

Sri Chaitanya IIT Academy, India

A.P., TELANGANA, KARNATAKA, TAMILNADU, MAHARASHTRA, DELHI, RANCHI
A right Choice for the Real Aspirant
ICON CENTRAL OFFICE, MADHAPUR-HYD

 Sec: Sr. IPLCO
 Date: 12-12-15

 Time: 9:00 AM to 12:00 Noon
 RPTM-14
 Max.Marks: 360

KEY SHEET

PHYSICS		CHEMISTRY		M	MATHS	
Q.NO	ANSWER	Q.NO	ANSWER	Q.NO	ANSWER	
1	4	31	2	61	3	
2	1	32	1	62	2	
3	3	33	1	63	4	
4	3	34	2	64	2	
5	4	35	3	65	3	
6	3	36	2	66	4	
7	1	37	1	67	3	
8	4	38	2	68	2	
9	1	39	2	69	4	
10	4	40	1	70	1	
11	4	41	1	71	3	
12	1	42	1	72	4	
13	2	43	1	73	3	
14	3	44	1	74	4	
15	2	45	4	75	2	
16	3	46	1	76	1	
17	2	47	3	77	3	
18	1	48	4	78	2	
19	2	49	3	79	4	
20	1	50	3	80	2	
21	1	51	3	81	2	
22	2	52	1	82	3	
23	1	53	3	83	1	
24	3	54	1	84	3	
25	4	55	2	85	4	
26	2	56	2	86	1	
27	1	57	3	87	4	
28	2	58	4	88	2	
29	3	59	4	89	4	
30	3	60	3	90	1	

MATHS

61.
$$AE + EB = 6$$
$$AE + 2(AE) = 6$$
$$AE = 2 = \frac{1}{3}(AB)$$

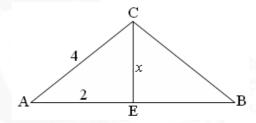
$$\therefore$$
 Area of $\Delta^{le}ACE = \frac{1}{3} (\text{Area of } \Delta^{le} ABC) \dots (1)$

Now: Area of
$$\Delta^{le}ABC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$s = \frac{4+5+6}{2} = \frac{15}{2} \Rightarrow \Delta = \sqrt{\frac{15}{2} \left(\frac{15}{2} - 5\right) \left(\frac{15}{2} - 4\right) \left(\frac{15}{2} - 6\right)}$$

$$= \sqrt{\frac{15}{2} \cdot \frac{5}{2} \cdot \frac{7}{2} \cdot \frac{3}{2}}$$

$$\Delta = \frac{15}{4} \sqrt{7} \dots (2)$$



Now Let CE = x,

:. Area of
$$\Delta^{le}ACE = \sqrt{\frac{6+x}{2} \cdot \frac{6-x}{2} \cdot \frac{x+2}{2} \cdot \frac{x-2}{2}}$$

$$= \frac{1}{4} \sqrt{(36 - x^2)(x^2 - 4)} \dots (3)$$

From (1), (2), (3) we have

$$\frac{1}{4}\sqrt{(36-x^2)(x^2-4)} = \frac{1}{3} \times \frac{15}{4}\sqrt{7}$$

$$\Rightarrow x^2 = 11 \Rightarrow x = \sqrt{11}$$

62. Clearly
$$AD = AC$$

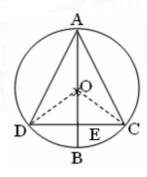
$$\therefore$$
 arc(AD) = arc (AC)

$$Arc (ADC) = \frac{2}{3}.2\pi r$$

$$=\frac{4\pi r}{3}$$

$$\therefore arc(AC) = \frac{2\pi}{3}r = arc(AD)$$

$$\therefore \angle AOD = \angle AOC = \frac{2\pi}{3} \Rightarrow \angle DOC = \frac{2\pi}{3}$$



 $\therefore \Delta^{le}$ ADC is equilateral Δ^{le} .

$$OA = 1 \Rightarrow OE = \frac{1}{2} \Rightarrow AE \Rightarrow \frac{3}{2} (\because AE \text{ is Median})$$

