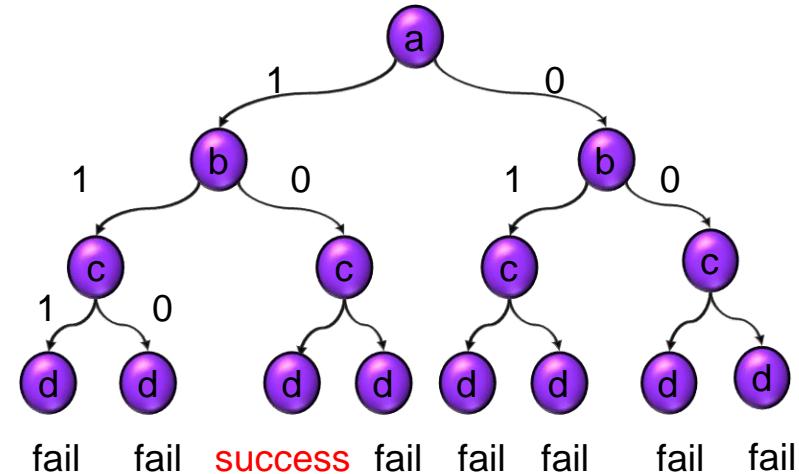


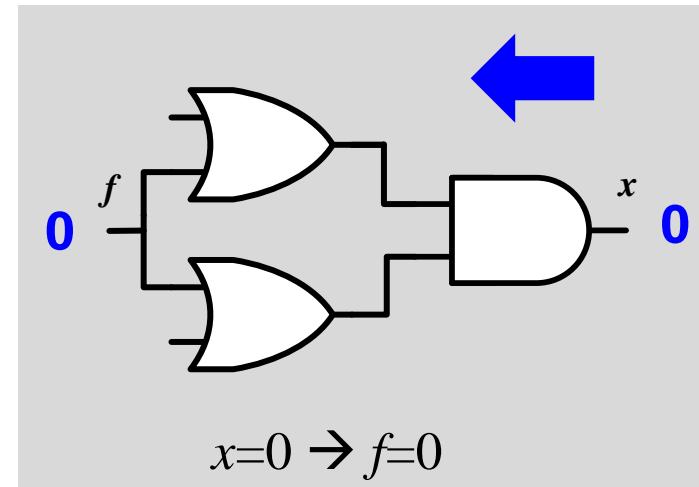
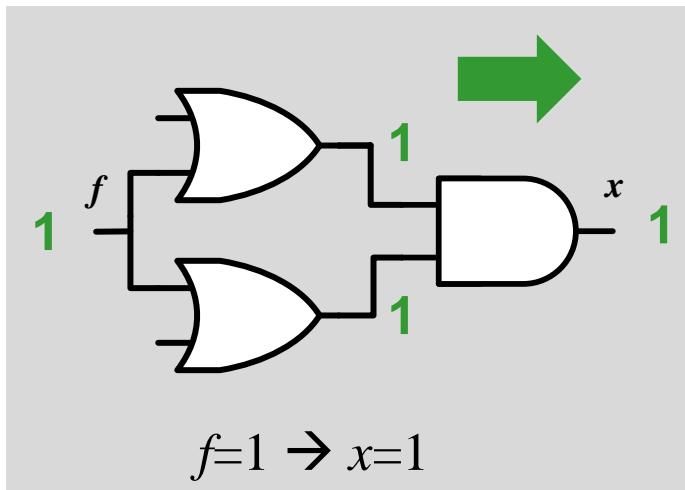
# Combinational ATPG

- Introduction
- Deterministic Test Pattern Generation
- Acceleration techniques
  - ◆ Learning [Schulz 1988]
  - ◆ Redundant fault identification [Iyer 1996]
- Concluding Remarks



# Learning

- **Learning** memorizes circuit information to speed up test generation
  - ◆ **Static learning:** performed in preprocess. no test pattern required.
  - ◆ **Dynamic learning:** performed in test generation (not in lecture)
- Static learning example: WWW Fig 4.22
  - ◆ Set  $f=1$ , implies  $x=1$
  - ◆ So we learn  $x=0$ , implies  $f=0$

