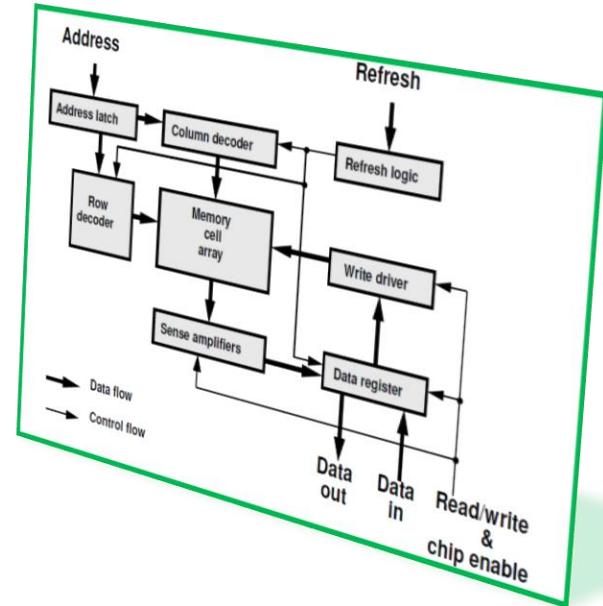


Memory Testing

- Introduction
- Memory Fault Model
- **Memory Test Algorithms**
 - ◆ Classical algorithms
 - ◆ March algorithms
- Memory Fault Simulation
- Memory Test Generation
- Memory BIST



Memory Test Algorithms

- A **Test algorithm** is a finite sequence of **test elements**
- A **test element** contains a number of
 1. **Memory operations**
 - * Read or Write
 2. **Data pattern** (aka. **data background**)
 - * Zero or One
 3. **Address sequence**
 - * Ascending or Descending
- **Test (time) Complexity** of test algorithm is expressed in terms of N
 - ◆ N = memory size = number of memory cells
 - ◆ Higher complexity means longer test time

Mem. Test Alg. is Different from ATPG Alg.

Memory Test (Time) Complexity

Size	N	$10N$	$N \lg N$	$N^{1.5}$	N^2
1M	0.01s	0.1s	0.2s	11s	3h
16M	0.16s	1.6s	3.9s	11m	33d
64M	0.66s	6.6s	17s	1.5h	1.43y
256M	2.62s	26s	1.23m	12h	23y
1G	10.5s	1.8m	5.3m	4d	366y
4G	42s	7m	22.4m	32d	59c
16G	2.8m	28m	1.6h	261d	936c

N = number of memory cells; 100MHz test speed

Linear Complexity Feasible for Production Tests

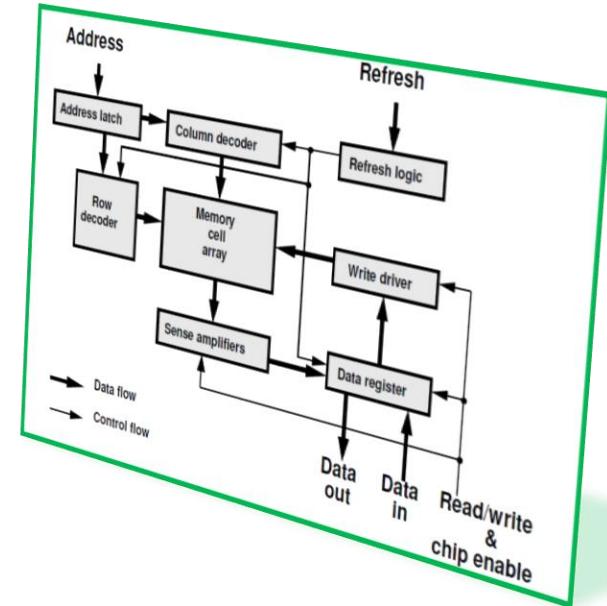
QUIZ

Q: Which one is correct about memory testing?

