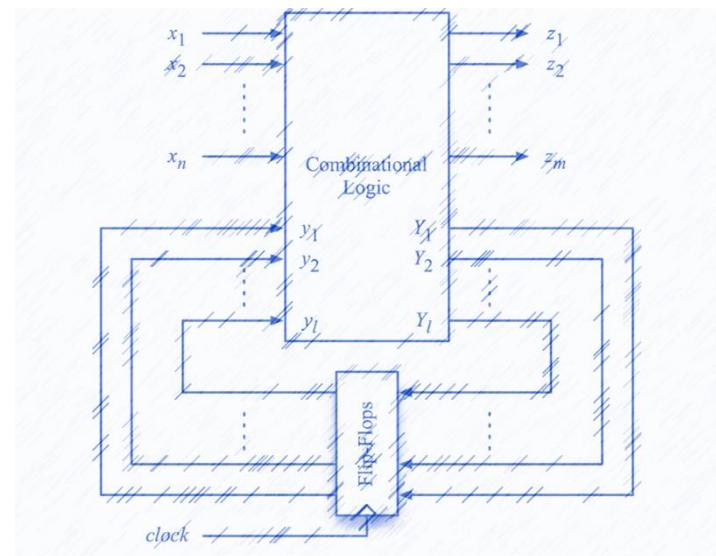


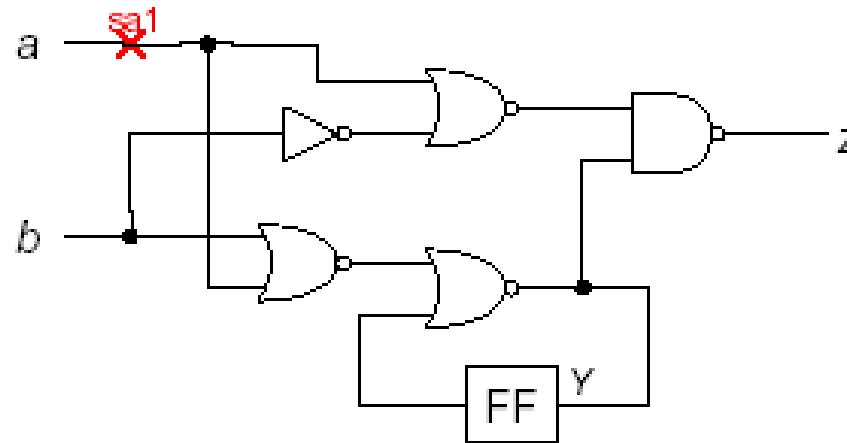
# Sequential ATPG

- Introduction
- Time-frame expansion methods
  - ◆ The Extended D-algorithm [Kubo 68]
  - ◆ 9-valued D algorithm [Muth 76]
  - ◆ EBT [Marlett 78], BACK [Cheng 88] \*
  - ◆ Summary
- Simulation-based methods\*
- Issues of Sequential ATPG\*
- Conclusions



