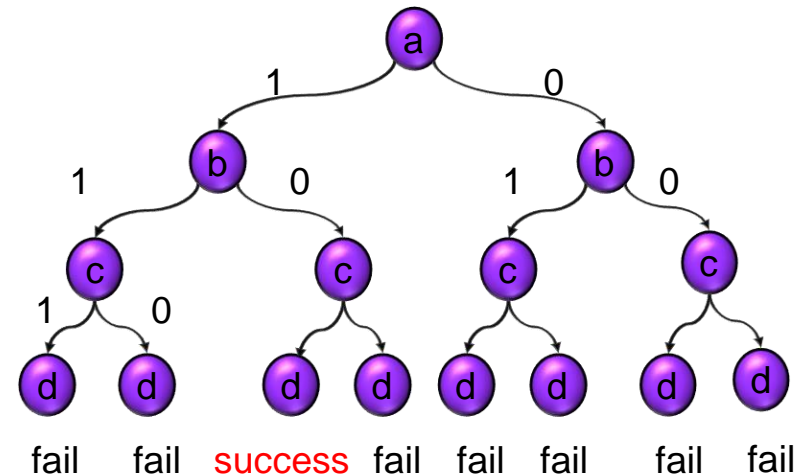


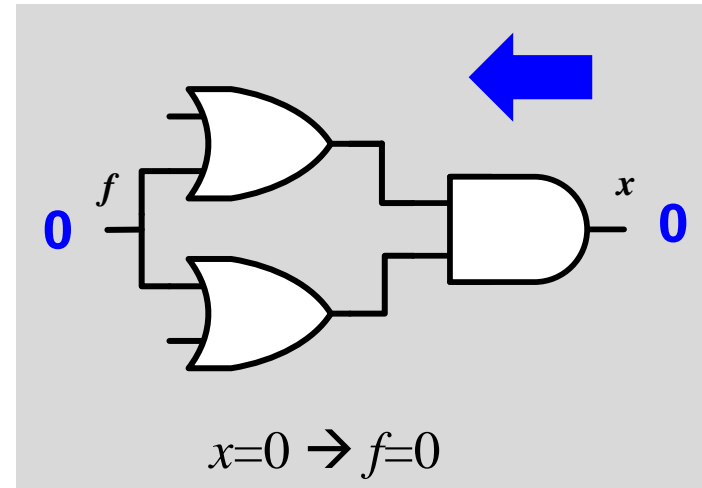
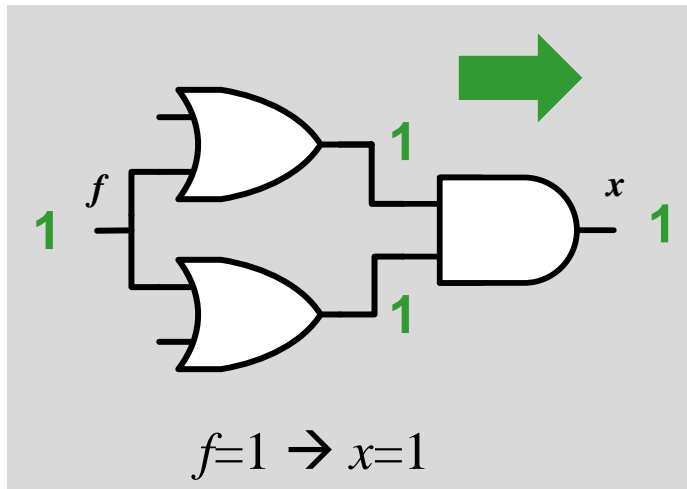
# Combinational ATPG

- Introduction
- Deterministic Test Pattern Generation
- Acceleration techniques
  - ♦ Learning [Schulz 1988]
  - ♦ Redundant fault identification [Iyer 1996]
- Concluding Remarks



# Learning

- **Learning** memorizes circuit information to speed up test generation
  - ♦ **Static learning:** performed in preprocess. no test pattern required.
  - ♦ **Dynamic learning:** performed in test generation (not in lecture)
- Static learning example: WWW Fig 4.22
  - ♦ Set  $f=1$ , implies  $x=1$
  - ♦ So we learn  $x=0$ , implies  $f=0$

