### ENV 790.30 - Time Series Analysis for Energy Data | Spring 2024 Assignment 3 - Due date 02/01/24

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#### **Directions**

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., "LuanaLima\_TSA\_A02\_Sp24.Rmd"). Then change "Student Name" on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

Please keep this R code chunk options for the report. It is easier for us to grade when we can see code and output together. And the tidy.opts will make sure that line breaks on your code chunks are automatically added for better visualization.

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

#### Questions

Consider the same data you used for A2 from the spreadsheet "Table\_10.1\_Renewable\_Energy\_Production\_and\_Consumption The data comes from the US Energy Information and Administration and corresponds to the December 2022 Monthly Energy Review. Once again you will work only with the following columns: Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption. Create a data frame structure with these three time series only.

R packages needed for this assignment: "forecast", "tseries", and "Kendall". Install these packages, if you haven't done yet. Do not forget to load them before running your script, since they are NOT default packages.\

```
library(lubridate)
library(ggplot2)
library(forecast)
library(Kendall)
library(tseries)
library(cowplot)
library(dplyr)
```

#### Inserting data

```
raw_data <- read.csv(file
="/Users/faustinkambale/Library/CloudStorage/OneDrive-DukeUniversity/Spring 2024 classes/Time Series 4</pre>
```

```
header=TRUE, skip=0)
head(raw_data, 10)
```

#### Set Dataset to work with

#### Transform Dataset in time series

```
ts_renerg <- ts(hw_data$renen, start=c(1980,1),frequency=12) # ts for Energy production
ts_bioenerg <- ts(hw_data$bioprod, start=c(1980,1), frequency=12) # ts for biomass energy production
ts_hydro <- ts(hw_data$hydrocon, start=c(1980,1),frequency=12) # ts for hydroelectric power consumption
```

##Trend Component

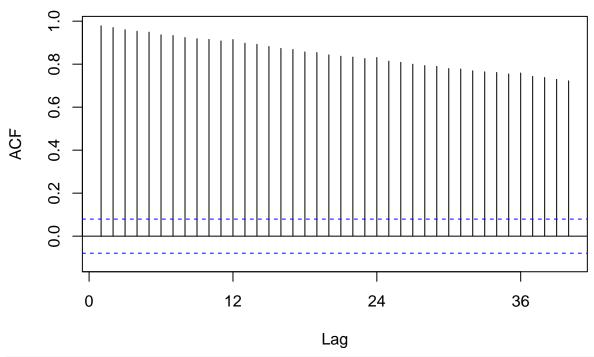
#### Q1

For each time series, i.e., Renewable Energy Production and Hydroelectric Consumption create three plots: one with time series, one with the ACF and with the PACF. You may use the some code form A2, but I want all the three plots side by side as in a grid. (Hint: use function plot\_grid() from the cowplot package)

#### Creating the plots

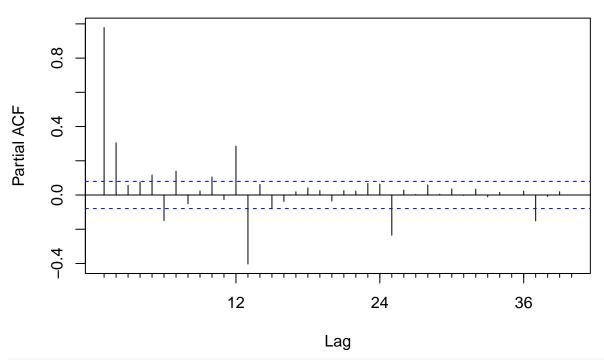
```
#Plots for Renewable energy production
reneg <- autoplot(ts_renerg, main="Energy Production", xlab = "Years", ylab = "Inflow")# autoplot for e
reneg_acf <- Acf(ts_renerg, lag.max = 40)</pre>
```

