

3NF and Dependency Preservation

Consider the Relation Contracts(*Cid, Sid, Pid, dept, part, qty*)

■ FD's

- *Cid* -> *Cid, Sid, Pid, Dept, Part, Qty*.
- *Pid, Part* -> *Cid*.
- *Sid, Dept* -> *Part*.
- *Pid* -> *Sid*

■ 3NF

- ***Pid* -> *Sid***
 - *R2(Pid, Sid)*
 - Now its in 3NF
 - *Contracts(Cid, Pid, Dept, Part, qty)*
 - In 3NF
 - But lost dependency ***Sid, Dept* -> *Part***

3NF decomposition:

if $X \rightarrow A$ holds in R , then either:

- X is a superkey of R , or
- A is a prime attribute of R

Keys are

Cid

Pid, Part

Pid, Dept

Dependency Preserving 3NF

■ Consider the Relation $R(A,B,C,D)$ with the following FDs

- $A \rightarrow B C D$

- $B \rightarrow D$

- $C \rightarrow D$

- 3NF Decomposition

- $R_1(B, D)$

- $R_2(A B C)$

- Dependencies are lost? $C \rightarrow D$

3NF decomposition:

if $X \rightarrow A$ holds in R , then either:

a) X is a superkey of R , or

b) A is a prime attribute of R

Key is **A**

Algorithm: Decomposition into 3NF

(with Dependency Preservation & Lossless Join)

Input: A universal relation R and a set of functional dependencies F on the attributes of R .

1. Find a **minimal cover** G for F
2. For each X of a FD in G , create a relation in D with attributes $\{X \cup \{A_1\} \cup \{A_2\} \dots \cup \{A_k\}\}$,
3. If none of the relation in D contains a key of R , then create one more relation in D that contains key of R .
4. Eliminate Redundant relations from D

Dependency Preserving 3NF

- Consider the Relation $R(A,B,C,D)$ with the following FDs

- $A \rightarrow B C D$
- $B \rightarrow D$
- $C \rightarrow D$

- 3NF Decomposition using synthesis Algorithm

- Minimal Cover

- $A \rightarrow B C$
- $B \rightarrow D$
- $C \rightarrow D$
- $A \rightarrow D$ is a transitive dependencies so no need to preserve

- Make a relation for each dependency

Example

- Consider $R(\text{ssn}, \text{pno}, \text{sal}, \text{phone}, \text{dno}, \text{pname}, \text{ploc})$
- Consider following FDs
 - $FD1: \text{ssn} \rightarrow \text{sal}, \text{phone}, \text{dno}$
 - $FD2: \text{pno} \rightarrow \text{pname}, \text{ploc}$
 - $FD3: \{\text{ssn}, \text{pno}\} \rightarrow \text{sal}, \text{phone}, \text{dno}, \text{pname}, \text{ploc}$
- Key: $\{\text{ssn}, \text{pno}\}$
- Step1: minimal cover
 - $G: \{\text{ssn} \rightarrow \text{sal}, \text{phone}, \text{dno} ; \text{pno} \rightarrow \text{pname}, \text{ploc}\}$
- Step2:
 - $R1(\text{ssn}, \text{sal}, \text{phone}, \text{dno})$
 - $R2(\text{pno}, \text{pname}, \text{ploc})$
- Step3:
 - $R3(\text{ssn}, \text{pno})$

Algorithm: Decomposition into 3NF

(with Dependency Preservation & Lossless Join)

Input: A universal relation R and a set of functional dependencies F on the attributes of R .

