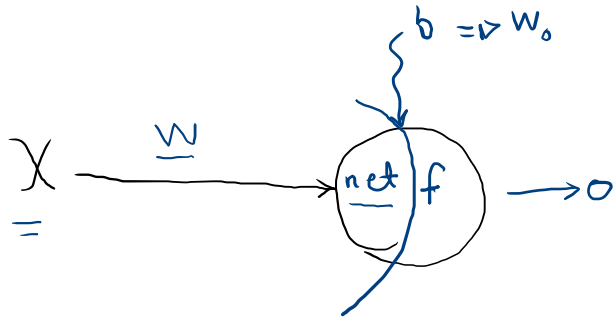


FFNN



Train \rightsquigarrow W :

area	NW	price-home
10	0.5	



$$net = wx + b$$

$$o = f(net)$$

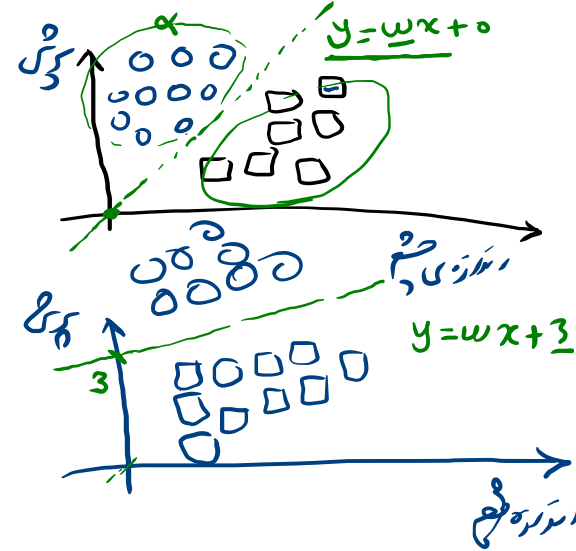
bias

$$net = wx + b$$

linear!

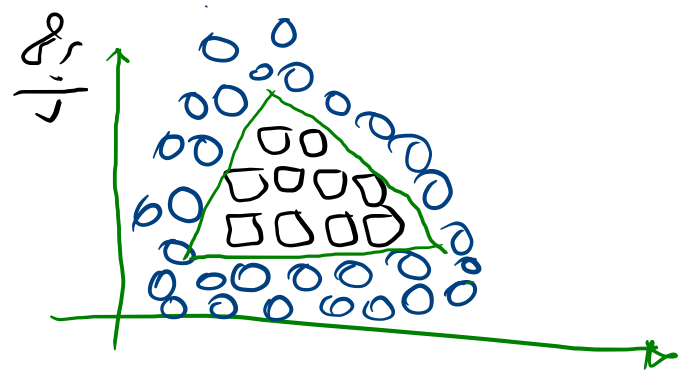
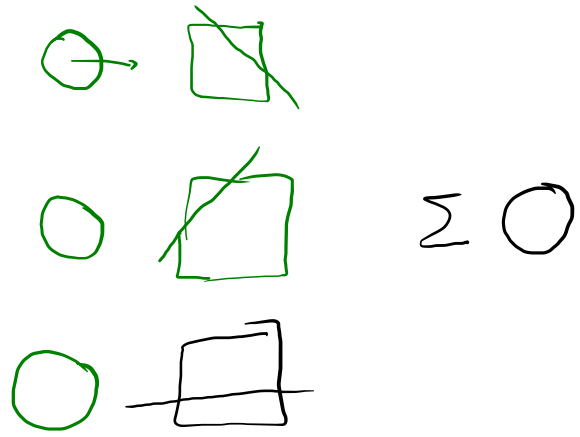
$$y = wx + b$$

