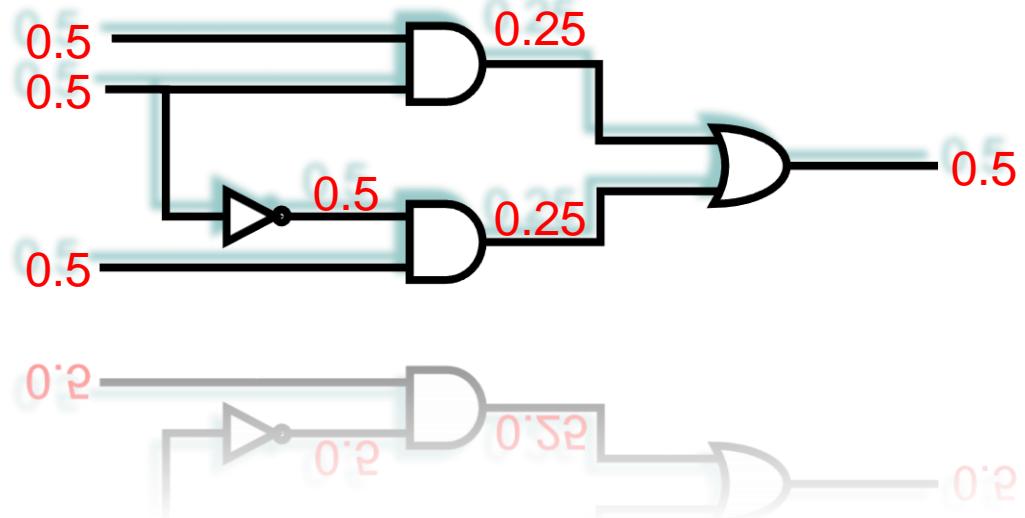


# Testability Measure

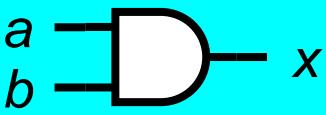
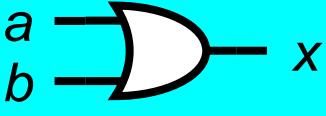
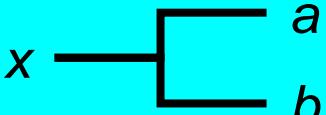
- Introduction
- SCOAP (1979)
- **COP (1984)**
- High-level testability measures
- Conclusion



# COP

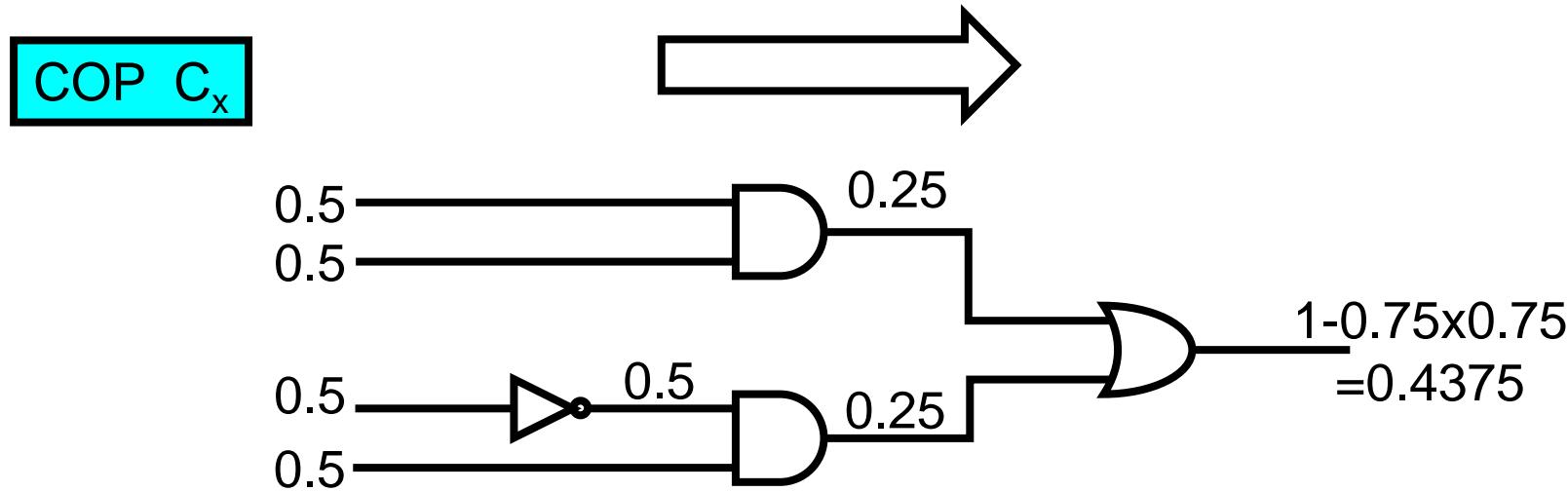
- **Signal probability of  $x$  = probability of  $x$  being logic 1**
  - ◆ Actual signal probability requires exhaustive simulation
  - ◆ Hard to obtain in practice
- **COP = Controllability/Observability Program [Brglez 84]**
  - ◆ Fast algorithm to estimate signal probability
  - ◆  $C_x$  = estimated prob( $x = 1$ )
  - ◆  $1-C_x$  = estimated prob( $x = 0$ )
  - ◆  $O_x$  = estimated probability of *fault effect* in  $x$  being observed at PO
- $C_x$  and  $O_x$  are numbers between 0 and 1
  - ◆ *Larger number* means *easier* to control or observe
- Assumptions
  - ◆ 1. Ignore fanout reconvergence for fast run time
  - ◆ 2. PI are independent random numbers:  $\frac{1}{2}$  zero and  $\frac{1}{2}$  one

