

Sri Chaitanya IIT Academy, India

A.P, TELANGANA, KARNATAKA, TAMILNADU, MAHARASHTRA, DELHI, RANCHI
A right Choice for the Real Aspirant

ICON CENTRAL OFFICE, MADHAPUR-HYD

 Sec: Sr. IPLCO
 JEE ADVANCED
 DATE : 06-12-15

 TIME : 3:00
 2013_P1 MODEL
 MAX MARKS : 180

KEY & SOLUTIONS

PHYSICS

1	A	2	В	3	В	4	D	5	D	6	C
7	C	8	В	9	D	10	C	11	A,B,C,D	12	A,C,D
13	A,C,D	14	A,C,D	15	A,C,D	16	3	17	4	18	2
19	3	20	1								

CHEMISTRY

21	D	22	C	23	A	24	A	25	В	26	A
27	D	28	C	29	В	30	В	31	AB	32	ABC
33	D	34	BD	35	C	36	4	37	3	38	1
39	5	40	2	X							

MATHEMATICS

41	С	42	C	43	A	44	A	45	A	46	В
47	A	48	В	49	В	50	D	51	AD	52	ABC
53	С	54	AB	55	AB	56	3	57	4	58	3
59	1	60	8								

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MATHS

41.
$$t^4 - 2(1 + t^2) + a^2 - 6 = 0 \Rightarrow (t^2 - 1)^2 = 9 - a^2$$

 $\therefore 9 - a^2 \ge 0 \Rightarrow |a| \le 3 \Rightarrow a \in [-3, 3] \text{ No. of int egers} = 7$

- 42. by eliminating "x" we have $2a^3 + c = 3a(1+b) \Rightarrow a(2a-3) = 3ab-c$
- 43. clearly $CHS \ge 2$, $RHS \le 2 \Rightarrow CHS = RHS = 2 \Rightarrow x = 1$, $y = \frac{1}{4}$
- 44. Use $\cos ec\theta + \cot \theta = \cot \left(\frac{\theta}{2}\right)$
- 45. $l^{2} + m^{2} = 3 + 2\left(\cos\frac{2\pi}{7} + \cos\frac{4\pi}{7} + \cos\frac{6\pi}{7}\right) = 2$ $l^{2} + m^{2} = -\left(\cos\frac{4\pi}{7} + \cos\frac{8\pi}{7} + \cos\frac{16\pi}{7}\right) 2\left(\cos\frac{6\pi}{7} + \cos\frac{12\pi}{7} + \cos\frac{10\pi}{7}\right)$ $= -\left(-\frac{1}{2}\right) 2\left(-\frac{1}{2}\right) = \frac{1}{2} + 1 = \frac{3}{2}$ $GE = \frac{2}{(3/2)} = \frac{4}{3}$
- 46. $\sin^2\left(\frac{x+y}{2}\right) = 1 & \cos\left(\frac{x-y}{2}\right) = \frac{1}{2}$ $GE = 1 + \left(\frac{1}{2}\right)^2 = \frac{5}{4}$
- 47. $b_0 = \frac{\cos\frac{\pi}{4}}{\sin\frac{\pi}{4}} = \frac{2\cos^2\frac{\pi}{4}}{2\sin\frac{\pi}{4}} = \frac{1 + \frac{\sqrt{3} + 1}{2\sqrt{2}}}{\frac{\sqrt{3} 1}{2\sqrt{2}}} = 2 + \sqrt{6} + \sqrt{2} + \sqrt{3} \Rightarrow b_0 = a_0 + 2$
- $48.(x-1)^{2} + 4 = -4\cos(\alpha x + \beta) \Rightarrow x = 1 \text{ and } \cos(\alpha x + \beta) = -1 \Rightarrow x = 1 \& \alpha + \beta = 3\pi$ $GE = \tan\left(\frac{\alpha + \beta}{4}\right) = \tan\left(\frac{3\pi}{4}\right) = -1 = \cos(\alpha + \beta)$
- 49. $\left(2\sin\left(x+\frac{\pi}{6}\right)\right)^{\left|2\sin\left(x+\frac{\pi}{6}\right)\right|} = 4 \Rightarrow \sin\left(x+\frac{\pi}{6}\right) = \pm 1 \Rightarrow x = \frac{\pi}{3} \text{ and } -\frac{2\pi}{3}$ No of solutions=2
- 50. $|2a\sin\theta 3| + |-a\sin\theta 1| + |5-a\sin\theta| \ge |2a\sin\theta 3 a\sin\theta 1 + 5 a\sin\theta| \ge 1$ G.E. has no solution for any $a \in R$

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06-12-15 Sr. IPLCO_Jee-Adv_2013-P1_Key Solutions

51.
$$\sin y = 2\sin x - (1)$$

$$\cos y = \frac{2}{3}\cos x - (2)$$

$$\sin^2 y + \cos^2 y = 4\sin^2 x + \frac{4}{9}\cos^2 x \Rightarrow \tan^2 x = \frac{5}{27}$$