### Series ts\_renerg



reneg\_pacf <- Pacf(ts\_renerg, lag.max = 40)</pre>

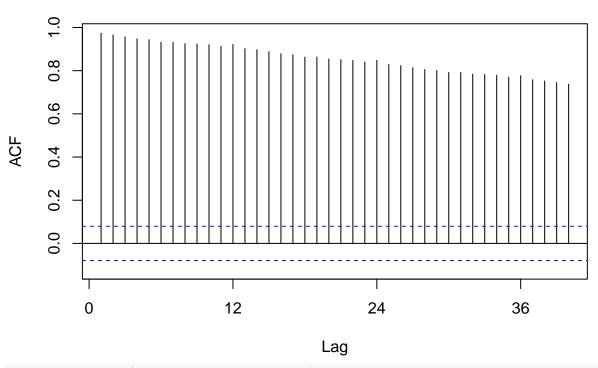
### Series ts\_renerg



plotenerg\_acf <- autoplot(reneg\_acf) #plot for Renewable energy production
plotenerg\_pacf <- autoplot(reneg\_pacf) #plot for Renewable energy production</pre>

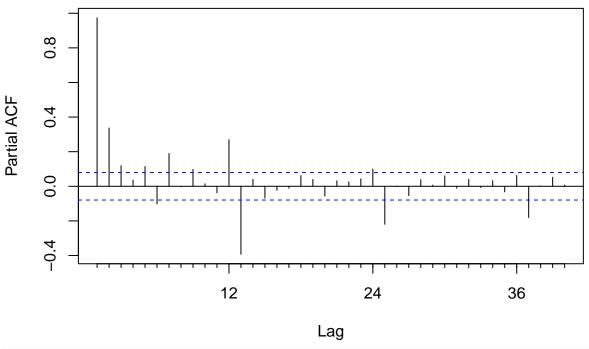
```
#Plot for Biomass Energy production
biom <- autoplot(ts_bioenerg, main="BiomEn. Production", xlab="Years", ylab="Inflow")
biom_acf <- Acf(ts_bioenerg, lag.max = 40)</pre>
```

# Series ts\_bioenerg



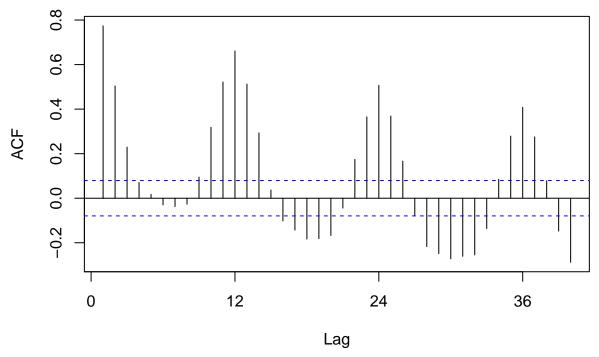
biom\_pacf <- Pacf(ts\_bioenerg, lag.max = 40)</pre>

# Series ts\_bioenerg



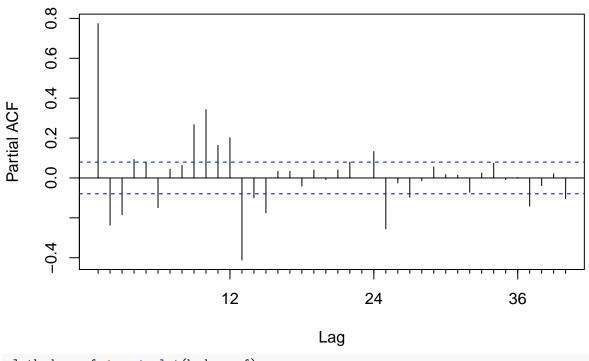
```
plotbiomeneg_acf <- autoplot(biom_acf)
plotbiomeneg_pacf <- autoplot(biom_pacf)
#Plot for Hydroelectric consumption
hydro <- autoplot(ts_hydro, main="Hydro Consum", xlab="Years", ylab="Inflow")
hydro_acf <- Acf(ts_hydro, lag.max = 40)</pre>
```

# Series ts\_hydro

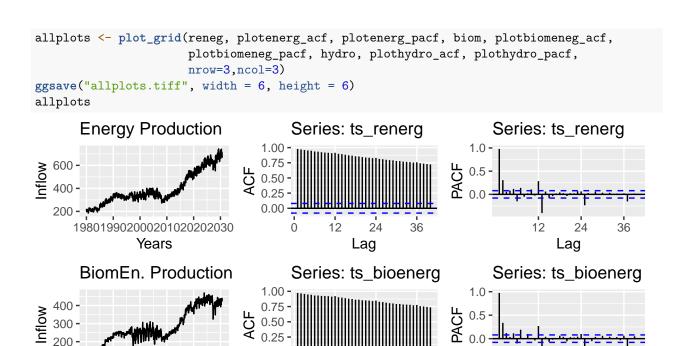


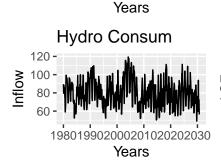
hydro\_pacf <- Pacf(ts\_hydro, lag.max = 40)</pre>