# COP

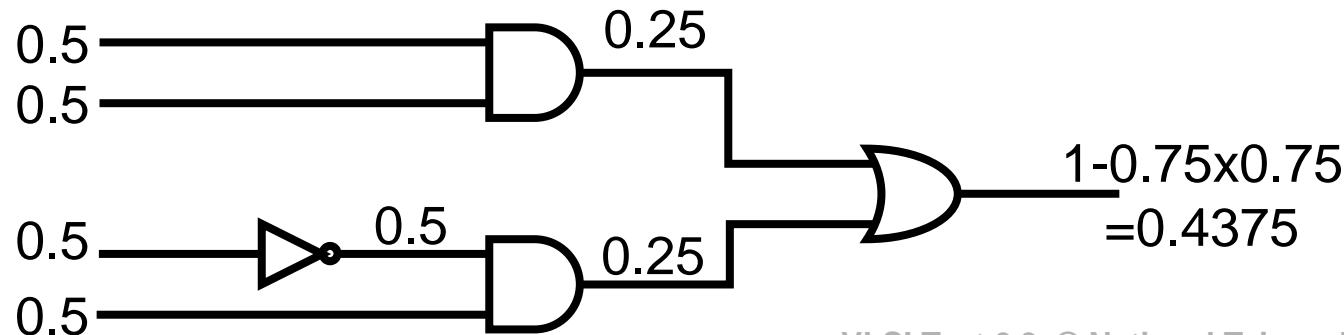
	$C_x$	$O_a$
$x = PI$	0.5	
$x = PO$		0.5
	$C_x = C_a \times C_b$	$O_a = O_x \times C_b$
	$C_x = 1 - (1 - C_a) \times (1 - C_b)$	$O_a = O_x \times (1 - C_b)$
	$C_x = C_a = C_b$	$O_x = 1 - (1 - O_a) \times (1 - O_b)$

# Example – Controllability

- Calculate from PI to PO
- **Fanout-free circuit, COP = actual signal probability**