- A) Higher complexity means longer CPU time
- B) Test algorithm means a finite sequence of test elements, which contain: memory operation, data pattern, and address sequence
- C) ($N \log N$) Complexity is acceptable for large memory

Memory Testing

- Introduction
- Memory Fault Model
- **Memory Test Algorithms**
 - ◆ Classical algorithms
 - * MSCAN
 - * Checkerboard
 - * GALPAT
 - * Butterfly
 - ◆ March algorithms
- Memory Fault Simulation
- Memory Test Generation
- Memory BIST

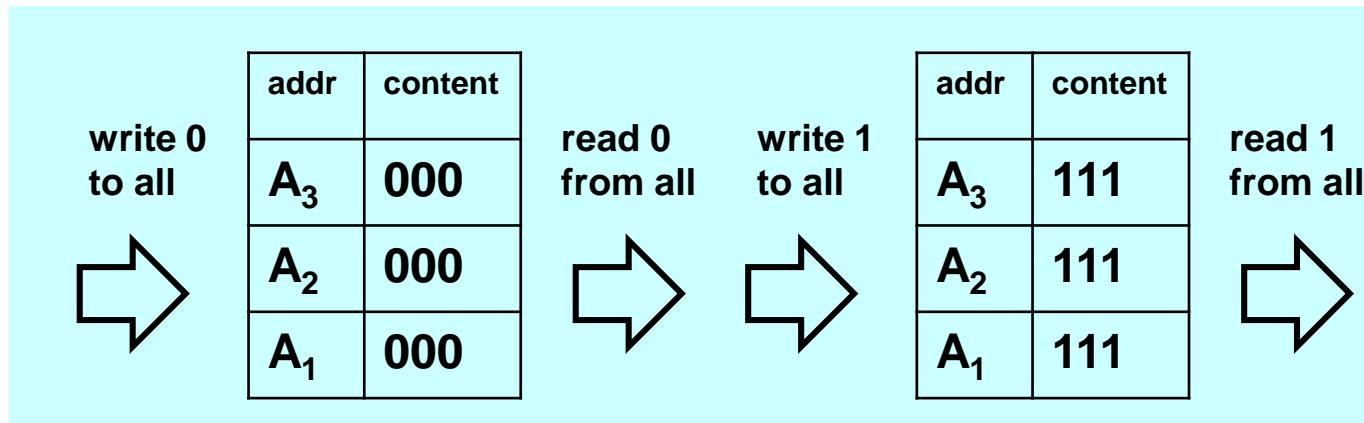


MSCAN

- aka. **zero-one algorithm**
- Detects all **SAF**
- Detects $\langle \uparrow/0 \rangle$ **TF**, not $\langle \downarrow/1 \rangle$
- Does NOT detect all **AF, CF**
- Complexity is **$4N$**
 - ◆ 4 operations each cell

MSCAN

1. **Write zero to every cell**
2. **Read zero from every cell**
3. **Write one to every cell**
4. **Read one from every cell**



Checkerboard

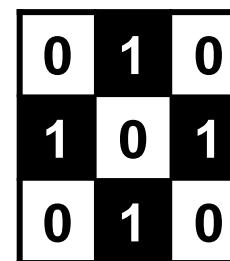
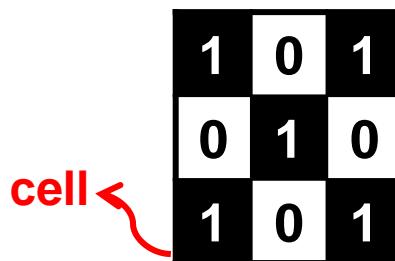
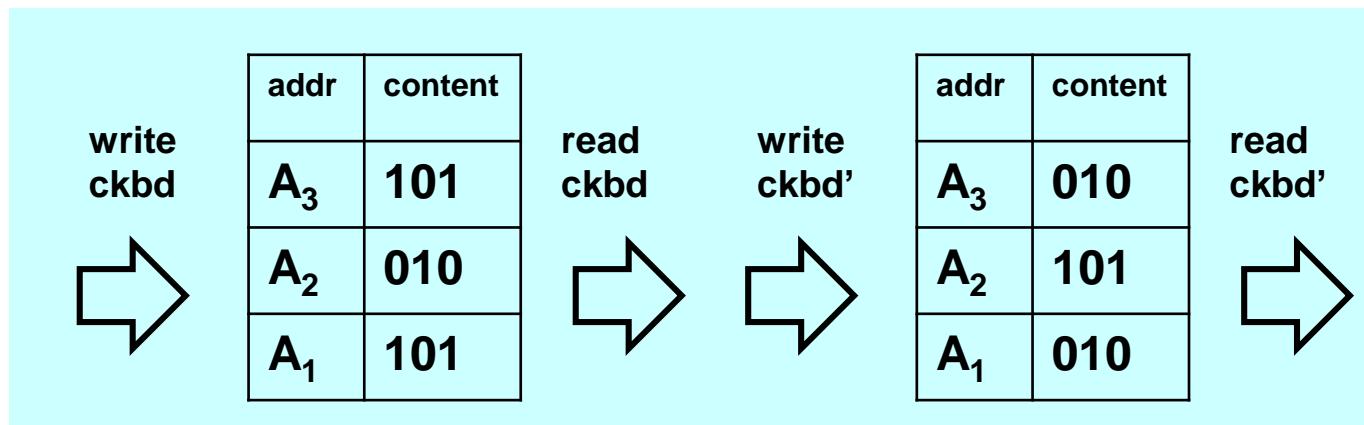
- Detects all **SAF** and half **TF**
- Does NOT detect all AF, CF
- Complexity is **4N**