# Series ts\_hydro

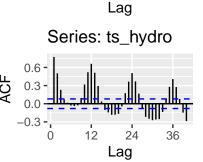


plothydro\_acf <- autoplot(hydro\_acf)
plothydro\_pacf <- autoplot(hydro\_pacf)</pre>





198019902000201020202030



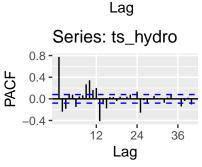
12

24

36

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12

24

36

#### $\mathbf{Q2}$

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From the plot in Q1, do the series Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption appear to have a trend? If yes, what kind of trend?

From these plots, the Renewable Energy Production plot and the biomass production have a significant decreasing trend (clearly shown through the Acf and Pcf plots). However, the hydroelectric power consumption plot displays an ambiguous trend.

#### Q3

Use the lm() function to fit a linear trend to the three time series. Ask R to print the summary of the regression. Interpret the regression output, i.e., slope and intercept. Save the regression coefficients for further analysis.

```
t <- 1:nobs #I create vector t

#combining *t* and each variable created into one data frame for nobs = 609
databio <- data.frame("t"=t[1:609],"original"=hw_data$bioprod)
dataenerg <- data.frame("t"=t[1:609],"original"=hw_data$renen)
datahydro <- data.frame("t"=t[1:609],"original"=hw_data$hydrocon)</pre>
```

```
#Running a multiple regression model
lintrend <- lm(ts_bioenerg ~ t + ts_renerg + ts_hydro, data = databio) #</pre>
summary(lintrend)
##
## Call:
## lm(formula = ts_bioenerg ~ t + ts_renerg + ts_hydro, data = databio)
##
## Residuals:
##
               10 Median
      Min
                               3Q
                                      Max
## -81.670 -10.845
                    3.344 14.464
                                   39.952
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 72.94619
                          5.18599 14.066 < 2e-16 ***
                          0.01090
## t
               0.06484
                                   5.946 4.66e-09 ***
## ts_renerg
               0.57829
                          0.01382 41.847 < 2e-16 ***
## ts_hydro
              -0.52375
                          0.05940 -8.817 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.92 on 605 degrees of freedom
## Multiple R-squared: 0.954, Adjusted R-squared: 0.9538
## F-statistic: 4185 on 3 and 605 DF, p-value: < 2.2e-16
```

This regression model is statistically significant given a high T-value for all the variables. The model, as well, is a good fit based on the high R-squared value of 95%.

#### Saving regression coefficients

```
beta0=as.numeric(lintrend$coefficients[1])
beta1=as.numeric(lintrend$coefficients[2:4])
```

#### $\mathbf{Q4}$

Use the regression coefficients from Q3 to detrend the series. Plot the detrended series and compare with the plots from Q1. What happened? Did anything change?

Detrending

```
#Create detrended series from linear trend
detrenerg <- hw_data$renen - (beta0+beta1*t[1:609])
detrendbio <- hw_data$bioprod - (beta0+beta1*t[1:609])
detrendhydro <-hw_data$hydrocon - (beta0+beta1*t[1:609])

ts_detrenerg <- ts(detrenerg, start= c(1980,1),frequency=12) #for Renewable Energy
#visualize the trend on observed data
plotdetener <- autoplot(ts_renerg, color="darkblue") +
    autolayer(ts_detrenerg,series="") +
    ylab("Inflows") +
    xlab("Years") +
    labs(color="", title = "RenErg Detr")

ts_detrebio <- ts(detrendbio, start= c(1980,1),frequency=12) #for Biomass Energy
#visualize the trend on observed data</pre>
```

```
plotdetbio <- autoplot(ts_bioenerg, color="green") +</pre>
  autolayer(ts_detrebio,series="") +
  ylab("Inflows") +
  xlab("Years") +
  labs(color="", title = "BioDetrended")
ts_dethydro <- ts(detrendhydro, start= c(1980,1),frequency=12) #for Hydro Energy
#visualize the trend on observed data
plotdethydro <- autoplot(ts_hydro, color="black") +</pre>
  autolayer(ts_dethydro,series="") +
  ylab("Inflows") +
  xlab("Years") +
  labs(color="", title = "HydroDetrended")
allplots1 <- plot_grid(reneg, plotdetener, biom, plotdetbio, hydro,
                        plotdethydro, #plotenerg_acf, #plotenerg_pcf, #plotbiomeneg_acf,
                       #plotbiomeneg_pcf, #plothydro_acf, #plothydro_pcf,
                       nrow=4, ncol=2)
ggsave("allplots1.tiff", width = 6, height = 6)
allplots1
       Energy Production
                                                      RenErg Detr
                                               Inflows
Molful 400 -
  400 -
200 -
                    2000
                                                      1980 1990 2000 2010 2020 2030
                                  2020
                                        2030
      1980
             1990
                           2010
                       Years
                                                                  Years
      BiomEn. Production
                                                     BioDetrended
                                  2020
                                                     1980 1990 2000 2010 2020 2030
      1980
             1990
                    2000
                           2010
                                        2030
                                                                 Years
                       Years
      Hydro Consum
                                                      HydroDetrended
                                                      1980 1990 2000 2010 2020 2030
      1980
             1990
                    2000
                           2010
                                  2020
                                        2030
                       Years
                                                                  Years
                                                                                           As
```