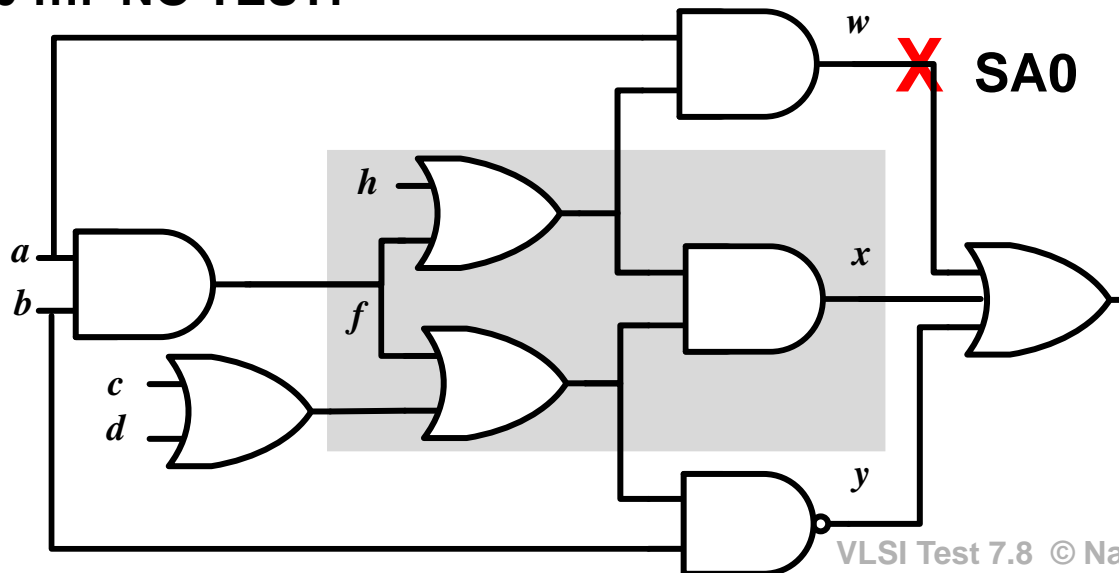


**Contrapositive Law:  $If\ p \rightarrow q\ then\ q' \rightarrow p'$**

# Learning Reduces Backtracks (1)

without learning

- Obj :  $w=1$ . assign  $h=1, a=1$
- Obj :  $x=0$ . assign  $c=0, d=0, b=0$ 
  - ♦  $y=1$  conflict!
- backtrack  $b=1$ 
  - ♦  $x=1$  conflict!
- backtrack  $d=1$ , conflict!
- backtrack  $c=1$ , conflict!
- backtrack  $a=0$ , conflict!
- backtrack  $h=0$  .... NO TEST!



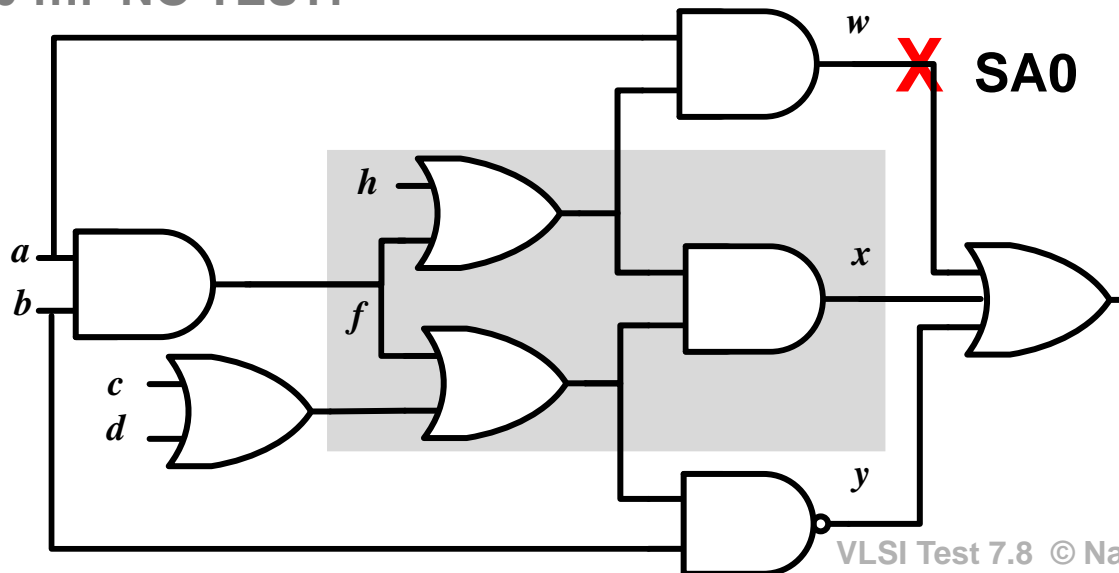
# Learning Reduces Backtracks (2)

## without learning

- Obj :  $w=1$ . assign  $h=1$ ,  $a=1$
- Obj :  $x=0$ . assign  $c=0$ ,  $d=0$ ,  $b=0$ 
  - ♦  $y=1$  conflict!
- backtrack  $b=1$ 
  - ♦  $x=1$  conflict!
- backtrack  $d=1$ , conflict!
- backtrack  $c=1$ , conflict!
- backtrack  $a=0$ , conflict!
- backtrack  $h=0$  .... NO TEST!

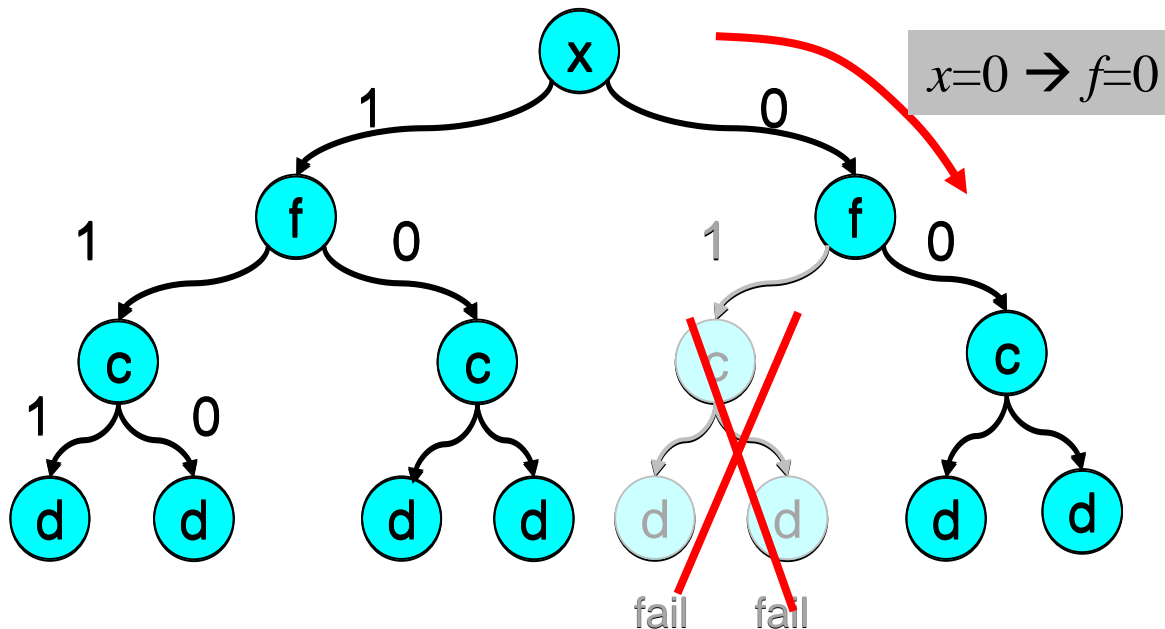
## with learning

- Obj :  $w=1$ . assign  $h=1$ ,  $a=1$
- Obj :  $x=0 \rightarrow f=0$ . assign  $b=0$ 
  - ♦  $y=1$  conflict!
- backtrack  $b=1$ 
  - ♦  $x=1$  conflict!
- backtrack  $a=0$ , conflict!
- backtrack  $h=0$  ... NO TEST!