Same as MSCAN but
Detects *Bridging Fault*

CHECKERBOARD

1. Write **chbd pattern** to all cells
2. **Read ckbd pattern from all cells**
3. Write **ckbd' pattern** to all cells
4. **Read ckbd' pattern from all cells**

ckbd means 01 alternating
ckbd' is complement of ckbd



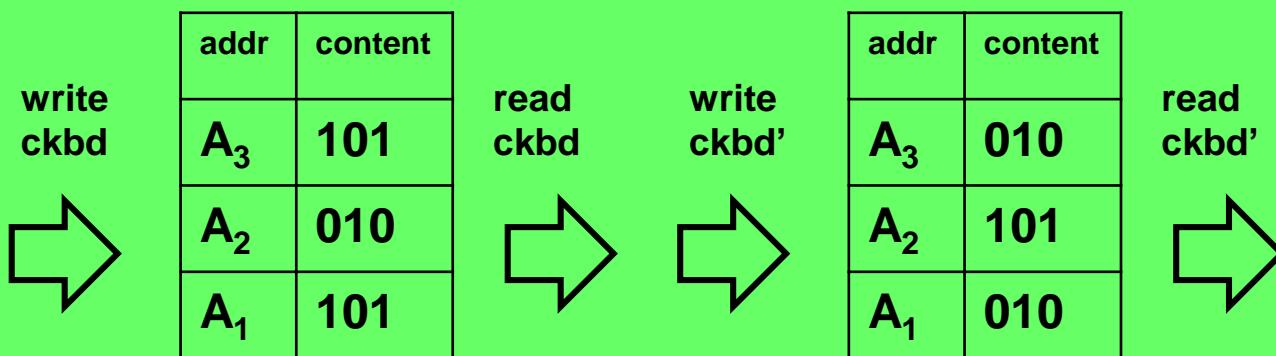
QUIZ

Q1: Can checkerboard detect OR-type AF between A₁ and A₂?

ANS:

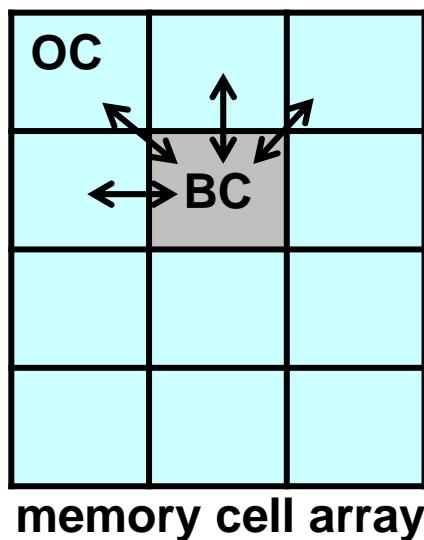
Q2: Can checkerboard detect OR-type AF between A₁ and A₃?