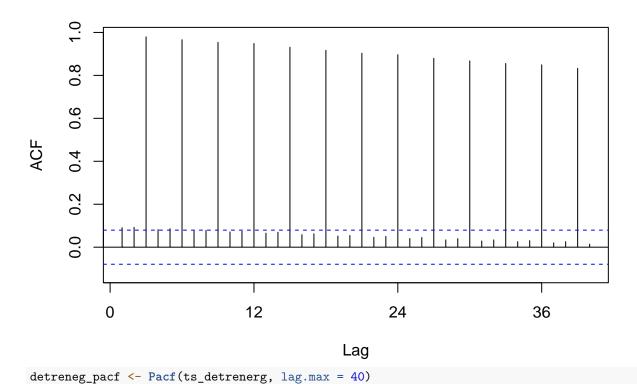
from these plots, the increase pattern in the data is clearly visible based on the plot with detrended series. For instance, the variability from the Hydroelectric consumption series was very fluctuating, but seems to be stabilized after detrending, displaying the increase over time. Same can be noticed with other variables as well.

#### $\mathbf{Q5}$

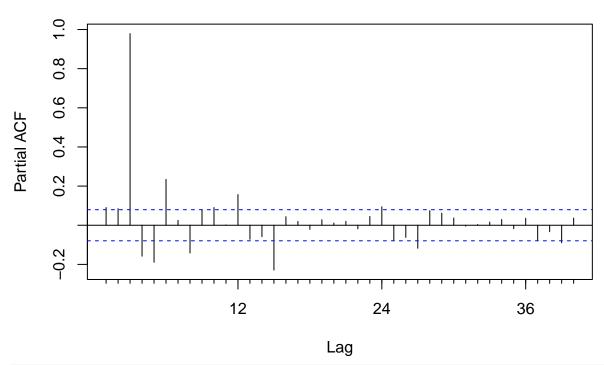
Plot ACF and PACF for the detrended series and compare with the plots from Q1. You may use plot\_grid() again to get them side by side, but mot mandatory. Did the plots change? How?

```
#plot for Detrended Renewable energy production
detreneg_acf <- Acf(ts_detrenerg, lag.max = 40)</pre>
```

