```
suppressMessages(library(psych))
suppressMessages(library(dplyr))
suppressMessages(library(tidyverse))
suppressMessages(library(ResourceSelection))
suppressMessages(library(lmtest))
suppressMessages(library(VGAM))
####Case 1
\#\#\# Data Preparation
##Data importing and cleaning
df <- read.csv("MIDUS_III_Final_Exam_Fall2023_data.csv") %>% drop_na
df1 <- df[,c("heart", "bp", "smoke", "age", "male", "exercise")]</pre>
#Data Description
describe(df1)
##
           vars
                   n mean
                              sd median trimmed
                                                  mad min max range skew
## heart
                                      0
                                           0.17 0.00
                                                        0
                                                                  1 1.22
              1 1979 0.24 0.43
                                                            1
## bp
              2 1979 0.51 0.50
                                           0.51 0.00
                                                        0
                                                           1
                                                                  1 -0.05
              3 1979 0.64 0.48
                                           0.67 0.00
                                                          1
                                                                  1 -0.57
## smoke
                                      1
                                                        0
                                                                53 0.16
## age
              4 1979 64.09 11.01
                                     64
                                          63.86 11.86 39 92
                                     0 0.49 0.00 0 1
              5 1979 0.49 0.50
                                                                1 0.03
## male
              6 1979 0.19 0.39
                                    0
                                         0.12 0.00 0 1
                                                                 1 1.55
## exercise
##
           kurtosis
                      se
## heart
              -0.51 0.01
              -2.00 0.01
## bp
              -1.67 0.01
## smoke
## age
              -0.68 0.25
## male
              -2.00 0.01
## exercise
              0.42 0.01
lapply(df1[-4], table)
## $heart
##
##
     0
          1
## 1505 474
##
## $bp
##
##
          1
##
   966 1013
##
## $smoke
##
##
     0
          1
##
  717 1262
##
## $male
##
##
     0
          1
## 1005 974
##
```

```
## $exercise
##
##
      0
## 1597
        382
#Bivariable Analysis
cor(df1,method = "spearman")[1, 2:6, drop = F]
                bp
                        smoke
                                   age
                                                     exercise
                                             male
## heart 0.2116867 0.07816263 0.229714 0.1035217 -0.00748379
heart is more related with bp and age
\#\#\#\mathrm{Step1}
##Modeling
#Since the outcome variable is binary, choose logistic regression (glm)
model1 <- glm(heart ~ ., family = binomial, data = df1)</pre>
summary(model1)
##
## Call:
## glm(formula = heart ~ ., family = binomial, data = df1)
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -4.909779 0.370817 -13.240 < 2e-16 ***
## bp
                           0.116975
                                     7.282 3.29e-13 ***
                0.851829
                0.282466
                           0.119265
                                      2.368
                                              0.0179 *
## smoke
                                    8.107 5.18e-16 ***
## age
                0.042696
                           0.005266
                0.444804
                           0.111906
                                     3.975 7.04e-05 ***
## male
## exercise
                0.189172
                           0.143432
                                    1.319
                                             0.1872
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 2179.0 on 1978 degrees of freedom
## Residual deviance: 1993.1 on 1973 degrees of freedom
## AIC: 2005.1
## Number of Fisher Scoring iterations: 4
###Step2
##Modeling
#Since the outcome variable is binary, choose logistic regression (glm)
model2 <- glm(heart ~ . + smoke*male, family = binomial, data = df1)</pre>
summary(model2)
##
## Call:
## glm(formula = heart ~ . + smoke * male, family = binomial, data = df1)
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept) -4.634221
                          0.384024 -12.068 < 2e-16 ***
## bp
              ## smoke
                                            0.8667
              -0.028744 0.171281 -0.168
              0.041602
                          0.005281
                                   7.878 3.33e-15 ***
## age
## male
              0.044772
                         0.196567
                                    0.228
                                            0.8198
              0.198499
                          0.143679 1.382
                                            0.1671
## exercise
## smoke:male 0.591985
                                   2.472
                                            0.0134 *
                          0.239503
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 2179 on 1978 degrees of freedom
## Residual deviance: 1987 on 1972 degrees of freedom
## AIC: 2001
##
## Number of Fisher Scoring iterations: 4
###Step3
##Model fit
#test overall model fit
hoslem.test(model1$y, model1$fitted.values)
##
##
   Hosmer and Lemeshow goodness of fit (GOF) test
##
## data: model1$y, model1$fitted.values
## X-squared = 13.53, df = 8, p-value = 0.09487
hoslem.test(model2$y, model2$fitted.values)
##
##
   Hosmer and Lemeshow goodness of fit (GOF) test
##
## data: model2$y, model2$fitted.values
## X-squared = 13.677, df = 8, p-value = 0.09058
#comparing 2 models
lmtest::lrtest(model2, model1)
## Likelihood ratio test
##
## Model 1: heart ~ bp + smoke + age + male + exercise + smoke * male
## Model 2: heart ~ bp + smoke + age + male + exercise
    #Df LogLik Df Chisq Pr(>Chisq)
## 1
     7 -993.51
## 2
      6 -996.57 -1 6.1138
                             0.01341 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
The Hosmer and Lemeshow Test result (p = 0.095 and 0.091) indicates that 2 models are good fit.
The likelihood ratio test has p-value = 0.0134, so we reject the null hypothesis and concludes that model2
```

