



Course Code: MT-1006

Course Title: Differential Equations

Fall 2023

Quiz#3

Maximum Marks: 10

Date: 06-10-2023

Name:

Time: 20 minutes

Roll No:

Q.1 Identify the type of differential equation  $xy' + (1+x)y = e^{-x} \sin 2x$  and solve.

$$xy' + (1+x)y = e^{-x} \sin 2x$$

Linear equation  
in general form.

or

$$\frac{dy}{dx} + \frac{(1+x)}{x} y = \frac{e^{-x} \sin 2x}{x}$$

$$\frac{dy}{dx} + \left(\frac{1}{x} + 1\right) y = \frac{e^{-x} \sin 2x}{x} \quad \text{--- (A)}$$

Multiply eq (A) by I.F. here  $P(x) = \frac{1}{x} + 1$

$$\int P(x) dx = \int \left(\frac{1}{x} + 1\right) dx$$

$$= \ln x + x$$

$$\text{I.F.} = e^{\int P(x) dx}$$

$$= e^{\ln x + x}$$

$$= e^{\ln x} \cdot e^x$$

$$\boxed{\text{I.F.} = x e^x}$$

$$x e^x \frac{dy}{dx} + \left(\frac{1}{x} + 1\right) x e^x y = x e^x \frac{e^{-x} \sin 2x}{x}$$

or  $x e^x \frac{dy}{dx} + (1+x) e^x y = \sin 2x$

$$\frac{d}{dx} (x e^x \cdot y) = \sin 2x$$

Apply integration

$$\Rightarrow (x e^x \cdot y) = \int \sin 2x dx$$

$$x e^x \cdot y = \frac{-\cos 2x}{2} + C$$

or  $y = \frac{1}{x e^x} \left[ \frac{-\cos 2x}{2} + C \right]$