### Series ts\_detrenerg

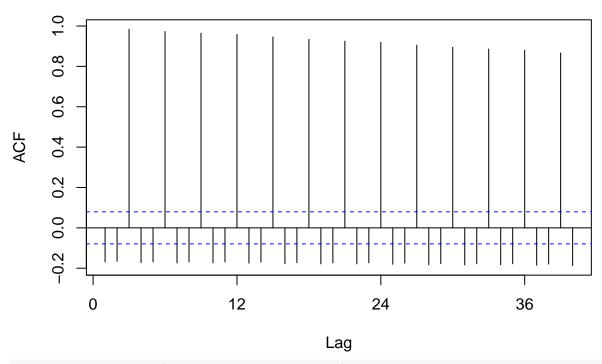


### Series ts\_detrenerg



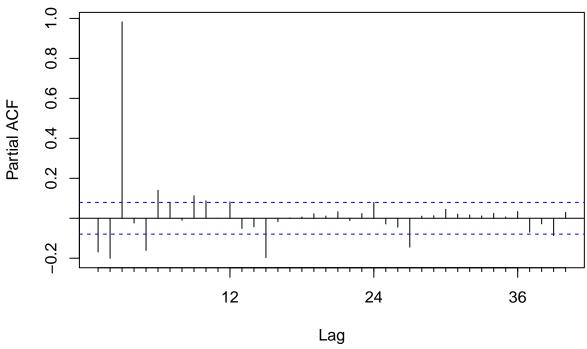
plotdetreneg\_acf <- autoplot(detreneg\_acf)
plotdetreneg\_pacf <- autoplot(detreneg\_pacf) #plot for Renewable energy production</pre>

# Series ts\_detrebio



detrbiom\_pacf <- Pacf(ts\_detrebio, lag.max = 40)</pre>

# Series ts\_detrebio

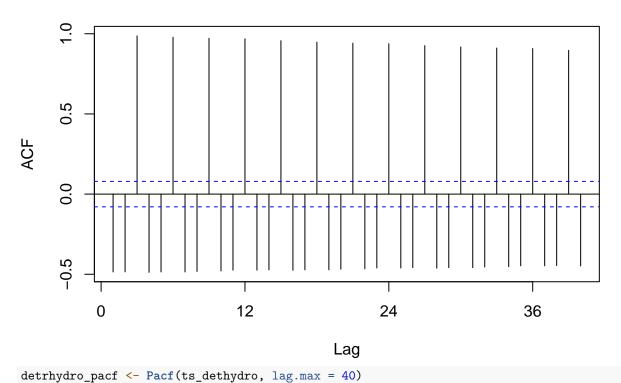


```
plotdetrbiom_acf <- autoplot(detrbiom_acf)
plotdetrbiom_pacf <- autoplot(detrbiom_pacf)

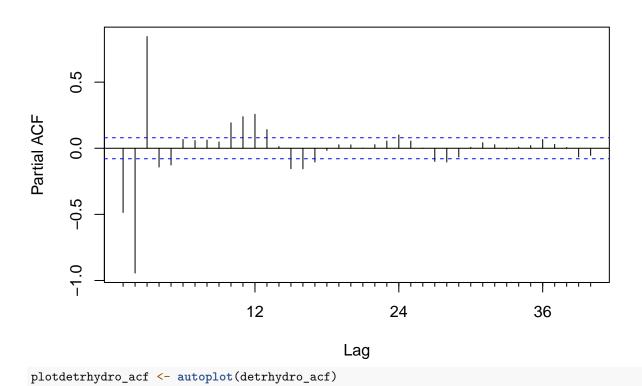
#Plot for Hydroelectric consumption

detrhydro_acf <- Acf(ts_dethydro, lag.max = 40)</pre>
```

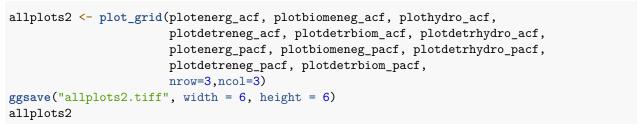
# Series ts\_dethydro

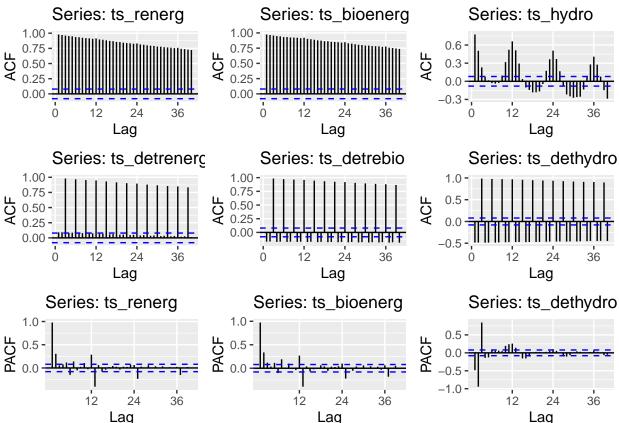


# Series ts\_dethydro



plotdetrhydro\_pacf <- autoplot(detrhydro\_pacf)</pre>





The most important change one can notice on the plots is that the trend is now stable, and one can easily identify the trend (either increase or decrease). Also, the detrendred variables variations are now close to zero while previously it was spread away from zero.