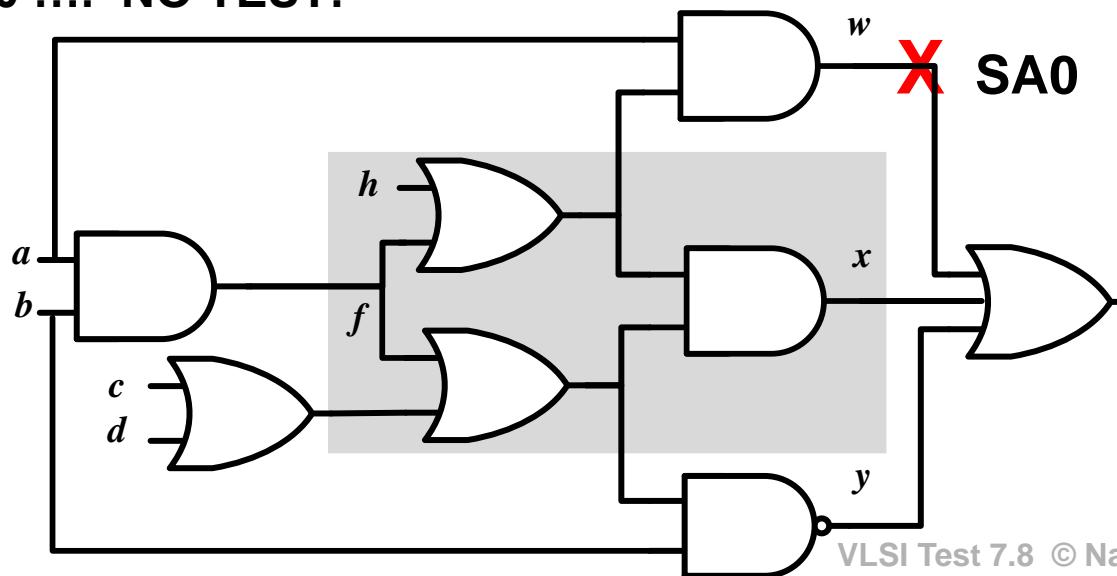


**Contrapositive Law: If  $p \rightarrow q$  then  $q' \rightarrow p'$**

# Learning Reduces Backtracks (1)

## without learning

- Obj : w=1. assign h=1, a=1
- Obj : x=0. assign c=0, d=0, b=0
  - ♦ y=1 conflict!
- backtrack b=1
  - ♦ x=1 conflict!
- backtrack d=1, conflict!
- backtrack c=1, conflict!
- backtrack a=0, conflict!
- backtrack h=0 .... NO TEST!



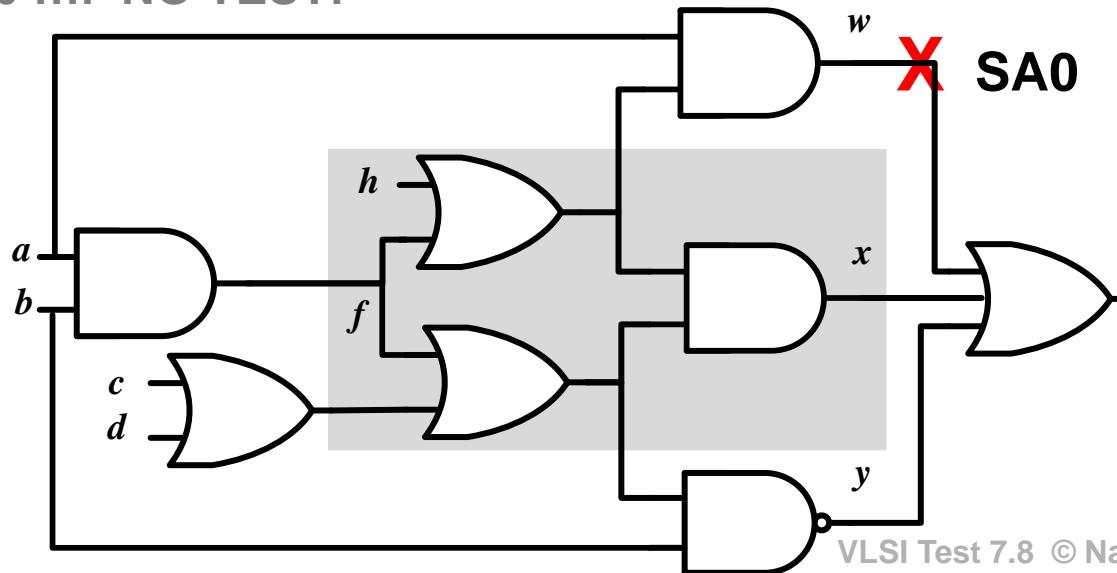
# Learning Reduces Backtracks (2)

## without learning

- Obj : w=1. assign h=1, a=1
- Obj : x=0. assign c=0, d=0, b=0
  - ◆ y=1 conflict!
- backtrack b=1
  - ◆ x=1 conflict!
- **backtrack d=1, conflict!**
- **backtrack c=1, conflict!**
- backtrack a=0, conflict!
- backtrack h=0 .... NO TEST!

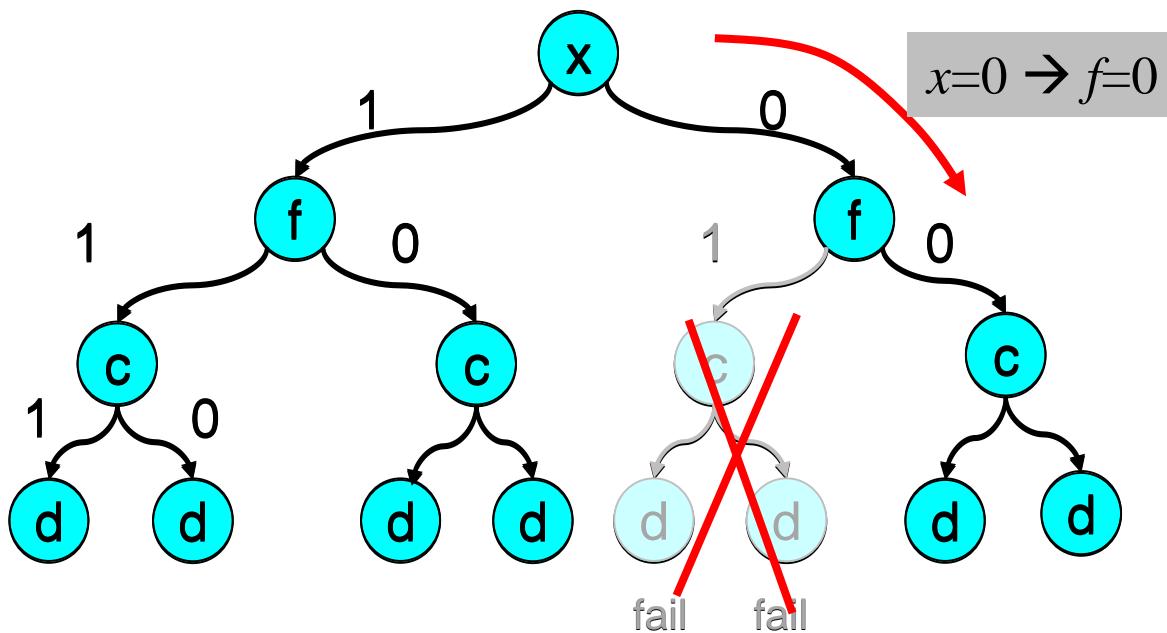
## with learning

- Obj : w=1. assign h=1, a=1
- Obj : **x=0 → f=0**. assign b=0
  - ◆ y=1 conflict!
- **backtrack b=1**
  - ◆ x=1 conflict!
- **backtrack a=0, conflict!**
- **backtrack h=0 ... NO TEST!**