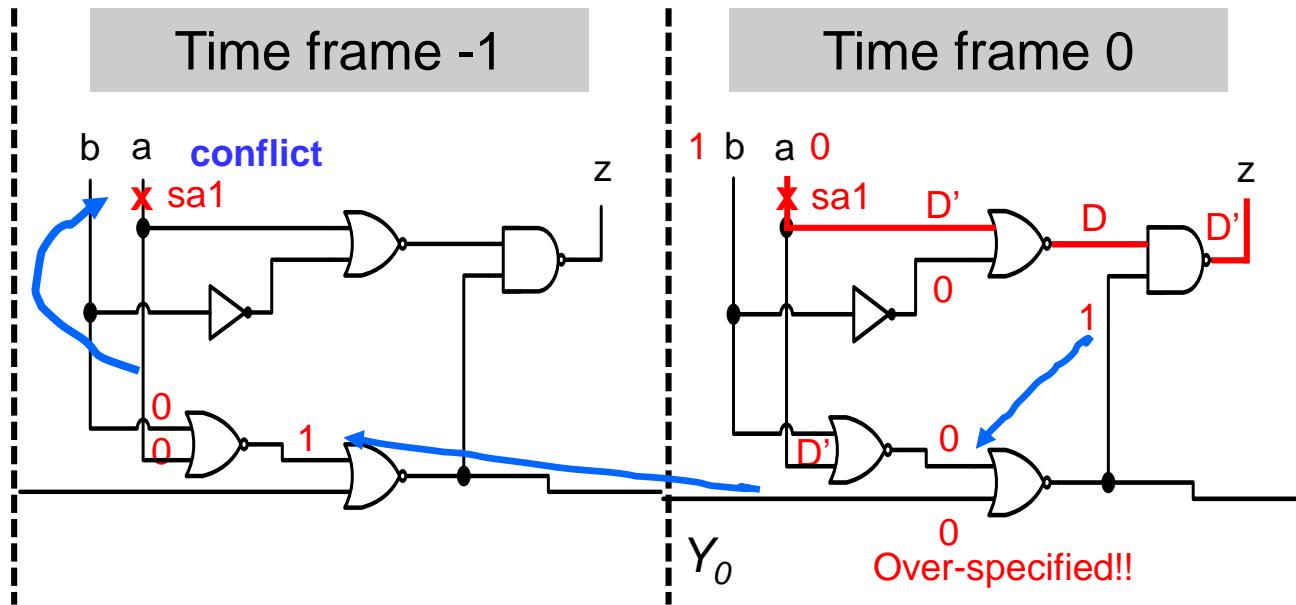
# Quiz

**Q: Given this test, can we detect the fault?**  
**ANS:**



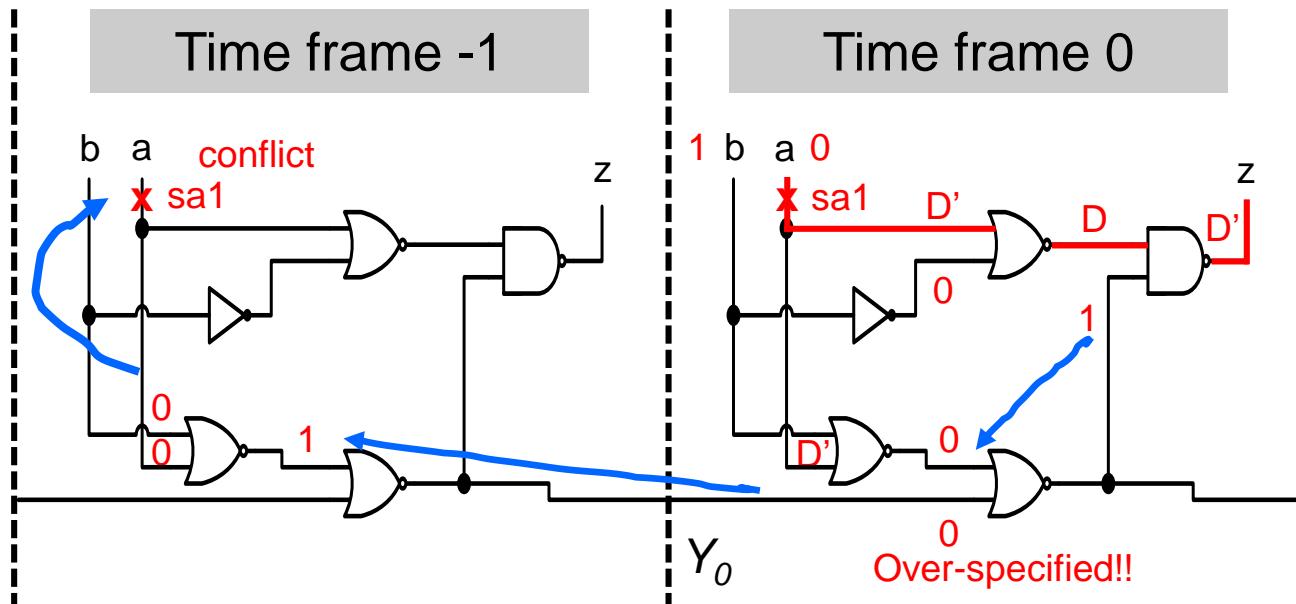
	$a$	$b$
$v_1$	0	0
$v_2$	0	1

# Extended D-algorithm Fails!



- Extended- D algorithm fails due to a conflict
  - ◆ Requires  $a=0$  in time frame -1, but SA1
  - ◆ Actually,  $Y_0$  is **over-specified** in 5-valued logic

# Why Fails?



- Traditional 5-valued logic (0/0, 1/1, x/x, 0/1, 1/0) is NOT sufficient
  - ◆ cannot express 1/x, 0/x, x/0, x/1