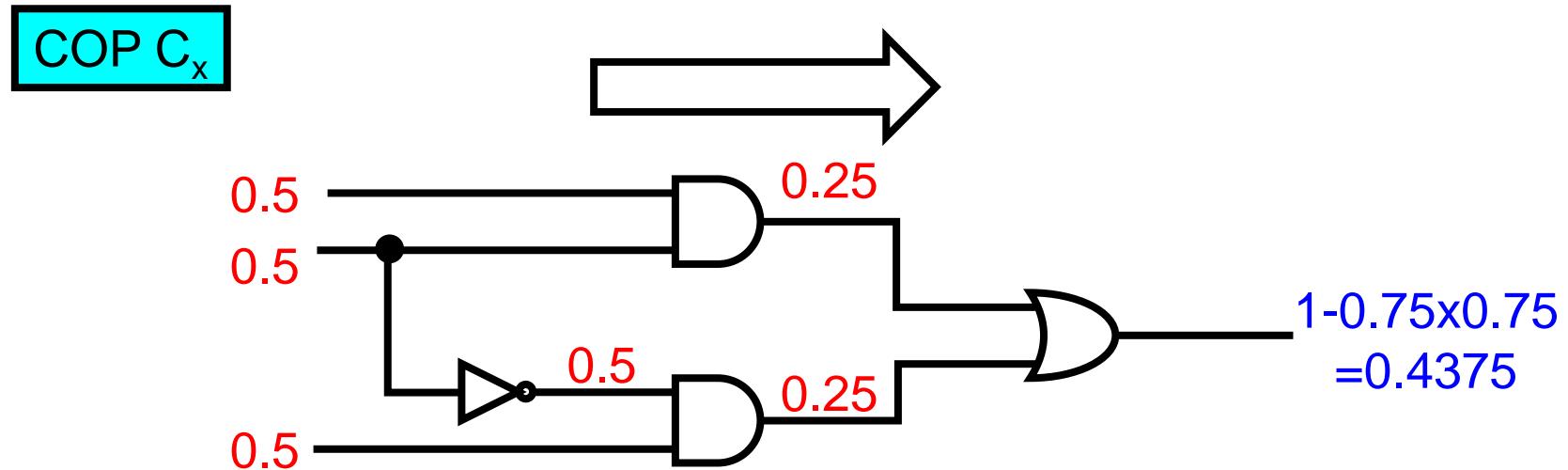


**Actual signal probability**

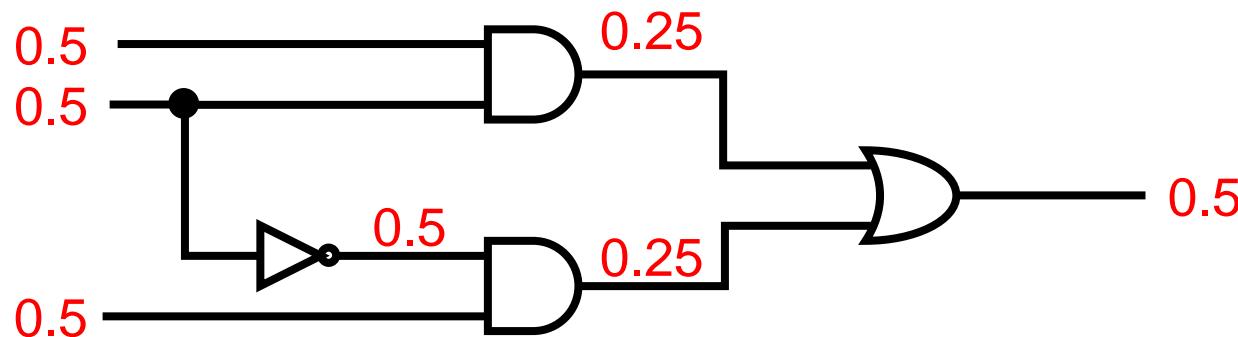


# Example (2) – Controllability