(interaction effect model) has better fit.

```
#unique(which(abs(rstandard(model1)) > 2))
#unique(which(abs(rstandard(model2)) > 2))
# Calculate Pearson Residuals
pearson_res1 <- residuals(model1, type = "pearson")
pearson_res2 <- residuals(model2, type = "pearson")

outlier_threshold1 <- 2 * sd(pearson_res1)
outliers1 <- which(abs(pearson_res1) > outlier_threshold1)
df1[outliers1, ]
```

```
##
        heart bp smoke age male exercise
## 4
            1 0
                      1 51
                               1
                                         1
## 5
            1
               0
                         66
                               0
                                         1
## 7
            1
               1
                      0
                         53
                               0
                                         0
## 25
            1
               1
                      0
                         58
                               0
                                         0
            1 0
                                         0
## 40
                         76
                               0
                      0
## 75
            1 0
                         65
                                         0
                      1
                               0
## 86
            1 0
                      1
                         74
                               0
                                         0
## 99
            1
               0
                      0
                         60
                               0
                                         1
                                         0
## 104
            1 1
                      1
                         54
                               0
## 124
            1 1
                                         0
                      0
                         50
                               1
               0
## 149
            1
                      0
                         51
                                         0
                               0
            1 1
                                         0
## 157
                      1
                         44
                               1
## 166
            1 0
                         62
                                         0
## 170
            1 1
                         54
                                         0
                      1
                               0
## 175
            1
               0
                      0
                         64
                               1
                                         0
## 176
            1 0
                      0
                         49
                                         0
                               0
## 189
            1 0
                      0
                         47
                               1
                                         0
## 259
            1
               0
                      0
                         59
                               0
                                         1
## 267
            1
               0
                      0
                         54
                               1
                                         0
## 305
            1 0
                         74
                                         0
                               0
                      1
## 337
            1 0
                         69
                               0
                                         1
                      1
               0
## 352
            1
                         52
                                         0
                      1
                               0
## 422
            1
               1
                      1
                         56
                               0
                                         0
## 423
            1 0
                                         0
                      0
                         62
                               1
## 458
            1
               0
                      1
                         45
                                         0
                               1
               0
## 466
                         70
                                         0
            1
                      1
                               0
## 469
            1
               0
                         67
                                         1
                      1
                               0
## 500
            1 0
                                         0
                      1
                         62
                               1
## 528
            1 0
                      1
                         65
                               0
                                         1
## 530
            1
               0
                      1
                         63
                               1
                                         0
## 552
            1 0
                         49
                                         0
                      1
                               1
## 566
            1 0
                      0
                         46
                               1
                                         0
## 573
            1
               0
                         64
                                         0
                      1
                               0
## 582
            1
               0
                      1
                         47
                               1
                                         0
## 610
            1 0
                         73
                                         0
                      1
                               0
## 617
            1 0
                      1
                         51
                               1
                                         0
## 634
            1 0
                         74
                                         0
                               0
                      1
## 657
            1
               0
                      0
                         53
                                         0
                               1
## 678
            1 0
                                         0
                      1
                         62
                               0
## 692
            1 1
                      0 63
                               0
                                         0
## 693
            1 0
                         62
                                         0
                      0
                               1
            1 0
## 714
                      0 64
                               1
                                         0
## 721
            1 0
                      1 58
                               1
```