ANS:



Galloping Test (GALPAT)

- Aka. *Ping-pong test*
- Detects all SAF, TF
- Detects CF, and AF
- Complexity is $4N^2$
 - ◆ Line 2: $2N^2$
 - ◆ Line 4: $2N^2$



GALPAT

1. Write background 0 to all cells;
2. For BaseCell = 0 to N-1
 Complement BC;
 For OtherCell = 0 to N-1, OC != BC;
 Read BC; Read OC;
 Complement BC;
3. Write background 1 to all cells;
4. Repeat Step 2;

Too Long! Only for Characterization

QUIZ

Suppose BC is aggressor and OC is victim.

Q1: Can we detect $CF_{st} <1; 0/1>$?

Q2: Can we detect $CF_{id} <\uparrow; 0/1>$?

Q3: Can we detect $CF_{in} <\uparrow ; \forall/\downarrow >$?

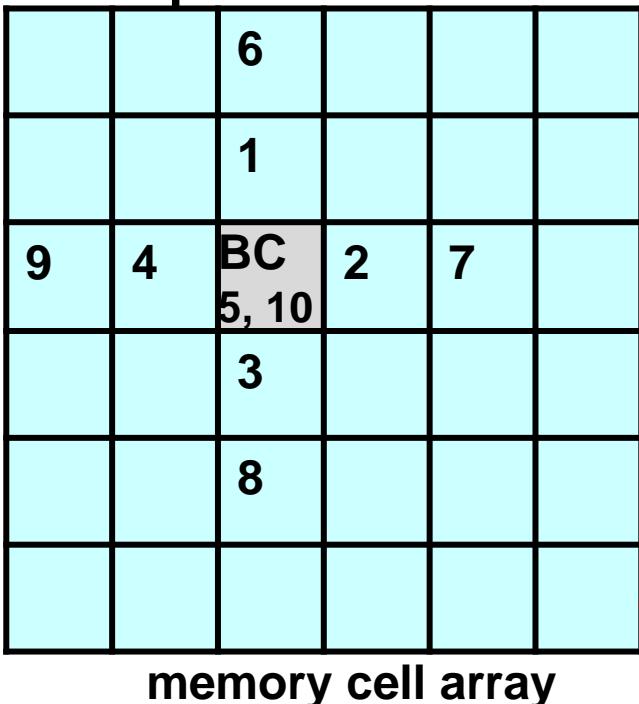
0 OC	0	0
0	BC $0 \rightarrow 1 \rightarrow 0$	0
0	0	0
0	0	0

GALPAT

1. Write background 0 to all cells;
2. For BaseCell = 0 to N-1
 Complement BC;
 For OtherCell = 0 to N-1, OC != BC;
 Read BC; Read OC;
 Complement BC;
3. Write background 1 to all cells;
4. Repeat Step 2;

Butterfly Algorithm

- Detects SAF and TF
- Does not detect all CF, AF
- Complexity is $10 N \log N$
 - ◆ 5 reads for each $dist$
 - ◆ $dist$ doubles each loop
 - ◆ Repeated in line 4



```
BUTTERFLY // given MAXDIST < 0.5 col/row size
1. Write background 0;
2. For BaseCell = 0 to N-1
   Complement BC; dist = 1;
   While dist ≤ MAXDIST
      Read cell @ dist north from BC;
      Read cell @ dist east from BC;
      Read cell @ dist south from BC;
      Read cell @ dist west from BC;
      Read BC;   dist = dist * 2;
   Complement BC;
3. Write background 1;
4. Repeat Step 2;
```

Summary

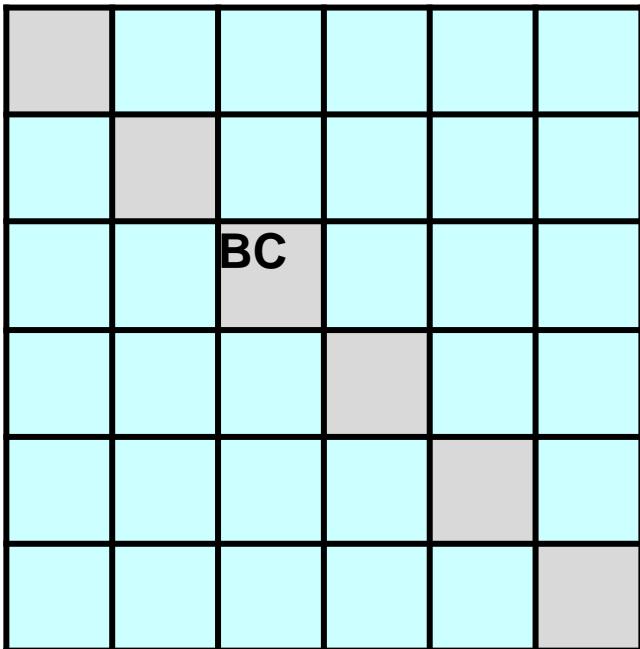
- **Test algorithm** is a finite sequence of **test elements**
 - ◆ which are: **Memory operation, Data pattern, Address sequence**
 - ◆ **Test complexity** means **test time** (not CPU time)
- Four classical test algorithms
 - ◆ MSCAN and Checkerboard's **fault coverage NOT good**
 - ◆ GALPAT and Butterfly are **too slow**
- Need **linear-time** test algorithms with good fault coverage
 - ◆ ***March test algorithms*** (see 16.3)

