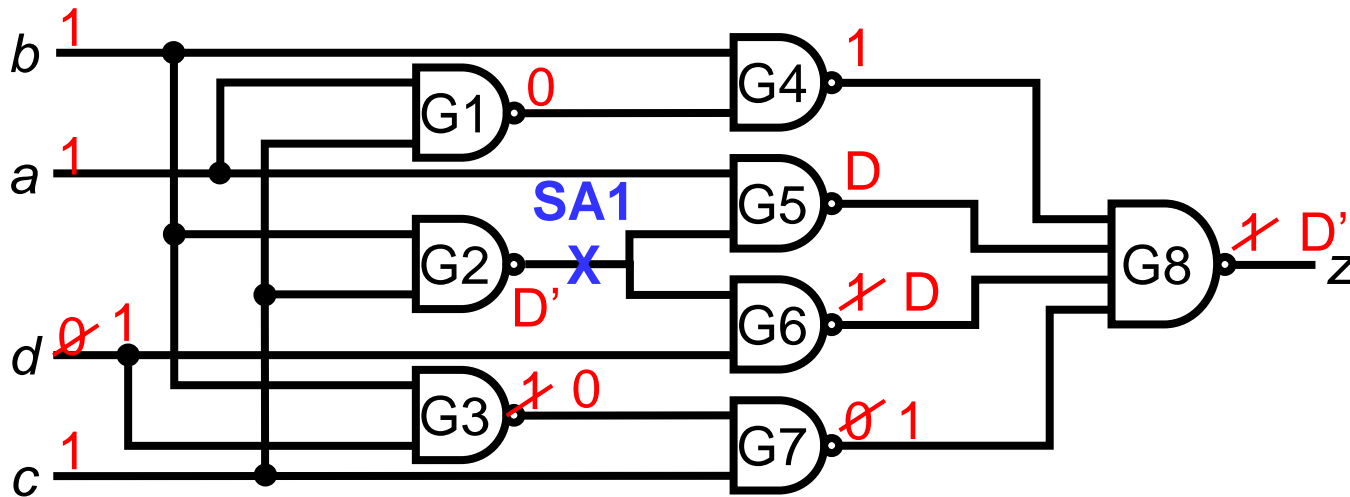
# Q3: What Path to Propagate ?

- All gate output of the chosen path must have X values
  - ♦ Called **X-PATH**
- If more than one X-path to choose,
  - ♦ chose shortest X-path to PO
- If X-path disappear,
  - ♦ **backtrack**



**Heuristic#3: X-path**

# PODEM Example w/ Backtrack



Initial objective: (G2, 0)

Backtrace to PI:  $b = 1$

Initial objective: (G2, 0)

Backtrace to PI:  $c = 1$

Implication:  $G2 = D'$

Choose shortest X-path {G5}

Objective  $a = 1$

Assign  $a=1$

Implication:  $G1 = 0, G4 = 1, G5 = D$

Try propagate through G8.

objective: (G6,1)

Backtrace to PI:  $d = 0$

Implication:  $G3 = 1, G7 = 0, G8 = 1$

X-path disappear!

Backtrack to most recent PI assignment:

$d = 0 \rightarrow d = 1$

Implication:  $G3 = 0, G6 = D, G8 = D'$

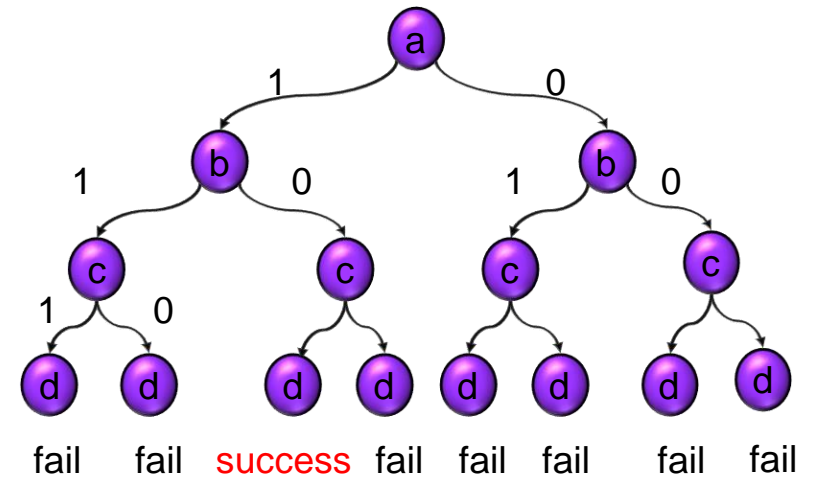
Test generated!