# Learning Speedup Decision

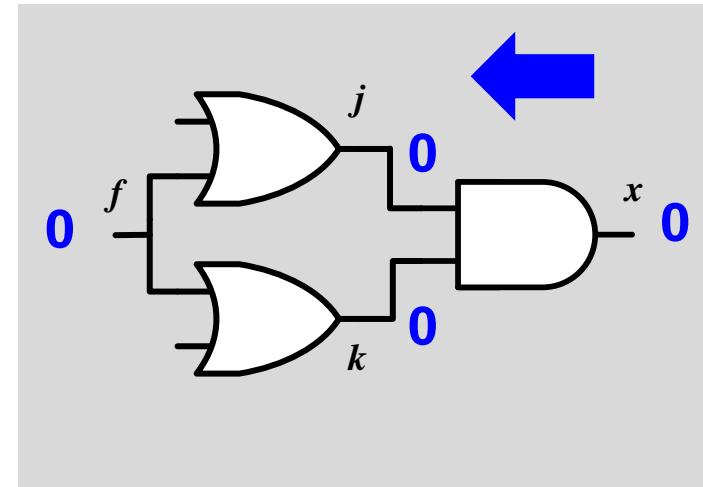
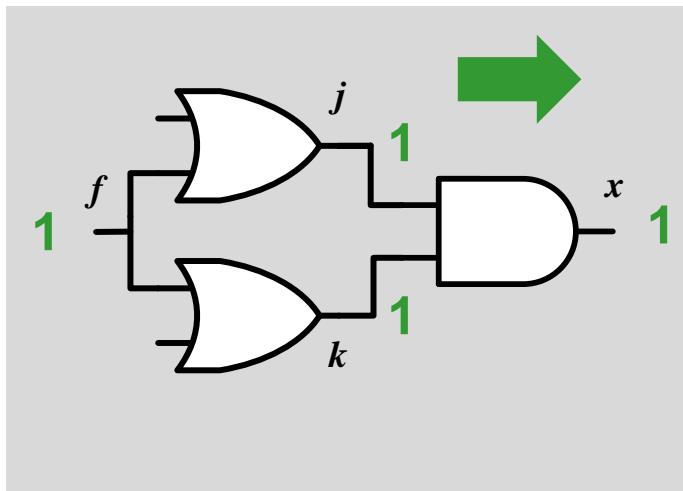
- Learning helps to
  - ◆ 1. Prune impossible sub-trees ASAP
  - ◆ 2. Find necessary assignments ASAP



Learning Trade-off Memory for Run Time

# But ... Too Many to Learn!

- $f=1 \rightarrow j=1$  so  $j=0 \rightarrow f=0$ 
  - ◆ Only local implication. not worth learning
- $f=1 \rightarrow k=1$  so  $k=0 \rightarrow f=0$ 
  - ◆ Only local implication. not worth learning
- $f=1 \rightarrow x=1$  so  $x=0 \rightarrow f=0$ 
  - ◆ global implication. **worth learning!**



**Which Are Worth Learning?**

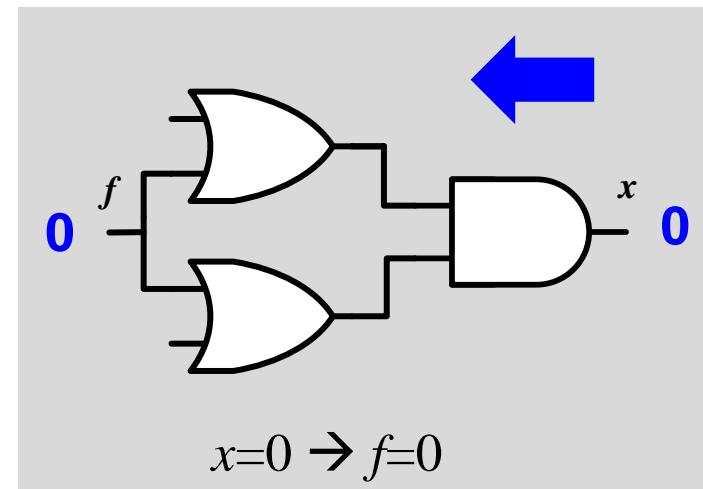
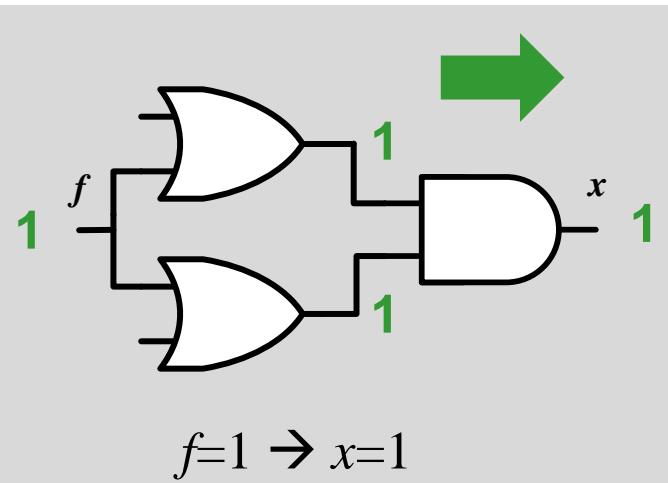
# SOCRATES Algorithm [Schulz 1988]