- When fanouts reconverge, COP  $\neq$  actual signal probability

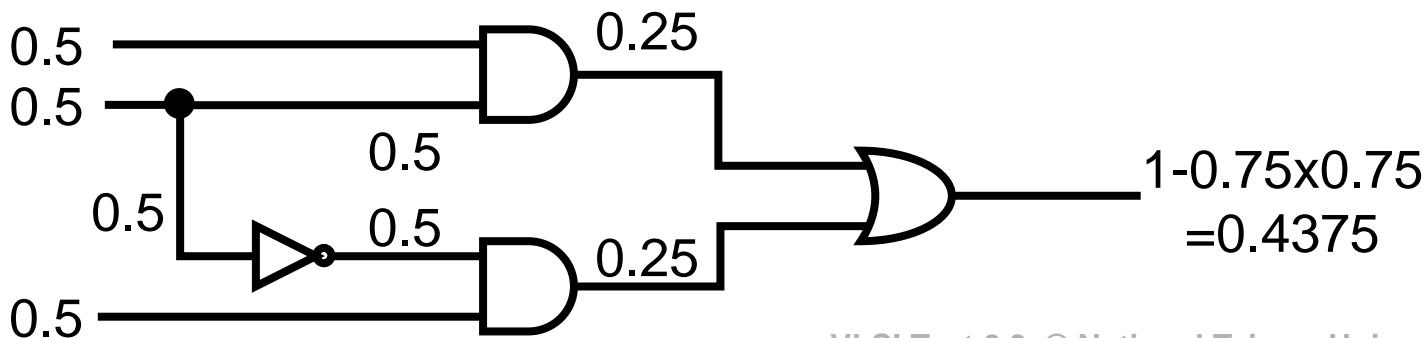
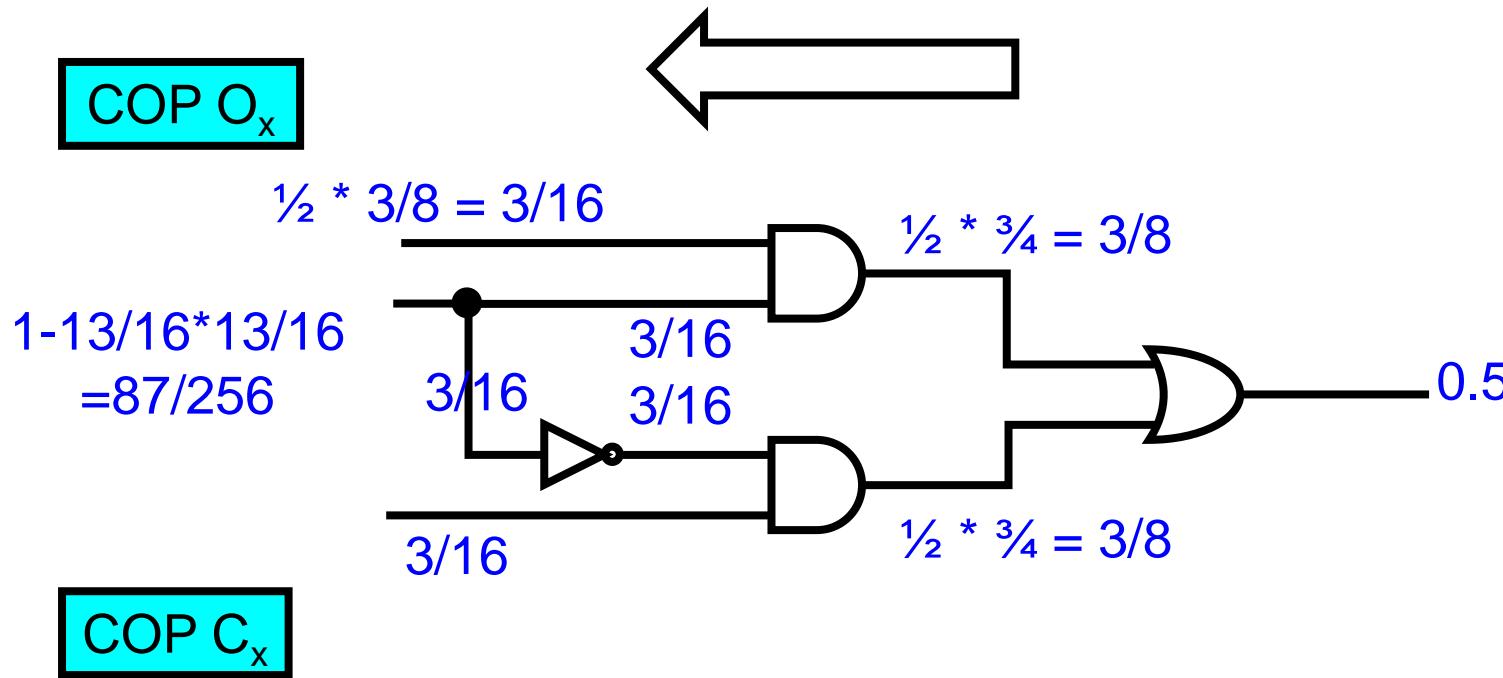


