

## Sri Chaitanya IIT Academy, India

A.P., TELANGANA, KARNATAKA, TAMILNADU, MAHARASHTRA, DELHI, RANCHI
A right Choice for the Real Aspirant

ICON CENTRAL OFFICE, MADHAPUR-HYD

 Sec: Sr. IPLCO
 Date: 05-09-15

 Time: 9:00 AM to 12:00 Noon
 RPTM-5
 Max.Marks: 360

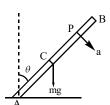
## **KEY SHEET**

PHYSICS		MATHS		CHEMISTRY	
Q.NO	ANSWER	Q.NO	ANSWER	Q.NO	ANSWER
1	2	31	3	61	4
2	1	32	1	62	2
3	1	33	4	63	1
4	2	34	3	64	4
5	3	35	3	65	4
6	2	36	1	66	4
7	1	37	4	67	2
8	1	38	1	68	4
9	3	39	1	69	3
10	1	40	3	70	2
11	2	41	2	71	3
12	3	42	1	72	4
13	2	43	4	73	1
14	2	44	1	74	2
15	2	45	4	75	3
16	2	46	4	76	3
17	4	47	2	77	3
18	1	48	3	78	3
19	3	49	3	79	4
20	3	50	1	80	4
21	2	51	4	81	4
22	3	52	4	82	4
23	3	53	1	83	3
24	4	54	3	84	3
25	2	55	2	85	2
26	2	56	3	86	2
27	1	57	1	87	2
28	4	58	3	88	2
29	2	59	2	89	4
30	1	60	2	90	2

## **PHYSICS**

- 1. Conceptual
- 2. Taking torque about A. when the rod has fallen through an angle  $\theta$

$$\tau = mg\frac{l}{2}\sin\theta = I\alpha = \left(\frac{1}{3}ml^2\right)\alpha$$



Or 
$$\alpha = \frac{3g}{2l}\sin\theta$$

For any point P on the rod, at a distance r from A, the liner acceleration is  $a = r\alpha = \frac{3gr}{2l}\sin\theta$ . P will also have centripetal acceleration.

3.

$$\vec{\tau}_{o} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 3 & 6 \\ 2 & -4 & 1 \end{vmatrix}$$
$$= 27\hat{i} + 10\hat{j} - 14\hat{k}$$

4.

Opposing couple is  $-mgR\sin\omega t$ 



5.

$$F\left(\frac{a+b}{2}\right) = 2F\left(\frac{b-a}{2}\right)$$
$$\therefore \frac{a}{b} = \frac{1}{3}$$

6

Time at which centre of mass is at highest point is

$$=\frac{u}{g}=\frac{10}{10}=2\sec$$

Rotation of the rod

$$=\omega t = \frac{\pi}{2} \Rightarrow a_A = \omega^2 R \hat{j} - g \hat{j}$$

$$3\hat{i} + 8\hat{j} = \vec{V}_{CM} + \frac{4}{\sqrt{3}} \left( \frac{\hat{i}}{2} + \frac{\sqrt{3}\hat{j}}{2} \right)$$

$$\vec{V}_A = \vec{V}_{CM} + \frac{4}{\sqrt{3}} \left( \frac{\hat{i}}{2} - \frac{\sqrt{3}\hat{j}}{2} \right)$$

$$\Rightarrow \overrightarrow{V}_A = 3\hat{i} + 4\hat{j}$$

$$\therefore V_{A} = 5 \ m/s$$

8. 
$$\frac{1}{2}(1+1)mv^2 + \frac{1}{2}m(2v)^2 + \frac{1}{2}m(v\sqrt{2})^2 + \frac{1}{2}m(v\sqrt{2})^2 = 5mv^2$$

9. Conceptual

10.

$$k = (1 + 2/3) \times \frac{1}{2}MV^{2} + \frac{1}{2}(2M)V^{2}$$
$$= \frac{11}{6}MV^{2}$$

11. 
$$f_{\text{max}} = \frac{kx_{\text{max}}}{1 + \frac{mR^2}{I}} = 10N$$

12.

