Homework 1

Out: 9.20.21 Due: 9.28.21

1. [Combinational Logic]

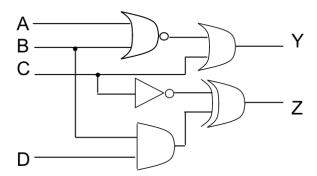
Given the following truth table:

Α	В	C	Out
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

- a) Write the sum-of-products formula for the truth table.
- b) Simplify your formula as much as you can. Show your work.
- c) Draw the gate-level logic circuit which corresponds to your simplified formula.

2. [Combinational Logic]

Write the (un-simplified) formulas expression for Y and Z below:



3. [Number Representation]

Convert the following numbers to 8 bit signed 2's complement binary, and to hexadecimal. Provide both answers and show your work – do not use a calculator.

- a) $(25)_{10}$
- b) $(-62)_{10}$
- c) $(127)_{10}$

4. [Number Representation]

Convert the following numbers to decimal. Show your work – do not use a calculator.

a) $(6AFA)_{16}$

- b) (0010 0001)₂'s complement
- c) $(1011\ 1001)_{2's\ complement}$

5. [Floating Point Representation]

- a) Convert the decimal number 63.25 to binary representation using the IEEE 754 single precision format. Represent your answer in binary and hex, and show your
- b) Convert the IEEE 754 single precision format number 0xC1300000 to decimal. Show your work.

6. [Binary Arithmetic]

Perform the following operations involving 8-bit 2's complement numbers and indicate whether arithmetic overflow occurs. Check your answers by converting to decimal sign and magnitude representation. Notice that part (d) involves multiplication.

7. [K-maps]

Simplify the following expressions using K-maps:

- a) F(x,y,z) = x'y'z' + x'y'z + x'yz + xy'z' + xy'z
- b) F(x,y,z) = x'y'z + x'yz + xy'z + xyz
- c) F(A,B,C,D) = A'B'C'D' + AC'D' + B'CD' + A'BCD + BC'D
- d) F(w,x,y,z) = x'z + w'xy' + w(x'y + xy')