Actual signal probability



# Example (2) – Observability

- Calculate from PO to PI

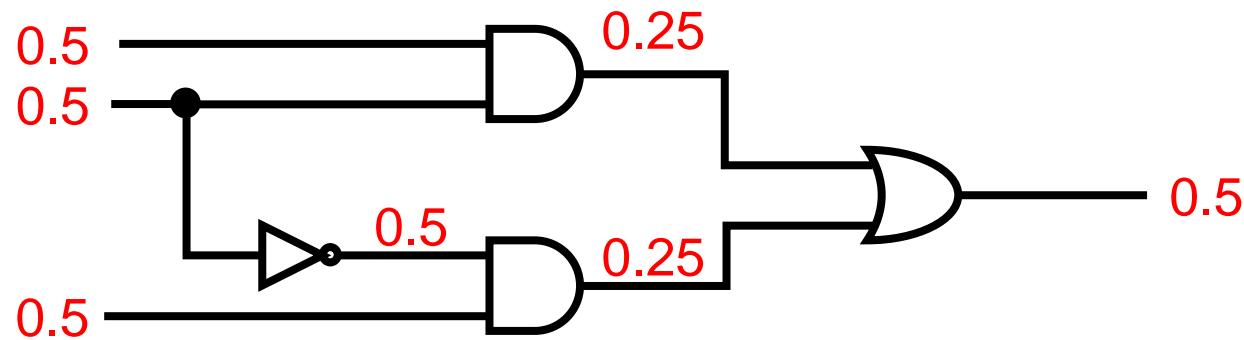


# Quiz

**Q: verify actual signal probability by exhaustive test patterns**

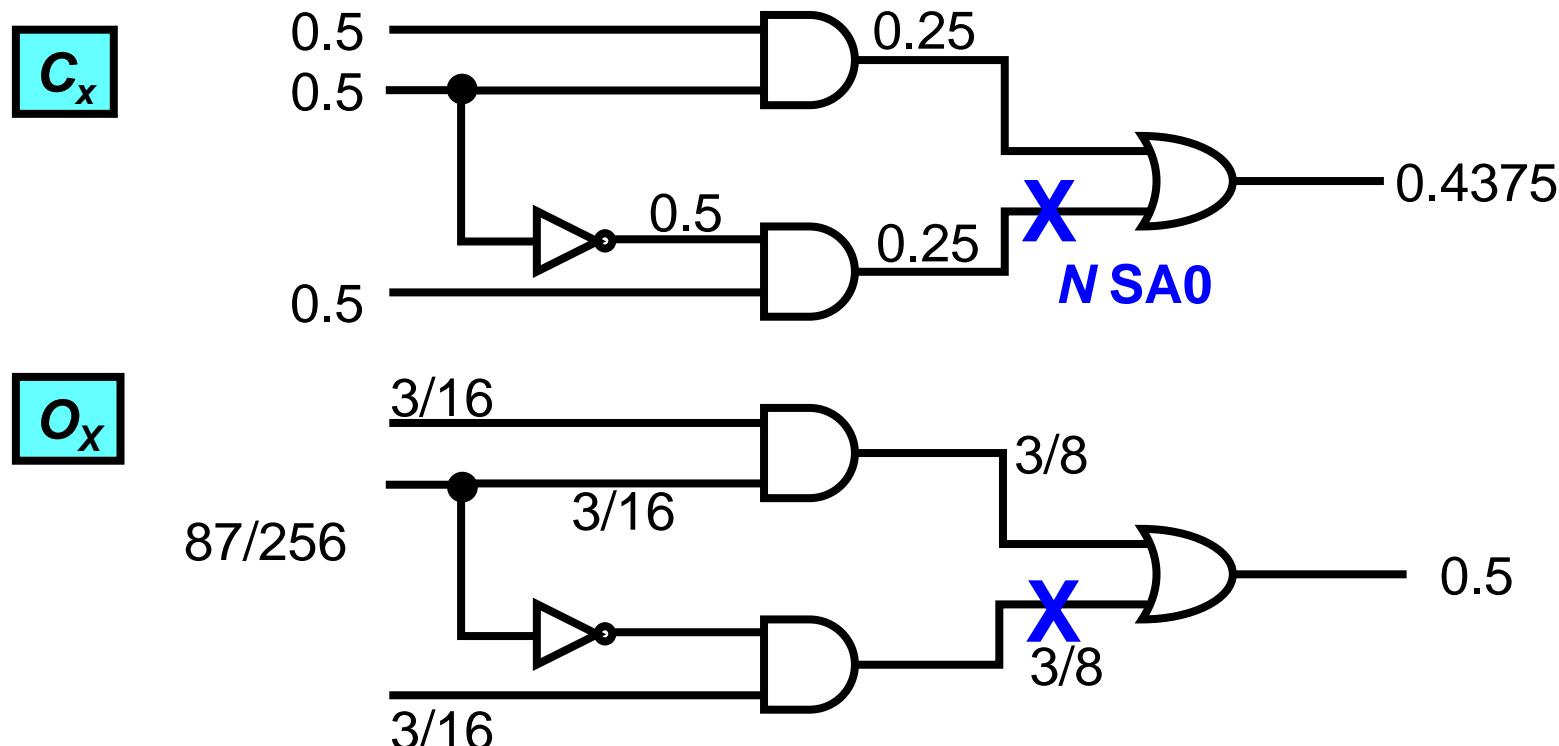
Actual signal probability

input	output
000	
001	
010	
011	
100	
101	
110	
111	



# Detection Probability, DP

- $DP_f$  = Probability of detecting a fault  $f$ 
  - ◆  $DP_{NSA0} = C_N \times O_N$
  - ◆  $DP_{NSA1} = (1-C_N) \times O_N$
- Larger  $DP_f$  means easier to detect fault  $f$
- Example:  $DP_{NSA0} = 1/4 \times 3/8 = 3/32$



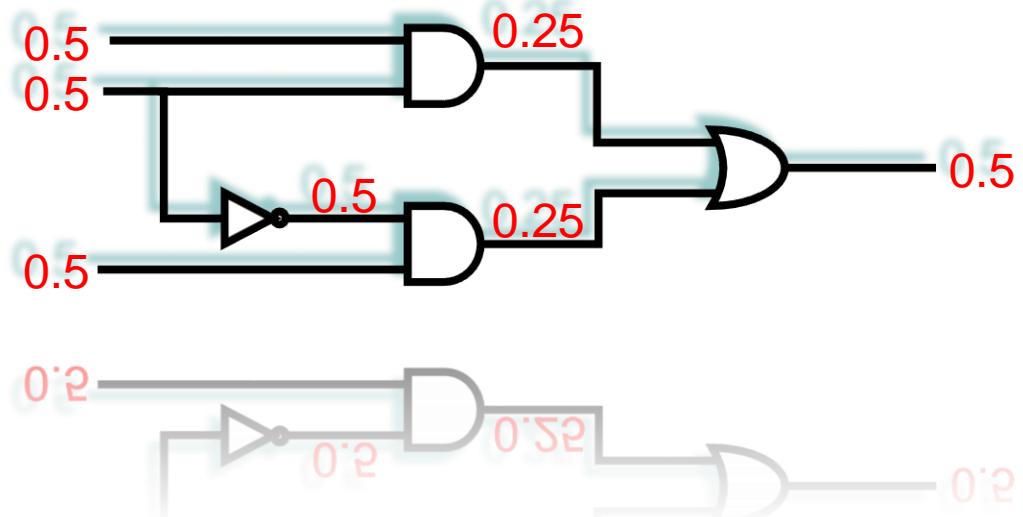
# Random Pattern Resistant Faults

- RPRF = Faults that are difficult to be tested by random patterns
  - ◆ *Low detectability*
  - ◆ aka. *Hard-to-detect faults, difficult faults*
- Example:
  - ◆ stuck-at-0 fault at an  $n$ -input AND gate output
  - ◆ Need test pattern  $(1,1,1,\dots,1)$
