

## 12-12-15\_Sr.IPLCO\_Jee-Main\_RPTM-14\_ Syllabus

### MATHS:

Complete Properties of Triangles and Inverse Trigonometric Functions

### PHYSICS

Geometrical & Wave Optics

Experiments:

1. Focal length of (i) Convex mirror  
(ii) Concave mirror, and (iii) convex lens using parallax method.
2. Plot of angle of deviation vs angle of incidence for a triangular prism.
3. Refractive index of a glass slab using a travelling microscope.

### CHEMISTRY

States of Matter, Solid State, Chemical Kinetics

**MATHS**

61. In a triangle ABC, AC = 4, BC = 5, AB = 6. A point E is taken on AB such that  $AE = \frac{1}{2}(EB)$  then CE = \_\_\_\_\_
- 1)  $\frac{\sqrt{11}}{2}$       2)  $\frac{3\sqrt{11}}{2}$       3)  $\sqrt{11}$       4)  $\frac{2\sqrt{11}}{3}$
62. AB is diameter of a circle of radius 1-unit CD is a chord perpendicular to AB that cuts AB at E. If the arc CAD is  $\frac{2}{3}$  of circumference of the circle then AE = \_\_\_\_\_
- 1)  $\frac{1}{2}$       2)  $\frac{3}{2}$       3)  $\frac{5}{2}$       D)  $\frac{7}{2}$
63. If  $h_1, h_2, h_3$  are lengths of altitude of a triangle ABC,  $r$  is inradius of  $\Delta^{le}ABC$  then minimum value of  $\frac{h_1+r}{h_1-r} + \frac{h_2+r}{h_2-r} + \frac{h_3+r}{h_3-r}$  is
- 1) 12      2) 4      3) 3      4) 6

64.  $\triangle ABC$  is an isosceles triangle with  $AC = CB$ ,  $\angle ABD = \frac{\pi}{3}$ ,  $\angle BAE = 50^\circ$ ,  $\angle C = 20^\circ$   
then  $\angle EDB = \underline{\hspace{2cm}}$  (Here D is a point on AC, E is a point on BC)  
1)  $20^\circ$                       2)  $30^\circ$                       3)  $45^\circ$                       4)  $55^\circ$
65. In a  $\triangle ABC$ ,  $AB = 20$ ,  $AC = \frac{45}{2}$ ,  $BC = 27$ . Point X and Y are taken on AB and AC respectively so that  $AX = AY$ . If Area of  $\triangle AXY = \frac{1}{2}$  (Area of  $\triangle ABC$ ) then  $AX = \underline{\hspace{2cm}}$   
1)  $\frac{45}{4}$                       2)  $\frac{15}{2}$                       3) 15                      4)  $\frac{15}{4}$
66. In a  $\triangle ABC$ ,  $AB = 13$ ,  $BC = 14$ ,  $CA = 15$ . F is a point on AC such that perpendicular drawn from F to the side BC, meets BC at E and EF divides  $\triangle ABC$ , into two regions of equal areas then  $EF = \underline{\hspace{2cm}}$   
1)  $\sqrt{7}$                       2)  $2\sqrt{7}$                       3)  $3\sqrt{7}$                       4)  $4\sqrt{7}$

67. Altitude AD of an equilateral triangle ABC is a diameter of circle. If this circle intersect the sides AB and AC at E and F then  $\frac{EF}{BC} =$
- 1)  $\frac{1}{2}$                       2)  $\frac{1}{4}$                       3)  $\frac{3}{4}$                       4)  $\frac{3}{8}$
68. In a  $\Delta^{le}ABC$ , the bisector of  $\angle B$  and  $\angle C$  meet AC and AB at D and E respectively BD and EC intersect at O. If  $OD = OE$  and  $\angle B \neq \angle C$  and  $\angle BAC =$
- 1)  $30^\circ$                       2)  $60^\circ$                       3)  $45^\circ$                       4)  $\left(\frac{45}{2}\right)^\circ$
69. In a triangle ABC if  $A - B = 120^\circ$  and  $R = 8r$  then  $\cos C =$
- 1)  $\frac{1}{8}$                       2)  $\frac{3}{8}$                       3)  $\frac{5}{8}$                       4)  $\frac{7}{8}$
70. In a triangle ABC if  $\frac{a}{b} = 2 + \sqrt{3}$  and  $\angle C = 60^\circ$  then
- 1)  $\angle A = 105^\circ, \angle B = 15^\circ$                       2)  $\angle A = 60^\circ, \angle B = 60^\circ$   
3)  $\angle A = 30^\circ, \angle B = 90^\circ$                       4)  $\angle A = 45^\circ, \angle B = 75^\circ$

71. In any triangle ABC the maximum value of  $\frac{a^2 + b^2 + c^2}{R^2}$  is  
1) 3                      2) 6                      3) 9                      4) 8
72. In a triangle ABC if  $\left(\cot\frac{A}{2}\right)^2 + 4\left(\cot\frac{B}{2}\right)^2 + 9\left(\cot\frac{C}{2}\right)^2 = \left(\frac{6s}{7r}\right)^2$  then the ratio of sides  $a:b:c =$   
1) 3:4:5                      2) 2:3:5                      3) 1:1: $\sqrt{2}$                       4) 13:40:45
73. If the lengths of medians of a triangle ABC are 6, 8, 10 then area of triangle ABC is  
1) 16 sq.units                      2) 24 sq.units                      3) 32 sq.units                      4) 48 sq.units
74. In the triangle ABC, D is on the side AC such that  $AD = BC$ ,  $BD = DC$   
 $\angle DBC = 2\theta$ ,  $\angle BAD = 3\theta$  then  $\theta =$  \_\_\_\_\_  
1)  $\frac{\pi}{2}$                       2)  $\frac{\pi}{6}$                       3)  $\frac{\pi}{12}$                       4)  $\frac{\pi}{18}$