	SAF	AF	TF	CF	Complexity
MSCAN	D	-	-	-	$4N$
Checkerboard	D	-	-	-	$4N$
GALPAT	D	D	D	D	$4N^2$
Butterfly	D	-	D	-	$10 N \log N$

D: all detected;
- : not all detected

FFT

- Q: In GALPAT, choosing all cells as base cell is slow. Can we choose only cells on the diagonal line as BC? What is complexity?
- Q: Why do we choose cells in the same column and row of BC in Butterfly test?



GALPAT-DIAGONAL

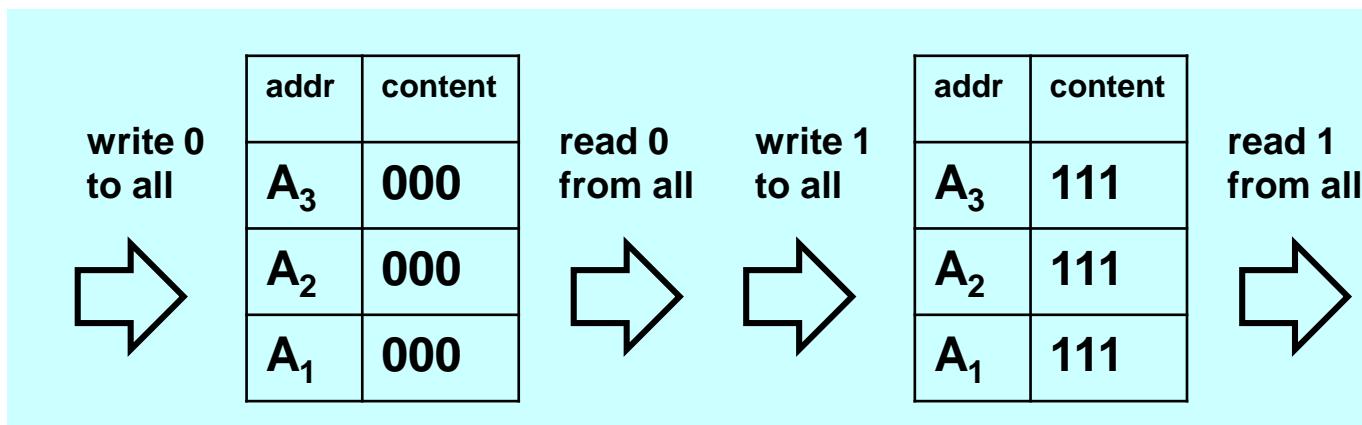
1. Write background 0 to all cells;
2. For BaseCell = 0 to N-1
 // BC must be on diagonal line
 Complement BC;
 For OtherCell = 0 to N-1, OC != BC;
 Read BC; Read OC;
 Complement BC;
3. Write background 1 to all cells;
4. Repeat Step 2;

MSCAN [Breuer & Friedman 1976]

- aka. **zero-one algorithm**
- Detects all **SAF**
- Detects $\uparrow/0$ **TF**, not $\downarrow/1$
- Does NOT detect all **AF**, **CF**
- Complexity is **4N**

MSCAN

1. **Write zero to every cell**
2. **Read zero from every cell**
3. **Write one to every cell**
4. **Read one from every cell**



	SAF	AF	TF	CF	Complexity
MSCAN	D	-	1/2	-	4N

D: all detected
- : not all detected