- In preprocess phase, sets **all signals** to 0 and 1
  - ◆ Discovers what other signals are implies
  - ◆ **Two criteria** to select **useful learning**

analyze\_results ( $f$ )

for every signal  $x$  whose value  $\neq$  unknown  
if (all gate inputs to  $x$  are **non-controlling**)  
& (there is **forward path** from  $f$  to  $x$ )  
save learning result ( $x=v_x \rightarrow f=v_f$ )

```
static_learning()  
for every signal  $f$   
    assign_value ( $f, 0$ )  
    implication()  
    analyze_results( $f$ )  
    assign_value ( $f, 1$ )  
    implication()  
    analyze_results( $f$ )
```



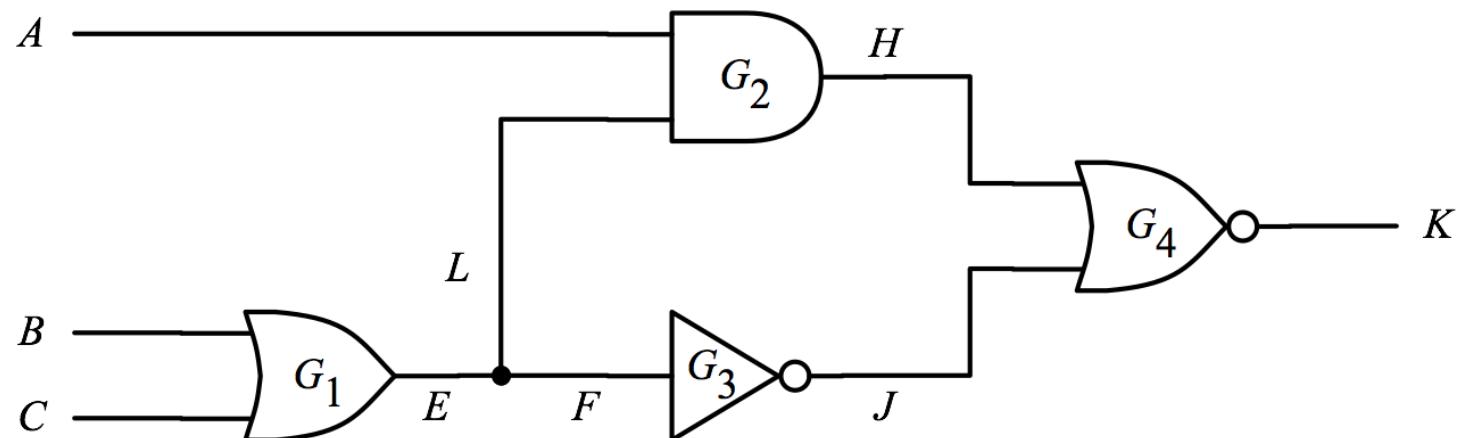
# Quiz

**Q1: Set  $E = 0$ . What can you learn about  $K$  using contrapositive law?**

A:

**Q2: (Cont'd) If we want to detect  $K$  SA 0 fault, what is value of  $E$ ?**

A:



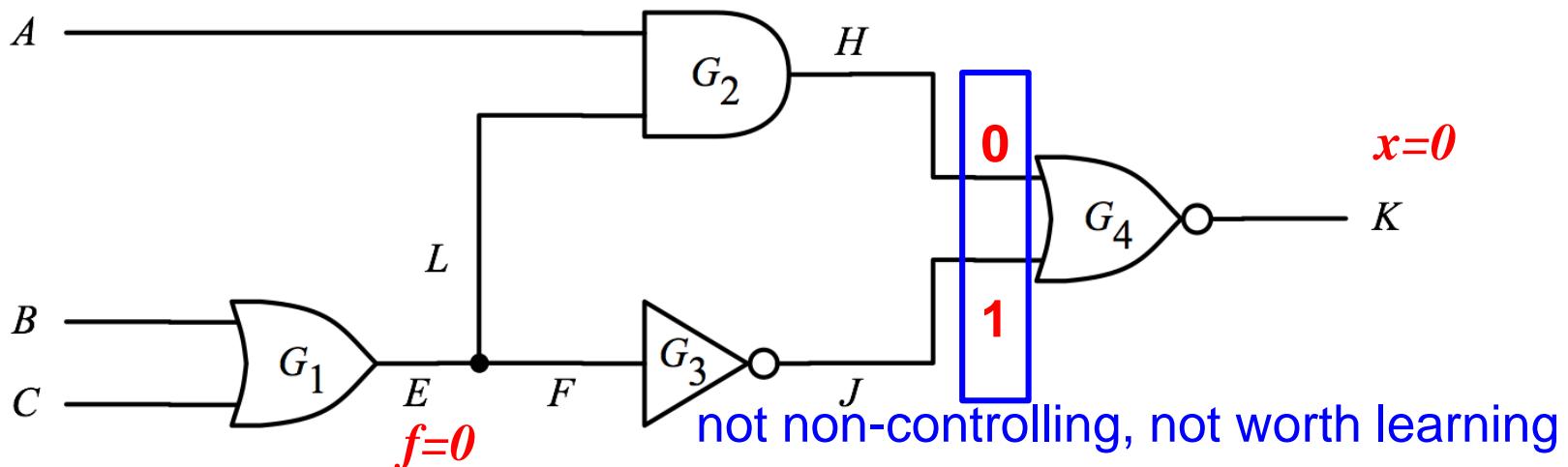
# FFT

- Q1: Why SOCRATES requires both inputs are non-controlling?
  - ◆ Hint: use following circuit as example
- Q2: Why forward path from  $f$  to  $x$ ?

analyze\_results ( $f$ )