# PODEM

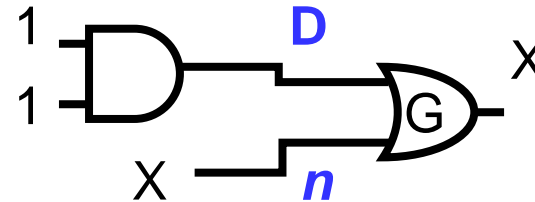
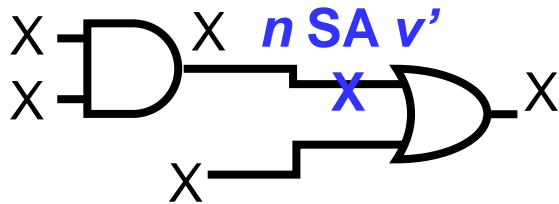
- PODEM [Goel 1981]

- ◆ Idea
- ◆ Heuristics
- ◆ Algorithms
- ◆ Summary



# Objective

- Pick an objective: (1) fault activation (2) propagate fault effect



**Objective** ( $n, v$ ) // target fault: **net  $n$  stuck-at  $v'$**   
// if fault has not been activated

1. if (net  $n$  is **unknown**)
2. return ( $n, v$ );

// else, propagate fault effect

3. select a gate **G** from D-frontier **on shortest X-path**
4. select an unassigned input  $n$  of  $G$
5. if (gate  $G$  has non-controlling value)
6.  $v =$  **non-controlling value of  $G$** ; // AND  $v=1$ ; OR,  $v=0$
7. return ( $n, v$ ); //  $n$  is objective net;  $v$  is objective value

# Backtrace

- Translates objective to PI assignment
- **Depth-first search**: recursively calls itself until hits PI

```
Backtrace (n, vs) /* n is objective net; vs is objective y; */  
1. v = vs;  
2. while (n is gate output)  
3.   if (n is NAND or INVERTER or NOR) v = v'; // inversion parity  
4.   if (objective requires setting all inputs) // imply gate  
5.     a = hardest gate input that is still X;  
6.   else // decision gate  
7.     a = easiest gate input that is still X;  
8.   n = a;  
9.   (n, v) = Backtrace (n, v); // recursive call  
   // out of while loop, n is now PI  
10. return (n, v) // assign PI n to value v
```