| ## | 735 | 1 | 0 | 1 | 64 | 1 | 0 |
|----|------|---|---|---|----|---|---|
| ## | 749 | 1 | 1 | 1 | 54 | 0 | 0 |
| ## | 755 | 1 | 0 | 1 | 61 | 1 | 1 |
| ## | 762 | 1 | 0 | 0 | 56 | 0 | 1 |
| ## | 784 | 1 | 0 | 1 | 65 | 0 | 0 |
| ## | 801 | 1 | 1 | 1 | 53 | 0 | 0 |
| | 809 | 1 | 1 | 1 | 52 | 0 | 0 |
| | 872 | 1 | 0 | 1 | 46 | 1 | 0 |
| | 877 | 1 | 1 | 1 | 45 | 1 | 0 |
| ## | 941 | 1 | 0 | 1 | 50 | 0 | 1 |
| ## | 947 | 1 | 0 | 1 | 76 | 0 | 0 |
| ## | 954 | 1 | 0 | 0 | 51 | 1 | 0 |
| | | 1 | | | 60 | | |
| ## | 971 | | 0 | 1 | | 1 | 0 |
| ## | 981 | 1 | 1 | 1 | 53 | 0 | 0 |
| ## | 991 | 1 | 0 | 0 | 76 | 0 | 0 |
| ## | 1003 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1071 | 1 | 0 | 0 | 66 | 1 | 1 |
| ## | 1088 | 1 | 1 | 0 | 56 | 0 | 0 |
| ## | 1114 | 1 | 0 | 0 | 43 | 1 | 0 |
| ## | 1121 | 1 | 0 | 0 | 53 | 1 | 1 |
| ## | 1128 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1142 | 1 | 0 | 1 | 59 | 0 | 0 |
| ## | 1149 | 1 | 1 | 0 | 56 | 0 | 0 |
| ## | 1209 | 1 | 0 | 1 | 62 | 0 | 0 |
| ## | 1221 | 1 | 1 | 0 | 52 | 1 | 0 |
| ## | 1231 | 1 | 1 | 1 | 45 | 0 | 0 |
| ## | 1271 | 1 | 1 | 0 | 52 | 1 | 0 |
| ## | 1292 | 1 | 0 | 1 | 64 | 1 | 0 |
| ## | 1300 | 1 | 0 | 0 | 48 | 0 | 0 |
| ## | 1345 | 1 | 0 | 0 | 77 | 0 | 1 |
| ## | 1353 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1363 | 1 | 0 | 0 | 76 | 0 | 0 |
| | | | | | | | |
| ## | 1383 | 1 | 1 | 0 | 55 | 0 | 0 |
| ## | 1398 | 1 | 0 | 1 | 74 | 0 | 0 |
| ## | 1413 | 1 | 0 | 1 | 52 | 1 | 0 |
| ## | 1447 | 1 | 1 | 1 | 48 | 0 | 0 |
| ## | 1461 | 1 | 0 | 1 | 73 | 0 | 0 |
| ## | 1489 | 1 | 0 | 1 | 67 | 0 | 0 |
| ## | 1504 | 1 | 0 | 0 | 50 | 0 | 1 |
| ## | 1530 | 1 | 1 | 0 | 52 | 1 | 0 |
| ## | 1535 | 1 | 0 | 1 | 70 | 0 | 0 |
| ## | 1539 | 1 | 0 | 0 | 78 | 0 | 0 |
| ## | 1569 | 1 | 1 | 0 | 58 | 0 | 0 |
| ## | 1576 | 1 | 1 | 0 | 56 | 0 | 0 |
| ## | 1582 | 1 | 1 | 0 | 46 | 0 | 0 |
| ## | 1606 | 1 | 0 | 0 | 53 | 1 | 0 |
| ## | 1611 | 1 | 0 | 1 | 59 | 0 | 0 |
| ## | 1612 | 1 | 1 | 1 | 54 | 0 | 0 |
| ## | 1628 | 1 | 0 | 0 | 63 | 1 | 1 |
| ## | 1640 | 1 | 0 | 1 | 61 | 1 | 0 |
| ## | 1650 | 1 | 0 | 0 | 64 | 1 | 0 |
| ## | 1671 | 1 | 0 | 0 | 57 | 0 | 0 |
| | | | | 1 | | | |
| ## | 1705 | 1 | 1 | | 53 | 0 | 0 |
| ## | 1768 | 1 | 0 | 0 | 73 | 0 | 0 |
| | | | | | | | |

```
## 1804
                 0
                           76
             1
                        0
                                  0
                                            0
                 0
## 1811
             1
                           71
                                  0
                                            0
                        1
## 1838
             1
                 0
                                            0
                           76
                                  0
## 1844
             1
                 0
                           58
                                            1
                        1
                                  1
## 1849
             1
                 1
                        1
                           50
                                  0
                                            0
## 1853
             1
                 0
                           59
                                            0
                        1
                                  1
## 1859
             1
                 1
                        0
                           51
                                  0
                                            0
## 1889
                 0
                           65
             1
                        0
                                  1
                                            1
## 1891
             1
                 0
                        1
                           72
                                  0
                                            0
## 1892
             1
                 0
                           46
                                  0
                                            0
                        1
## 1906
             1
                 0
                        0
                           63
                                  0
                                            1
## 1915
                           49
                                            0
             1
                 1
                        0
                                  1
## 1920
             1
                 0
                           58
                                  0
                                            0
                        1
                 0
                                            0
## 1955
             1
                        0
                           57
                                  1
## 1959
             1
                 1
                           52
                                  0
                                            0
                        1
## 1969
             1
                 0
                        1
                           65
                                  1
                                            0
outlier_threshold2 <- 2 * sd(pearson_res2)</pre>
outliers2 <- which(abs(pearson_res2) > outlier_threshold2)
df1[outliers2, ]
```

