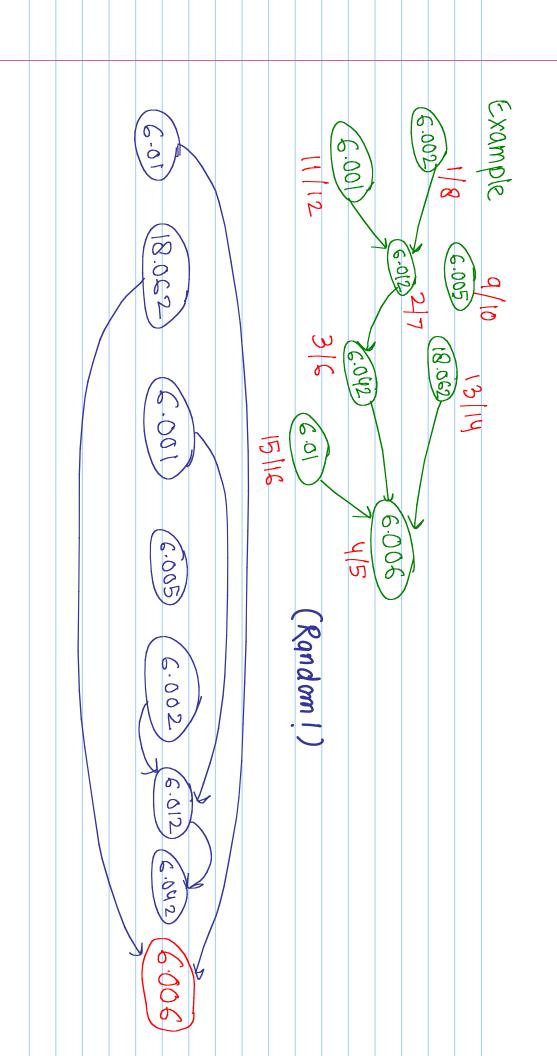
					O(V+E) Hme	3. refusio L	2. As each vertex tinishes, insert in faint of 1 (0(1)	(C: Imked list)	0	TOPOLOGICAL - SORT (G)	

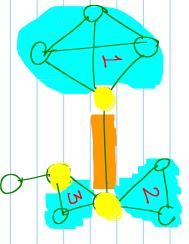


G=(V,E) connected, undirected graph Articulation Problem (curs Problem 22,2)

articulation point -> vertex whose removal disconnects G

bridge -> edge whose removal disconnects G

biconnected component -> maximal set of edges, any two edges in the set



a) Prove that roof of GII is an auticulation point of GIH it has at least thro child ren => if root is anticulation point, than it has at least two children Case 1, because of backedge, a simple cycle is formed involving or or belongs to only one biconnected component. Removing or doesn't dusconnect or Cause 2, removing it only removed one edge, can't disconnect on Consider root or with only one children Case 1: there is a back edge from a node in subtree pointing back to y Cases 2: Y have no back Edge pointing back to itself

If noof how of least two children, than it is an ordiculation point

removing y would disconnect these throfor more) components. If root has two or more children, and these can not be any cross edges

5 let u be a non-root vertier of G. T. Prove that u is an auticulation point of G. If I have that u is an auticulation point descendant of s to a proper ancestor of v.

or any du condant of s to a proper an cestar of v.

hack edges to a proper anciestal of v. If we remove v, every subtree ,

of v is still reachable through back edges. G is still connected. Contradiction ! ancestor of 1, then V is an asticulation point.

I no back edges from subtree to any ancestor of v, there can only be subtree from root. Hence, v is an anticulation point.

UN [V] = min of actual: (u,w) is a back edge for some descendant of v (d[v]

compute low [N] for all NEV (CI) in O(E) time

```
time = time +1
                                                                                                                                 いらせ (く,し)
                                                                     for all venex war and (w,v) e E(G)
                                                 if d[w]=0 than
( CM) ( V) = min ( low(V), d(M))
                     Unisit (w,v)
                                                                                                                                   A Cisit of han CR
```

initially call visit (v, o)

														2	
(OW (U) CO) CAN = Cr) O(M)	else	print v is an outiculation point	If (d(v) + (and low [w) > d(v))	print v is outiculation point	if (dry)= 1 and drw) = 2 arot = 1	(ON [U] = min((on(U), low(W))	Visit(N, U)	ACMJ= O	for all vellex wto, (w,v) eE(G)	(ONSU) = d(V)			Visit (V, u)	I show how to convoute all alliculation points in o(E) time	
					4						122 LONG(N) S V POR some child N OS V	o on surjection point		うの(で)がから、	

0 1 Prove that e is a bridge iff it does not be on any simple eyel. Show how to compute all bridges of G in O(E) in. (nk Johnson thom. It a does not be on only simple cycle, then It is a bridge. Removing e disconnects the two companions as it is the only connecting if e is a bridge, it does not lie on any simple cycle.

bridge either connects two aniculation points or a leaf vertex in G

(vestax with one edge)

if us v one onticulation points, or degree (v) =1 or degree (v)=)

for all eff(G), e=(UN)