# Learning Speedup Decision

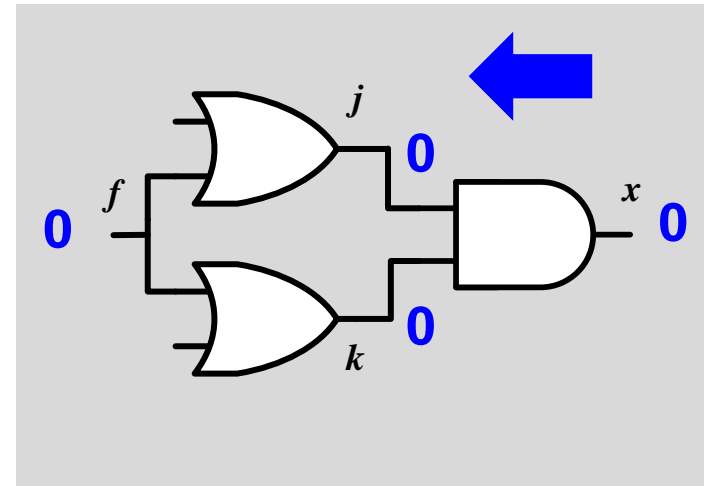
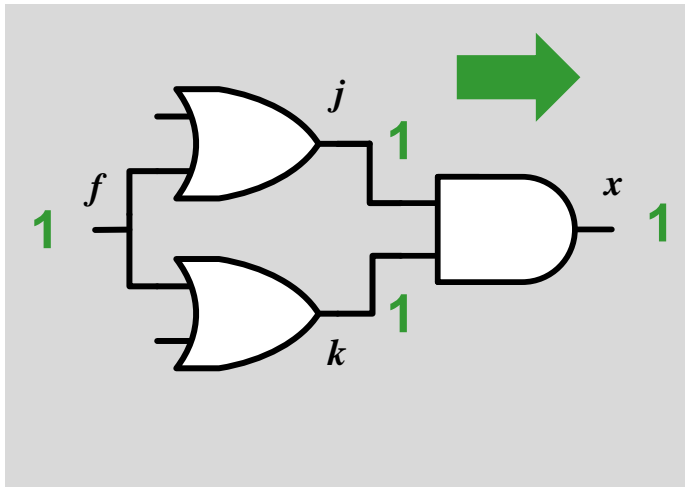
- Learning helps to
  - ♦ 1. Prune impossible sub-trees ASAP
  - ♦ 2. Find necessary assignments ASAP



**Learning Trade-off Memory for Run Time**

# But ... Too Many to Learn!

- $f=1 \rightarrow j=1$  so  $j=0 \rightarrow f=0$ 
  - ♦ Only local implication. not worth learning
- $f=1 \rightarrow k=1$  so  $k=0 \rightarrow f=0$ 
  - ♦ Only local implication. not worth learning
- $f=1 \rightarrow x=1$  so  $x=0 \rightarrow f=0$ 
  - ♦ global implication. **worth learning!**



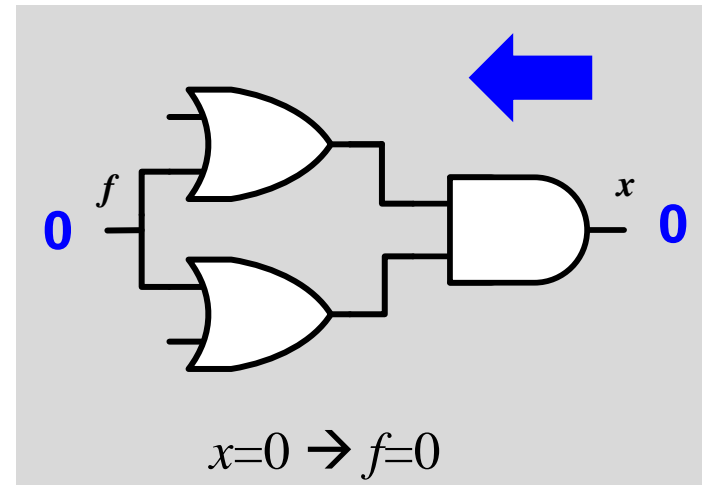
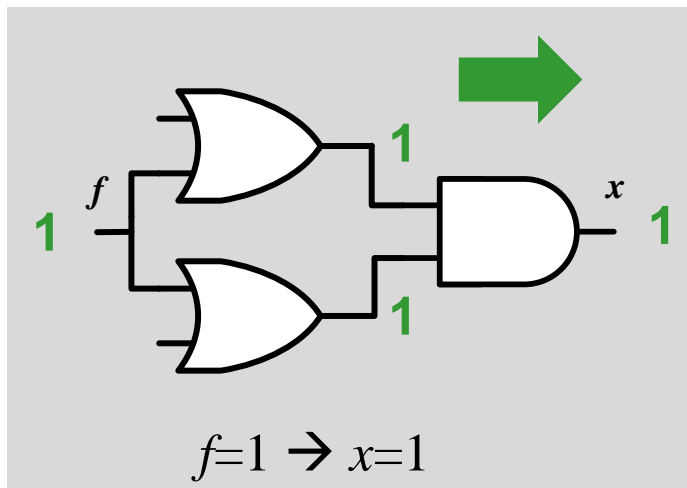
**Which Are Worth Learning?**