| ## | 552 | 1 | 0 | 1 | 49 | 1 | 0 |
|----|------|---|---|---|----------------|---|---|
| ## | 566 | 1 | 0 | 0 | 46 | 1 | 0 |
| ## | 573 | 1 | 0 | 1 | 64 | 0 | 0 |
| ## | 582 | 1 | 0 | 1 | 47 | 1 | 0 |
| | | | | 1 | | | |
| ## | 586 | 1 | 1 | | 58 | 0 | 0 |
| ## | 610 | 1 | 0 | 1 | 73 | 0 | 0 |
| ## | 617 | 1 | 0 | 1 | 51 | 1 | 0 |
| ## | 634 | 1 | 0 | 1 | 74 | 0 | 0 |
| ## | 657 | 1 | 0 | 0 | 53 | 1 | 0 |
| ## | 678 | 1 | 0 | 1 | 62 | 0 | 0 |
| ## | 693 | 1 | 0 | 0 | 62 | 1 | 0 |
| ## | 714 | 1 | 0 | 0 | 64 | 1 | 0 |
| ## | 721 | 1 | 0 | 1 | 58 | 1 | 0 |
| ## | 749 | 1 | 1 | 1 | 54 | 0 | 0 |
| ## | 751 | 1 | 1 | 1 | 58 | 0 | 0 |
| ## | 762 | 1 | 0 | 0 | 56 | 0 | 1 |
| ## | 784 | 1 | 0 | 1 | 65 | 0 | 0 |
| ## | 801 | 1 | 1 | 1 | 53 | 0 | 0 |
| ## | 809 | 1 | 1 | 1 | 52 | 0 | 0 |
| ## | 872 | 1 | 0 | 1 | 46 | 1 | 0 |
| ## | 899 | 1 | 1 | 1 | 58 | 0 | 0 |
| ## | 941 | 1 | 0 | 1 | 50 | 0 | 1 |
| ## | 947 | 1 | 0 | 1 | 76 | 0 | 0 |
| ## | 954 | 1 | 0 | 0 | 51 | 1 | 0 |
| ## | 971 | 1 | 0 | 1 | 60 | 1 | 0 |
| ## | 981 | 1 | 1 | 1 | 53 | 0 | 0 |
| ## | 991 | 1 | 0 | 0 | 76 | 0 | 0 |
| ## | 1003 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1003 | 1 | 1 | 0 | 5 9 | 1 | 0 |
| ## | 1013 | 1 | 1 | 1 | | 0 | 0 |
| | 1013 | | | | 58 | | 1 |
| ## | | 1 | 0 | 0 | 66 | 1 | |
| ## | 1087 | 1 | 1 | 1 | 54 | 0 | 1 |
| ## | 1088 | 1 | 1 | 0 | 56 | 0 | 0 |
| ## | 1114 | 1 | 0 | 0 | 43 | 1 | 0 |
| ## | 1121 | 1 | 0 | 0 | 53 | 1 | 1 |
| ## | 1128 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1131 | 1 | 0 | 0 | 76 | 1 | 0 |
| ## | 1142 | 1 | 0 | 1 | 59 | 0 | 0 |
| ## | 1149 | 1 | 1 | 0 | 56 | 0 | 0 |
| ## | 1209 | 1 | 0 | 1 | 62 | 0 | 0 |
| ## | 1221 | 1 | 1 | 0 | 52 | 1 | 0 |
| ## | 1231 | 1 | 1 | 1 | 45 | 0 | 0 |
| ## | 1271 | 1 | 1 | 0 | 52 | 1 | 0 |
| ## | 1300 | 1 | 0 | 0 | 48 | 0 | 0 |
| ## | 1350 | 1 | 0 | 0 | 76 | 1 | 0 |
| ## | 1353 | 1 | 0 | 1 | 59 | 1 | 0 |
| ## | 1363 | 1 | 0 | 0 | 76 | 0 | 0 |
| ## | 1383 | 1 | 1 | 0 | 55 | 0 | 0 |
| ## | 1398 | 1 | 0 | 1 | 74 | 0 | 0 |
| ## | 1413 | 1 | 0 | 1 | 52 | 1 | 0 |
| ## | 1447 | 1 | 1 | 1 | 48 | 0 | 0 |
| ## | 1450 | 1 | 0 | 0 | 76 | 1 | 0 |
| ## | 1461 | 1 | 0 | 1 | 73 | 0 | 0 |
| ## | 1489 | 1 | 0 | 1 | 67 | 0 | 0 |
| | | | | | | | |

```
## 1504
            1 0
                      0 50
                                0
            1 1
## 1530
                      0
                         52
                                1
                                         0
## 1535
            1 0
                         70
                                         0
## 1539
            1 0
                         78
                                0
                                         0
                      0
## 1569
            1
               1
                      0
                         58
                                0
                                         0
## 1576
            1
               1
                      0
                         56
                                0
                                         0
## 1579
            1
               0
                      0
                         75
                                         0
                                1
## 1582
            1
               1
                      0
                         46
                                         0
                                0
## 1606
            1
               0
                      0
                         53
                                1
                                         0
            1 0
## 1611
                         59
                                0
                                         0
                      1
## 1612
            1 1
                      1
                         54
                                0
                                         0
## 1628
            1
               0
                         63
                      0
                                         1
                                1
## 1640
            1
               0
                         61
                                         0
                      1
                                1
## 1650
               0
                                         0
            1
                      0
                         64
                                1
## 1671
            1
               0
                      0
                         57
                                0
                                         0
## 1705
            1
               1
                      1
                         53
                                0
                                         0
## 1768
            1
               0
                      0
                         73
                                0
                                         0
## 1775
            1 0
                         71
                      0
                                1
                                         1
## 1802
            1 1
                         52
                                0
                                         1
                      1
## 1804
            1
               0
                         76
                                         0
                      0
                                0
## 1811
            1
               0
                      1
                         71
                                0
                                         0
## 1838
            1
               0
                         76
                                         0
## 1844
            1
               0
                         58
                                         1
                      1
                                1
## 1849
            1
               1
                      1
                         50
                                0
                                         0
## 1853
            1 0
                                         0
                      1
                         59
                                1
## 1859
            1 1
                      0
                         51
                                0
                                         0
## 1889
            1
               0
                      0
                         65
                                1
                                         1
## 1891
            1
               0
                         72
                                0
                                         0
                      1
            1 0
## 1892
                         46
                                0
                                         0
                      1
## 1906
            1 0
                      0
                         63
                                0
                                         1
## 1915
            1 1
                      0
                         49
                                1
                                         0
## 1920
            1
               0
                      1
                         58
                                0
                                         0
