

Step 4: Adaptive Time Stepping

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The following plots are for the distance as time increases to $1e4$ and for the force as the distance changes before including adaptive time stepping (step 3 results):

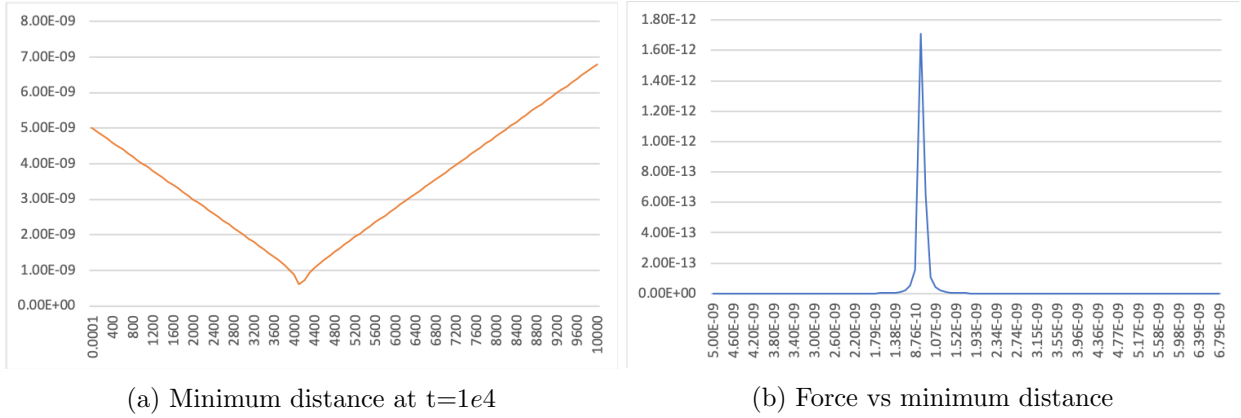


Figure 1: Time step constant at $\delta t = 10^{-4}$

After including adaptive time stepping with a minimum time step of 10^{-8} , the minimum distance value remained less than 10^{-10} and the particles were in constant oscillation (the particles were in a constant attraction and repulsion motion). The following plots demonstrate this result:

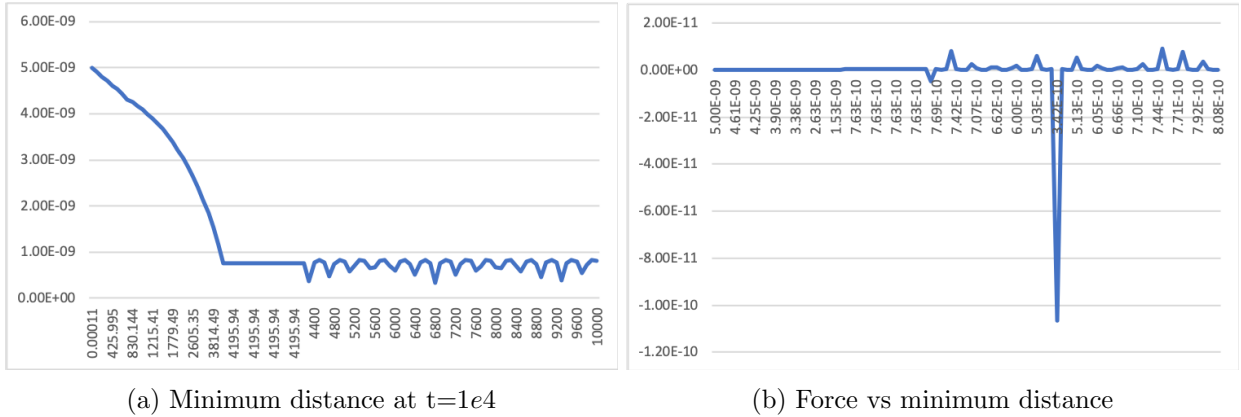


Figure 2: Adaptive time step with minimum $\delta t = 10^{-8}$

The following condition were followed when including adaptive time stepping:

- time step cannot be less than $\delta t = 10^{-18}$.

- minimum distance less than 10^{-9} , the time step must be set to the minimum. This value can be determined by studying the relationship between the distance, the force and the potential. When the particles reach minimum potential the derivative of the force is zero at that point [1]. The distance for the Argon of when this happens is around 3.816×10^{-10} . the force becomes repulsive after this distance is reached hence the negative force in plot-3b, making this a point of interest. This value is overstepped in plot-1b.
- To avoid particles jumping through or into each other, the time step was constantly reduced by a factor of 2 until this expression was satisfied:

$$\delta t \times \max V < \min D x$$

- if non of the above was satisfied the time step increased by a factor of 1.1.

The running time for the algorithm increased significantly after including the adaptive time step compared to the results from step 3. Similar behaviour were obtained when another particle was introduced to the system, however the influence of the third particle affected the force applied on other particles (reduced repulsion force). The following plot demonstrate this:

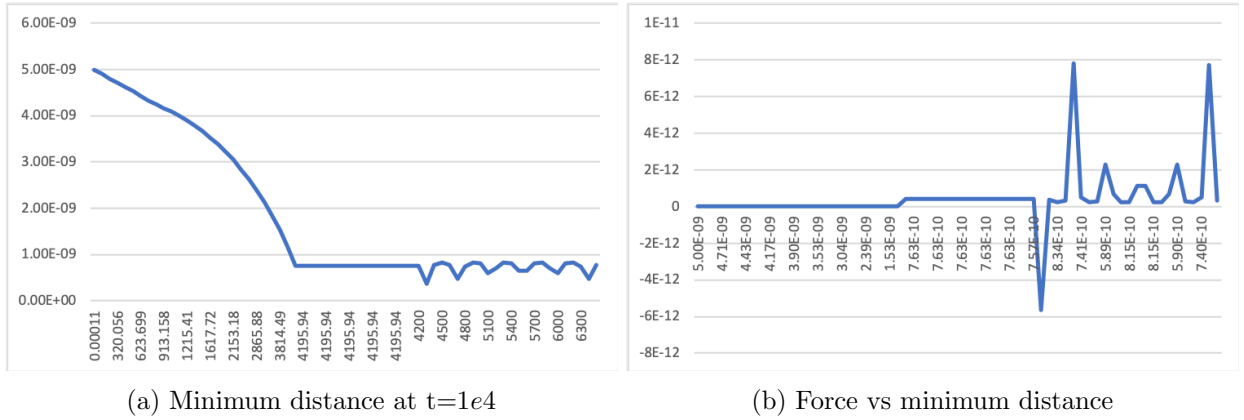


Figure 3: Adaptive time step with minimum $\delta t = 10^{-8}$ for 3 particles

References

- [1] *Lennard-Jones Potential*. [https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Supplemental_Modules_\(Physical_and_Theoretical_Chemistry\)/Physical_Properties_of_Matter/Atomic_and_Molecular_Properties/Intermolecular_Forces/Specific_Interactions/Lennard-Jones_Potential](https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Supplemental_Modules_(Physical_and_Theoretical_Chemistry)/Physical_Properties_of_Matter/Atomic_and_Molecular_Properties/Intermolecular_Forces/Specific_Interactions/Lennard-Jones_Potential). 2018.