**Q: How many total cases do we need?**

**ANS:**

# Nine-valued D-algorithm [Muth 76]

- Solution: use **9-valued logic**, instead of 5-valued logic

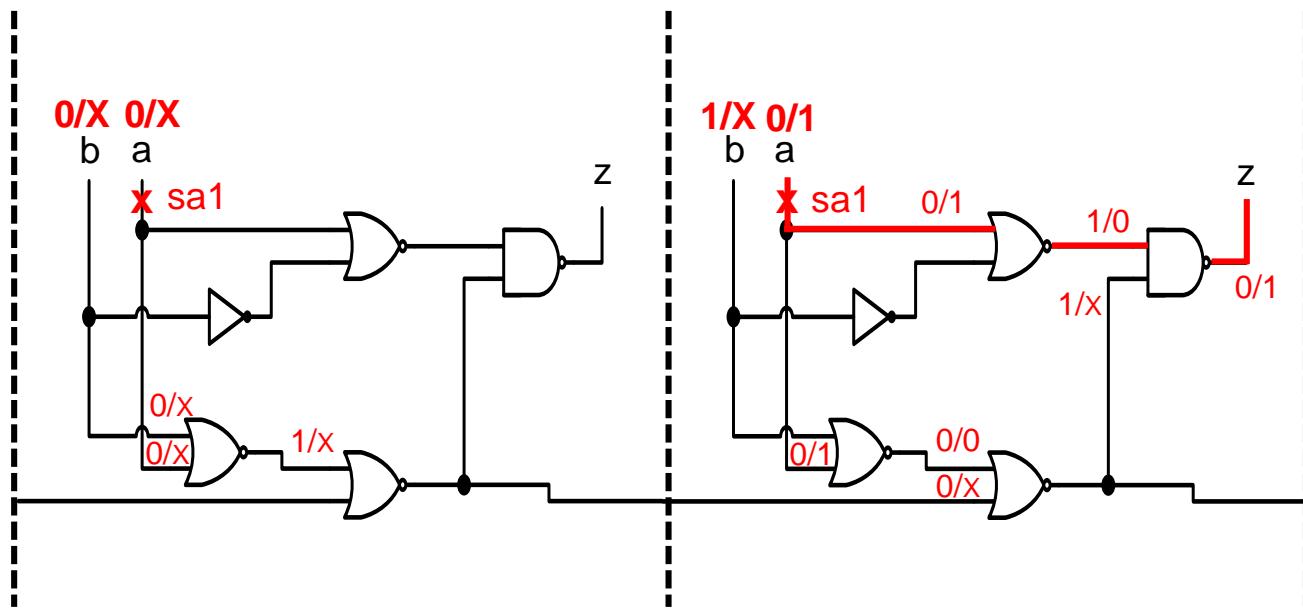
Symbol	Meaning	Roth's 5-valued logic		Muth's 9 valued logic	
		Fault-free	faulty	Fault-free	faulty
D	(1/0)	1	0	1	0
D'	(0/1)	0	1	0	1
0	(0/0)	0	0	0	0
1	(1/1)	1	1	1	1
X	(x/x)	X	X	X	X
G0	(0/x)	-	-	0	X
G1	(1/x)	-	-	1	X
F0	(x/0)	-	-	X	0
F1	(x/1)	-	-	X	1

# Nine-valued Truth Table

- Example of AND gate

AND	0	0/x	D'	x/0	x/x	x/1	D	1/x	1
0	0	0	0	0	0	0	0	0	0
0/x	0	0/x	0/x	0	0/x	0/x	0	0/x	0/x
D'	0	0/x	D'	0	0/x	D'	0	0/x	D'
x/0	0	0	0	x/0	x/0	x/0	x/0	x/0	x/0
x/x	0	0/x	0/x	x/0	x/x	x/x	x/0	x/x	x/x
x/1	0	0/x	D'	x/0	x/x	x/1	x/0	x/x	x/1
D	0	0	0	x/0	x/0	x/0	D	D	D
1/x	0	0/x	0/x	x/0	x/x	x/x	D	1/x	1/x
1	0	0/x	D'	x/0	x/x	x/1	D	1/x	1