## 1955
            1 0
                         57
                                         0
                      0
                                1
## 1959
            1 1
                      1 52
                                0
                                         0
# Calculate Deviance Residuals
deviance_res1 <- residuals(model1, type = "deviance")</pre>
deviance_res2 <- residuals(model2, type = "deviance")</pre>
outlier_threshold1 <- 2 * sd(deviance_res1)</pre>
outliers1 <- which(abs(deviance_res1) > outlier_threshold1)
df1[outliers1, ]
##
        heart bp smoke age male exercise
## 5
            1
               0
                         66
                                0
                      0
                                         1
## 75
               0
            1
                         65
                                         0
                      1
                                0
## 99
            1
               0
                      0
                         60
                                0
                                         1
## 149
            1 0
                                         0
                         51
                                0
                      0
## 176
            1 0
                      0
                         49
                                0
                                         0
## 189
               0
                         47
                                         0
            1
                      0
                                1
## 259
            1 0
                      0
                         59
                                0
                                         1
## 267
            1 0
                                         0
                      0
                         54
                                1
## 352
            1 0
                      1
                         52
                                0
                                         0
## 458
            1 0
                                         0
                      1 45
                                1
            1 0
## 552
                      1 49
                                1
                                         0
```

```
## 566
             1
                0
                          46
                                            0
                        0
                                  1
## 573
             1
                 0
                        1
                           64
                                  0
                                            0
## 582
             1
                 0
                                            0
                           47
## 617
             1
                 0
                           51
                                            0
                        1
                                  1
                 0
## 657
             1
                        0
                           53
                                  1
                                            0
## 678
             1
                 0
                        1
                           62
                                  0
                                            0
## 762
             1
                 0
                        0
                           56
                                  0
                                            1
## 784
                 0
             1
                           65
                                            0
                        1
                                  0
## 872
             1
                 0
                        1
                           46
                                  1
                                            0
## 941
             1
                 0
                           50
                                  0
                                            1
                        1
## 954
             1
                 0
                        0
                           51
                                  1
                                            0
## 1114
             1
                 0
                           43
                                            0
                        0
                                  1
## 1121
             1
                 0
                        0
                           53
                                  1
                                            1
                 0
                                            0
## 1142
             1
                        1
                           59
                                  0
## 1209
             1
                 0
                        1
                           62
                                  0
                                            0
## 1231
             1
                 1
                        1
                           45
                                  0
                                            0
## 1300
             1
                 0
                        0
                           48
                                  0
                                            0
## 1413
             1
                 0
                           52
                                            0
                                  1
## 1504
                 0
             1
                        0
                           50
                                  0
                                            1
## 1582
             1
                           46
                                            0
                 1
                        0
                                  0
## 1606
             1
                 0
                        0
                           53
                                  1
                                            0
## 1611
             1
                 0
                        1
                           59
                                  0
                                            0
## 1671
             1
                 0
                                            0
                        0
                           57
                                  0
## 1859
             1
                 1
                        0
                           51
                                  0
                                            0
## 1892
             1
                0
                                            0
                        1
                           46
                                  0
## 1906
             1
                0
                        0
                           63
                                  0
                                            1
## 1920
             1
                 0
                        1
                           58
                                  0
                                            0
## 1955
             1
                 0
                        0
                           57
                                  1
                                            0
```

