

JEE-ADVANCE-2014-P1-Model

Time: 09:00 AM to 12:00 Noon

IMPORTANT INSTRUCTIONS

Max Marks: 180

PHYSICS:

Section	Question Type	+Ve Marks	- Ve Marks	No.of Qs	Total marks
Sec – I(Q.N : 1 – 10)	Questions with Multiple Correct Choice	3	0	10	30
Sec – II(Q.N : 11 – 20)	Questions with Integer Answer Type	3	0	10	30
Total				20	60

CHEMISTRY:

Section	Question Type	+Ve Marks	- Ve Marks	No.of Qs	Total marks
Sec – I(Q.N : 21 – 30)	Questions with Multiple Correct Choice	3	0	10	30
Sec – II(Q.N : 31 – 40)	Questions with Integer Answer Type	3	0	10	30
Total				20	60

MATHEMATICS:

Section	Question Type	+Ve Marks	- Ve Marks	No.of Qs	Total marks
Sec – I(Q.N : 41 – 50)	Questions with Multiple Correct Choice	3	0	10	30
Sec – II(Q.N : 51 – 60)	Questions with Integer Answer Type	3	0	10	30
Total				20	60

PART-III_MATHEMATICS**Max Marks : 60****Section-1****(One or More options Correct Type)**

This section contains 10 multiple choice questions. Each question has four choices (A) (B)(C) and (D) out of which **ONE or MORE** are correct.

41. The locus of a point, which is such that the lengths of tangents from it to two concentric circles having centre at (α, β) and radii λ and μ , are inversely proportional to their radii, is a circle C of area 10π then
- A) centre of C is at centre of given circles
 - B) Centre of C is at $\sqrt{10}$ from centre of given circles
 - C) $\lambda^2 + \mu^2 = 10$
 - D) $\lambda^2 + \mu^2 = 100$
42. Tangents from $P(2,3)$ to a circle C touch at $A(1,4)$ and $B(3,4)$ then
- A) $a + b + c = 13$ if equation of C is $x^2 + y^2 + ax + by + c = 0$
 - B) The radius of the circle is $\sqrt{2}$
 - C) The circumcentre of $\triangle PAB$ lies inside C
 - D) The area of $\triangle QAB$, where Q is centre of C, is 1 square unit
43. A circle C which touches the curve $y^2 + xy - x^2 = 4$ at $(2,2)$ and also touches the line $x - 3y - 6 = 0$ then
- A) The number of possible circles C is infinite
 - B) Equation of C can be $x^2 + y^2 - 5x - y + 4 = 0$
 - C) Equation of C can be $x^2 + y^2 - 8x - 2y + \frac{29}{2} = 0$
 - D) The point $(1,0)$ lies inside C

44. Five circles $S_i = 0, i = 1, 2, 3, 4, 5$ have centres respectively at $C_1(0,0), C_2(2,2), C_3(6,10), C_4(1,-2), C_5(4,-3)$ and the line $y = mx + c$ is common tangent to all five circles such that C_1, C_2, C_3 lie on one side and C_4, C_5 lie on other side of the tangent. It is given that sum of radii of $S_1 = 0$ and $S_2 = 0$ is equal to radius of $S_4 = 0$ and also sum of radii of $S_2 = 0, S_3 = 0$ is equal to the radius of $S_5 = 0$ then
- A) $m = c$ B) $m + c = 0$ C) $m^2 + c^2 = 2$ D) $|m| = |c|$
45. Let the tangents drawn to the circle $x^2 + y^2 = 16$ from the point $P(0, h)$ meet the x-axis at A and B. If the area of $\triangle APB$ is minimum then which may be true
- A) $h = 4\sqrt{2}$ B) $AB = 8\sqrt{2}$
C) in radius of $\triangle APB$ is $4(2 - \sqrt{2})$ D) Perimeter of $\triangle APB$ is $8 + 4\sqrt{2}$
46. If ABCD is a square of side 4 units M is the midpoint of CD. Now circle with radius 2 and centre M intersects another circle with radius 4 and centre A at the points P and Q. If A is the origin and B is (4,0) and if P is (α, β) then $[|\alpha| + |\beta|]$ is ([] is G.I.F)
- A) 3 B) 4 C) 5 D) 6
47. If a chord of the circle $x^2 + y^2 - 4x - 2y - c = 0$ is trisected at the points $\left(\frac{1}{3}, \frac{1}{3}\right)$ and $\left(\frac{8}{3}, \frac{8}{3}\right)$ then
- A) Length of the chord $7\sqrt{2}$ B) $c = 20$
C) Length of intercept of the circle on x-axis $4\sqrt{6}$
D) The circle passes through $(-2, -2)$