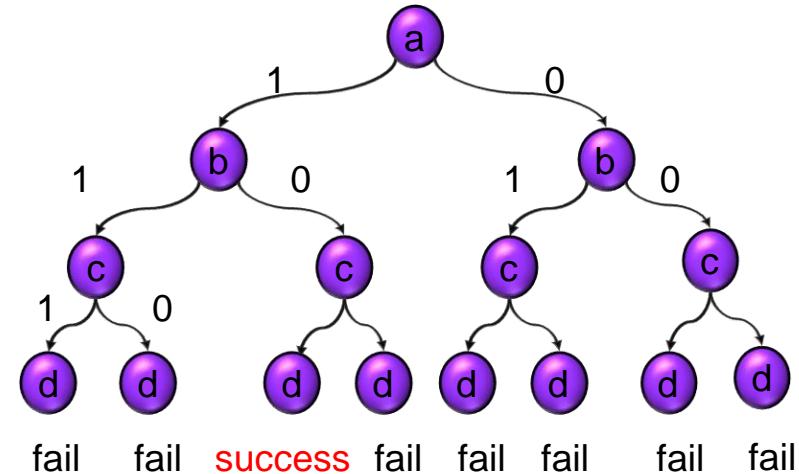
for every signal  $x$  whose value  $\neq$  unknown  
if (all gate inputs to  $x$  are non-controlling)  
& (there is forward path from  $f$  to  $x$ )  
save learning result ( $x=v_x \rightarrow f=v_f$ )

```
static_learning()  
for every signal  $f$   
assign_value ( $f, 0$ )  
implication()  
analyze_results( $f$ )  
assign_value ( $f, 1$ )  
implication()  
analyze_results( $f$ )
```



# Combinational ATPG

- Introduction
- Deterministic Test Pattern Generation
- Acceleration techniques
  - ◆ Learning [Schulz 1988]
  - ◆ Redundant fault identification [Iyer 1996]
- Concluding Remarks

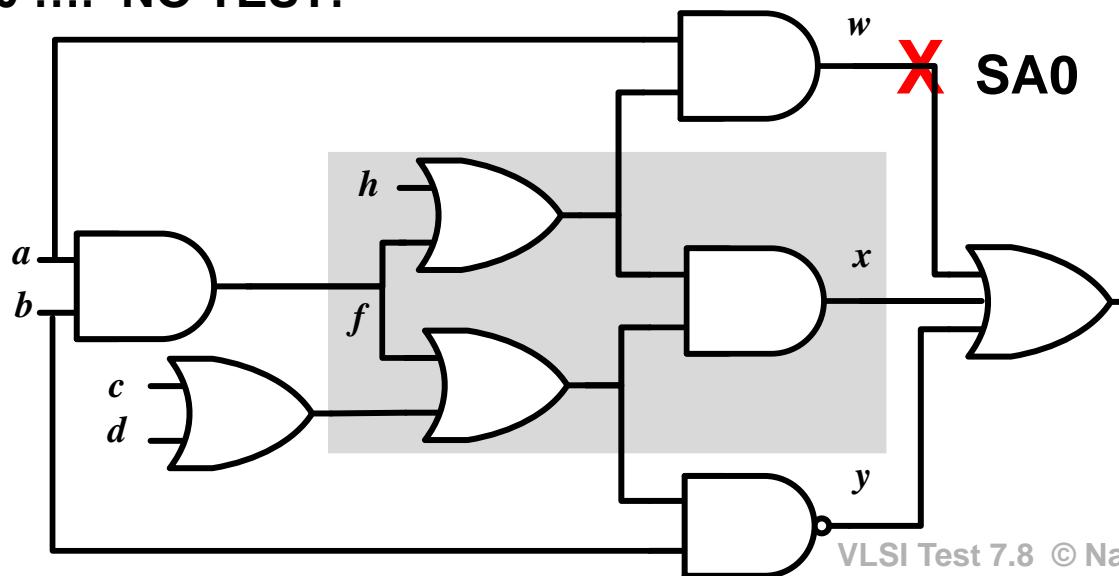


# Proving Redundant Fault is Difficult

without learning

- Obj :  $w=1$ . assign  $h=1, a=1$
- Obj :  $x=0$ . assign  $c=0, d=0, b=0$ 
  - ♦  $y=1$  conflict!
- backtrack  $b=1$ 
  - ♦  $x=1$  conflict!
- backtrack  $c=1$ , conflict!
- backtrack  $d=1$ , conflict!
- backtrack  $a=0$ , conflict!
- backtrack  $h=0$  .... NO TEST!

Can We Find  
Redundant Fault  
Faster?



# Redundant Fault Identification

- **Untestable faults** (aka. **redundant faults**)
  - ◆ faults that cannot be **excited**, or
  - ◆ faults that cannot be **propagated**, or
  - ◆ faults that cannot be **simultaneously** excited and propagated
- Why redundant fault identification?
  - ① Speed up ATPG
    - \* ATPG spend long time on untestable faults
  - ② Reduce area
    - \* Redundant logic can be removed
- To prove redundant fault is **NP-complete**
  - ◆ Quickly identify many redundant fault (not all) is good enough