63.
$$\Delta = \frac{1}{2}h_1.a$$

$$h_1 = \frac{2\Delta}{a}$$

$$lly h_2 = \frac{2\Delta}{b}$$

$$\mathbf{b}$$

$$h_3 = \frac{2\Delta}{c}$$

$$\frac{h_1 + r}{h_1 - r} = \frac{\frac{2\Delta}{a} + \frac{\Delta}{s}}{\frac{2\Delta}{a} - \frac{\Delta}{s}} = \frac{2s + a}{2s - a}, lly \frac{h_2 + r}{h_2 - r} = \frac{2s + b}{2s - b}, \frac{h_3 + r}{h_3 - r} = \frac{2s + c}{2s - c}$$

$$\frac{h_1 + r}{h_1 - r} + \frac{h_2 + r}{h_2 - r} + \frac{h_3 + r}{h_3 - r} = \sum \frac{2s + a}{2s - a} = \sum \left(\frac{4s}{2s - a} - 1\right) = \left(\sum \frac{4s}{2s - a}\right) - 3 \dots (1)$$

$$\text{Now } \frac{4s}{2s - a} + \frac{4s}{2s - b} + \frac{4s}{2s - c} \ge \frac{9}{2s - a} + \frac{2s - b}{4s} + \frac{2s - c}{4s}$$

$$\left(\sum \frac{h_1 + r}{h_1 - r}\right) + 3 \ge \frac{9}{(1)}$$

$$\therefore \sum \left(\frac{h_1 + r}{h_1 - r}\right) \ge 6$$

64. Let
$$\angle EDB = \alpha$$

Let
$$\angle CAB = \angle CBA = \theta$$

$$\therefore 20 + \theta + \theta = 180^{\circ}$$

$$2\theta = 180 - 20 \Rightarrow \theta = 80^{\circ}$$

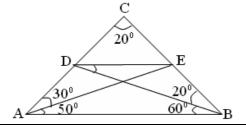
$$\therefore \angle CAE = 30^{\circ} \Rightarrow \angle CEA = 130^{\circ} \text{ and } \angle AEB = 50^{\circ} \Rightarrow AB = EB = y$$

Let
$$AC = BC = x$$
 and $BA = y$ Now $CE = x - y$

Apply – sine – rule in $\Delta^{le}AEC$

$$\frac{x}{\sin 130^{0}} = \frac{x - y}{\sin 30^{0}} \Rightarrow \frac{x - y}{x} = \frac{1}{2\sin 50^{0}} \text{ or } \frac{x}{x - y} = 2\cos 40^{0} \dots (1)$$

In Δ^{le} ABD - apply sine – rule.



$$\frac{BD}{\sin 80} = \frac{AB}{\sin 40} \Rightarrow \frac{BD}{v} = 2\cos 40 \dots (2)$$

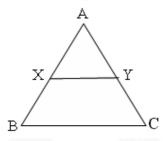
From (1) & (2)
$$\frac{BD}{y} = \frac{x}{x-y}$$

 $\therefore \Delta^{le} AEC, \Delta^{le} DEB$ are similar

$$\Rightarrow \angle BDE = \angle EAC = \frac{\pi}{6} = 30^{\circ}$$

65. Area of Δ^{le} ABC

$$\Delta = \frac{1}{2} \times (AB) \times (AC) \times \sin A$$



$$= \frac{1}{2} \times 20 \times \frac{45}{2} \times \sin A$$

$$\Delta = 225 \sin A \dots (1)$$

Area of
$$\Delta^{le} AXY$$
 is $\frac{1}{2}(AX) \times (AY) \times \sin A = \frac{1}{2}(AX)^2 \sin A \dots (2)$

$$\therefore \frac{1}{2} (AX)^2 \sin A = \frac{225 \sin A}{2}$$

$$(AX)^2 = 225 \Rightarrow AX = 15$$

66.
$$2s = 13 + 14 + 15$$

$$s = \frac{42}{2} = 21$$

Area of
$$\Delta^{le} ABC = \sqrt{21 \times 8 \times 7 \times 6}$$

$$=7\times12=84$$

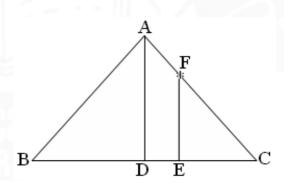
Now
$$\frac{1}{2} \times AD \times BC = 84$$

$$AD = \frac{2 \times 84}{14} = 12 \Rightarrow BD = 5, DC = 9$$

 Δ^{le} ADC, Δ^{le} EFC are similar.