48. Consider the family of circles $x^2 + y^2 - 2x - 2\lambda y - 8 = 0$ passing through two fixed points

A and B. Also $S=0$ is a circle of this family, the tangents to which at A and B intersect on the line $x + 2y + 5 = 0$ then

A) $AB=6$

B) radius of $S=0$ is $3\sqrt{2}$

C) $\alpha + \beta = 4$ where centre of $S=0$ is (α, β)

D) Common chord of family of circles is y-axis

49. The locus of the centre of the circles which touches the circle $x^2 + y^2 - 2x - 4y + (1 - 2\sqrt{3}) = 0$ internally and the tangents to which from $(1, 2)$ is making 60° angle with each other is

A) a circle

B) curve with perimeter $\frac{4}{3}(1 + \sqrt{3})\pi$

C) an ellipse

D) a curve which bounds an area $\frac{8}{9}(2 + \sqrt{3})\pi$

50. If the lines $x + 2y = 1$ and $\lambda x + y = 4$ cut the lines of the pair $xy - x - y + 1 = 0$ at A, B, C, D which are concyclic then

A) $\lambda = 2$

B) $\lambda = -2$

C) radius of circle $= \sqrt{5}$

D) radius of circle $5/2$

Section-2
(Integer Value Correct Type)

This section contains 10 questions. The answer to each question is a **single digit integer, ranging** from 0 to 9 (both inclusive).

51. Tangents are drawn to the circle $x^2 + y^2 = 1$ at the points where it is met by the circles $x^2 + y^2 - (\lambda + 6)x + (8 - 2\lambda)y - 3 = 0$, λ being parameter. If the locus of point of intersection of these tangents is $y = mx + c$ then $\frac{c}{m}$ equals
52. If (α, β) is a point on the circle whose centre is on x-axis and which touches the line $x + y = 1$ at $(3, -2)$ then greatest value of $\alpha + \beta$ equals
53. Two circles can be drawn to pass through $(1, 0), (4, 0)$ and touch y-axis. If they intersect at an angle θ , then the value of $25\cos\theta - 2$ equals
54. Consider a square ABCD of side length 2. Let P be the set of all segments of length 2 with end points on adjacent sides of square ABCD. The mid points of the segments in P enclose a region with area Δ then the value of $\lceil \Delta - \pi \rceil$ equals where $\lceil \rceil$ is G.I.F
55. Two parallel chords of a circle of radius 2 are distance $\sqrt{3} + 1$ apart. If the chords subtend at the centre, angles of $\frac{\pi}{k}$ and $\frac{2\pi}{k}$, where $k > 0$, then the value of $\lceil k \rceil$ equals ($\lceil \rceil$ is G.I.F)
56. Let AB be a chord of the circle $x^2 + y^2 - 4x - 4y + 4 = 0$ which subtend an angle 90° at the point $(2, 3)$, and if locus of the mid point of AB is a circle having centre at (α, β) then $\alpha\beta$ equals

57. The number of integral values of x for which the chord of the circle $x^2 + y^2 = 125$ passing through the point $P(x, 8)$ gets bisected at the point $P(x, 8)$ and has integral slope is
58. If the equation of the locus of the middle point of a chord of the circle $x^2 + y^2 = 2(x + y)$ such that the pair of lines joining the origin to the point of intersection of the chord and the circle are equally inclined to the x -axis is $ax + by = 1$ then $a + b$ equals
59. Two chords of lengths $a^2 - 1$ and $3(a + 1)$ of a circle with centre at $(2, 1)$, bisect each other and if length of the chord of the circle subtending 90° at its centre is k then the value of $\frac{\sqrt{2}}{3}k$ equals
60. If the in circle of $\triangle ABC$ touches the sides BC, CA, AB respectively are $D(3, 4), E(4, 3), F(5, 0)$ and if the slope of internal bisector of $\angle A$ is $\frac{m}{n}, m, n \in N, G.C.D(m, n) = 1$ then $m + n =$