# PODEM

- **Branch and bound** search algorithm

**PODEM** (*fault* ,  $v_{\text{fault}}$ )

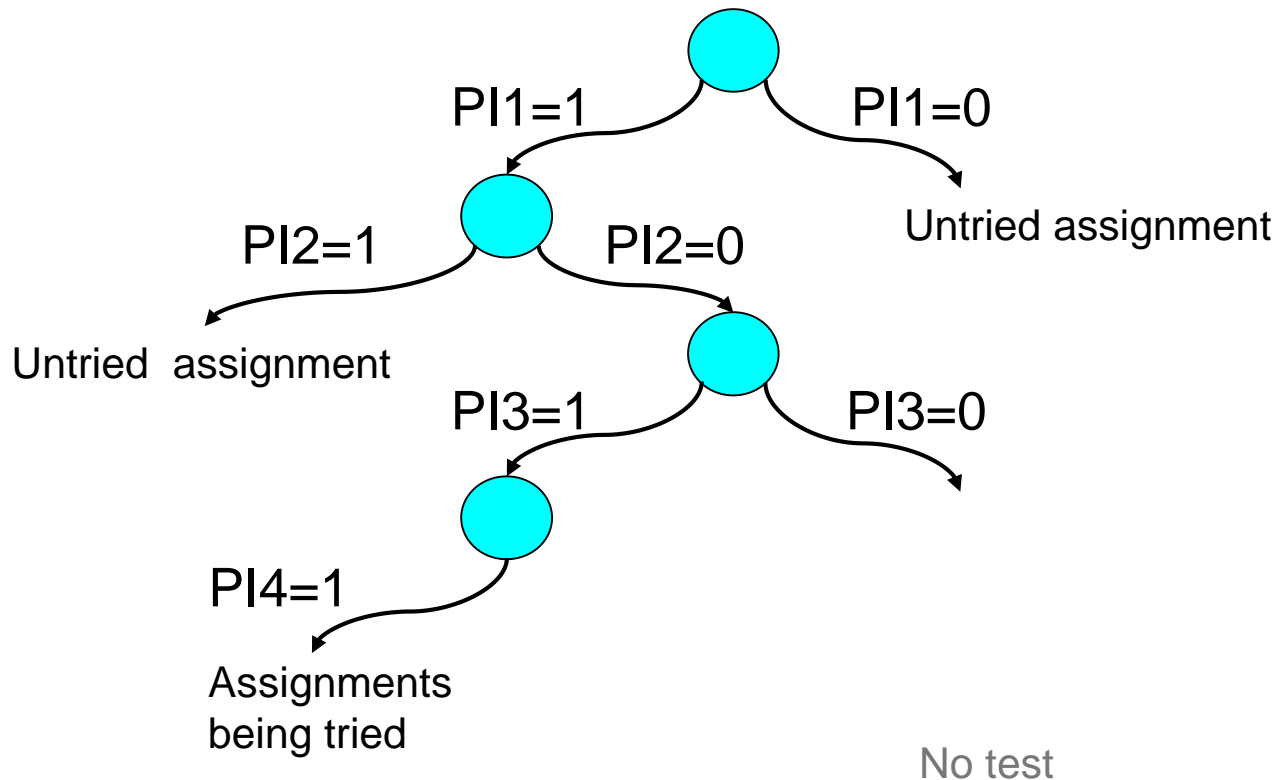
1. if (D or D' at PO) return (SUCCESS)
2. if (test impossible) return (FAILURE)
3. else ( $n, v_s$ ) = *Objective* (*fault*,  $v_{\text{fault}}$ );
4.     ( $pi, v$ ) = *Backtrace* ( $n, v_s$ );
5.     *Imply* ( $pi, v$ ); // assign pi, forward implication
6.     if (*PODEM* (*fault*,  $v_{\text{fault}}$ ) == SUCCESS) return (SUCCESS);  
      // backtrack
7.     *Imply* ( $pi, v'$ );
8.     if (*PODEM* (*fault*,  $v_{\text{fault}}$ ) == SUCCESS) return (SUCCESS);
9.     *Imply* ( $pi, \text{"X"}$ ); // release PI as unknown
10.    return (FAILURE); // this node is pruned
11. end;

test impossible for 2 reasons:

- (1) target fault cannot be activated
- (2) X-path disappear

# Decision Tree of PODEM (1)

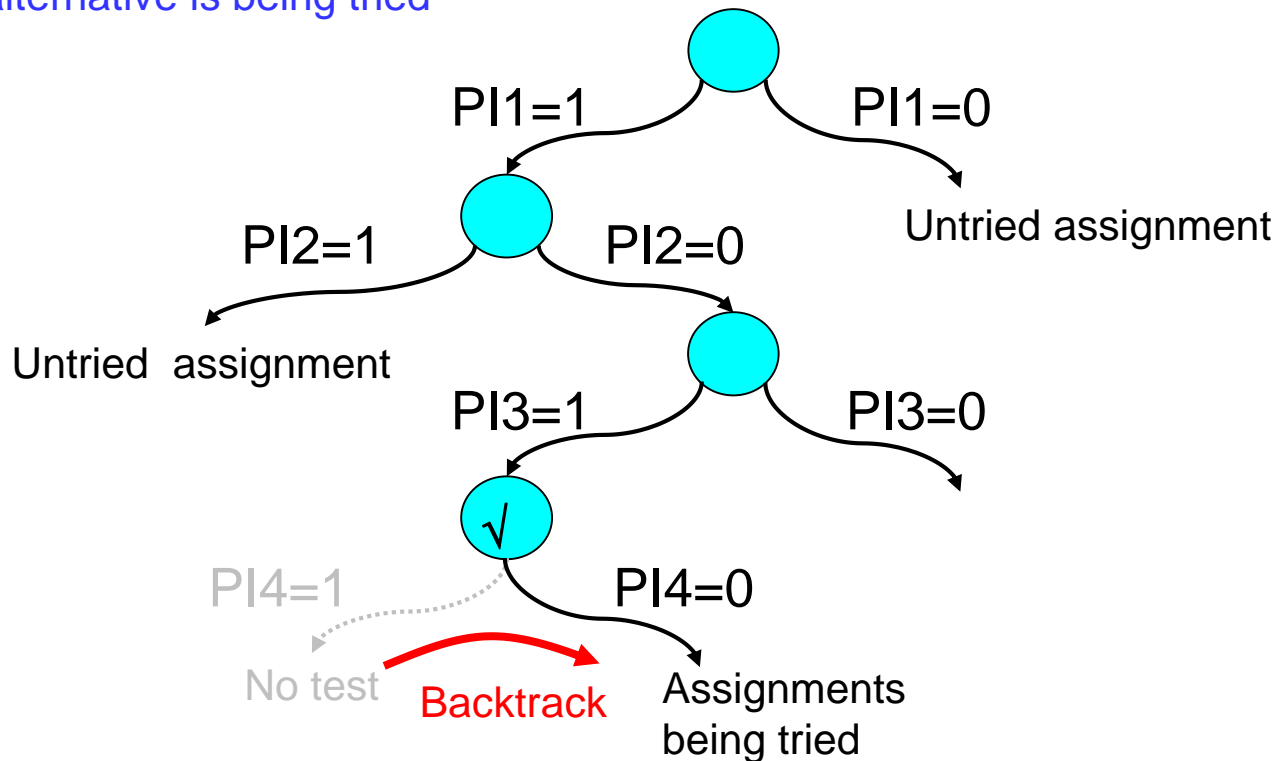
- **Branch and bound** search algorithm
  - ♦ Each decision is a PI