**Redundant Faults are Trouble for ATPG**

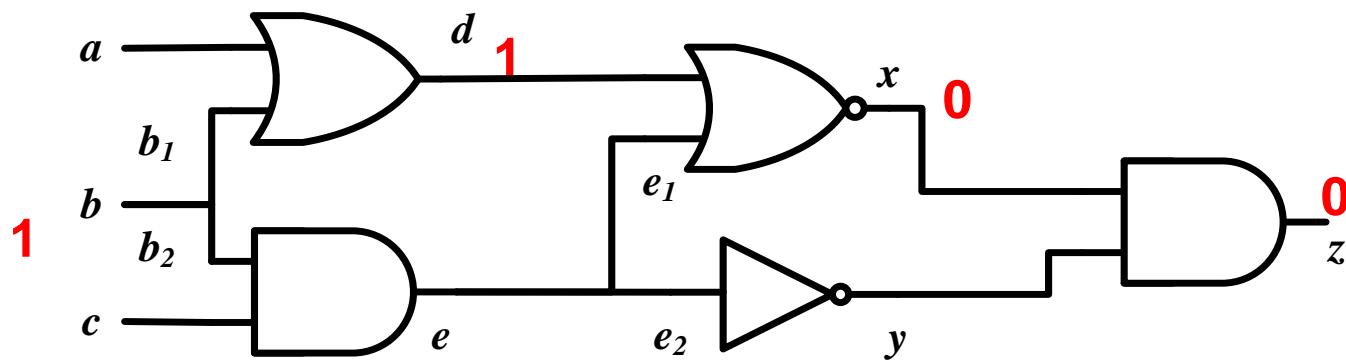
# FIRE [Iyer 1996]

- **Fault Independent Redundant Identification (FIRE)**
  - ◆ based on single-line conflict analysis
- **Idea**
  - ◆ **S<sub>0</sub>** = set of faults untestable when signal s=0
  - ◆ **S<sub>1</sub>** = set of faults untestable when signal s=1
  - ◆ intersection **S<sub>0</sub>∩S<sub>1</sub>** are untestable faults
- **To find unexcitable faults**
  - ◆ use **forward implication**
- **To find unobservable faults**
  - ◆ use **backward tracing**
- **Advantage: close to linear time complexity (for one signal)**
  - ◆ FFT: can we solve NPC problem in linear time?

# FIRE Example

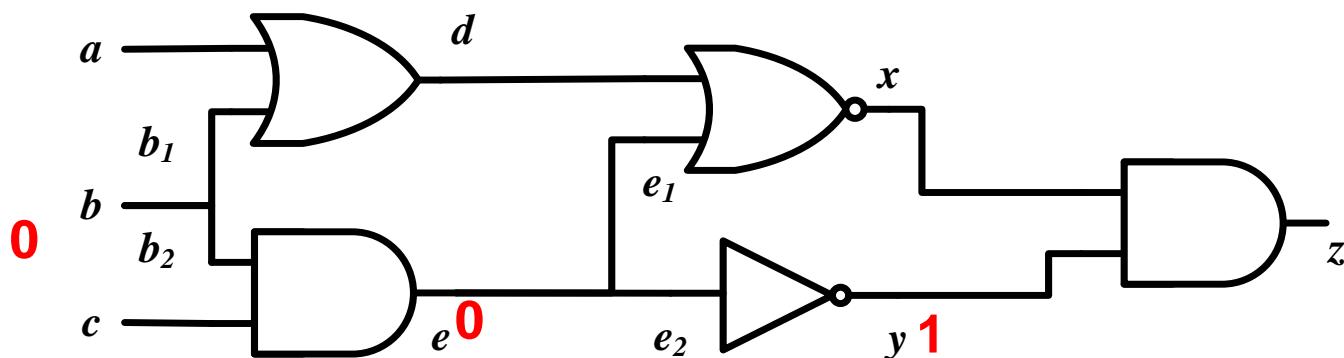
- set  $b=1$  implies  $\rightarrow \{b=1, b_1=1, b_2=1, d=1, x=0, z=0\}$ 
  - ◆ Faults unexcitable when  $b=1$ :  $\{b/1, b_1/1, b_2/1, d/1, x/0, z/0\}$
  - ◆ Faults unobservable when  $b=1$ :  $\{a/0, a/1, e_1/0, e_1/1, y/0, y/1, e_2/0, e_2/1, e/0, e/1, b_2/0, b_2/1, c/0, c/1\}$ 
    - \* Q: why  $b/0$  not in the list?
  - ◆ Faults untestable when  $b=1$ : union of above two sets
    - \*  $S1=\{a/0, a/1, b/1, b_1/1, b_2/1, d/1, e_1/0, e_1/1, e_2/0, e_2/1, e/0, e/1, x/0, y/0, y/1, z/0, b_2/0, c/0, c/1\}$

$b/1 = b$  SA1 fault



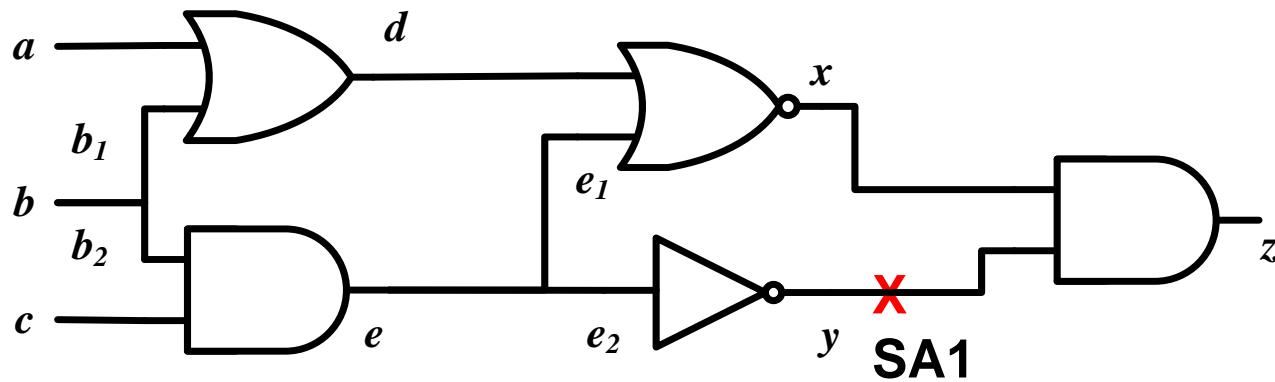
# FIRE Example (cont'd)