linear classifier

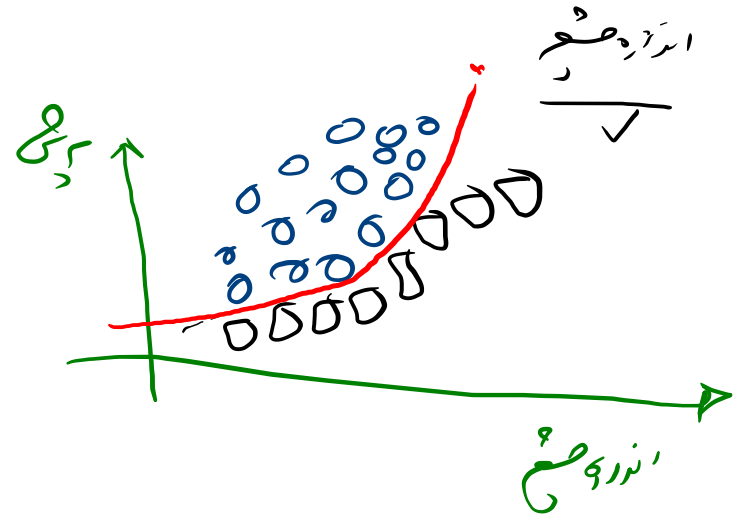


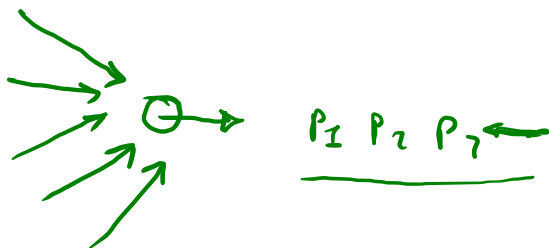
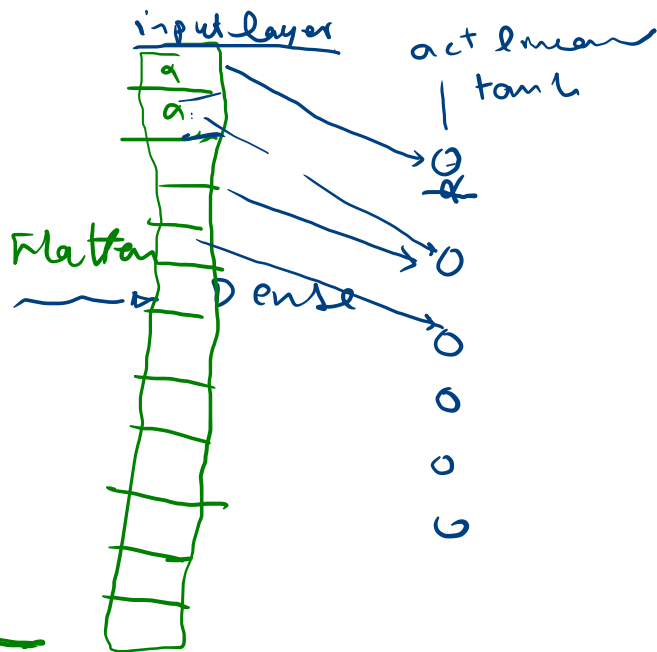
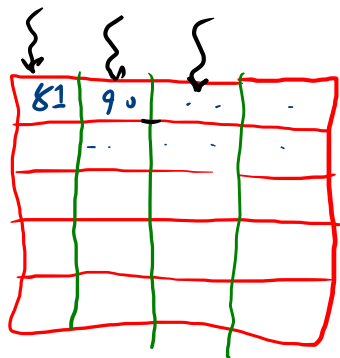
$\frac{\partial f}{\partial x_1}$

$\frac{\partial f}{\partial x_2}$



activat —
non linear.



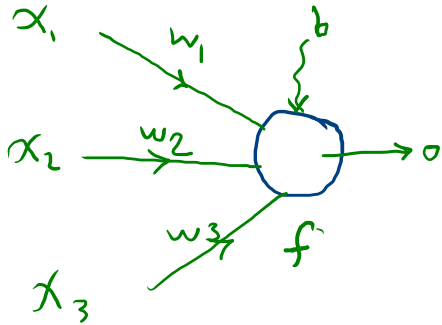


$P_1 P_2 P_3$

\bigcirc $P_1 P_2 P_3 \dots$

\bigcirc P_1
 \bigcirc

$P_1 P_2, P_3 - \bigcirc \rightarrow \text{class!}$



$$\rightarrow \text{net} = \sum_{i=1}^3 \underline{w_i \cdot x_i} + \underline{b}$$