# Decision Tree of PODEM (2)

- **Branch and bound** search algorithm
- **Chronological backtrack**: [DPLL satisfiability 1962]
  - ♦ Flip **last PI** that has not been tried

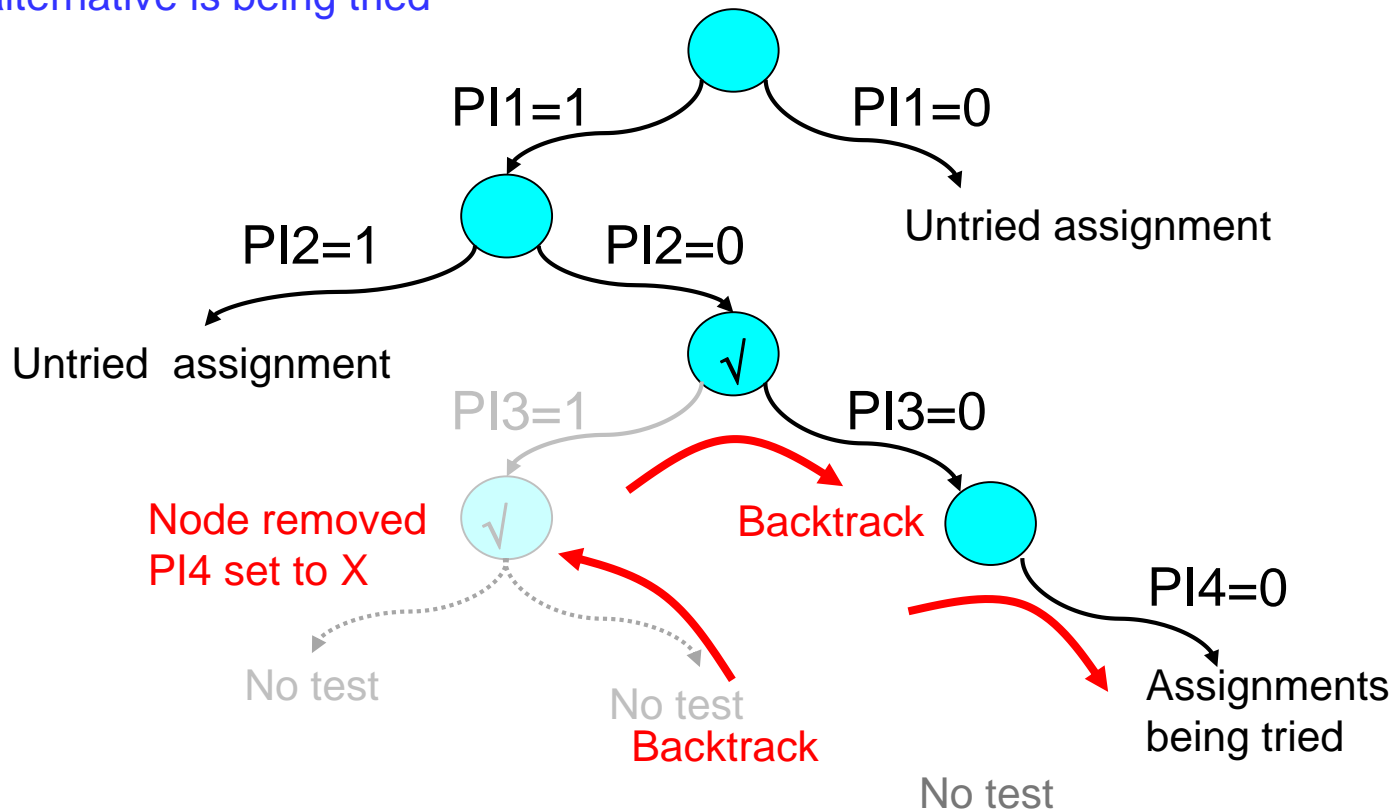
✓ : initial assignment rejected  
alternative is being tried