Let P = external force F = force of friction between A and B.

$$P-F = ma_1$$
 and  $P = ma_2$ .  $\therefore a_2 > a_1$ .

Let  $\alpha$  = angular acceleration between A and B. For one rotation,

$$\theta = 2\pi = \frac{1}{2}\alpha T^2 \text{ or }$$

$$T = (4\pi/\alpha)^{1/2}$$
 = time of travel from A to B.

Angular velocity at  $B = \omega_B = \alpha T$ .

For one rotation to the right to B,

$$\theta = 2\pi = \omega_B t$$
 or  $t = \frac{2\pi}{\alpha T} = \frac{\frac{1}{2}T^2}{T} = \frac{T}{2}$ 

13. Conceptual

$$Mg.R = \frac{MR^2}{2}\alpha \Rightarrow \alpha = \frac{2g}{R} = \frac{w}{t}$$

$$v = 2RW \Rightarrow 4gt = \frac{ds}{dt}$$

$$\int_0^s ds = \int_0^{WR/2g} 4gt \, dt \Rightarrow s = \frac{R^2 W^2}{2g}$$

15

$$T + f = mg \sin \theta$$

$$T \cdot R = f \cdot R \Rightarrow T = f$$

$$\therefore f = \frac{mg \sin \theta}{2} = T$$

16. Conceptual

17.

$$U_1 = MgR$$

$$U_2 = \frac{M}{4}g\left(\frac{R}{2}\right)$$

18.

$$mg\frac{L}{2} = \frac{mL^2}{3}\alpha$$
$$\Rightarrow \alpha = \frac{3g}{2L}$$

19. Conceptual

20.

$$Mgx = \left(\frac{Ma^2 \times 4}{12 \times 4} + \frac{Ma^2}{48} + \frac{3Ma^2}{16 \times 3} + \frac{Mx^2 \times 48}{48}\right)\alpha$$

$$\Rightarrow \alpha = \frac{48gx}{8a^2 + 48x^2} \alpha \frac{x}{a^2 + 6x^2}$$

$$\frac{d\alpha}{dx} = 0 \Rightarrow x = \frac{a}{\sqrt{6}}$$

21.

$$|\tau_A| = |\tau_B| = (F\sin\theta) \frac{L}{2} = I\alpha$$
  
 $\therefore \alpha \propto \frac{1}{I}$ 

22. The distance of mass is the nearest to axis xx, hence moment of inertia is least about xx-axis.

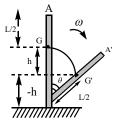
23.

$$\frac{2}{3}ML^2\omega^2 = \frac{3}{2}MgL \qquad \qquad \omega = \frac{3}{2}\sqrt{\frac{g}{L}}$$

24. Conceptual

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$$Mg\frac{L}{2}(1-\cos\theta) = \frac{ML^2}{6}\omega^2$$

$$\therefore \qquad \omega = \sqrt{6g/L}\sin\left(\frac{\theta}{2}\right)$$

26.

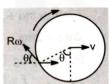
$$2\pi = \frac{1}{2} \times \frac{\pi}{4} \times t^2$$

$$\therefore t = 4$$

27.

$$\frac{I_1}{I_2} = \frac{1}{8} = \frac{mR^2}{m_2 (nR)^2} = \frac{mR^2}{mn (nR)^2}$$
or  $\frac{1}{8} = \frac{1}{n^3}$  or  $n = 2$ 

28. Torque is always perpendicular to  $\vec{F}$  as well as  $\vec{r} : \vec{r} : \vec{\tau} = 0$  as well as  $\vec{F} : \vec{\tau} = 0$  29.



$$v = R\omega\cos\theta$$

$$\cos\theta = \frac{v}{R\omega}$$

$$h = R - R\cos\theta$$

$$V_{P} = 2V \cos \frac{\theta}{2}$$

$$K_{ABC} = \int \frac{1}{2} \lambda R d\theta V_{P}^{2}$$

$$= \int_{-\pi/2}^{\pi/2} 2\lambda V^{2} R \cos^{2} \frac{\theta}{2} d\theta$$

$$= MV^{2} \left(\frac{\pi + 2}{2\pi}\right)$$