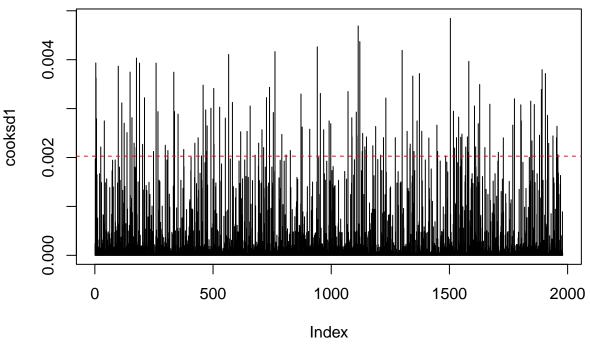
```
outlier_threshold2 <- 2 * sd(deviance_res2)
outliers2 <- which(abs(deviance_res2) > outlier_threshold2)
df1[outliers2, ]
```

```
##
         heart bp smoke age male exercise
## 75
             1
                0
                       1
                           65
                                  0
                                            0
## 99
             1
                0
                       0
                           60
                                  0
                                            1
## 149
             1
                0
                       0
                           51
                                  0
                                            0
## 166
                0
                           62
                                            0
             1
                       0
                                  1
## 175
             1
                0
                           64
                                            0
                       0
                                  1
## 176
             1
                0
                                            0
                       0
                           49
                                  0
## 189
             1
                0
                       0
                           47
                                            0
                                  1
## 259
             1
                0
                       0
                           59
                                  0
                                            1
## 267
             1
                0
                       0
                           54
                                            0
                                  1
## 352
             1
                0
                       1
                           52
                                  0
                                            0
## 423
             1
                0
                           62
                                            0
                       0
                                  1
## 458
             1
                0
                       1
                           45
                                  1
                                            0
## 552
             1
                0
                           49
                                            0
                       1
                                  1
## 566
             1
                0
                           46
                                  1
                                            0
## 573
                0
                                            0
             1
                           64
                                  0
                       1
## 582
             1
                0
                       1
                           47
                                            0
                                  1
                0
## 617
             1
                       1
                           51
                                  1
                                            0
## 657
             1
                0
                       0
                           53
                                            0
                                  1
## 678
                0
                           62
                                            0
             1
                       1
                                  0
## 693
             1
                0
                       0
                           62
                                  1
                                            0
             1
                0
                           64
                                            0
## 714
                       0
                                  1
```

```
## 762
              1
                 0
                            56
                                   0
                                              1
              1
                 0
                                              0
##
   784
                         1
                            65
                                   0
   872
                                              0
                            46
## 941
              1
                 0
                            50
                                              1
                         1
                                   0
                 0
                                              0
## 954
              1
                         0
                            51
                                   1
## 1114
              1
                 0
                         0
                            43
                                              0
                                   1
## 1121
              1
                 0
                         0
                            53
                                   1
                                              1
                                              0
## 1142
              1
                 0
                            59
                         1
                                   0
## 1209
              1
                 0
                         1
                            62
                                   0
                                              0
## 1231
              1
                 1
                            45
                                   0
                                              0
                         1
## 1300
              1
                 0
                         0
                            48
                                   0
                                              0
## 1413
              1
                 0
                            52
                                              0
                         1
                                   1
## 1489
              1
                 0
                         1
                            67
                                   0
                                              0
## 1504
              1
                 0
                         0
                            50
                                   0
                                              1
## 1582
              1
                 1
                         0
                            46
                                   0
                                              0
                 0
## 1606
              1
                         0
                            53
                                   1
                                              0
## 1611
              1
                 0
                            59
                                   0
                                              0
                         1
## 1650
              1
                 0
                            64
                                              0
                                   1
                                              0
## 1671
              1
                 0
                         0
                            57
                                   0
## 1892
              1
                 0
                                              0
                            46
                                   0
                                              0
## 1920
              1
                 0
                         1
                            58
                                   0
## 1955
              1
                                              0
```

```
# Cook's distance
cooksd1 <- cooks.distance(model1)
plot(cooksd1, type="h", main="Cook's Distance") %>%
abline(h = 4/(nrow(df1)-length(coef(model1))), col = "red", lty = 2)
```

