

Homework #1, due on Wednesday, 13 September 2023 [Attention: Late homework won't be graded.]

1. Solve the following first-order differential equations

(1)  $y' - 2y = x^2$

(2)  $y' - 2y = y^{-2}$

(3)  $y' - 3xy = x$

(4)  $xy' = y + \sqrt{xy}$

(5)  $y' = \frac{x + 2y + 3}{2x - y + 5}$

(6)  $y' = \frac{x + 2y + 3}{x + 2y + 5}$

(7)  $y' = -\frac{y \cos(x + y) + x + y}{\sin(x + y) + y \cos(x + y) + x + y}$

2. Consider the following ODE

$$y' = 2y/x$$

- a. Please state the condition on the initial values  $y(x_0) = y_0$  that is sufficient to guarantee a unique solution that passing through  $(x_0, y_0)$ .
- b. If the initial value is given by
  - i.  $y(0) = 0$ ,
  - ii.  $y(0) = 1$ ,
  - iii.  $y(1) = 0$ ,

Solve the problem and verify the conclusion drew from (a).