#### Seasonal Component

Set aside the detrended series and consider the original series again from Q1 to answer Q6 to Q8.

#### Q6

Just by looking at the time series and the acf plots, do the series seem to have a seasonal trend? No need to run any code to answer your question. Just type in you answer below.

Time series and Acf plot display different view of the data. For the variables Renewable Energy production and biomass energy production, ts display seasonal trend, but the seasonal trends variability is more visible through the acf than the time series plots.

#### **Q7**

Use function lm() to fit a seasonal means model (i.e. using the seasonal dummies) the two time series. Ask R to print the summary of the regression. Interpret the regression output. From the results which series have a seasonal trend? Do the results match you answer to Q6?

```
#for detrendred Renewable Energy
dummiesenerg <- seasonaldummy(ts_detrenerg)</pre>
#Then fit a linear model to the seasonal dummies
seas means_model=lm(detrenerg~dummiesenerg)
summary(seas_means_model)
##
## Call:
## lm(formula = detrenerg ~ dummiesenerg)
## Residuals:
       Min
                10 Median
                                30
                                       Max
## -349.21 -85.00 -28.33
                                   483.33
                             57.53
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                21.895 22.464 < 2e-16 ***
## (Intercept)
                    491.849
## dummiesenergJan -176.822
                                30.812 -5.739 1.52e-08 ***
## dummiesenergFeb -369.389
                                30.812 -11.988 < 2e-16 ***
## dummiesenergMar
                                30.812
                                         0.077
                                                  0.939
                      2.358
## dummiesenergApr -188.674
                                30.812
                                       -6.123 1.66e-09 ***
## dummiesenergMay -330.003
                                30.812 -10.710 < 2e-16 ***
## dummiesenergJun
                     -4.198
                                30.812 -0.136
                                                  0.892
## dummiesenergJul -177.714
                                30.812 -5.768 1.29e-08 ***
## dummiesenergAug -343.409
                                30.812 -11.145
                                                < 2e-16 ***
## dummiesenergSep -27.547
                                30.812 -0.894
                                                  0.372
## dummiesenergOct -200.047
                                30.964 -6.461 2.17e-10 ***
## dummiesenergNov -356.994
                                30.964 -11.529 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 154.8 on 597 degrees of freedom
## Multiple R-squared: 0.4562, Adjusted R-squared: 0.4462
## F-statistic: 45.54 on 11 and 597 DF, p-value: < 2.2e-16
#for detrendred Biomass Production
dummiesbiom <- seasonaldummy(ts_detrebio)</pre>
#Then fit a linear model to the seasonal dummies
seas means model1=lm(detrendbio~dummiesbiom)
summary(seas_means_model1)
##
## Call:
## lm(formula = detrendbio ~ dummiesbiom)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
                             45.71 315.82
           -60.49 -14.65
##
  -314.63
##
## Coefficients:
```

```
##
                  Estimate Std. Error t value Pr(>|t|)
                                16.74 22.571 < 2e-16 ***
## (Intercept)
                    377.79
## dummiesbiomJan
                  -181.46
                                23.55 -7.704 5.53e-14 ***
## dummiesbiomFeb
                  -366.20
                                23.55 -15.547 < 2e-16 ***
## dummiesbiomMar
                   -10.42
                                23.55
                                      -0.443
                                                 0.658
## dummiesbiomApr -201.58
                                23.55 -8.558
                                              < 2e-16 ***
## dummiesbiomMay
                  -350.58
                                23.55 -14.884
                                              < 2e-16 ***
## dummiesbiomJun
                   -19.32
                                23.55 -0.820
                                                 0.412
## dummiesbiomJul
                  -183.74
                                23.55 -7.801 2.76e-14 ***
## dummiesbiomAug
                  -338.88
                                23.55 -14.387
                                              < 2e-16 ***
## dummiesbiomSep
                   -11.61
                                23.55 -0.493
                                                 0.622
                                23.67 -7.773 3.37e-14 ***
## dummiesbiomOct
                  -183.99
## dummiesbiomNov
                  -346.31
                                23.67 -14.630 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 118.4 on 597 degrees of freedom
## Multiple R-squared: 0.5851, Adjusted R-squared: 0.5774
## F-statistic: 76.53 on 11 and 597 DF, p-value: < 2.2e-16
#for detrendred Hydroenergy Consumption
dummieshydro <- seasonaldummy(ts dethydro)</pre>
#Then fit a linear model to the seasonal dummies
seas_means_model2=lm(detrendhydro~dummieshydro)
summary(seas_means_model2)
##
## Call:
## lm(formula = detrendhydro ~ dummieshydro)
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -187.299
            -43.067
                        1.775
                                41.795
                                       180.468
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   167.604
                                11.434 14.658
                                                 <2e-16 ***
## dummieshydroJan -174.977
                                16.091 -10.874
                                                 <2e-16 ***
## dummieshydroFeb -337.639
                                16.091 -20.983
                                                 <2e-16 ***
## dummieshydroMar
                      5.254
                                16.091
                                         0.327
                                                  0.744
                                16.091 -10.855
                                                 <2e-16 ***
## dummieshydroApr -174.660
## dummieshydroMay -322.726
                                16.091 -20.057
                                                 <2e-16 ***
                                                  0.508
## dummieshydroJun
                    10.650
                                16.091
                                        0.662
## dummieshydroJul -176.261
                                16.091 -10.954
                                                 <2e-16 ***
                                                 <2e-16 ***
## dummieshydroAug -344.060
                                16.091 -21.382
## dummieshydroSep -15.226
                                16.091 -0.946
                                                  0.344
## dummieshydroOct -196.447
                                16.170 -12.149
                                                 <2e-16 ***
## dummieshydroNov -347.533
                                16.170 -21.492
                                                 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 80.85 on 597 degrees of freedom
## Multiple R-squared: 0.7495, Adjusted R-squared: 0.7449
## F-statistic: 162.4 on 11 and 597 DF, p-value: < 2.2e-16
```