$$\therefore \frac{AD}{EF} = \frac{DC}{EC}$$

$$EC = \frac{9}{12}EF$$

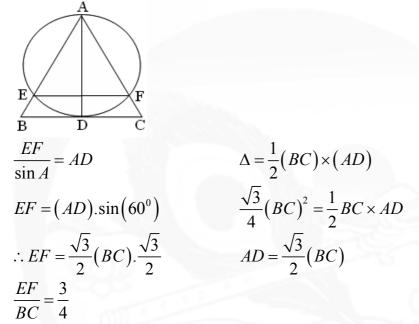


$$EC = \frac{3}{4}EF$$
Area of Δ^{le} FEC = 42
$$\frac{1}{2} \times (EF) \times EC = 42$$

$$\frac{EF}{2} \times \frac{(EF)3}{4} = 42 \Rightarrow (EF)^2 = \frac{2 \times 4 \times 42}{3}$$

$$EF = 4\sqrt{7}$$

In Δ^{le} AEF 67.



Clearly O is Incentre of Δ^{le} ABC. 68.

$$\angle ODA = 180 - \left(A + \frac{B}{2}\right)$$

$$= B + C - B/2 = \frac{B}{2} + C$$

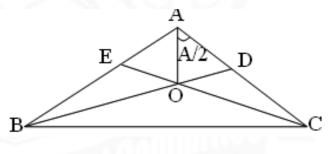
$$\therefore \angle AOD = 180 - \left(\frac{B}{2} + C + \frac{A}{2}\right)$$

$$= A + B - \left(\frac{A + B}{2}\right)$$

$$= \frac{A + B}{2} = 90 - C/2$$
Similarly $\angle AOE = 90 - B/2$

Apply sine – rule in Δ^{le} AOD

$$\frac{OD}{\sin A/2} = \frac{AO}{\sin(B/2 + C)}$$



$$OD = \frac{(AO)(\sin A/2)}{\sin(B/2 + C)}$$
Similarly $OE = \frac{(AO)\sin A/2}{\sin(B + C/2)}$
But $OD = OE \Rightarrow \sin(B + C/2) = \sin(B/2 + C)$

$$\therefore B + C/2 = 180 - (B/2 + C)$$

$$3\left(\frac{B+C}{2}\right) = 180^{\circ}$$

$$B+C=120^{0}$$

$$180 - A = 120^{\circ} \Rightarrow \angle A = 60^{\circ}$$

69. We know that
$$\cos A + \cos B + \cos C = 1 + \frac{r}{R}$$

$$\Rightarrow 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right) + 1 - 2\sin^2\frac{C}{2} = 1 + \frac{1}{8}$$

$$\sin\frac{c}{2} \cdot \frac{1}{2} - \sin^2\frac{c}{2} = \frac{1}{16}.$$

$$\frac{1}{16} - 2.\frac{1}{4}\sin\frac{c}{2} + \sin^2\frac{c}{2} = 0$$

$$\left(\frac{1}{4} - \sin\frac{c}{2}\right)^2 = 0$$

$$\Rightarrow \sin \frac{C}{2} = \frac{1}{4}$$

$$\cos C = 1 - 2\sin^2\frac{C}{2} = 1 - \frac{1}{8} = 7/8$$

70.
$$\tan\left(\frac{A-B}{2}\right) = \frac{a-b}{a+b}\cot c/2$$

$$= \frac{\frac{a}{b} - 1}{\frac{a}{b} + 1} \cot c / 2$$

$$=\frac{2+\sqrt{3}-1}{2+\sqrt{3}+1}.\cot(30^{\circ})$$

$$= \frac{\sqrt{3}+1}{\sqrt{3}(\sqrt{3}+1)}.\sqrt{3} = 1: \frac{A-B}{2} = 45^{\circ} \Rightarrow A-B = 90^{\circ} \text{ and } A+B = 120^{\circ}$$

$$\therefore 2A = 210^{\circ} \Rightarrow \underline{A} = 105^{\circ} \text{ and } \therefore \underline{B} = 15^{\circ}$$