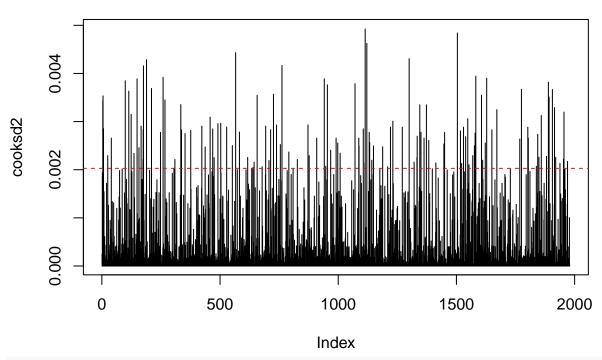
Cook's Distance



```
cooksd2 <- cooks.distance(model2)
plot(cooksd2, type="h", main="Cook's Distance") %>%
```

```
abline(h = 4/(nrow(df1)-length(coef(model2))), col = "red", lty = 2)
```

Cook's Distance



```
summary(cooksd1)
```

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 9.134e-06 6.223e-05 1.753e-04 5.140e-04 5.166e-04 4.844e-03

summary(cooksd2)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 1.273e-05 6.175e-05 1.818e-04 5.138e-04 5.048e-04 4.925e-03

We find the cook's distance is small suggests the outliers do not affect the model that much.