$$\leadsto \text{net} = w_1 x_1 + w_2 x_2 + w_3 x_3 + b$$

$$o = f(\text{net})$$

$$\text{net} = \sum_{i=0}^3 w_i \cdot x_i$$

\downarrow $w_0 = b$
 $x_0 = 1$

M/P

l_0
 $n=1$
input
↓

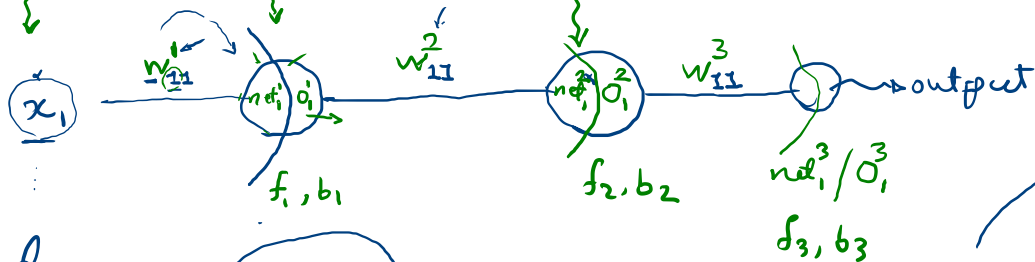
$n=1$
 l_1
↓

$n=2$
 l_2
↓

$n=3$
 l_3

layer
W
act
bias

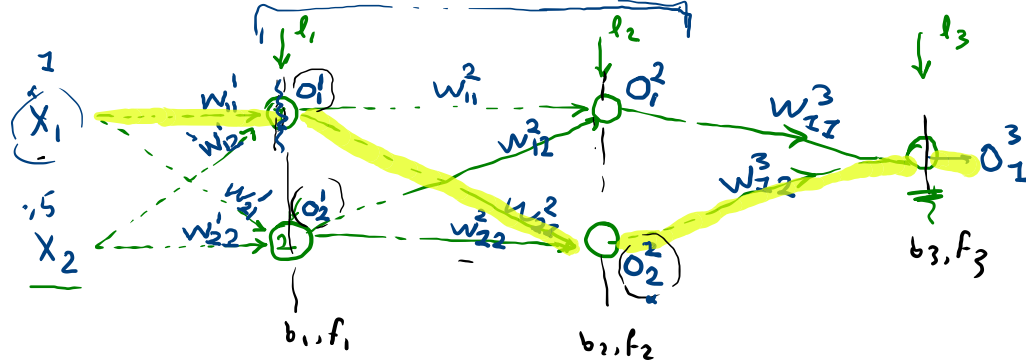
layer
W
act
bias



Feed Forward

$$\begin{aligned} net_1^1 &= w_{11}^1 x_1 + b_1 \\ O_1^1 &= f_1(net_1^1) \\ net_1^2 &= w_{11}^2 O_1^1 + b_2 \\ O_1^2 &= f_2(net_1^2) \end{aligned}$$

$$\begin{aligned} net_1^3 &= w_{11}^3 O_1^2 + b_3 \\ \text{output} &= \underline{O_1^3} = f_3(net_1^3) \end{aligned}$$



n-Hidden Layer > 2

FFNN == Fully Connected

$$net_1^1 = w_{11}^1 X_1 + w_{12}^1 X_2 + b_1$$

$$o_1^1 = f_1(net_1^1)$$

$$net_2^2 = w_{21}^2 o_1^1 + w_{22}^2 \underline{o_2^1} + b_2$$

$$o_2^2 = f_2(net_2^2)$$

$$net_1^3 = w_{11}^3 o_1^2 + w_{12}^3 \underline{o_2^2} + b_3$$

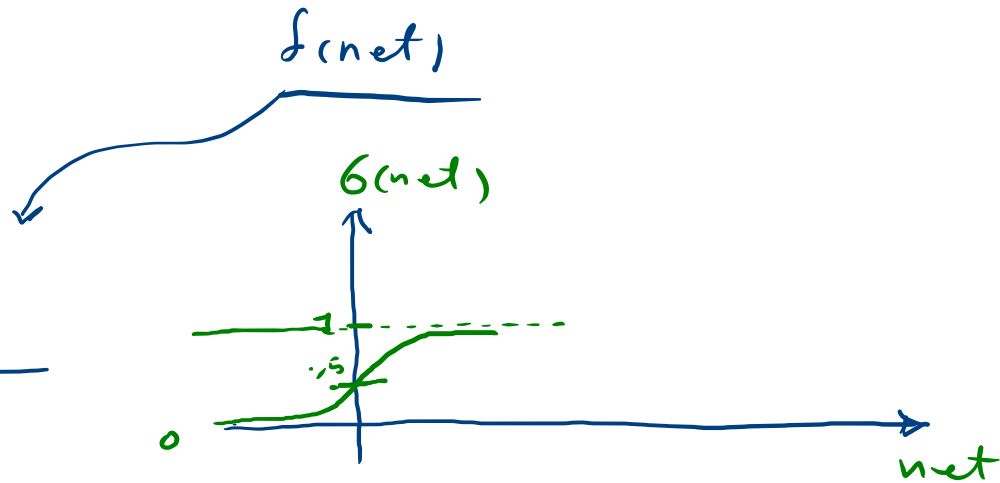
$$o_1^3 = f_3(net_1^3)$$

$$output = o_1^3$$

Activation functions

1. Sigmoid

$$G(\text{net}) = \frac{1}{1 + e^{-\text{net}}}$$



× در این مورد output

× این یک Binary classification داریم!