# SOCRATES Algorithm [Schulz 1988]

- In preprocess phase, sets **all signals** to 0 and 1
  - ♦ Discovers what other signals are implied
  - ♦ **Two criteria** to select **useful** learning

```
analyze_results(f)
  for every signal x whose value  $\neq$  unknown
    if (all gate inputs to x are non-controlling)
      & (there is forward path from f to x)
        save learning result ( $x=v_x' \rightarrow f=v_f'$ )
```

```
static_learning()
  for every signal f
    assign_value(f, 0)
    implication()
    analyze_results(f)
    assign_value(f, 1)
    implication()
    analyze_results(f)
```



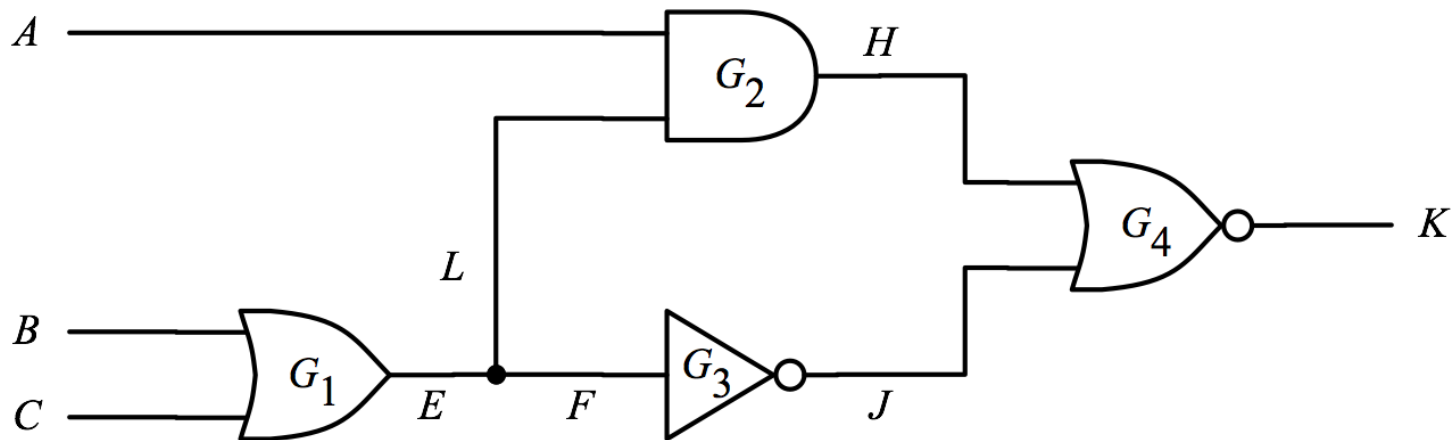
# Quiz

**Q1: Set  $E = 0$ . What can you learn about  $K$  using contrapositive law?**

**A:**

**Q2: (Cont'd) If we want to detect  $K$  SA 0 fault, what is value of  $E$ ?**

**A:**





# FFT

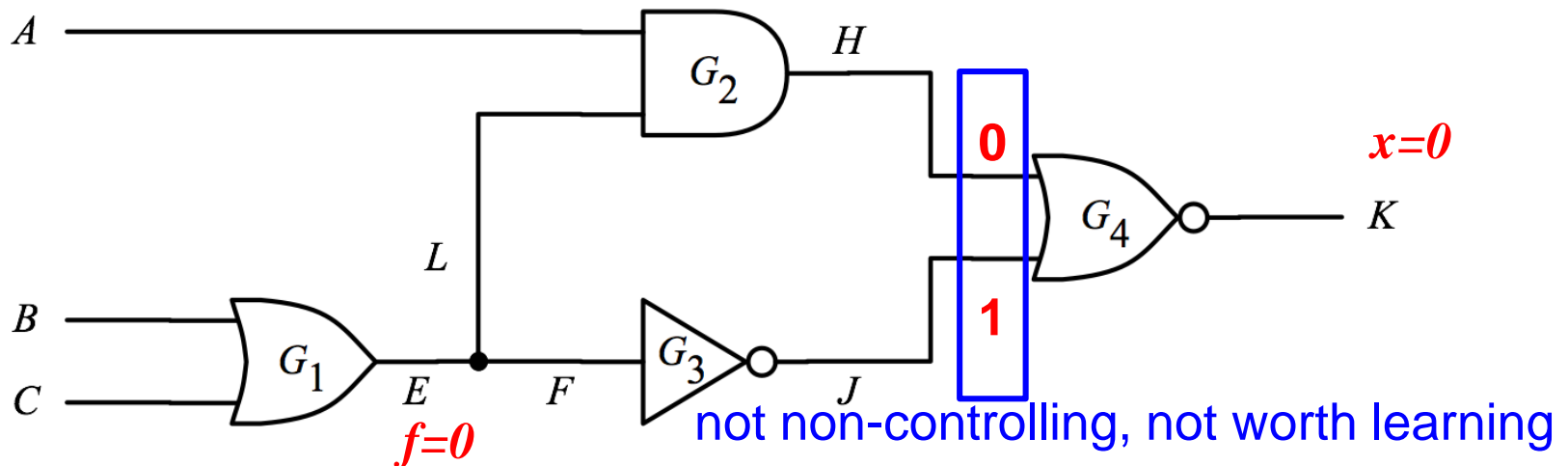
- Q1: Why SOCRATES requires both inputs are non-controlling?  
 ♦ Hint: use following circuit as example
- Q2: Why forward path from  $f$  to  $x$ ?

```

analyze_results (f)
  for every signal x whose value  $\neq$  unknown
    if (all gate inputs to x are non-controlling)
      & (there is forward path from f to x)
        save learning result ( $x=v_x' \rightarrow f=v_f'$ )
    
```