###Case 2

###Data Preparation

##Data importing

df2 <- df[,c("health", "depress", "alcage", "cigage", "age", "bp")]</pre>

#Data Description

describe(df2)

```
##
                               sd median trimmed
                                                                        skew kurtosis
                      mean
                                                    mad min max range
## health
              1 1979
                      1.74
                             0.87
                                       2
                                             1.62
                                                   1.48
                                                          1
                                                                        0.98
                                                                                 0.14
                      0.08
                            0.27
                                             0.00
                                                   0.00
                                                                        3.10
                                                                                 7.60
## depress
                1979
                                       0
                                                          0
                                                              1
                                                                     1
                                      17
## alcage
              3 1979 17.66
                            3.83
                                            17.51
                                                   1.48
                                                             69
                                                                        2.53
                                                                                25.49
                                                          1
                                                                    68
                                                   2.97
                                                          3
                                                                        2.02
                                                                                14.80
## cigage
              4 1979 15.63 4.33
                                      16
                                            15.47
                                                             60
                                                                    57
## age
              5 1979 64.09 11.01
                                      64
                                            63.86 11.86
                                                         39
                                                             92
                                                                    53
                                                                       0.16
                                                                                -0.68
## bp
              6 1979 0.51 0.50
                                             0.51 0.00
                                                                     1 -0.05
                                                                                -2.00
                                       1
                                                          0
                                                              1
##
             se
```

```
## health 0.02
## depress 0.01
## alcage 0.09
## cigage 0.10
## age
          0.25
          0.01
## bp
lapply(df2[,c(1,2,6)], table)
## $health
##
##
    1
        2
            3
## 963 659 257 100
##
## $depress
##
##
          1
## 1821
       158
##
## $bp
##
##
     0
          1
## 966 1013
#Bivariable Analysis
cor(df2, method = "spearman")[1, 2:6, drop = F]
##
           depress
                        alcage
                                    cigage
                                                 age
## health 0.1510899 -0.01427585 -0.01183471 0.06569963 0.2452973
health is more related with depress and bp
###Step1
##Modeling
#Since the outcome variable is multicategorical and ordered, we choose cumulative logit model (vglm)
model3 <- vglm(health ~ ., family = cumulative(parallel = TRUE), data = df2)</pre>
summary(model3)
##
## vglm(formula = health ~ ., family = cumulative(parallel = TRUE),
##
      data = df2)
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept):1 0.870987 0.305714
                                      2.849 0.00439 **
## (Intercept):2 2.547893 0.310849
                                     8.197 2.47e-16 ***
## (Intercept):3 4.033825 0.323450 12.471 < 2e-16 ***
                -1.201805
                            0.154374 -7.785 6.97e-15 ***
## depress
## alcage
                 0.003656 0.011935
                                      0.306 0.75934
## cigage
                -0.005030 0.010421 -0.483 0.62931
## age
                ## bp
                -0.945530 0.090151 -10.488 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Names of linear predictors: logitlink(P[Y<=1]), logitlink(P[Y<=2]),</pre>
## logitlink(P[Y<=3])</pre>
##
## Residual deviance: 4305.659 on 5929 degrees of freedom
##
## Log-likelihood: -2152.83 on 5929 degrees of freedom
##
## Number of Fisher scoring iterations: 5
##
## No Hauck-Donner effect found in any of the estimates
##
##
## Exponentiated coefficients:
     depress
                alcage
                           cigage
                                                     bp
## 0.3006510 1.0036629 0.9949824 0.9945215 0.3884738
###Step2
###Step3
##modeling
model4 <- glm(bp ~ age + depress + factor(health), family = 'binomial', data = df2)</pre>
summary(model4)
##
## Call:
## glm(formula = bp ~ age + depress + factor(health), family = "binomial",
##
       data = df2)
##
## Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                    -3.156634 0.299377 -10.544 < 2e-16 ***
                     0.043069
                               0.004533
                                           9.501 < 2e-16 ***
## age
## depress
                    -0.135462
                                0.182238 -0.743
                                                      0.457
## factor(health)2 0.691221
                                0.105434
                                            6.556 5.53e-11 ***
## factor(health)3 1.098250
                                0.153704
                                            7.145 8.98e-13 ***
## factor(health)4 1.968987
                                0.272189
                                            7.234 4.69e-13 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 2742.4 on 1978 degrees of freedom
## Residual deviance: 2517.5 on 1973 degrees of freedom
## AIC: 2529.5
##
## Number of Fisher Scoring iterations: 4
\exp(-3.156634 + 0.043069 \text{age} - 0.135462 \text{depress} + 0.691221 \text{f2} + 1.098250 \text{f3} + 1.968987 \text{f4}) Excellent (health =
1) 1)age=64,depress=0 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 0))) = 40.1\%
2)age=64,depress=1 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 1))) = <math>36.9\%
Diff=40.1\% - 36.9\% = 3.2
Good (health = 2) 1)age=64,depress=0 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 0 +
```

```
(0.691221)) = 57.2\% 2)age=64,depress=1 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 1 + 0.691221))) = 53.9\% Diff=57.2% - 53.9% = 3.3
```

Fair (health = 3) 1)age=64,depress=0 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 0 + 1.098250))) = 66.8% 2)age=64,depress=1 Prob=1/(1 + exp(-(-3.156634 + 0.043069 * 64 - 0.135462 * 1 + 1.098250))) = 63.7% Diff=66.8% -63.7% = 3.1

Poor (health = 4) 1)age=64,depress=0 df2bp < -factor(dfbp, labels = lev Prob=1/(1 + exp(-(-3.156634 + 0.043069*64 - 0.135462*0 + 1.968987))) = 82.8% 2)age=64,depress=1 Prob=1/(1 + exp(-(-3.156634 + 0.043069*64 - 0.135462*1 + 1.968987))) = 80.7% Diff=82.8% - 80.7% = 2.1