1. Find a minimal cover G for F
2. For each X of a FD in G , create a relation in D with attributes $\{X \cup \{A_1\} \cup \{A_2\} \dots \cup \{A_k\}\}$,
3. If none of the relation in D contains **a key** of R , then create one more relation in D that contains key of R .
4. Eliminate Redundant relations

a key

Note we do not have to preserve all keys

3NF and Dependency Preservation

Consider the Relation Contracts(*Cid, Sid, Pid, dept, part, qty*)

■ FD's

- *Cid* -> *Cid, Sid, Pid, Dept, Part, Qty*.
- *Pid, Part* -> *Cid*.
- ***Sid, Dept* -> *Part*.**
- ***Pid* -> *Sid***

Create a relation for each FD

- R1 (*Cid, Pid, Dept, Qty*)
- R2 (*Pid, Part, Cid*)
- R3(*Sid, Dept, Part*)
- R4(*Pid, Sid*)

3NF decomposition Rule

if $X \rightarrow A$ holds in R, then either:

- a) X is a superkey of R, or
- b) A is a prime attribute of R

Keys are

Cid

Pid, Part

Pid, Dept

REAL WORLD EXAMPLES



Example: Designing a Student Database

1. Students take courses
2. Students typically take more than one course
3. Students can fail courses and can repeat the same course in different semesters =>
Students can take the same course more than once.
4. Students are assigned a grade for each course they take.

studentID(sID),
sname,
dept,
advisor,
course(ID),
credit,
semester,
grade,
course-room,
instr,
instr-office

Example: Designing a Student Database

- Student_course(sID, sname, dept, advisor, course, credit, semester, grade, course-room, instr, instr-office)
- 1NF: Flat table
- Problems:
 - Redundancy
 - Insert anomalies
 - Delete anomalies
 - Update problems

Example: Designing a Student Database

■ Define FDs

- **sname, dept, advisor** are dependent only upon **sID**
 - **sID -> sname, dept, advisor**
- **credit** dependent only on **course** and is independent of which **semester** it is offered and which **student** is taking it.
 - **Course -> credit**
- **course-room, instructor and instructor-office** only depend upon the **course** and the **semester** (are independent of which student is taking the course).
 - **Course, Semester -> course-room, instructor, instructor-office**
- Only **grade** is dependent upon all 3 parts of the original key.
 - **Stud-Id, Course, Semester -> grade**
- **Instructor -> instructor-office**

Example: Designing a Student Database

Student_course(sID, sname, dept, advisor, course, credit, semester, grade, course-room, instr, instr-office)

- Student (sID, sname, dept, advisor)
- Student_Reg (sID, course, semester, grade)
- Course (course, credit)
- Course_Offering (course, semester, course-room, instructor)
- Instructor (instructor, instructor-office)
 - More organized, Less redundancy (save space??)
 - Performance problems?? (indirect references)

Normalization Example -- Sales Order

Sales Order

*Fiction Company
202 N. Main
Manhattan, KS 66502*

CustomerNumber:	1001	Sales Order Number:	405
Customer Name:	ABC Company	Sales Order Date:	2/1/2000
Customer Address:	100 Points Manhattan, KS 66502	Clerk Number:	210
		Clerk Name:	Martin Lawrence

Item Ordered	Description	Quantity	Unit Price	Total
800	widgit small	40	60.00	2,400.00
801	tingimajigger	20	20.00	400.00
805	thingibob	10	100.00	1,000.00

Order Total

Fields will be as follows:

SalesOrderNo, Date,
CustomerNo, CustomerName,
CustomerAdd,
ClerkNo, ClerkName,
ItemNo, Description, Qty,
UnitPrice

ItemNo -> Description

SalesOrderNo, ItemNo -> Qty, UnitPrice

SalesOrderNo -> Date, CustomerNo, CustomerName,
CustomerAdd, ClerkNo, ClerkName

CustomerNo -> CustomerName, CustomerAdd

ClerkNo -> ClerkName

Normalization: First Normal Form

- Separate Repeating Groups into New Tables.
- **Repeating Groups:** Fields that may be repeated several times for one document/entity
- The primary key of the new table (repeating group) is always a composite key;
- Relations in 1NF:
 - SalesOrderNo, ItemNo, Description, Qty, UnitPrice
 - SalesOrderNo, Date, CustomerNo, CustomerName, CustomerAdd, ClerkNo, ClerkName

