

Sri Chaitanya IIT Academy, India

A.P., TELANGANA, KARNATAKA, TAMILNADU, MAHARASHTRA, DELHI, RANCHI A right Choice for the Real Aspirant ICON CENTRAL OFFICE, MADHAPUR-HYD

Sec: Sr. IPLCO

Time: 9:00 AM to 12:00 Noon

RPTM-14

Date: 12-12-15

Max.Marks: 360

KEY SHEET

PHYSICS		CHEMISTRY		M	MATHS	
Q.NO	ANSWER	Q.NO	ANSWER	Q.NO	ANSWER	
1	4	31	2	61	3	
2	1	32	1	62	2	
3	3	33	1	63	4	
4	3	34	2	64	2	
5	4	35	3	65	3	
6	3	36	2	66	4	
7	1	37	1	67	3	
8	4	38	2	68	2	
9	1	39	2	69	4	
10	4	40	1	70	1	
11	4	41	1	71	3	
12	1	42	1	72	4	
13	2	43	1	73	3	
14	3	44	1	74	4	
15	2	45	4	75	2	
16	3	46	1	76	1	
17	2	47	3	77	3	
18	1	48	4	78	2	
19	2	49	3	79	4	
20	1	50	3	80	2	
21	1	51	3	81	2	
22	2	52	1	82	3	
23	1	53	3	83	1	
24	3	54	1	84	3	
25	4	55	2	85	4	
26	2	56	2	86	1	
27	1	57	3	87	4	
28	2	58	4	88	2	
29	3	59	4	89	4	
30	3	60	3	90	1	

PHYSICS

- 1. conceptual
- 2. Deviation produced by one is cancelled by the other.

use
$$\delta = A(\mu - 1)$$

3.
$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right) = 3$$

$$\therefore 3 = (1.25 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right) \qquad \dots \dots (1)$$
and
$$-2 = \left(\frac{1.25}{\mu} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right) \qquad \dots \dots (2)$$

$$\frac{3}{R_1} = 0.25 \, \mu \qquad \Rightarrow 0.5 \, \mu = 2.75 \quad 3 \, \mu$$

$$-\frac{3}{2} = \frac{0.25\,\mu}{1.25 - \mu} \implies -0.5\,\mu = 3.75 - 3\,\mu$$

$$\Rightarrow \mu = 3.75 / 2.5 = 1.5$$

4. Case I : When tank is filled with water given the apparent depth = 9.4 cm Height of water t=12.5 cm

Refractive index of water

$$\mu_{\rm w} = \frac{\text{Re al depth}}{\text{Apparent depth}} = \frac{12.5}{9.4} = 1.33$$

Case II: When tank is filled with the liquid refractive index of liquid $\mu = 1.63$

Again
$$\mu = \frac{\text{Re al depth}}{\text{Apparent depth}}$$

Apparent depth=
$$\frac{12.5}{1.63}$$
 = 7.67 cm

- \therefore The microscope is shifted by = 9.4 7.67 = 1.73 cm
- 5. The glass plate produces a shift of $1\left[1-\frac{2}{3}\right] = \frac{1}{3}$ cm. So when plate is placed required

image distance =
$$12 - \frac{1}{3}$$
 cm

$$\therefore \frac{1}{240} + \frac{1}{12} = \frac{1}{7} = \frac{1}{f} \quad \text{and } \frac{1}{v} = \frac{1}{12 - \frac{1}{3}}$$

$$\frac{1}{u} = \frac{1}{240} + \frac{1}{12} - \frac{3}{35} = \frac{1}{240} - \frac{1}{12 \times 35}$$

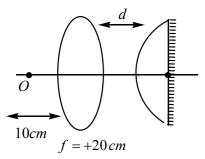
$$\therefore$$
 u = 560 cm

6. The silvered lens can be replaced by a mirror of focal length given as (DIAGRAM)

$$\frac{1}{F_M} = \frac{1}{f_m} - \frac{2}{f_1}$$

for lens
$$v = \frac{uf}{u+f}$$

$$v = \frac{-10 \times 20}{-10 + 20} = -20$$



So this position has to be centre of curvature of mirror in order for the ray to retrace its path so d=40-20=20cm.

