

MATHS

31. The curve $y = ax^3 + bx^2 + cx$ is inclined at 45° to the x-axis at $(0, 0)$ but it touches x-axis at $(1, 0)$ then $(a, b, c) =$
- 1) $(1, -2, 1)$ 2) $(1, 2, 2)$ 3) $(-1, 2, -1)$ 4) $(1, 0, 2)$
32. The abscissa of the point other than origin on the curve $ay^2 = x^3$ the normal at which cuts off equal intercepts on the coordinate axes
- 1) $\frac{a}{2}$ 2) $\frac{4a}{9}$ 3) $\frac{2a}{3}$ 4) $\frac{a}{3}$
33. The value of n for which length of the sub normal of the curve $xy^n = a^{n+1}$ is constant.
- 1) -1 2) -2 3) -3 4) -4
34. If $x = y^2, xy = k$ cut orthogonally then $8k^2 =$
- 1) $\frac{1}{2}$ 2) $\frac{1}{3}$ 3) $\frac{1}{4}$ 4) 1

35. If two curves $\frac{x^2}{a^2} + \frac{y^2}{4} = 1$ and $y^3 = 16x$. Intersect orthogonally then $3a^2 = \underline{\hspace{2cm}}$
- 1) 1 2) 2 3) 3 4) 4
36. If at each point of the curve $y = x^3 - ax^2 + x + 1$ the tangent is inclined at an acute angle with positive direction of x-axis then range of a is
- 1) $(1, \infty)$ 2) $(0, \infty)$ 3) $(-1, 4)$ 4) $(-\sqrt{3}, \sqrt{3})$
37. If the tangent at (a, b) to the curve $x^3 + y^3 = c^3$ meets the curve again at (a_1, b_1) then $\frac{a_1}{a} + \frac{b_1}{b} =$
- 1) 1 2) -1 3) 2 4) -2
38. The equation of tangent to the curve $y = (2x - 1)e^{2(1-x)}$ at the point of its maximum.
- 1) $x = 1$ 2) $y = 1$ 3) $x + y = 1$ 4) $x - y = 1$

39. If the tangent to the curve $2y^3 = ax^2 + x^3$ at the point (a, a) cuts off intercepts α, β on the coordinate axes where $\alpha^2 + \beta^2 = 61$ then $|a| =$ _____
- 1) 16 2) 28 3) 30 4) 31
40. If the tangent at $(1, 1)$ on $y^2 = x(2 - x)^2$ meets the curve again at P then P =
- 1) $\left(\frac{9}{4}, \frac{3}{8}\right)$ 2) $(2, 0)$ 3) $\left(\frac{9}{8}, \frac{3}{4}\right)$ 4) $\left(\frac{1}{2}, \frac{3}{2}\right)$
41. An electric lamp is at a height of 20ft above the floor. An object falls freely under gravity starting from the rest at the same height as the lamp but at a horizontal distance 5ft from it. The speed of the shadow of the object on the floor when it has fallen through 16 ft.
- 1) $\frac{-5}{2} \text{ ft/sec}$ 2) $\frac{-15}{4} \text{ ft/sec}$ 3) $\frac{-25}{2} \text{ ft/sec}$ 4) -25 ft/sec
42. A point P – moves on the curves $y = 2x^2$ at 4 feet per second. At what rate the inclination of tangent to the curve at P changing when P – passes through $(1, 2)$.
- 1) $\frac{16}{\sqrt{17}} \text{ rad/sec}$ 2) $\frac{16}{17\sqrt{17}} \text{ rad/sec}$ 3) $\frac{16}{17} \text{ rad/sec}$ 4) $\frac{1}{\sqrt{17}} \text{ rad/sec}$

43. An aeroplane flying horizontally at a height of $\frac{2}{3}$ miles with a velocity 15 mph the rate at which it is moving away from a fixed point on the ground when it passed over the fixed point two minutes ago
1) 6 mph 2) 9 mph 3) 8 mph 4) 16 mph
44. A circular disc of area 10 sq.feet is at a distance $2\frac{1}{2}$ feet from a wall and parallel to the wall. A point source of light is moving in a straight line passing through the centre of the disc and perpendicular to it at the rate of 5 ft/sec. The rate of growth of the area of shadow of the disc on the wall when light is at 20 ft from the wall
1) $\frac{320}{343} \text{ sq.ft / sec}$ 2) $\frac{124}{343} \text{ sq.ft / sec}$ 3) $\frac{1}{343} \text{ sq.ft / sec}$ 4) 2 sq.ft / sec
45. If in a triangle the side a and angle A remains constant while other elements changed slightly then $\delta b \sec B + \delta c \sec C =$
1) 0 2) 1 3) 2 4) 3
46. Let $g(x) = 2f\left(\frac{x}{2}\right) + f(2-x)$ and $f''(x) < 0$ for all $x \in (0,2)$ then the interval in which $g(x)$ is decreasing
1) $\left(0, \frac{4}{3}\right)$ 2) $\left(\frac{4}{3}, 2\right)$ 3) $(2, \infty)$ 4) $(-\infty, 0)$