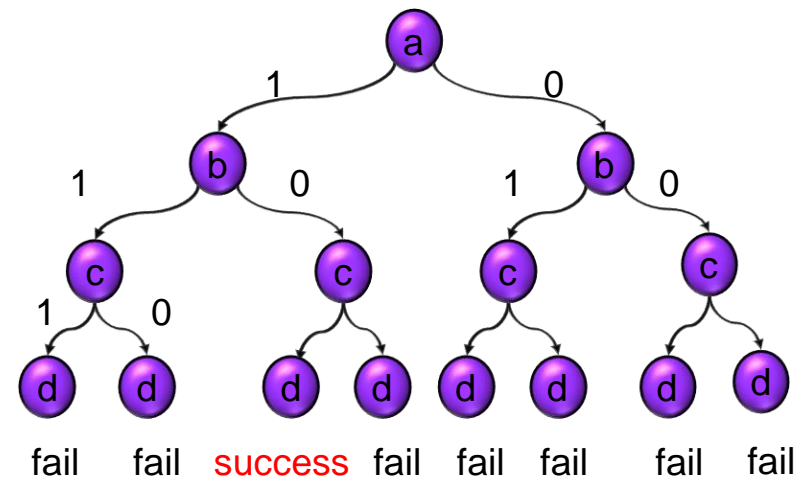
```

static_learning()
  for every signal f
    assign_value (f, 0)
    implication()
    analyze_results(f)
    assign_value (f, 1)
    implication()
    analyze_results(f)
  
```



# Combinational ATPG

- Introduction
- Deterministic Test Pattern Generation
- Acceleration techniques
  - ♦ Learning [Schulz 1988]
  - ♦ Redundant fault identification [Iyer 1996]
- Concluding Remarks

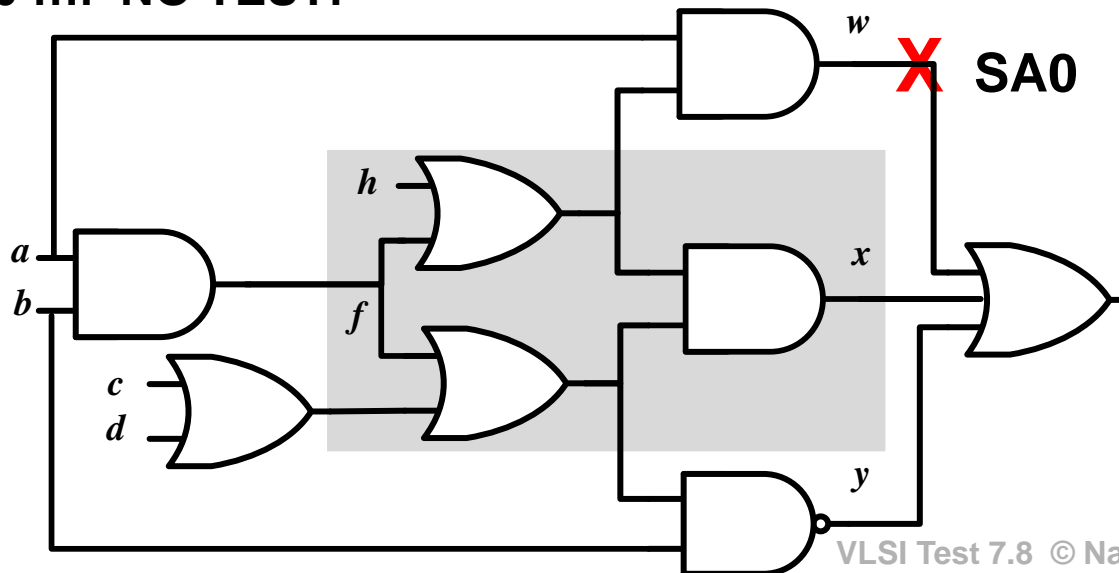


# Proving Redundant Fault is Difficult

without learning

- Obj :  $w=1$ . assign  $h=1, a=1$
- Obj :  $x=0$ . assign  $c=0, d=0, b=0$ 
  - ♦  $y=1$  conflict!
- backtrack  $b=1$ 
  - ♦  $x=1$  conflict!
- backtrack  $c=1$ , conflict!
- backtrack  $d=1$ , conflict!
- backtrack  $a=0$ , conflict!
- backtrack  $h=0$  .... NO TEST!

**Can We Find  
Redundant Fault  
Faster?**



# Redundant Fault Identification

- **Untestable faults** (aka. **redundant faults**)
  - ♦ faults that cannot be **excited**, or
  - ♦ faults that cannot be **propagated**, or
  - ♦ faults that cannot be **simultaneously** excited and propagated
- Why redundant fault identification?
  - ① Speed up ATPG
    - \* ATPG spend long time on untestable faults
  - ② Reduce area
    - \* Redundant logic can be removed
- To prove redundant fault is **NP-complete**
  - ♦ Quickly identify many redundant fault (not all) is good enough