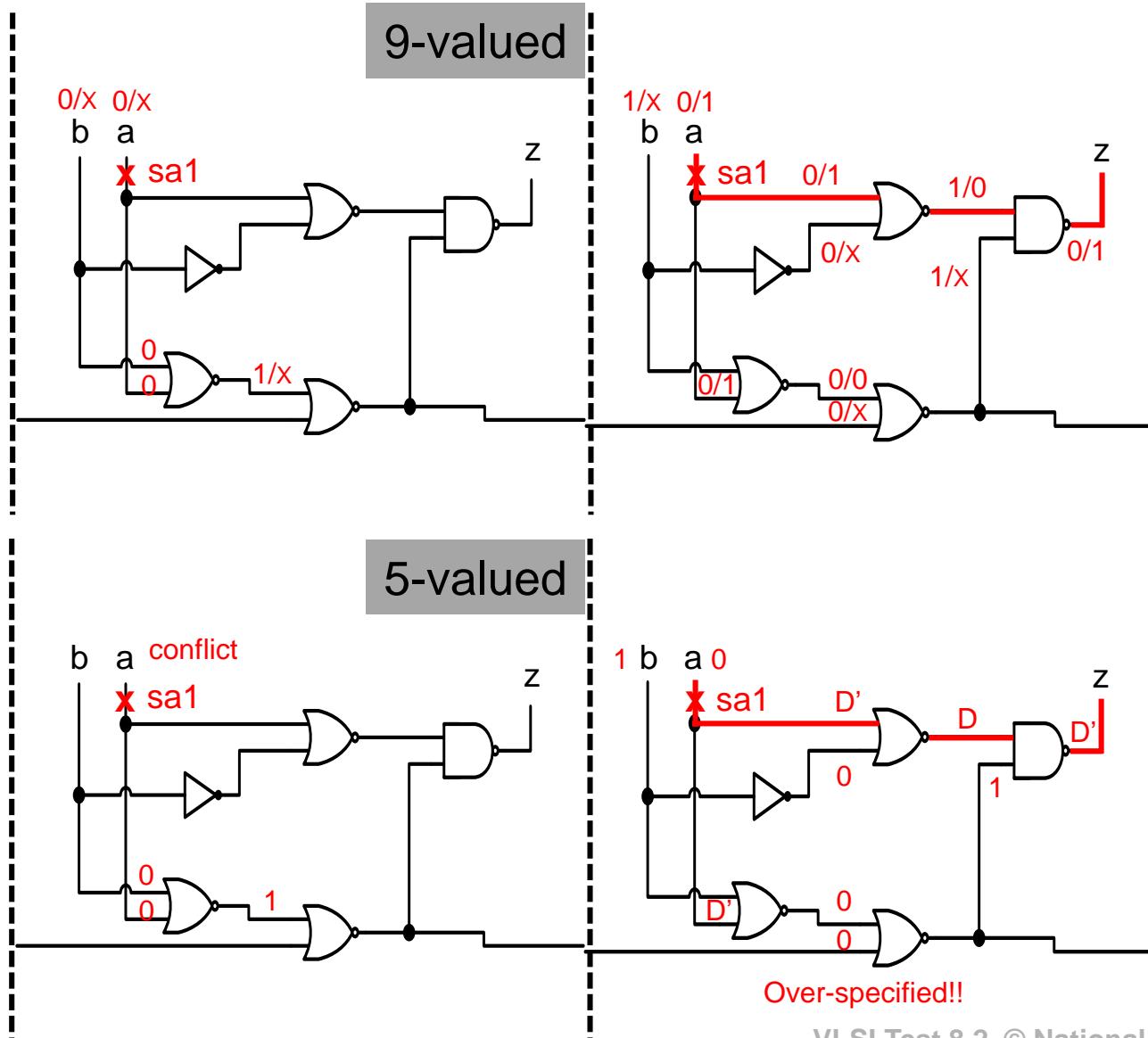
# Nine-Valued Test Generation



**Test pattern successfully generated**

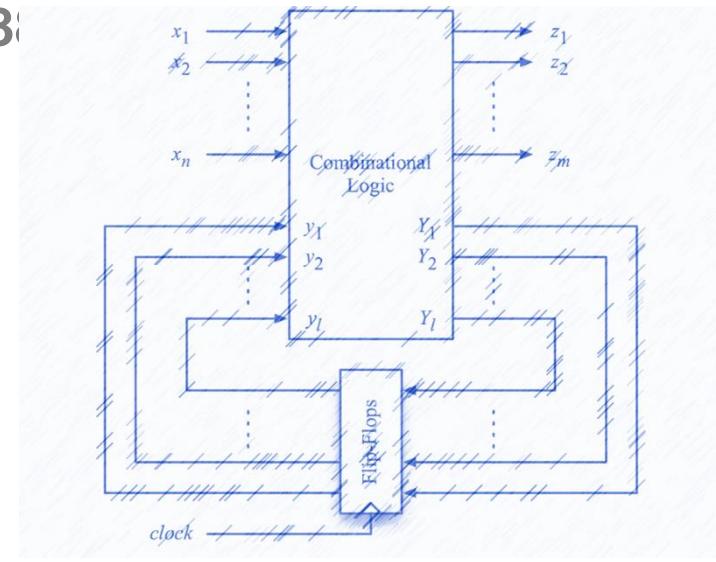
	$a$	$b$
$v_1$	0	0
$v_2$	0	1

# Comparison: 9 v.s. 5 valued



# Sequential ATPG

- Introduction
- Time-frame expansion methods
  - ◆ The Extended D-algorithm [Kubo 68]
  - ◆ 9-valued D algorithm [Muth 76]
    - express **all nine** possible logic states
    - avoid **over-specification**
  - ◆ EBT [Marlett 78], BACK [Cheng 81]
  - ◆ Summary
- Simulation-based methods\*
- Issues of Sequential ATPG\*
- Conclusions



# FFT

- Q1: Why NOT consider  $1/x$ ,  $0/x$ ,  $x/0$ ,  $x/1$  in combinational ATPG?
- Q2: Why NOT backtrace  $Y_{-1}$  one more time frame to the left?

