SYDE 556/750

Simulating Neurobiological Systems Lecture 7: Analysing Representations

Chris Eliasmith

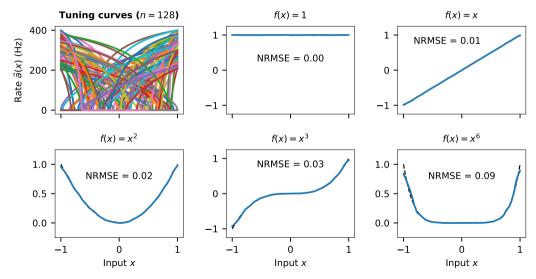
Nov 4, 2022

- ► Slide design: Andreas Stöckel
- ► Content: Terry Stewart, Andreas Stöckel, Chris Eliasmith

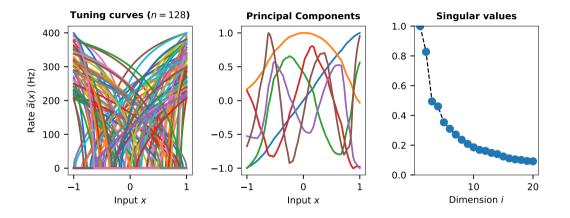




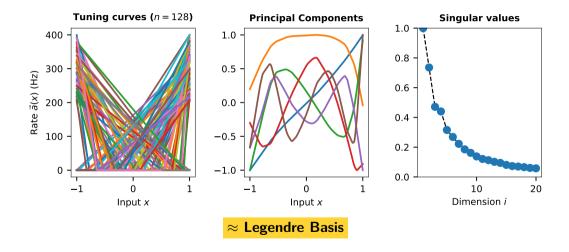
Decoding Polynomials



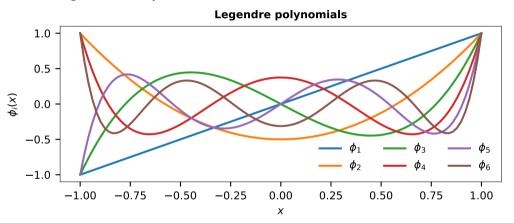
LIF Tuning Curve Principal Components



ReLU Tuning Curve Principal Components

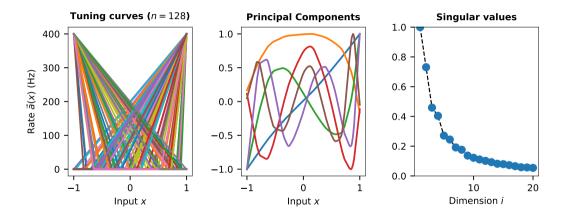


Reminder: Legendre Polynomials

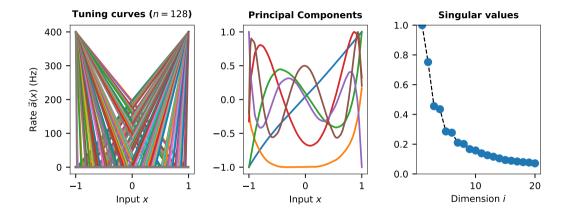


$$\varphi_i(x) = \frac{1}{2^i} \sum_{k=0}^n {i \choose k}^2 (x-1)^{i-k} (x+1)^k$$

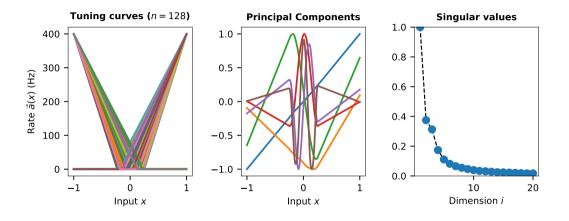
Modifying the Basis – Same Maximum Rate (I)



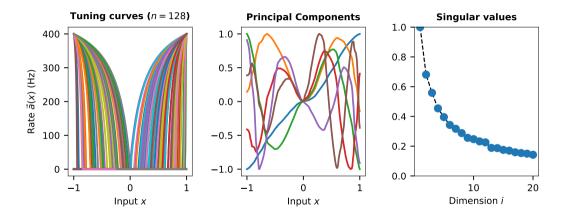
Modifying the Basis – Equidistant x-Intercepts (II)



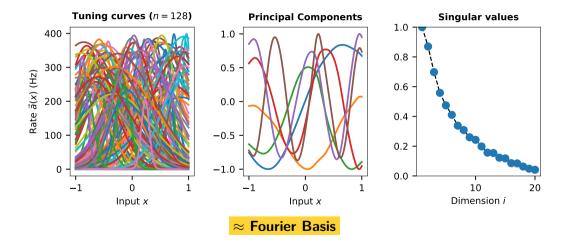
Modifying the Basis – Limited *x*-Intercepts (III)



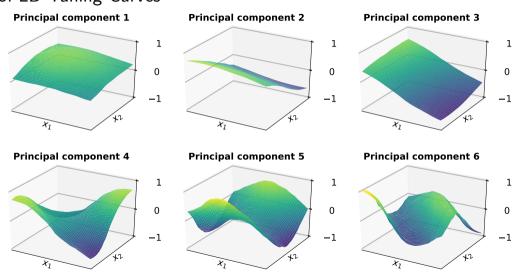
Modifying the Basis – Symmetric Tuning Curves (IV)



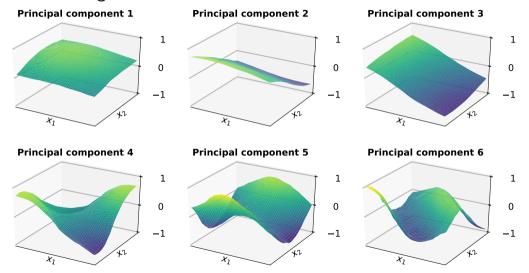
Gaussian Tuning Curve Principal Components



PCA of 2D Tuning Curves



PCA of 2D Tuning Curves



Combination of 2D Polynomials

Conclusions

- ► Can use **PCA** to find the basis functions underlying neural representations
- ► Singular values inversely proportional to noise
- Basis function shape depends on
 - x-intercept distributions
 - Neuron response curve G[J]
- Finding optimal tuning curves for computing particular functions
 - ⇒ Full network optimization (must use gradient descent)

Image sources

Title slide

Maurice Denis: Homage to Cézanne, 1900

From Wikimedia.