**Redundant Faults are Trouble for ATPG**

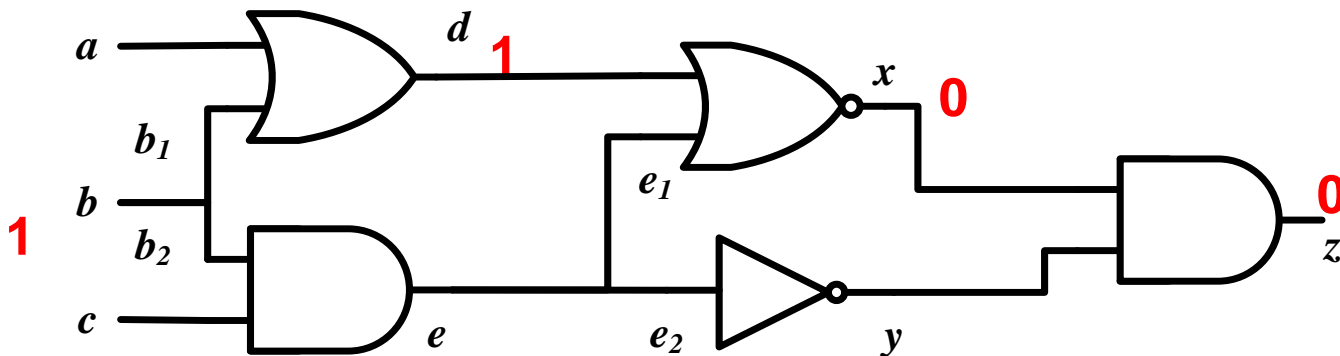
# FIRE [Iyer 1996]

- **Fault Independent Redundant Identification (FIRE)**
  - ◆ based on single-line conflict analysis
- **Idea**
  - ◆ **S0** = set of faults untestable when signal  $s=0$
  - ◆ **S1** = set of faults untestable when signal  $s=1$
  - ◆ intersection **S0** $\cap$ **S1** are untestable faults
- To find unexcitable faults
  - ◆ use **forward implication**
- To find unobservable faults
  - ◆ use **backward tracing**
- Advantage: close to **linear time** complexity (for one signal)
  - ◆ FFT: can we solve NPC problem in linear time?

# FIRE Example

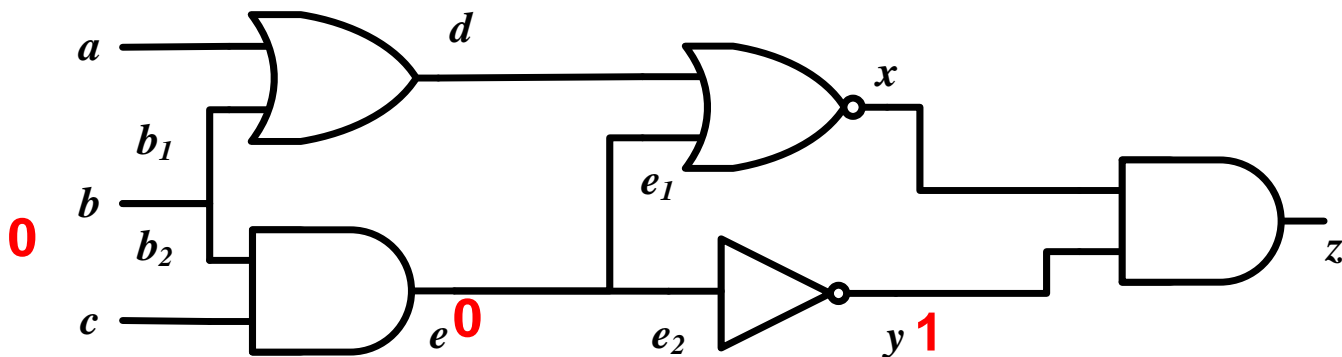
- set  $b=1$  implies  $\rightarrow \{b=1, b_1=1, b_2=1, d=1, x=0, z=0\}$ 
  - ◆ Faults unexcitable when  $b=1$ :  $\{b/1, b_1/1, b_2/1, d/1, x/0, z/0\}$
  - ◆ Faults unobservable when  $b=1$ :  $\{a/0, a/1, e_1/0, e_1/1, y/0, y/1, e_2/0, e_2/1, e/0, e/1, b_2/0, b_2/1, c/0, c/1\}$ 
    - \* Q: why  $b/0$  not in the list?
  - ◆ Faults untestable when  $b=1$ : union of above two sets
    - \* **S1** =  $\{a/0, a/1, b/1, b_1/1, b_2/1, d/1, e_1/0, e_1/1, e_2/0, e_2/1, e/1, e/1, x/0, y/0, y/1, z/0, b_2/0, c/0, c/1\}$

$b/1 = b$  SA1 fault



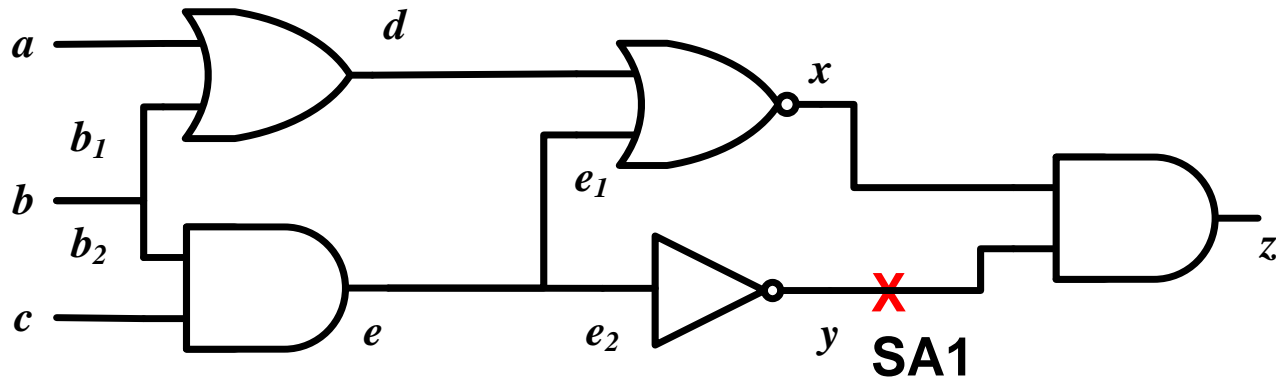
# FIRE Example (cont'd)