7.
$$\frac{1}{V} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{u}{V} = 1 + \frac{f}{u+f}$$

$$m = \frac{v}{u} = \frac{f}{u+f}$$

$$\frac{f}{-12+f} = -\left(\frac{f}{-16+f}\right)$$

m is same in both the cases f=14cm

- 8. Using lens makers formula
- 9. Given distance between screen and object a=90 cm Distance between screen and object the lens d=20 cm Using the displacement formula

$$f = {a^2 - d^2 \over 4a} = {(90)^2 - (20)^2 \over 4 \times 90} = {7700 \over 360} = 21.4cm$$

10. Focal length for upper half is

$$f_1 = \left(\frac{\mu - 1}{\mu / \mu_1 - 1}\right) f_{air} = \left(\frac{1.5 - 1}{\frac{1.5}{2.5} - 1}\right) 20 = 40cm$$

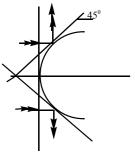
Focal length for lower half is,

$$f_2 = \left(\frac{\mu - 1}{\mu / \mu_2 - 1}\right) f_{air} = \left(\frac{1.5 - 1}{\frac{1.5}{2.5} - 1}\right) \times 20 = -25cm$$

If the object is at infinity two images will form at corresponding focuses. So, the required separation is

$$x = |f_1| + |f_2| = 40 + 25 = 65cm$$

11. At the point of incidence slope should be ± 1



$$y^{2} = 2x$$

$$y = \sqrt{2x}$$

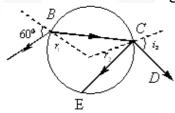
$$\frac{dy}{dx} = \sqrt{2} \cdot \frac{1}{2\sqrt{x}} = \frac{1}{\sqrt{2x}} = 1$$

$$\sqrt{2x} = 1$$

$$2x = 1$$

$$x = \frac{1}{2} \Rightarrow y = \pm 1$$

- 12. Dimension parallel to surface does not change
- 13. The path of ray AB after refraction at opposite face and reflection at opposite face as shown in the figure. We have to find <DCE



By snell's law $(\sin 60^{\circ} / \sin r_1) = \sqrt{3}$

Or
$$\sin r_1 = \sin 60^0 / \sqrt{3} = 1/2$$

$$\therefore r_1 = 30^{\circ} \text{ and hence } \therefore r_2 = 30^{\circ}$$

Considering refraction at $C(\sin r_2 / \sin i_2) = 1/\sqrt{3}$

$$Or \sin i_2 = \sqrt{3} / 2$$

$$\therefore i_2 = 60^0$$

$$\angle ECD = 180^{\circ} - (i_2 + r_2)$$

$$=180^{0}-90^{0}=90^{0}$$

14.
$$r = \frac{4}{\sqrt{\mu^2 - 1}} = \frac{12}{\sqrt{\frac{16}{9} - 1}} = \frac{12 \times 3}{\sqrt{7}} cm$$

- 15. Conceptual
- 16. 3

$$\begin{split} I_{\text{max}} &= \left(\sqrt{I_1} + \sqrt{I_2}\right)^2 = \left(\sqrt{4I} + \sqrt{I}\right)^2 = 9I \\ I_{\text{min}} &= \left(\sqrt{I_1} - \sqrt{I_2}\right)^2 = \left(\sqrt{4I} - \sqrt{I}\right)^2 = I \ \Delta x = \left(\mu - 1\right)t = n\lambda \end{split}$$

- 17. 2
- 18. 1

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$$I = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$$

$$I_0 = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$$

$$\therefore \cos\left(\frac{\phi}{2}\right) = \frac{1}{2}$$
or
$$\frac{\phi}{2} = \frac{\pi}{3}$$
or
$$\phi = \frac{2\pi}{3} = \left(\frac{2\pi}{\lambda}\right) \Delta x$$
or
$$\frac{1}{3} = \left(\frac{1}{\lambda}\right) y \cdot \frac{d}{D}$$

$$\Delta x = \frac{yd}{D}$$

19. 2

$$S_1P - S_2P = \frac{\lambda}{4} \Longrightarrow \triangle \phi = 90^0$$

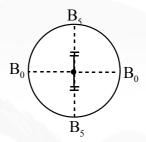
Initial
$$\triangle \phi = \frac{\pi}{6} = 30^{\circ}$$

: Final phase diff =
$$90^{\circ} + 30^{\circ} = 120^{\circ} (or) 90^{\circ} - 30^{\circ} = 60^{\circ}$$

$$I^{1} = 4I_{0} \cos^{2} \frac{\phi}{2} = 4I_{0} \times \frac{1}{4} = I_{0} = I/4$$

(or)
$$I^1 = 4I_0 \cos^2 \frac{\phi}{2} = 4I_0 \cdot \cos^2 \frac{60^0}{2} = 4I_0 \times \frac{3}{4}$$
 = $3I_0 = 3I/4$

20. : no of maximas formed = 20



21.