71.
$$\frac{a^2 + b^2 + c^2}{R^2} = 4\left(\sin^2 A + \sin^2 B + \sin^2 C\right) = 8\left(1 + \cos A \cos B \cos C\right) \le 8\left(1 + \frac{1}{8}\right) = 9$$

72.
$$r = (s-a)\tan A/2 \Rightarrow \cot A/2 = \frac{s-a}{r} = u$$

and $\cot B/2 = \frac{s-b}{r} = v$

$$\cot C/2 = \frac{s-c}{r} = w$$

$$u + v + w = \frac{s - a + s - b + s - c}{r} = \frac{s}{r}$$

:. Given expression is

$$49(u^2 + 4v^2 + 9w^2) = 36(u + v + w)^2$$

$$\Rightarrow 13 u^2 + 160v^2 + 405w^2 - 72uv - 72vw - 72wu = 0$$

$$\Rightarrow (9u^2 - 72uv + 144v^2) + (16v^2 - 72vw + 81w^2) + (324w^2 - 72wu + 4u^2) = 0$$

$$(3u-12v)^{2} + (4v-9w)^{2} + (18w-2u)^{2} = 0$$

$$\Rightarrow u:v:w=1:\frac{1}{4}:\frac{1}{9}$$

$$\frac{s-a}{r}: \frac{s-b}{r}: \frac{s-c}{r} = 36:9:4$$

$$\therefore \frac{s-a}{36} = \frac{s-b}{9} = \frac{s-c}{4}$$

$$= \frac{2s - (b + c)}{9 + 4} = \frac{2s - (a + b)}{36 + 9} = \frac{2s - (a + c)}{36 + 4}$$

$$=\frac{a}{13}=\frac{c}{45}=\frac{b}{40}$$

$$\therefore a:b:c=13:40:45$$

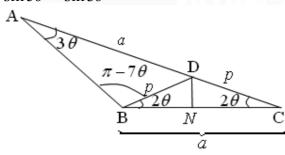
73. Use the formula
$$\Delta = \frac{4}{3} \sqrt{m(m-m_1)(m-m_2)(m-m_3)}$$

Where
$$m = \frac{m_1 + m_2 + m_3}{2}$$
, $m_1 = 6$, $m_2 = 8$, $m_3 = 10$

74. In $\Delta^{le}ABC$

$$\frac{a+p}{\sin 5\theta} = \frac{a}{\sin 3\theta} \dots (1)$$

$$N = mid(BC)$$



In
$$\Delta^{le}BDN$$
, $\frac{BN}{P} = \cos 2\theta$

since BDC is Isosceles

$$a = 2p\cos 2\theta \dots (2)$$

BN = a/2

 \therefore from (1) and (2)

$$\frac{2p\cos 2\theta + p}{\sin 5\theta} = \frac{2p\cos 2\theta}{\sin 3\theta}$$

 $(2\cos 2\theta + 1)\sin 3\theta = \sin 5\theta (2\cos 2\theta)$

 $2\sin 3\theta\cos 2\theta + \sin 3\theta = 2\sin 5\theta\cos 2\theta$

 $\sin \theta = \sin 7\theta - \sin 5\theta$

 $\sin \theta = 2\cos 6\theta \sin \theta$

$$\cos 6\theta = \frac{1}{2}$$

$$6\theta = 60^{\circ}$$

$$\theta = 10^{\circ} = \frac{\pi}{18^{\circ}}$$

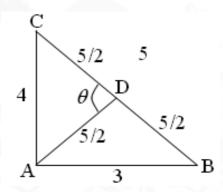
75.
$$\frac{r_1}{6} = \frac{r_2}{3} = \frac{r_3}{2} = \lambda$$
$$r_1 = 6\lambda, r_2 = 3\lambda, r_3 = 2\lambda \Rightarrow r = \lambda$$