- set  $b=0$  implies  $\rightarrow \{b=0, b_1=0, b_2=0, e=0, e_1=0, e_2=0, y=1\}$ 
  - ♦ Faults unexcitable when  $b=0$ :  $\{b/0, b_1/0, b_2/0, e/0, e_1/0, e_2/0, y/1\}$
  - ♦ Faults unobservable when  $b=0$ :  $\{c/0, c/1\}$
  - ♦ Faults untestable when  $b=0$ : union of above two sets
    - \*  $S_0 = \{b/0, b_1/0, b_2/0, c/0, c/1, e/0, e_1/0, e_2/0, y/1\}$
    - \*  $S_1 = \{a/0, a/1, b/1, b_1/1, b_2/1, d/1, e_1/0, e_1/1, e_2/0, e_2/1, e/1, e/1, x/0, y/0, y/1, z/0, b_2/0, c/0, c/1\}$
- Intersection of  $S_1$  and  $S_0$  are untestable faults
  - ♦  $S_1 \cap S_0 = \{b_2/0, c/0, c/1, e/0, e_1/0, e_2/0, y/1\}$



# FFT

- Q1: Use PODAM to find a test for **y/1** fault. Prove y/1 is untestable.
- Q2: Can we use linear time algorithm to solve NPC problem?





# Quiz

**Q1: Set B=0. Find set of faults undetectable.**

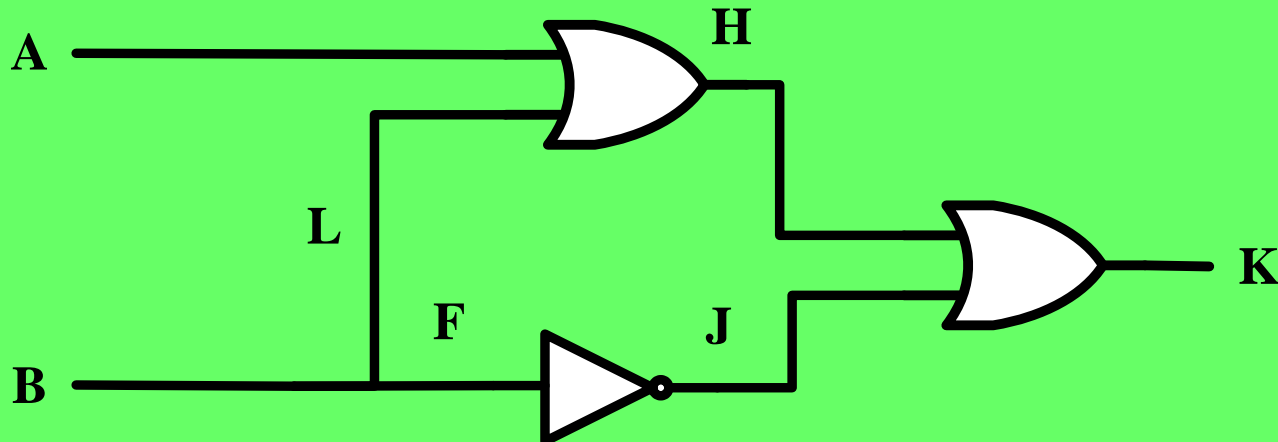
**A:** faults unexcitable = { }  
      faults unobservable = { }

**Q2: Set B=1. Find set of faults undetectable.**

**A:** faults unexcitable = { }  
      faults unobservable = { }

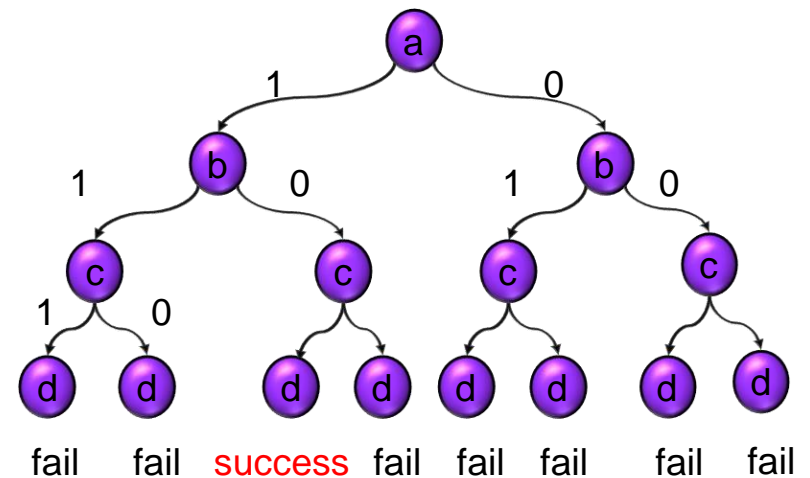
**Q3: (cont'd) Which faults are redundant ?**