In interference we know that

$$I_{\text{max}} = \left(\sqrt{I_1} + \sqrt{I_2}\right)^2 \text{ and } I_{\text{min}} = \left(\sqrt{I_1} \sim \sqrt{I_2}\right)^2$$

Under normal conditions (when the widths of both the slits are equal)

$$I_1 = I_2 = I \text{ (say)}$$

$$\therefore I_{\text{max}} = 4I \text{ and } I_{\text{min}} = 0$$

When the width of one of the slits is increased. Intensity due to that slit would increase, while that of the other will remain same. So let:

$$I_1 = I$$
 and $I_2 = \eta I$ $(\eta > I$

Then,
$$I_{\text{max}} = I \left(1 + \sqrt{\eta}\right)^2 > 4I$$

and
$$I_{\min} = I \left(\sqrt{\eta} - 1 \right)^2 > 0$$

: Intensity of both maxima and minima is increased.

22. 2

$$I(\phi) = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

Here,
$$I_1 = I$$

And
$$I_2 = 4I$$

At point A,
$$(\phi) = \frac{\pi}{2}$$

$$\therefore I_A = I + 4I = 5I$$

At point B,
$$\phi = \pi$$

$$\therefore I_B = 1 + 4I - 4I = I$$

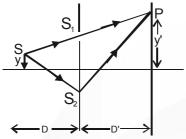
$$\therefore I_A - I_B = 4I$$

23.

$$y' = \frac{d}{2}$$
 at point P exactly infront of S_1

$$\therefore \Delta x = \frac{yd}{D} + \frac{d^2}{2D'}$$

For minimum intensity $\therefore \Delta x = (2n-1)\frac{\lambda}{2}(n=1)$

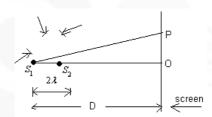


Putting the value we get

$$\left(0.5\sin\pi t\right)\times 10^{-6} + 0.25\times 10^{-6} = \frac{500}{2}\times 10^{-9} \qquad 0.5\sin\pi t + 0.25 = \frac{0.5}{2}$$

$$\sin \pi t = 0 \Rightarrow \pi t = 0, \pi, 2\pi, \dots \Rightarrow t = 1s$$

24.



Referring to the figure, the path difference between the two waves starting from S_1 and S_2 turns out to be $(2\lambda\cos\theta) = n\lambda$ where n is taken as 1 to get the point of maximum intensity which is the same as a point O. Therefore, the above relation gives $\cos\theta = 1/2$ so that $\theta = 60^\circ$

and
$$\tan \theta = PO/D = \sqrt{3}$$
, giving $PO = D\sqrt{3}$

25. Let *l* be the distance between the two slits, at any instant, then

It is given that
$$v = \frac{d\ell}{dt}$$
 ...(i

The path difference reaching the point P from the slits is evidently $\Delta = y \frac{\ell}{D}$

Differentiating both sides with respect to time t, we get

$$\frac{d\Delta}{dt} = \frac{y}{D} \cdot \frac{d\ell}{dt} = \frac{yv}{D} \qquad \dots (ii)$$

[From eqn. (i)]

Since, a change in optical path difference of λ , corresponds to one fringe, so the number of fringe crossing point P, per unit time is

$$\left(\frac{\mathrm{d}\Delta}{\mathrm{d}t}\right)\frac{1}{\lambda} = \frac{\mathrm{y}\mathrm{v}}{\lambda\mathrm{D}}$$

26.
$$\mu = \frac{\sin 60}{\sin \theta} = \frac{\sin 2\theta}{\sin \theta}$$

$$27. \quad \frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

28. Given radius of curvature of concave mirror, R=-36 m

(For concave mirror radius of curvature of concavature is taken a negative)

:. For length
$$f = \frac{R}{2} = \frac{36}{2} = -18cm$$

Distance of object u = -27cm (object distance is always taken as negative)

Height of object O = 2.5 cm

Use the mirror formula

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \Rightarrow -\frac{1}{18} = \frac{1}{v} - \frac{1}{27}$$

$$\frac{1}{v} = -\frac{1}{18} + \frac{1}{27} = \frac{-3+2}{54} = -\frac{1}{54}$$

Distance of screen from mirror y = -54cm

Let the size of image be I. By using the formula of magnification for mirror.

$$m = \frac{v}{u} = \frac{I}{O} \Rightarrow \frac{-(-54)}{-27} = \frac{I}{2.5}$$

$$I = -5 \text{ cm}$$

The negative sign shown that the images is formed in front of the mirror and it is inverted. Thus, the screen should be placed at a distance 54c m and the size of images is 5 cm, real, inverted and magnified in nature.

29. Angular dispersion is zero if $(\mu_v - \mu_R) A + (\mu_v - \mu_R) A = 0$

Dispersive power:
$$\omega = \frac{(\mu_V - \mu_R)A}{d}$$

30. C

$$\overline{v_{i/l}} = m^2 \overline{v_{o/l}}$$

$$\overrightarrow{v_o} = \overrightarrow{v_l} (1 - \frac{1}{m^2})$$