47. The range of a for which $f(x) = x^3 + (a+2)x^2 + 3ax + 5$ is invertible.
1) $(1, \infty)$ 2) $(4, \infty)$ 3) $(1, 4)$ 4) $(0, 1)$
48. $f(x) = x + \cos x - a$ then number of positive roots of $f(x) = 0$ when $a > 1$
1) 4 2) 2 3) 0 4) 1
49. $f(x) = x^{\frac{1}{x}} (x > 0)$ then the interval in which $f(x)$ is decreasing is _____ and if $a = e^\pi$ $b = \pi^e$ then which of the following options are true
1) $(e, \infty), a < b$ 2) $(0, e), a < b$ 3) $(e, \infty), a > b$ 4) $(0, e), a > b$
50. Number of real roots of the equation $f(x) = (x-a)^3 + (x-b)^3 + (x-c)^3 = 0$
1) 1 2) 2 3) 3 4) 0
51. The equation $2\sin x = |x| + a$ has no-solution then range of a is
1) $\left(\frac{3\sqrt{3}-\pi}{3}, \infty\right)$ 2) $\left(-\infty, \frac{3\sqrt{3}-\pi}{3}\right)$ 3) $(0, 1)$ 4) $\left(0, \frac{3\sqrt{3}-\pi}{3}\right)$

52. If $a^2 + b^2 + c^2 = 1$, $x^2 + y^2 + z^2 = 1$ then maximum value of $|ax + by + cz|$ is
- 1) 1 2) 2 3) 4 4) 6
53. A cubic polynomial vanishes at $x = -2$ and has relative minimum and maximum at $x = -1$ and $x = \frac{1}{3}$. If $\int_{-1}^{+1} f(x) dx = \frac{14}{3}$ then $f(x) =$ _____
- 1) $x^3 - 4x$ 2) $x^3 + x^2 - x + 2$ 3) $x^3 - x^2 + x - 2$ 4) $x^3 - x + 1$
54. Minimum value of $(12x + 5y + 6)$. If $x^2 + y^2 = 4$
- 1) -5 2) -10 3) -15 4) -20
55. The semi-vertical angle of cone of maximum volume and given slant height
- 1) $\frac{\pi}{3}$ 2) $\frac{\pi}{4}$ 3) $\tan^{-1} 2$ 4) $\tan^{-1} \sqrt{2}$
56. The sum of hypotenuse and one side of a right angled triangle is given then angle between these sides is _____. So that area of triangle is maximum
- 1) $\frac{\pi}{2}$ 2) $\frac{\pi}{4}$ 3) $\frac{\pi}{3}$ 4) $\tan^{-1}(2)$

57. $f(x) = a \log_e |x| + bx^2 + x$ has extreme values at $x=1$ and $x=3$ then values of a and b
- 1) $a = -3/4, b = \frac{-1}{8}$ 2) $a = 3/4, b = \frac{1}{8}$
- 3) $a = \frac{-3}{4}, b = \frac{+1}{8}$ 4) $a = 3/4, b = -1/8$
58. $f(x) = x^\alpha \log_e x$ If $x > 0$
 $= 0$ If $x = 0$
- If Rolle's theorem can be applied on $[0, 1]$ then $\alpha =$
- 1) -1 2) $\frac{-1}{2}$ 3) 0 4) $\frac{1}{2}$
59. If $2a + 3b + 6c = 0$ ($a, b, c \in R$) then quadratic $ax^2 + bx + c = 0$ has
- 1) atleast one root in $[0, 1]$ 2) atleast one root in $[2, 3]$
- 3) It has no real roots 4) None of the above
60. A value of c for which Lagrange's mean value theorem holds good for $g(x) = \log_e x$ in $[1, 3]$
- 1) $2\log_3 e$ 2) $\frac{1}{2} \log_e 3$ 3) $\log_e 3$ 4) $\frac{1}{2}$