**A:**  $Q1 \cap Q2 = \{ \}$



# Combinational ATPG

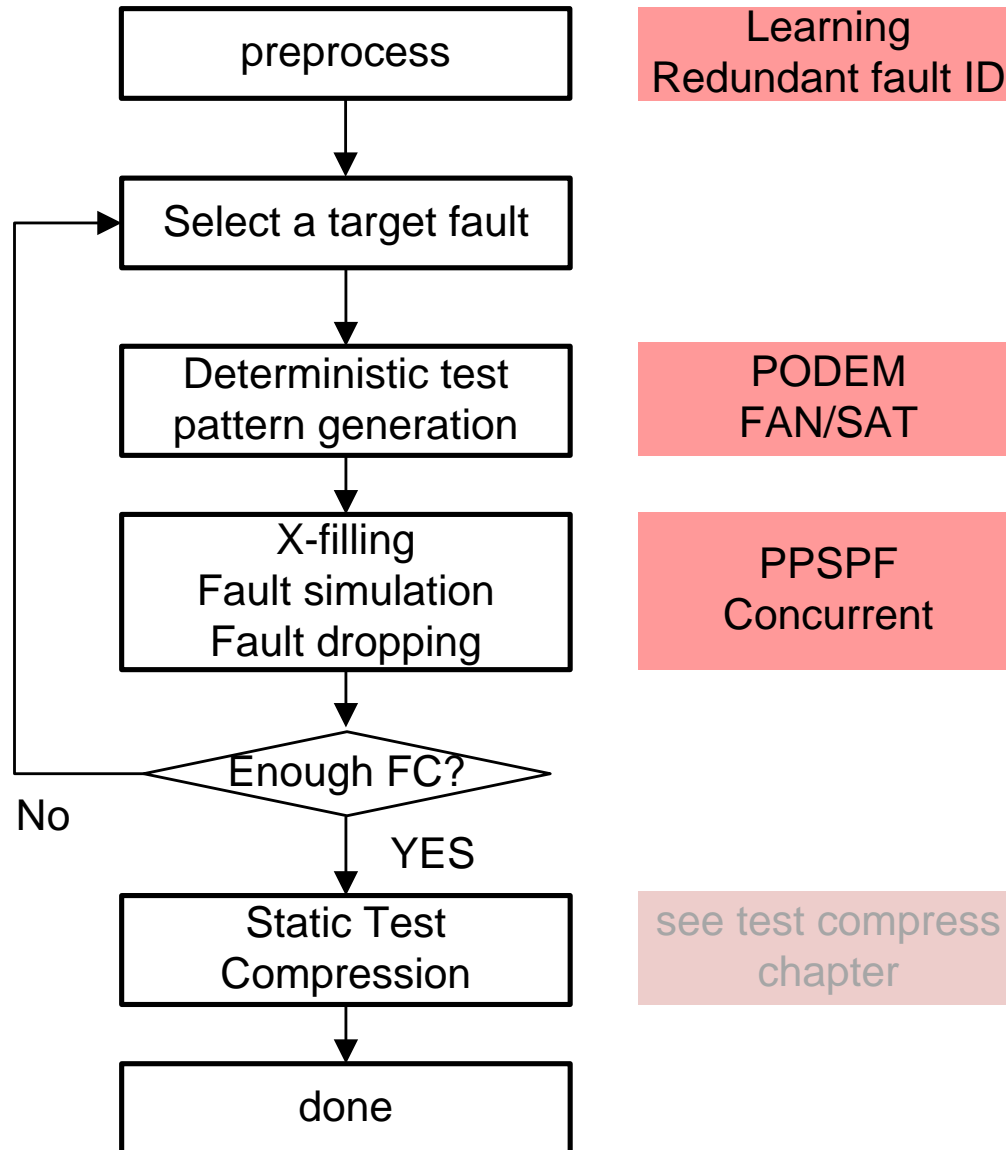
- Introduction
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# Summary

- ATPG is NPC. Many acceleration techniques needed
- **Static learning (SOCRATES)** trade off memory for run time
  - ♦ Setting all signals to 0 and 1. imply other signals
  - ♦ Apply contrapositive law: if  $p \rightarrow q$  then  $q' \rightarrow p'$
- **Redundant fault identification (FIRE)**
  - ♦ Setting a signal to 0 and 1
    - \* unexcitable faults  $\cup$  unobservable faults
  - ♦ Redundant fault =  $S1 \cap S0$
- Many other acceleration techniques
  - ♦ Dominator (TOPS) [Kirkland 87]
  - ♦ Recursive learning [Kunz 92]
  - ♦ Transitive Closure Graph (NNATPG) [Chakradhar 93]
  - ♦ ...

# ATPG Review



# How to Read ATPG Report?

	Uncollapsed	Collapsed
<b>Total Faults</b>	<b>1234</b>	<b>800</b>
<b>Detected faults</b>	<b>1000</b>	<b>700</b>
<b>Redundant faults</b>	<b>230</b>	<b>98</b>
<b>Aborted faults</b>	<b>4</b>	<b>2</b>
<b>Fault coverage</b>	<b>1000/1234</b> %	<b>700/800</b> %
<b>ATPG effectiveness</b>	<b>1230/1234</b> %	<b>798/800</b> %
<b>Test Length</b>	<b>328 patterns</b>	
<b>Run Time</b>	<b>10:57</b>	

*proven redundant by ATPG*

*undetected. not sure redundant or not.*

$$\frac{\text{detected faults}}{\text{total faults}} \times 100\%$$

$$\frac{\text{detected} + \text{redundant faults}}{\text{total faults}} \times 100\%$$

*less are better*

# References

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- [Larrabee 92] T. Larrabee, “Test pattern generation using Boolean satisfiability,” IEEE Trans. Computer-Aided Design of Integrated Circuits and Systems, Volume 11, Issue 1, Jan 1992, pp. 4-15.
- [Iyer 96] Iyer, M.A. Abramovici, M. “FIRE: a fault-independent combinational redundancy identification algorithm,” Very Large Scale Integration (VLSI) Systems, IEEE Transactions on, Jun 1996, Volume: 4, Issue: 2 page(s): 295-301
- [Schulz 88] M.H Schulz, et al “SOCRATES: A highly efficient automatic test pattern generation system IEEE TCAD, vol.7 no.1 pp.126, 1988.
- [Marques 94] J. Marques, S. Karen, A. Sakallah, “Dynamic search-space Pruning Techniques in Path Sensitization’ DAC 1994.

# Commercial Tools

- **Mentor Graphics**
  - ◆ **Fastscan**
- **Synposys**
  - ◆ **Tetramax**
- **Syntest**
  - ◆ **Turboscan**
- **Cadence**
  - ◆ **Encounter Test**