Also
$$2^2 - 1^2 \Rightarrow \cos 2y = \frac{4}{9}\cos^2 x - 4\sin^2 x = \frac{4}{9}\cos^2 x - 4(1 - \cos^2 x) = \frac{40}{9}(10\cos^2 x - 1)$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y} = \frac{4 \tan x}{1 - 3 \tan x} = \frac{4 \times \frac{\sqrt{5}}{3\sqrt{3}}}{1 - \frac{15}{27}} = \frac{4\sqrt{5}}{3\sqrt{3}} \times \frac{27}{12} = \sqrt{15}$$

52. A) Now
$$\frac{x \tan A + y \tan B}{x + y} = \frac{k(\sin A + \sin B)}{k(\cos A + \cos B)} = \tan\left(\frac{A + B}{2}\right)$$

B) Now
$$\frac{x \tan A + y \tan B}{x + y} = \frac{\sin A - \sin B}{\cos A + \cos B} = \tan \left(\frac{A - B}{2}\right)$$

$$C)\frac{y\sin A + x\sin B}{x + y} = \frac{\sin A\cos B + \cos A\sin B}{\sin A\cos B + \cos A\sin B} = \frac{\sin(A + B)}{\sin(A - B)}$$

- D) $x \tan A + y \tan B = k \cos A \tan A + k \cos B \tan B = k (\sin A + \sin B) \neq 0$
- 53.
- 54.
- 55.

56.
$$\cos\left(\frac{\pi}{4} - x\right)\cos 2x - \cos\left(\frac{\pi}{4} + x\right)\cos 2x + \sin x.2\sin x\cos x\sec x = \cos x.2\sin x\cos x\sec x$$
$$\Rightarrow \cos 2x\left(\sqrt{2}\sin x\right) + 2\sin^2 x - 2\sin\cos x = 0 \Rightarrow \sqrt{2}\sin x\left(\cos 2x + \sqrt{2}\sin - \sqrt{2}\cos x\right) = 0$$

 $\Rightarrow \sin x = 0 (or) \cos x - \sin x = 0 (or) \cos x + \sin x = \sqrt{2} \Rightarrow \sin x = 0, \tan x = 1 (or) \cos x + \sin x = \sqrt{2} \Rightarrow \sec x = \phi (or) \sec x = \sqrt{2} \therefore GE = (1)^2 + (\sqrt{2})^2 = 3$

57.
$$2\sin^2\left(\frac{\pi}{2}\cos^2x\right) = 1 - \cos\left(\pi\sin^22x\right) \Rightarrow 2\sin^2\left(\frac{\pi}{2}\cos^2x\right) = 2\sin^2\left(\frac{\pi}{2}\sin^22x\right)$$

$$\Rightarrow \frac{\pi}{2}\cos^2 x = n\pi \pm \frac{\pi}{2}\sin^2 2x \Rightarrow \cos^2 x = 2n\pi \pm \sin 2x$$

$$n = 0 \text{ and } \cos^2 x = \sin^2 2x \Rightarrow \sin^2 x = \frac{1}{4} \Rightarrow \cos 2x = \frac{1}{2} \Rightarrow \cos 4x = -\frac{1}{2} \Rightarrow \left[\left[8\cos 4x \right] \right] = 4$$

$$58. \quad \frac{1+\tan\frac{y}{2}}{1-\tan\frac{y}{2}} = \left(\frac{1+\tan\frac{x}{2}}{1-\tan\frac{x}{2}}\right)^3 \Rightarrow SOBS \Rightarrow \frac{1+\sin y}{1-\sin y} = \frac{\left(1+\sin x\right)^3}{\left(1-\sin x\right)^3} \Rightarrow \sin y = \sin x \frac{\left(3+\sin^2 x\right)}{1+3\sin^2 x} \Rightarrow \lim_{x\to 0} \frac{\sin y}{x} = 3$$

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59. Consider
$$\sum_{n=0}^{10} \cos^3 \left(\frac{\pi r}{3} \right) = \frac{1}{4} \left\{ \sum_{n=0}^{10} \cos(\pi r) + 3 \sum_{n=0}^{10} \cos\frac{\pi r}{3} \right\}$$

$$= \frac{1}{4} \left\{ 1 + 3\left(-\frac{1}{2}\right) \right\} = -\frac{1}{8} : GE = \left| 8\left(-\frac{1}{8}\right) \right| = 1$$

60.
$$\sin \frac{x}{3} = 1 \Rightarrow \frac{x}{3} = 2n\pi + \frac{\pi}{2} \Rightarrow x = \frac{3}{2}(4n+1)\pi$$

$$\sin \frac{x}{11} = 1 \Rightarrow \frac{x}{11} = 2m\pi + \frac{\pi}{2} \Rightarrow x = \frac{11}{2} (4m + 1)\pi$$

$$3(4m+1) \Rightarrow 3,15,27,39,51,63,75,99 \ (c.d=12)$$

$$11(4m+1) \Rightarrow 11,55,99 \ (c.d = 44)$$

$$\therefore x = 99 \times \frac{\pi}{2} = 99 \times 90^{\circ} = 8910^{\circ}$$

First digit=8