# Decision Tree of PODEM (3)

- **Branch and bound** search algorithm
  - ♦ A node is removed when **both** alternatives have been tried
  - ♦ Prune **PI3=1** subtree

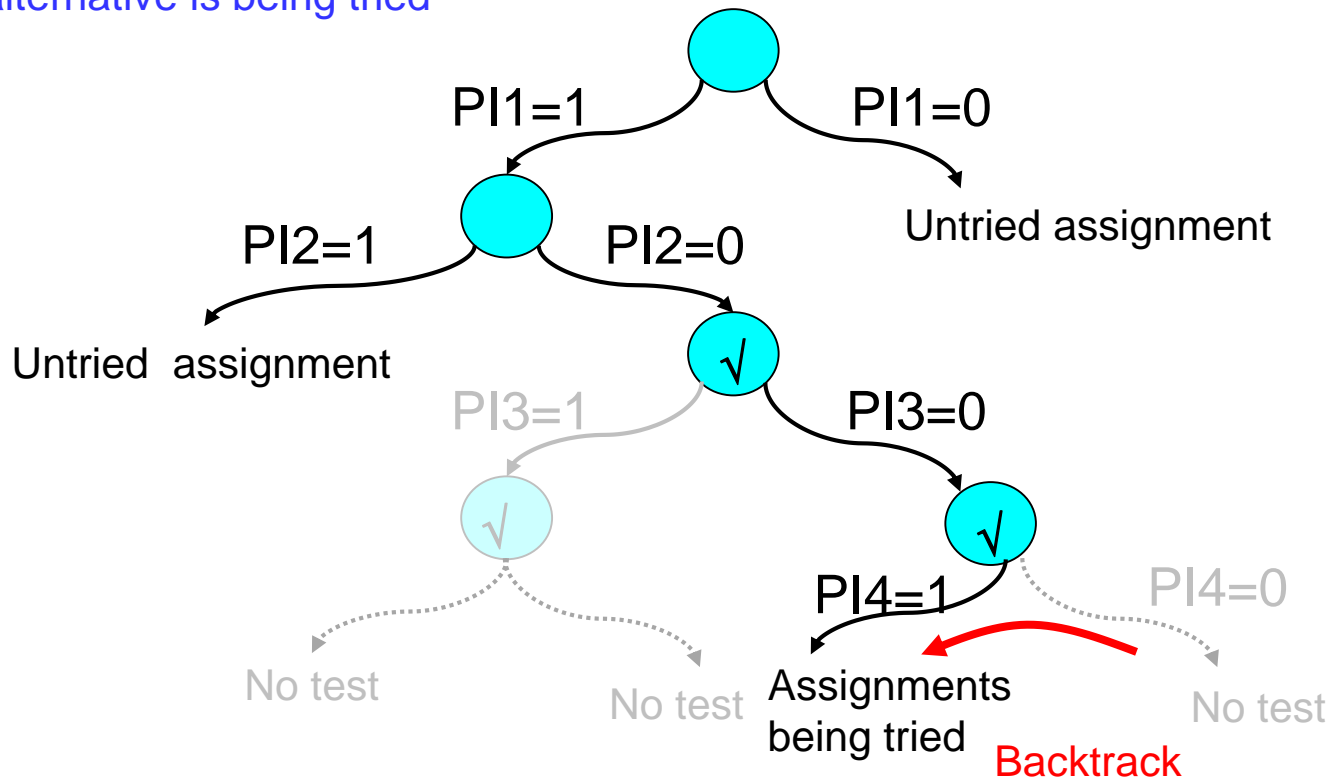
✓ : initial assignment rejected  
alternative is being tried