- set  $b=0$  implies  $\rightarrow \{b=0, b_1=0, b_2=0, e=0, e_1=0, e_2=0, y=1\}$ 
  - ◆ Faults unexcitable when  $b=0$ :  $\{b/0, b_1/0, b_2/0, e/0, e_1/0, e_2/0, y/1\}$
  - ◆ Faults unobservable when  $b=0$ :  $\{c/0, c/1\}$
  - ◆ Faults untestable when  $b=0$ : union of above two sets
    - \*  $S0 = \{b/0, b_1/0, b_2/0, c/0, c/1, e/0, e_1/0, e_2/0, y/1\}$
    - \*  $S1 = \{a/0, a/1, b/1, b_1/1, b_2/1, d/1, e1/0, e_1/1, e_2/0, e_2/1, e/1, x/1, y/0, y/1, z/0, b_2/0, c/0, c/1\}$
- Intersection of  $S1$  and  $S0$  are untestable faults
  - ◆  $S1 \cap S0 = \{b_2/0, c/0, c/1, e/0, e_1/0, e_2/0, y/1\}$



# FFT

- Q1: Use PODAM to find a test for  $y/1$  fault. Prove  $y/1$  is untestable.
- Q2: Can we use linear time algorithm to solve NPC problem?



# Quiz

**Q1: Set B=0. Find set of faults undetectable.**

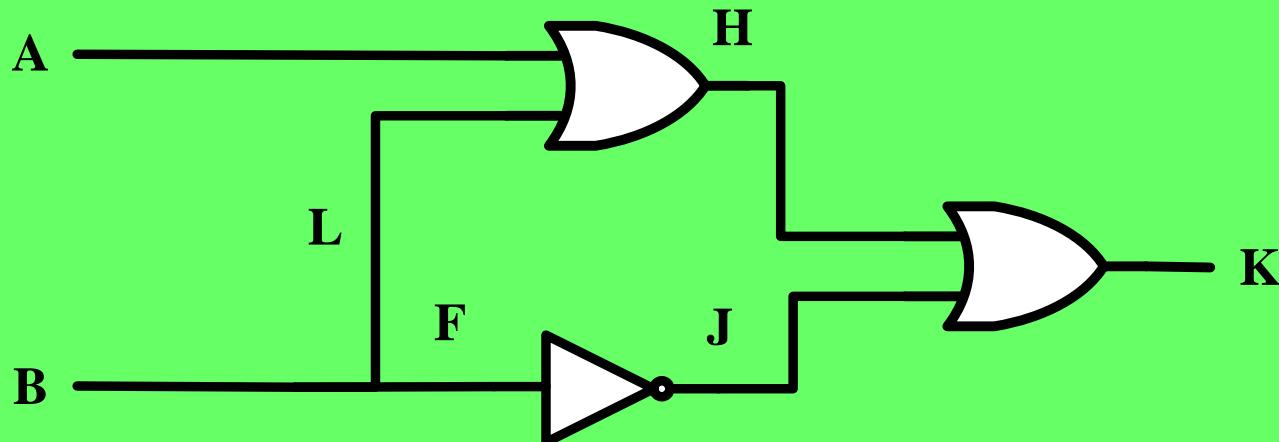
A: faults unexcitable = { }  
faults unobservable= { }

**Q2: Set B=1. Find set of faults undetectable.**

A: faults unexcitable = { }  
faults unobservable= { }

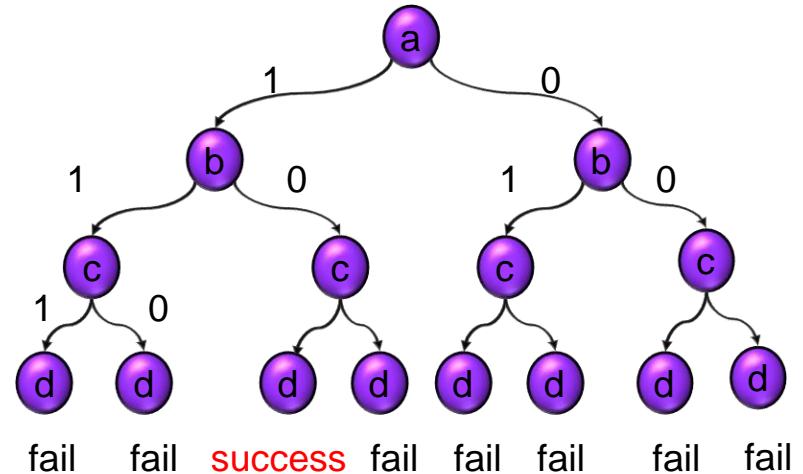
**Q3: (cont'd) Which faults are redundant ?**

