

## ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT)

ORGANISATION OF ISLAMIC COOPERATION (OIC)

Department of Computer Science and Engineering (CSE)MID SEMESTER EXAMINATION  
DURATION: 1 Hour 30 Minutes

SUMMER SEMESTER, 2016-2017

FULL MARKS: 75

**CSE 4835: Pattern Recognition**

Programmable calculators are not allowed. Do not write anything on the question paper.  
There are **4 (four)** questions. Answer any **3 (three)** of them.

Figures in the right margin indicate marks.

1. a) Briefly explain why generalization issue should be considered rather than overfitting in classification. 5
- b) What characteristics should an ideal feature extractor hold during extracting a feature vector representing a sample object? Explain each of them with examples 7
- c) For a 'minimum distance to class member' classifier, find the weight vector  $w$  and bias  $w_0$  of its discriminant function  $g(x)$ . Show that this piecewise linear classifier can be viewed in terms of a linear machine for classifying subclasses of patterns. 8+5

2. a) Show that the distance from the hyperplane  $g(x) = w^T x + w_0 = 0$  to the point  $x_a$  is  $|g(x_a)| / \|w\|$ . 5+5  
Also prove that the projection  $x_p$  on the hyperplane is given by

$$x_p = x_a - \frac{|g(x_a)|}{\|w\|^2} w$$

- b) There are generally three ways to devise multicategory classifiers employing linear discriminant functions. Describe each of such designs along with their pros and cons. Use necessary illustrations. 9
- c) Define the Perceptron criterion function  $J$  for finding the augmented weight vector of a linear discriminant function  $g(x)$  in a two-class problem. Fit this criterion function into the steps of a basic Gradient Descent technique for getting solution vector. 1+5
3. a) In many pattern classification problems, one has the option either to assign the pattern to one of  $c$  classes, or to *reject* it as being unrecognizable. If the cost for rejects is not too high, rejection may be a desirable action. 10

$$\text{Let } \lambda(\alpha_i | \omega_j) = \begin{cases} 0 & i = j \quad i, j = 1, 2, \dots, c \\ \lambda_r & i = c+1 \\ \lambda_s & \text{otherwise} \end{cases}$$

where,  $\lambda_r$  is the loss incurred for choosing the  $(c+1)^{\text{th}}$  action that is rejection, and  $\lambda_s$  is the loss incurred for making a substitution error. Show that the minimum risk is obtained if we decide  $\omega_i$  if  $P(\omega_i | x) \geq P(\omega_j | x)$  for all  $j$  and if  $P(\omega_i | x) \geq 1 - \lambda_r / \lambda_s$ , and reject otherwise.

- b) Devise the decision rule for the Bayes classifier with minimum risk. Explain the effects of increasing the loss function  $\lambda_{21}$ . 5
- c) Suppose, in a Bayes classifier the likelihood probability follows a normal distribution and all classes have the same covariance matrix but with different prior probabilities. Devise the equation of the decision boundary for each pair classes. 10



4. a) How are the estimates from Maximum Likelihood Estimation (MLE) different or similar to the estimates of Bayes Parameter Estimation?
- b) Use MLE method for estimating the unknown parameter  $\theta = \{\mu, \sigma^2\}$  of a univariate Gaussian distribution.
- c) In nonparametric density estimation techniques which conditions are required for the estimate  $p_n(x)$  to converge to true  $p(x)$ ? What do they assure?
- d) Describe the general principal of Bayes Parameter Estimation technique for approximating the unknown parameters.