  - ◆ Assume equal signal probability of 0.5 at each input
    - \*  $C_x = 0.5^n$
- Test generation for RPRF is difficult
  - ◆ Solutions:
    - \* 1. Insert test points (See DFT lecture)
    - \* 2. Weighted random patterns (see BIST lecture)

# Summary

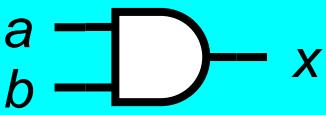
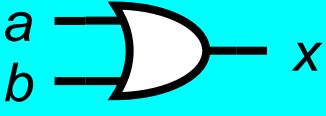
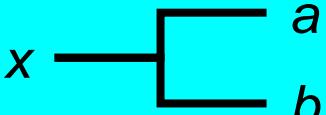
- **COP**

- $C_x = \text{estimated prob}(x = 1)$
- $1-C_x = \text{estimate prob}(x = 0)$
- $O_x = \text{estimated probability of } \textit{fault effect} \text{ in } x \text{ being observed}$
- $\text{COP} \neq \text{actual signal probability}$  because fanout reconvergence



# FFT

- Q: Why observability at PO is 0.5, not 1?

	$C_x$	$O_a$
$x = PI$	0.5	
$x = PO$		0.5
	$C_x = C_a \times C_b$	$O_a = O_x \times C_b$
	$C_x = 1 - (1 - C_a) \times (1 - C_b)$	$O_a = O_x \times (1 - C_b)$
	$C_x = C_a = C_b$	$O_x = 1 - (1 - O_a) \times (1 - O_b)$