

# ASSIGNMENT 5

Subject : Introduction To Data Science

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SP20 - BCS - 145

Section : B

Q1

- S1 "Sunshine state enjoy sunshine"  
 S2 "Brown fox jump high, brown fox run"  
 S3 "Sunshine state fox run fast"

### BoW Model

Output	Input									Total length
	Sunshine	state	enjoy	Brown	fox	jump	high	run	fast	
S1	2	1	1	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	0	7
S3	1	1	0	0	1	0	0	1	1	5

Vector S1 : [ 2 1 1 0 0 0 0 0 0 ]

Vector S2 : [ 0 0 0 2 2 1 1 1 0 ]

Vector S3 : [ 1 1 0 0 1 0 0 1 1 ]

## Term Frequency Model

	Sunshine	state	enjoy	Brown	fox	jump	high	run	fast
Tf-S1	$\frac{2}{2}$	$\frac{1}{4}$	$\frac{1}{4}$	0	0	0	0	0	0
Tf-S2	0	0	0	$\frac{2}{7}$	$\frac{2}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	0
Tf-S3	$\frac{1}{5}$	$\frac{1}{5}$	0	0	$\frac{1}{5}$	0	0	$\frac{1}{5}$	$\frac{1}{5}$

## IDF Model

Sunshine	idf	idf (sunshine) = $\log(\frac{3}{2}) = 0.18$
state	0.18	idf (state) = $\log(\frac{3}{2}) = 0.18$
enjoy	0.48	idf (enjoy) = $\log(\frac{3}{1}) = 0.48$
Brown	0.48	idf (Brown) = $\log(\frac{3}{1}) = 0.48$
fox	0.48	idf (fox) = $\log(\frac{3}{2}) = 0.18$
jump	0.48	idf (jump) = $\log(\frac{3}{1}) = 0.48$
high	0.48	idf (high) = $\log(\frac{3}{1}) = 0.48$
run	0.18	idf (run) = $\log(\frac{3}{2}) = 0.18$
fast	0.48	idf (fast) = $\log(\frac{3}{1}) = 0.48$

## TFIDF

S1

$$\begin{aligned} \text{tf-idf}(\text{sunshine}) &= \text{tf} * \text{idf} = 72 * 0.18 = 0.09 \\ \text{tf-idf}(\text{state}) &= \text{tf} * \text{idf} = 74 * 0.18 = 0.045 \\ \text{tf-idf}(\text{enjoy}) &= \text{tf} * \text{idf} = 74 * 0.48 = 0.12 \end{aligned}$$

S2

$$\begin{aligned} \text{tf-idf}(\text{Brown}) &= 2/7 * 0.48 = 0.137 \\ \text{tf-idf}(\text{fox}) &= 2/7 * 0.18 = 0.051 \\ \text{tf-idf}(\text{jump}) &= 7/7 * 0.48 = 0.07 \\ \text{tf-idf}(\text{high}) &= 7/7 * 0.48 = 0.07 \\ \text{tf-idf}(\text{run}) &= 7/7 * 0.18 = 0.026 \end{aligned}$$

S3

$$\begin{aligned} \text{tf-idf}(\text{sunshine}) &= 1/5 * 0.18 = 0.036 \\ \text{tf-idf}(\text{state}) &= 1/5 * 0.18 = 0.036 \\ \text{tf-idf}(\text{fox}) &= 1/5 * 0.18 = 0.036 \\ \text{tf-idf}(\text{run}) &= 1/5 * 0.18 = 0.036 \\ \text{tf-idf}(\text{fast}) &= 1/5 * 0.48 = 0.096 \end{aligned}$$

	idf(S1)	idf(S2)	idf(S3)
Sunshine	0.09	0	0.036
state	0.045	0	0.036
enjoy	0.12	0	0
Brown	0	0.137	0.036
fox	0	0.051	0
jump	0	0.07	0
high	0	0.07	0.036
run	0	0.026	0.096
fast	0	0	

Q2

Similarity between  $S1$  and  $S3$ .

$$\cos(S1, S3) = (S1 \cdot S3) / \|S1\| \|S3\|$$

$$S1 = [2 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

$$S3 = [1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1]$$

$$\begin{aligned} S1 \cdot S3 &= 2*1 + 1*1 + 1*0 + 0*0 + 0*1 + 0*0 + 0*0 + \\ &\quad 0*1 + 0*1 \\ &= 3 \end{aligned}$$

$$\begin{aligned} \|S1\| &= 2^2 + 1^2 + 1^2 + 0^2 + 0^2 + 0^2 + 0^2 + \\ &\quad 0^2 + 0^2 \\ &= 6^{0.5} = 2.45 \end{aligned}$$

$$\begin{aligned} \|S3\| &= 1^2 + 1^2 + 0^2 + 0^2 + 1^2 + 0^2 + 0^2 + \\ &\quad 1^2 + 1^2 \\ &= 5^{0.5} = 2.24 \end{aligned}$$

$$\cos(S1, S3) = \frac{3}{(2.45)(2.24)}$$

$$\cos(S1, S3) = 0.55$$