From this linear regression, we can assert that the biomass production variable and the hydro energy consumption variables have a seasonal variability given the significance of the regression model. Nevertheless, the renewable energy detrended regression output appears to be not statistically significant (R-square less that 50%).

#### $\mathbf{Q8}$

Use the regression coefficients from Q7 to deseason the series. Plot the deseason series and compare with the plots from part Q1. Did anything change?

```
## Saving regression coefficients for model1
beta01=as.numeric(seas_means_model1$coefficients[1])
beta11=as.numeric(seas means model1$coefficients[2:12])
## Saving regression coefficients for model2
beta02=as.numeric(seas_means_model2$coefficients[1])
beta12=as.numeric(seas_means_model2$coefficients[2:12])
#Deseason series for model1
seas_component=array(0,nobs)
for(i in 1:nobs){
seas_component[i]=(beta01+beta11%*%dummiesbiom[i,])
}
#Transform into a ts object
ts deseasbiom <- ts(seas component, start=c(1980,1), frequency=12)
#Understanding what we did
deseasbiom <-autoplot(ts detrebio,series="Observed - Trend") +</pre>
  autolayer(ts_deseasbiom, series="seasonal_component", alpha=0.5) +
  ylab("Biomass Production") +
  xlab("Years") +
  labs(color="", title = "Seasonal Component")
#Deseason series for model2
seas_component=array(0,nobs)
for(i in 1:nobs){
seas_component[i]=(beta02+beta12%*%dummieshydro[i,])
#Transform into a ts object
ts_deseashydro <- ts(seas_component,start=c(1980,1),frequency=12)</pre>
#Understanding what we did
deseashydro <- autoplot(ts_dethydro,series="Observed - Trend") +</pre>
  autolayer(ts_deseashydro,series="seas_component",alpha=0.5) +
  ylab("Hydro Energy") +
  xlab("Years") +
  labs(color="", title = "Seasonal Component")
```

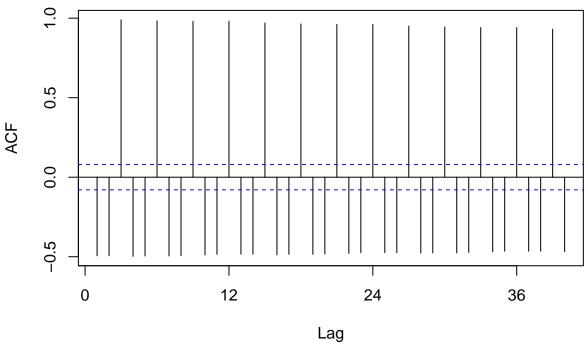
Compared to the Plots from Q1, it is clear now that the trend in these detrended plots are now stabilized. The seasonal component, for sure, is clearly visible.