$$a = \sqrt{(r_1 - r)(r_2 + r_3)} = 5\lambda$$

$$b = \sqrt{(r_2 - r)(r_1 + r_3)} = 4\lambda$$

$$c = \sqrt{(r_3 - r)(r_1 + r_2)} = 3\lambda$$

$$\therefore \cos \theta = \frac{\left(\frac{5}{2}\right)^2 + \left(\frac{5}{2}\right)^2 - 4^2}{2 \cdot \left(\frac{5}{2}\right) \cdot \left(\frac{5}{2}\right)} = \frac{-7}{25}$$



76.
$$r = (s - a) \tan A/2$$

$$\sqrt{3} = (s - a) \tan 60^{\circ}$$

$$\Rightarrow s - a = 1$$

11y
$$s - b = \sqrt{3}(2 + \sqrt{3})$$

$$s - b = \sqrt{3} \left(2 + \sqrt{3} \right)$$

$$s-c = \sqrt{3}(2+\sqrt{3}) \Rightarrow s = 7+4\sqrt{3} \Rightarrow \Delta = 12+7\sqrt{3}$$
 sq.units

77.
$$r = \frac{\Delta}{s} = 1 \Rightarrow \frac{7}{s} = 1 \Rightarrow s = 7 \Rightarrow a + b + c = 14$$
.

Now
$$\Delta = 7 \Rightarrow \frac{abc}{\Delta R} = 7 \Rightarrow abc = 84$$

$$\Delta^2 = s(s-a)(s-b)(s-c)$$

$$49 = 7(7-a)(7-b)(7-c)$$

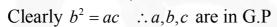
$$\Rightarrow 7 = 343 - 49(a+b+c) + 7(ab+bc+bc) - abc$$

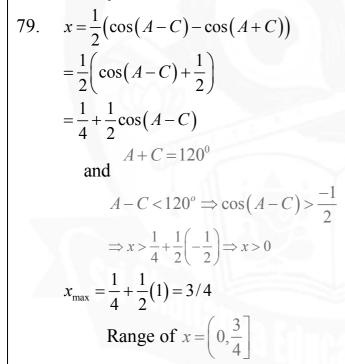
$$\Rightarrow ab+bc+ca = 62$$

$$a^{2}+b^{2}+c^{2} = (a+b+c)^{2} - 2(ab+bc+ca) = 72$$

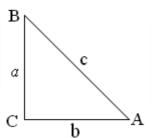
$$\therefore \sum \frac{\cos A}{a} = \frac{a^{2}+b^{2}+c^{2}}{2abc} = \frac{72}{2\times84} = \frac{3}{7}$$

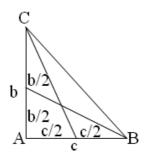
78.
$$\tan A = \frac{a}{b} = \frac{\sqrt{\sqrt{5} - 1}}{\sqrt{2}}$$
$$\frac{a}{\sqrt{\sqrt{5} - 1}} = \frac{b}{\sqrt{2}} = \lambda$$
$$a = \lambda \sqrt{\sqrt{5} - 1}$$
$$b = \lambda \sqrt{2}$$
$$c = \sqrt{a^2 + b^2} = \lambda \sqrt{(\sqrt{5} + 1)}$$





80.
$$c^2 + \frac{b^2}{4} = 16$$
....(1)
 $b^2 + \frac{c^2}{4} = 9$(2)



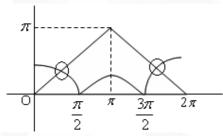


On solving (1) & (2)
$$b = \frac{4}{\sqrt{3}}$$

$$c = \frac{2\sqrt{11}}{\sqrt{3}}$$

Area of
$$\Delta^{le}ABC = \frac{1}{2}bc = \frac{1}{2} \times \frac{4}{\sqrt{3}} \cdot \frac{2\sqrt{11}}{\sqrt{3}} = \frac{4\sqrt{11}}{3}$$

81.
$$\cos^{-1}(\cos x) = x$$
 If $0 < x < \pi$
= $2\pi - x$ If $\pi < x < 2\pi$



 \therefore 2-solution between 0 and 2π

By symmetry it will have an other 2 – solution between -2π and O total 4 – solutions are possible.