A:  $Q1 \cap Q2 = \{ \}$



# Combinational ATPG

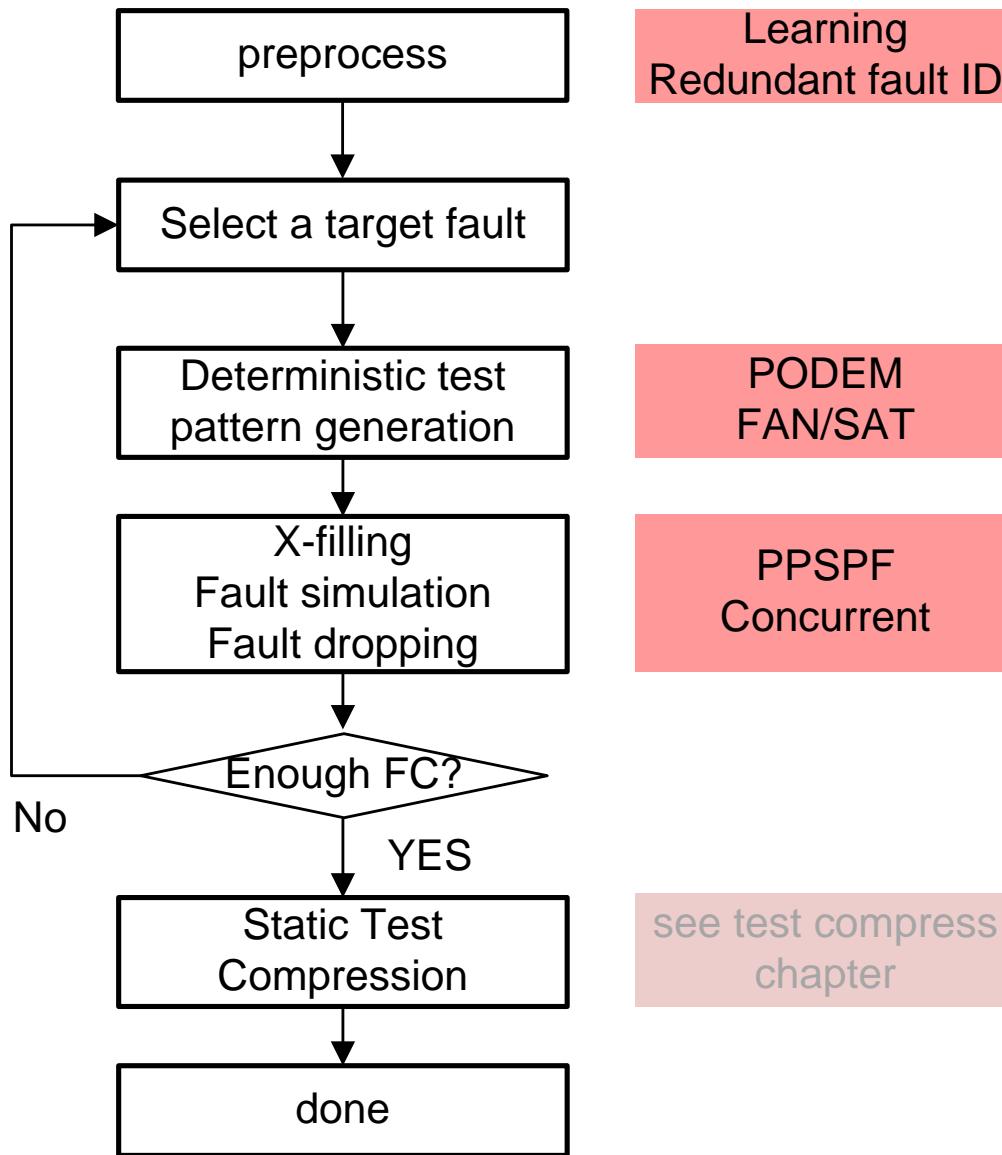
- Introduction
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# Summary

- ATPG is NPC. Many acceleration techniques needed
- Static learning (SOCRATES) trade off memory for run time
  - ◆ Setting all signals to 0 and 1. imply other signals
  - ◆ Apply contrapositive law: if  $p \rightarrow q$  then  $q' \rightarrow p'$
- Redundant fault identification (FIRE)
  - ◆ Setting a signal to 0 and 1
    - \* unexcitable faults  $\cup$  unobservable faults
  - ◆ Redundant fault =  $S_1 \cap S_0$
- Many other acceleration techniques
  - ◆ Dominator (TOPS) [Kirkland 87]
  - ◆ Recursive learning [Kunz 92]
  - ◆ Transitive Closure Graph (NNATPG) [Chakradhar 93]
  - ◆ ...

# ATPG Review



# How to Read ATPG Report?

	Uncollapsed	Collapsed
Total Faults	1234	800
Detected faults	1000	700
Redundant faults	230	98
Aborted faults	4	2
Fault coverage	1000/1234 %	700/800 %
ATPG effectiveness	1230/1234 %	798/800 %
Test Length	328 patterns	
Run Time	10:57	

*proven redundant by ATPG*  
*undetected. not sure redundant or not.*  
 $\frac{\text{detected faults}}{\text{total faults}} \times 100\%$   
 $\frac{\text{detected} + \text{redundant faults}}{\text{total faults}} \times 100\%$   
*less are better*

# References

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- [Goel 81] P. Goel, “An Implicit Enumeration Algorithm to Generate Tests for Combinational Logic Circuits,” IEEE Trans. On Computers, Vol. C-30, No. 3, pp.215-222. Mar. 1981.
- [Roth 66] J. P. Roth, “Diagnosis of Automata Failures: A Calculus and a Method,” IBM Journal of Research and Development, vol. 10, no. 4, pp278-291, 1966.
- [Larrabee 92] T. Larrabee, “Test pattern generation using Boolean satisfiability,” IEEE Trans. Computer-Aided Design of Integrated Circuits and Systems, Volume 11, Issue 1, Jan 1992, pp. 4-15.
- [Iyer 96] Iyer, M.A. Abramovici, M. “FIRE: a fault-independent combinational redundancy identification algorithm,” Very Large Scale Integration (VLSI) Systems, IEEE Transactions on, Jun 1996, Volume: 4, Issue: 2 page(s): 295-301
- [Schulz 88] M.H Schulz, et al “SOCRATES: A highly efficient automatic test pattern generation system IEEE TCAD, vol.7 no.1 pp.126, 1988.
- [Marques 94] J. Marques, S. Karen, A. Sakallah, “Dynamic search-space Pruning Techniques in Path Sensitization’ DAC 1994.

# Commercial Tools

- **Mentor Graphics**
  - ◆ Fastscan
- **Synopsys**
  - ◆ Tetramax
- **Syntest**
  - ◆ Turboscan
- **Cadence**
  - ◆ Encounter Test