# Decision Tree of PODEM (4)

- **Branch and bound** search algorithm

✓ : initial assignment rejected  
alternative is being tried





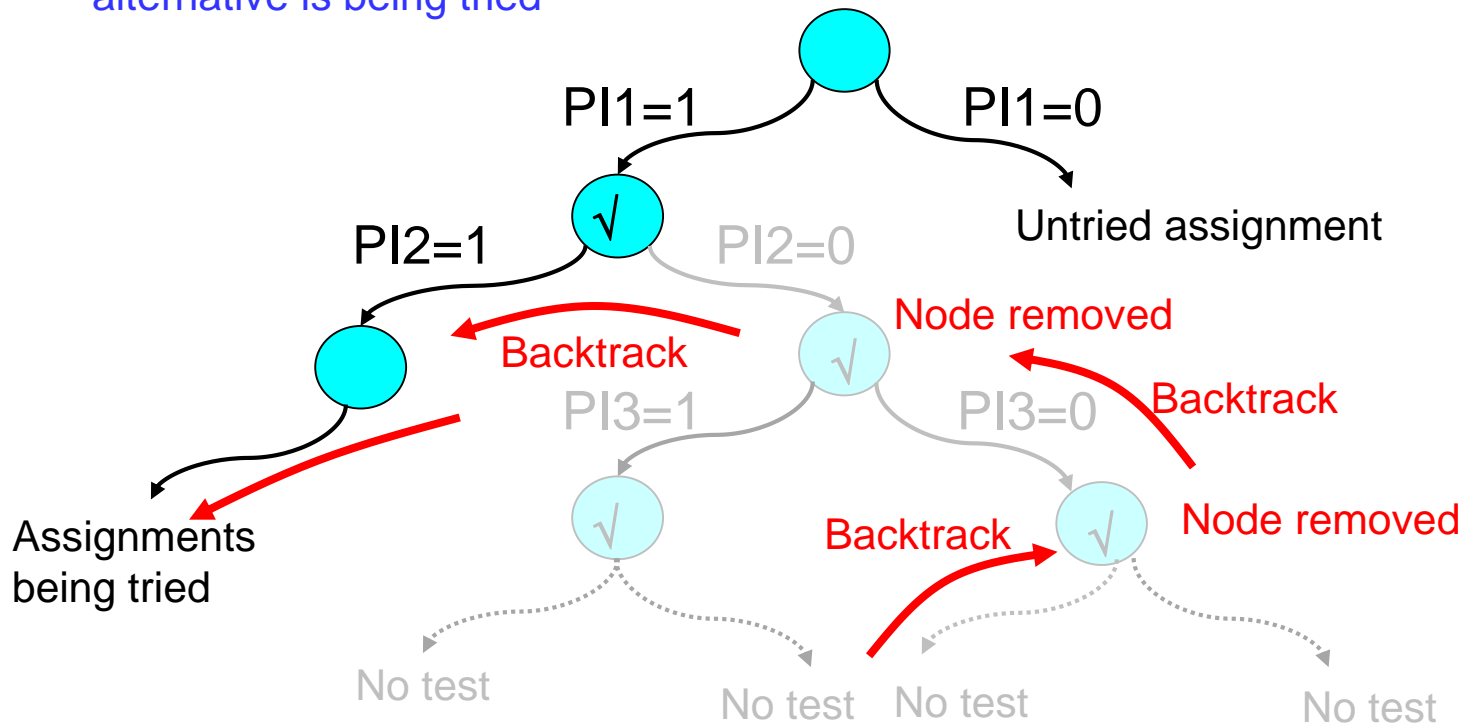
# Decision Tree of PODEM (5)

- **Branch and bound** search algorithm

- ## ◆ Prune $PI3=0$ subtree

- ## ◆ Prune $PI_2=0$ subtree

✓ : initial assignment rejected  
alternative is being tried



# PODEM: Summary

- **PODEM [Goel 1981]**
  - ◆ **Idea:**
    - \* assign PI, not internal nodes
    - \* forward implication only, no justification
  - ◆ **Heuristics**
    - \* (1) backtrace easy/hard input for decision/imply gate
    - \* (2) keep path inversion parity
    - \* (3) propagate along X-path
  - ◆ **Algorithms**
    - \* branch and bound search

# FFT

- **Q1: Is PODEM a complete ATPG algorithm?**
- **Q2: Why does PODEM have no justification?**
- **Q3: Please give examples where heuristic #1/#2 gives wrong guess**