82.
$$\angle A = \angle B = \frac{1}{2} \left[\tan^{-1} \left(\frac{\sqrt{6} + 1}{\sqrt{3} - \sqrt{2}} \right) + \tan^{-1} \left(\frac{1}{\sqrt{2}} \right) \right]$$

$$= \frac{1}{2} \left[\pi + \tan^{-1} \left(\frac{2\sqrt{3} + \sqrt{3}}{-3} \right) \right] \qquad \left(\because \frac{\sqrt{6} + 1}{\sqrt{3} - \sqrt{2}} \cdot \frac{1}{\sqrt{2}} > 1 \right)$$

$$= \frac{1}{2} \left[\pi - \frac{\pi}{3} \right] = \frac{\pi}{3}$$

 $\therefore \angle C = \frac{\pi}{3} \quad \Delta^{le} \text{ ABC is equilateral}$

$$\Delta = \frac{\sqrt{3}}{4} (c^2) = \frac{\sqrt{3}}{4} \times 36. (\sqrt{3}) = 27 \text{ sq.units}$$

83.
$$(\sin^{-1} x)^3 + (\cos^{-1} x)^3 = (\sin^{-1} x + \cos^{-1} x)^3 - 3\sin^{-1} x \cos^{-1} x (\sin^{-1} x + \cos^{-1} x)$$

$$= \frac{\pi^3}{8} - 3\sin^{-1} x \left(\frac{\pi}{2} - \sin^{-1} x\right) \cdot \frac{\pi}{2}$$

$$= \frac{\pi^3}{8} - \frac{3\pi^2}{4} \sin^{-1} x + \frac{3\pi}{2} (\sin^{-1} x)^2$$

$$= \frac{\pi^{3}}{8} + \frac{3\pi}{2} \left[\left(\sin^{-1} x \right)^{2} - \frac{\pi}{2} \sin^{-1} x \right]$$

$$= \frac{\pi^{3}}{8} + \frac{3\pi}{2} \left[\left(\sin^{-1} x - \frac{\pi}{4} \right)^{2} - \frac{\pi^{2}}{16} \right]$$

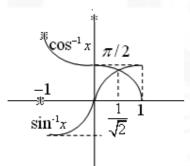
$$= \frac{\pi^{3}}{8} + \frac{3\pi}{2} \left(\sin^{-1} x - \frac{\pi}{4} \right)^{2} - \frac{3\pi^{3}}{32}$$

$$= \frac{\pi^{3}}{32} + \frac{3\pi}{2} \left(\sin^{-1} x - \frac{\pi}{4} \right)^{2}$$

$$= \frac{\pi^{3}}{32} + \frac{3\pi}{2} \left(\sin^{-1} x - \frac{\pi}{4} \right)^{2}$$
Its min $\rightarrow \frac{\pi^{3}}{32}$, max $\rightarrow \frac{\pi^{3}}{32} + \frac{3\pi}{2} \times \frac{9\pi^{2}}{16}$

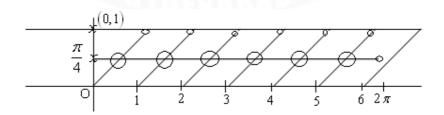
$$= \frac{28\pi^{3}}{32} = \frac{7\pi^{3}}{8}$$
Range $\left[\frac{\pi^{3}}{32}, \frac{7\pi^{3}}{8} \right] \Rightarrow \alpha \in \left[\frac{1}{32}, \frac{7}{8} \right]$