#### $\mathbf{Q}\mathbf{9}$

Plot ACF and PACF for the deseason series and compare with the plots from Q1. You may use plot\_grid() again to get them side by side. but mot mandatory. Did the plots change? How?

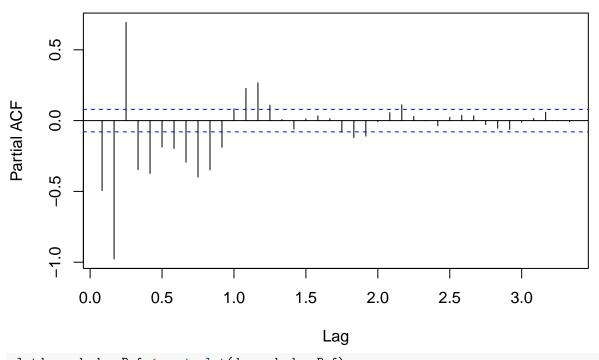
```
deseashydro_acf <- Acf(ts_deseashydro, lag.max = 40)</pre>
```

# Series ts\_deseashydro



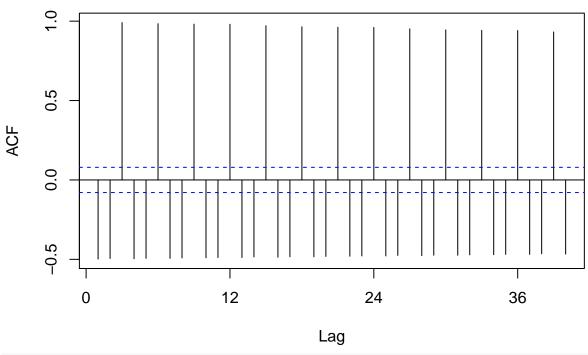
plotdeseashydro\_acf <- autoplot(deseashydro\_acf)
deseashydro\_Pcf <- pacf(ts\_deseashydro, lag.max = 40)</pre>

### Series ts\_deseashydro



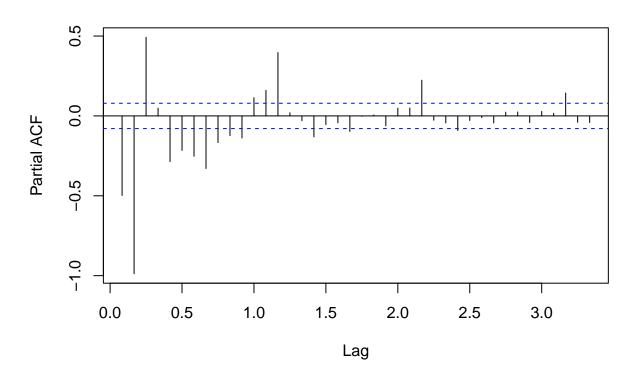
plotdeseashydro\_Pcf <- autoplot(deseashydro\_Pcf)</pre>

# Series ts\_deseasbiom



plotdeseasbiom\_acf <- autoplot(deseasbiom\_acf)
deseasbiom\_pacf <- pacf(ts\_deseasbiom, lag.max = 40)</pre>

### Series ts\_deseasbiom



```
plotdeseasbiom_pacf <- autoplot(deseasbiom_pacf)</pre>
allplots3 <- plot_grid(plotbiomeneg_acf, plotbiomeneg_pacf, plotdeseasbiom_acf,</pre>
                       plotdeseasbiom_pacf, plothydro_acf, plotdetrhydro_pacf,
                       plotdeseashydro_acf, plotdeseashydro_Pcf,
                       nrow=4,ncol=2)
ggsave("allplots3.tiff", width = 6, height = 6)
allplots3
       Series: ts_bioenerg
                                                  Series: ts_bioenerg
                12
                           .
24
                                     36
                                                             12
                                                                       24
       Ö
                                                                                 36
                       Lag
                                                                   Lag
                                                    Series: ts_deseasbiom
       Series: ts_deseasbiom
                12
                                     36
                           24
                                                                    Lag
                       Lag
                                                   Series: ts_dethydro
       Series: ts_hydro
                                     36
                                                                       24
                                                                                 36
                           24
                                                              12
                                                                    Lag
                       Lag
       Series: ts_deseashydro
                                                   Series: ts_deseashydro
             12
                                    36
                           24
```

Lag

Lag