Normalization: Third Normal Form

A relation R is in **3NF** if $X \rightarrow A$ holds in R, then either:

- a) X is a superkey of R, or
- b) A is a prime attribute of R

■ Relations in 3NF

- Customers: CustomerNo, CustomerName, CustomerAdd
- Clerks: ClerkNo, ClerkName
- Inventory Items: ItemNo, Description
- Sales Orders: SalesOrderNo, Date, CustomerNo, ClerkNo
- SalesOrderDetail: SalesOrderNo, ItemNo, Qty, UnitPrice

DECOMPOSITION REVISITED



Properties of Relational Decomposition

Attribute preservation condition:

- *Each attribute in R will appear in at least one relation schema R_i in the decomposition*

Dependency Preservation Property

- It is not necessary that the exact dependencies specified in F appear themselves in individual relations of the decomposition D .
- It is sufficient that the union of the dependencies that hold on the individual relations in D be equivalent to F .

Lossless (Non-additive) Join Property

- *lossless refers to loss of information, not to loss of tuples.*
- *In fact, for “loss of information” a better term is “addition of spurious information”*

Testing Binary Decompositions for Lossless Join Property

- **Binary Decomposition:** decomposition of a relation R into two relations.
- **Lossless join test for binary decompositions:**
 - A decomposition $D = \{R_1, R_2\}$ of R has the lossless join property with respect to a set of functional dependencies F on R if and only if either
 - **FD $((R_1 \cap R_2) \rightarrow (R_1 - R_2))$ is in F^+ , or**
 - **FD $((R_1 \cap R_2) \rightarrow (R_2 - R_1))$ is in F^+ .**

In other words,
the decomposition is lossless if the set of attributes that are used to join R_1 and R_2 i.e. $(R_1 \cap R_2)$ should be key either in R_1 or R_2

Example

A universal relation $R(SSN, Ename, Pnumber, Pname, Plocation, Hours)$,
with FDs

$SSN \rightarrow Ename$

$Pnumber \rightarrow Pname, Plocation$

$SSN, Pnumber \rightarrow Hours$

is decomposed into

$R_1(Ename, Pnumber)$

$R_2(SSN, Pnumber, Pname, Plocation, Hours)$

Is it lossy or lossless ?

Activity: Decompositions Lossless or Lossy ?

A universal relation $R(SSN, Ename, Pnumber, Pname, Plocation, Hours)$,
with FDs

SSN \rightarrow Ename

Pnumber \rightarrow Pname, Plocation

SSN, Pnumber \rightarrow Hours

is decomposed into

EMP		PROJECT			WORKS_ON		
SSN	ENAME	PNUMBER	PNAME	PLOCATION	SSN	PNUMBER	HOURS

Is it lossy or lossless ?

Decompositions

- Determine whether each decomposition has
 - The dependency preservation property, and
 - the lossless join property, with respect to F .
- Also determine the normal form of each relation in the decomposition

$$R = \{A, B, C, D, E, F, G, H, I, J\}$$

$$F = \{ \{A, B\} \rightarrow \{C\}, \\ \{A\} \rightarrow \{D, E\}, \\ \{B\} \rightarrow \{F\}, \\ \{F\} \rightarrow \{G, H\}, \\ \{D\} \rightarrow \{I, J\} \}.$$

- $D1 = \{R1, R2, R3, R4, R5\};$
 - $R1 = \{A, B, C\}, R2 = \{A, D, E\}, R3 = \{B, F\}, R4 = \{F, G, H\}, R5 = \{D, I, J\}$
- $D2 = \{R1, R2, R3\};$
 - $R1 = \{A, B, C, D, E\}, R2 = \{B, F, G, H\}, R3 = \{D, I, J\}$
- $D3 = \{R1, R2, R3, R4, R5\};$
 - $R1 = \{A, B, C, D\}, R2 = \{D, E\}, R3 = \{B, F\}, R4 = \{F, G, H\}, R5 = \{D, I, J\}$