84. Clearly
$$\sin^{-1} x > \cos^{-1} x$$
 Iff $x \in \left(\frac{1}{\sqrt{2}}, 1\right]$.



85.
$$\tan^2 \{x\} = 1 \Rightarrow \tan\{x\} = \pm 1$$

But $0 \le \{x\} < 1 \Rightarrow \{x\} \in \text{ quadrant } 1$
 $\Rightarrow \tan\{x\} > 0$
 $\therefore \tan\{x\} = 1 \Rightarrow \{x\} = \tan^{-1}(1) = \pi/4$

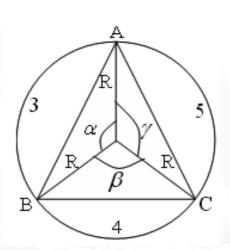


Only 6 – values of x are possible.

86.
$$\cot^{-1} x = t$$
, $4t^2 - 16t + 15 \le 0$
 $(2t - 5)(2t - 3) \le 0$
 $\frac{3}{2} \le t \le \frac{5}{2}$
 $\frac{3}{2} \le \cot^{-1} x \le \frac{5}{2}$
 $\cot 3/2 \ge x \ge \cot 5/2$
 $\therefore \cot \frac{5}{2} \le x \le \cot 3/2$

87.
$$2\pi R = 12 \Rightarrow \pi R = 6$$

 $\Rightarrow R = \frac{6}{\pi}$
 $arc(AB) = R.\alpha$
 $3 = \frac{6}{\pi}.\alpha \Rightarrow \alpha = \frac{\pi}{2}$
 $arc(BC) = R.\beta \Rightarrow \beta = \frac{4}{R}$
 $\beta = \frac{4}{6} \times \pi = \frac{2\pi}{3}$
 $arc(AC) = R\gamma \Rightarrow = \frac{5}{6}\pi$



Area of Δ^{le} ABC

= Area of
$$\Delta^{le}OAB$$
 + Area of $\Delta^{le}OBC$ + Area of $\Delta^{le}OAC$

$$= \frac{1}{2}R^{2} \sin \alpha + \frac{1}{2}R^{2} \sin \beta + \frac{1}{2}R^{2} \sin \gamma$$

$$= \frac{1}{2} \times R^{2} \left(\sin \frac{\pi}{2} + \sin \frac{2\pi}{3} + \sin \frac{5\pi}{6} \right)$$

$$= \frac{1}{2} \times \frac{36}{\pi^{2}} \left(1 + \frac{\sqrt{3}}{2} + \frac{1}{2} \right) \qquad = \frac{18}{\pi^{2}} \left(\frac{3 + \sqrt{3}}{2} \right)$$

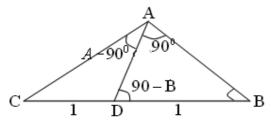
$$= \frac{9\sqrt{3} \left(\sqrt{3} + 1 \right)}{\pi^{2}} \text{ sq.units}$$

88.
$$\frac{\cot A + \cot C}{\cot B} = \frac{\sin^2 B}{\sin A \sin C \cos B} = \frac{b^2}{ac \frac{\left(a^2 + c^2 - b^2\right)}{2ac}}$$

$$= \frac{2b^2}{a^2 + c^2 - b^2} = \frac{2b^2}{(2014)b^2} = \frac{2}{2014}$$

89. By m – n theorem
$$(1+1)\cot(90-B) =$$

 $1.\cot(A-90)-1.\cot 90$



 $2 \tan B = - \tan A$

$$\frac{\tan A}{\tan B} = -2$$

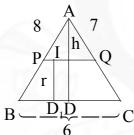
90.
$$\Delta = rs$$

$$\frac{1}{2} \times h \times 6 = r \times \frac{21}{2}$$

$$\frac{h}{r} = \frac{7}{2} \dots (1)$$

 $\Delta^{le}APQ$ and $\Delta^{le}ABC$ are similar

$$\frac{h-r}{h} = \frac{PQ}{6} \implies 1 - \frac{r}{h} = \frac{PQ}{6} \implies 1 - \frac{2}{7} = \frac{PQ}{6} \implies PQ = \frac{30}{7}$$



 $AB=8, BC=6, AC=7, AD = h, ID_1 = r$