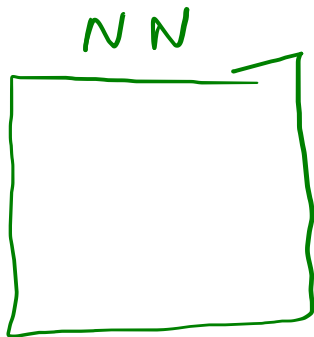
× خیلی محدودیت امکان است!

img



اقدام گزین کردن!

out



Sigmoid



لغات



3, 5

گزینه!

گزینه! 3, 5

گزینه یا نود!

2. Softmax

$$\begin{bmatrix} 1 \\ 4 \\ 5 \end{bmatrix} \text{softmax} \rightarrow \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$b(x_j) = \frac{e^{x_j}}{\sum_i e^{x_i}}$$

$$\frac{e^1}{e^1 + e^4 + e^5} = \frac{e}{e + e^4 + e^5} = \dots$$

$$\frac{e^4}{e^1 + e^4 + e^5} = \dots$$

output α (ناتج)

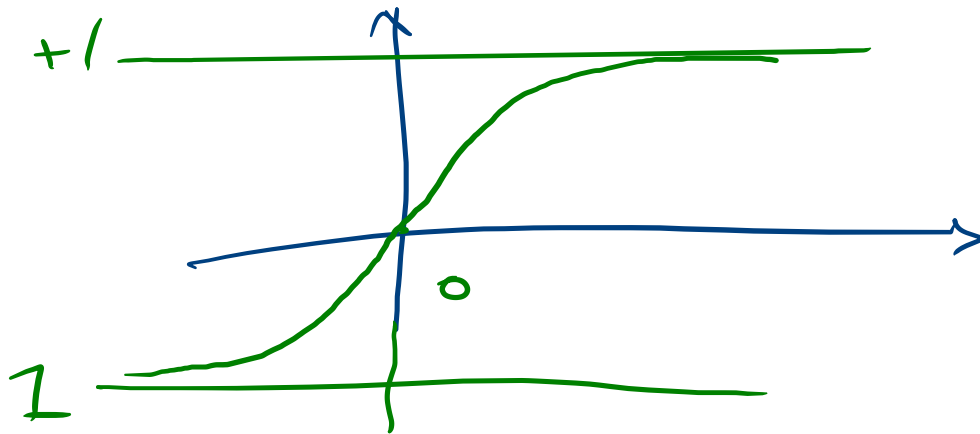
multiclass
classification

تصنيف ثلاثي - ثنائي - ثنائي

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \xrightarrow{\text{softmax}} \begin{bmatrix} 0.7 \rightarrow \text{الاحتمال الأكبر} \\ 0.2 \rightarrow \text{الاحتمال المتوسط} \\ 0.1 \rightarrow \text{الاحتمال الأقل} \end{bmatrix}$$

ناتج

$$3. \tanh = \frac{\sinh(x)}{\cosh(x)} = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