75. In a triangle ABC if  $r_1 = 2r_2 = 3r_3$  D is mid point of BC and if  $\angle ADC = \theta$  then  $\cos \theta =$
- 1)  $\frac{7}{25}$                       2)  $\frac{-7}{25}$                       3)  $\frac{3}{25}$                       4)  $\frac{-3}{25}$
76. If radius of a circle which is inscribed in an Isosceles triangle with maximum angle  $120^\circ$  is  $\sqrt{3}$  then area of  $\Delta^e$  is \_\_\_\_\_
- 1)  $12 + 7\sqrt{3}$  sq.units                      2)  $12 - 7\sqrt{3}$  sq.units  
3)  $12 + 5\sqrt{3}$  sq.units                      4)  $12 - 5\sqrt{3}$  sq.units
77. In a triangle ABC if  $r = 1, R = 3, \Delta = 7$  then  $\sum \left( \frac{\cos A}{a} \right) =$
- 1)  $\frac{1}{7}$                       2)  $\frac{2}{7}$                       3)  $\frac{3}{7}$                       4)  $\frac{4}{7}$
78. In a triangle ABC,  $\angle C = 90^\circ$  and  $\tan A = \frac{\sqrt{\sqrt{5}-1}}{2}$  then  $a, b, c$  are
- 1) in A.P                      2) in G.P                      3) in H.P                      4) satisfying  $a + c = b$

79. In a triangle ABC if  $\angle B = \frac{\pi}{3}$  and  $x = \sin A \cdot \sin C$  then range of  $x$  is
- 1)  $(0,1)$       2)  $\left[\frac{1}{2}, 1\right)$       3)  $\left[\frac{1}{4}, \frac{3}{4}\right]$       4)  $\left(0, \frac{3}{4}\right]$
80. The lengths of medians of a right angled triangle through its acute angles are 3 and 4 then area of triangle is
- 1)  $\frac{2\sqrt{11}}{3}$       2)  $\frac{4\sqrt{11}}{3}$       3)  $\frac{3\sqrt{11}}{4}$       4)  $\frac{5\sqrt{11}}{3}$
81. The number of ordered pairs  $(x, y)$  satisfying  $y = |\cos x|$  and  $y = \cos^{-1}(\cos x)$  in  $[-2\pi, 2\pi]$  is
- 1) 2      2) 4      3) 6      4) 8
82. In a  $\Delta^{le} ABC$ ,  $\angle A = \angle B = \frac{1}{2} \left( \sin^{-1} \left( \frac{\sqrt{6}+1}{2\sqrt{3}} \right) + \sin^{-1} \left( \frac{1}{\sqrt{3}} \right) \right)$  and  $C = 6(3^{1/4})$  then area of  $\Delta^{le} ABC$  is
- 1) 9 sq.units      2) 18 sq.units      3) 27 sq.units      4) 54 sq.units

83. If  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3 = \alpha \cdot \pi^3$  where  $\alpha$  is real then range of  $\alpha$  is

- 1)  $\left[\frac{1}{32}, \frac{7}{8}\right]$       2)  $\left[\frac{1}{8}, \frac{7}{8}\right]$       3)  $\left[\frac{1}{32}, \frac{7}{32}\right]$       4)  $\left[\frac{1}{16}, \frac{7}{8}\right]$

84.  $\sin^{-1} x > \cos^{-1} x$  then range of  $x$  is

- 1)  $\left(-1, \frac{-1}{\sqrt{2}}\right)$       2)  $\left(0, \frac{1}{\sqrt{2}}\right)$       3)  $\left(\frac{1}{\sqrt{2}}, 1\right]$       4)  $\left(\frac{-1}{\sqrt{2}}, 0\right)$

85. Number of value of  $x$  for which  $\tan\{x\} = \cot\{x\}$  where  $\{\cdot\}$  represents fractional part of  $x, x \in [0, 2\pi]$

- 1) 12      2) 7      3) 8      4) 6

86. The range of  $x$  for which  $4(\cot^{-1} x)^2 - 16(\cot^{-1} x) + 15 \leq 0$

- 1)  $\left[\cot \frac{5}{2}, \cot \frac{3}{2}\right]$       2)  $\left[-\cot \frac{3}{2}, -\cot \frac{5}{2}\right]$       3)  $[0, 1]$       4)  $\mathbb{R}$



87. A triangle is inscribed in a circle such that the vertices of the triangle divide the circumference of circle into 3-arcs of lengths 3, 4, 5 then area of the triangle is

1)  $\frac{9(\sqrt{3}+1)}{\pi^2}$ sq.units

2)  $\frac{9\sqrt{3}(\sqrt{3}+1)^2}{\pi^2}$ sq.units

3)  $\frac{(\sqrt{3}+1)^2}{\pi^2}$ sq.units

4)  $\frac{9(\sqrt{3}+1)\sqrt{3}}{\pi^2}$ sq.units

88. In a triangle ABC if  $a^2 + c^2 = 2015b^2$  then  $\frac{\cot A + \cot C}{\cot B} =$

1)  $\frac{2}{2015}$

2)  $\frac{2}{2014}$

3)  $\frac{2}{2016}$

4)  $\frac{2}{2013}$

89. If the median AD of a triangle ABC is perpendicular to AB then  $\frac{\tan A}{\tan B} =$  \_\_\_\_\_

1) 1

2) -1

3) 2

4) -2

90. A  $\Delta^{le}$  ABC has sides 6, 7, 8. The line through its incentre parallel to shortest side is drawn to meet the other two sides at P and Q then PQ=

1)  $\frac{30}{7}$

2) 5

3)  $\frac{15}{4}$

4) 3