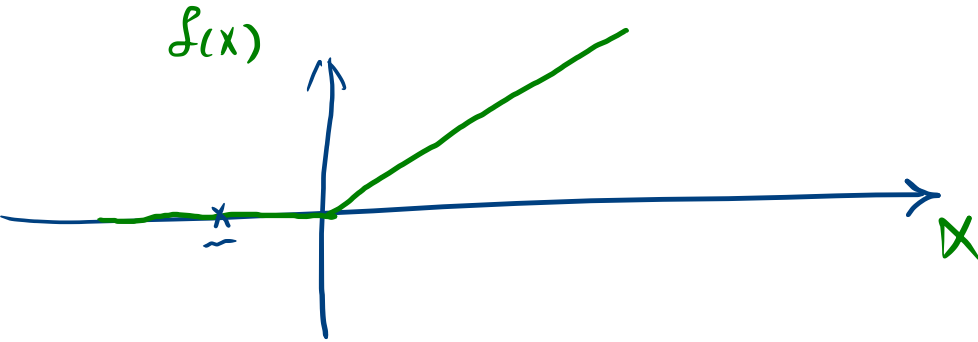
hidden layer

4. Relu

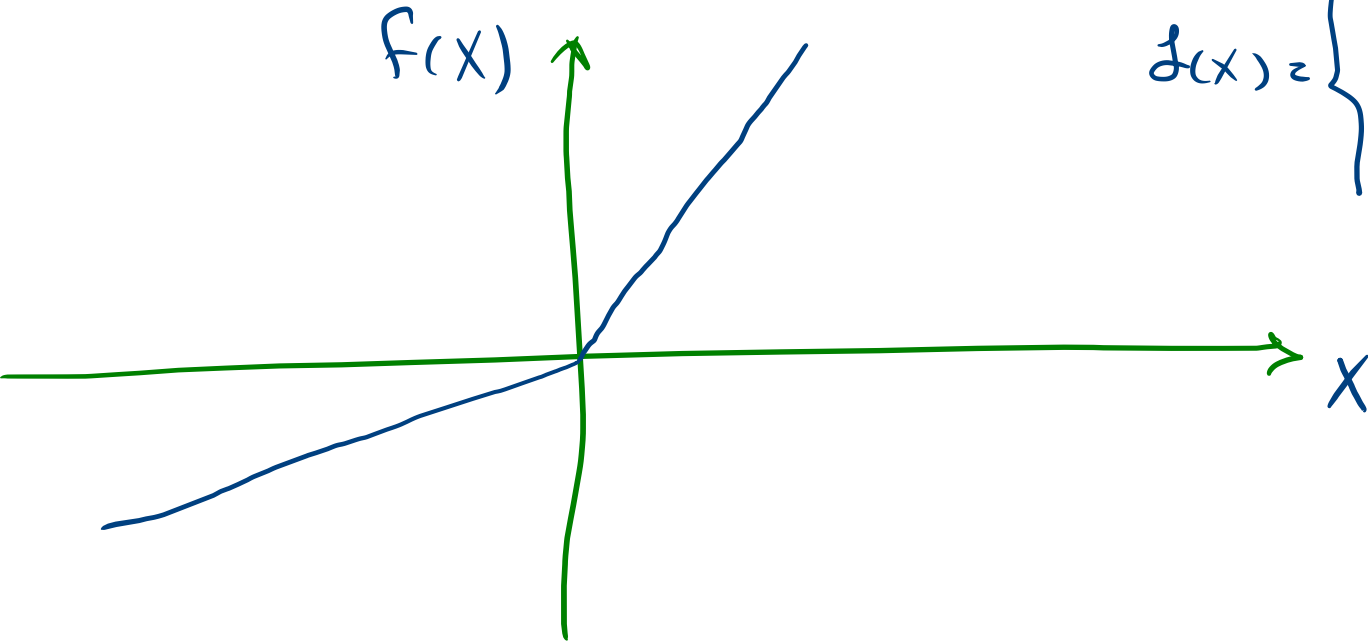
Rectified linear unit

$$f(x) = \max(0, x)$$

$$\text{Relu}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$



5. Leaky Relu



$$f(x) = \begin{cases} x & x \geq 0 \\ \frac{0.5}{1} x & x < 0 \end{cases}$$

tanh vs sigmoid

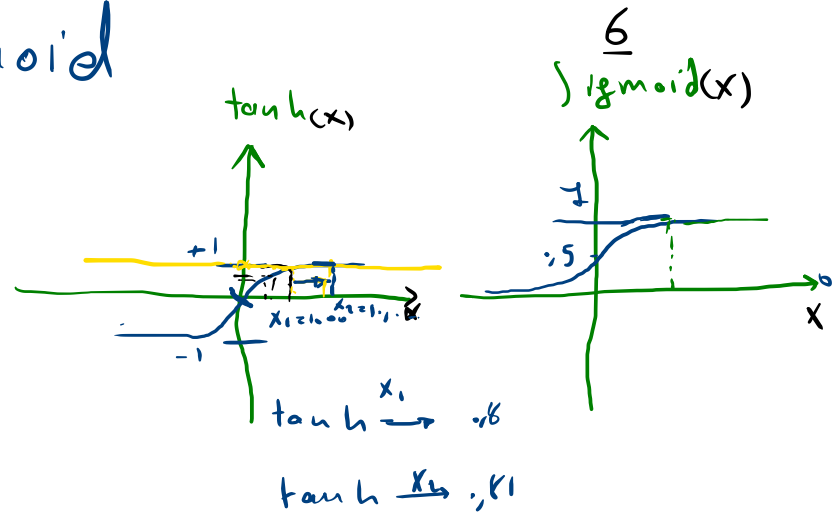
Similarly:

مماثل

diff \rightarrow

tanh \rightarrow mean
0

Sigmoid \rightarrow .5



$0 \leq \sigma \leq 1 \rightarrow$ نسبة

$-1 \leq \tanh \leq 1 \rightarrow$ x

End

