

Regular Expressions Practice Set

Did you know: *Regular expressions have been studied for nearly 50 years, yet many intriguing problems about their descriptive capabilities remain open [to interpretation].*

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How I attempt solving Regular Expressions:

Step 1: Enumerate the simple obvious cases for the language (only give it 15 seconds)

Step 2: Enumerate ALL the possible EDGE cases (give it a good hard 3 to 4 minutes)

Step 3: Start thinking about the regular expression from the PoV of Edge cases NOT the simple cases

Step 4: After drawing up an RE, brute force check it for all obvious and edge cases and see if any missing string is found or wrong string is generated

Step 5: If the RE is incorrect, identify the 'Leak(s)' and start fixing it by rearranging the RE appropriately

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Quiz 1 Regular Expressions

$\Sigma = \{a, b\}$

$L = \{x \mid x \in \Sigma^* \text{ and } x \text{ has at most 2 occurrences of } bb\}$

$L = \{ \epsilon, ba^*, bb, bbb, a^*bba^+bba^*, bbb a^*, a^*bbb, \dots \}$

A) $a^*(\epsilon + (b+bb+bbb+bba^+bb+bba^+(b^*a^+)^*bb) + ((aba^*)^* + (a^*ba)^*))a^*$

This above RE is partially incorrect! It fails to generate the edgecase "bbababb". If you are able to solve it, Email me your Solution. This error was pointed out by a student. Can YOU solve it? Try to. And let me know as well!

Update: I have solved it with another student, Let me know if you guys find further issues in it!

$\Sigma = \{a, b\}$

$L = \{x \mid x \in \Sigma^* \text{ and } x \text{ ends with either } ba \text{ or } ab\}$

$L = \{ ba, ab, a^*ab, a^*ba, b^+ab, b^+ba, \dots \}$

A) $(a^*b^*)^*(ab+ba)$

$$\Sigma = \{a, b\}$$

$$L = \{x \mid x \in \Sigma^* \text{ and } x \text{ has at least 2 occurrences of } bb\}$$

$$L = \{bbb, a^* bbb a^*, a^* bba^* bba^* (bb)^* a^*, \dots\}$$

A) $(a^*b^*)^*(bbb+a^*bba^*bba^*(bb)^*)(a^*b^*)^*$

Assignment Solution of RE will be posted here later after submission of assignment

My quiz when I was studying Automata

$$\Sigma = \{a, b\}$$

$$L = \{x \mid x \in \Sigma^* \text{ \& } |x| \text{ is multiple of 3 and every } i\text{th position in } x \text{ should contain } b, \text{ where } i \equiv 2 \pmod{3}\}$$

A) $a^3 + (aba + abb + bbb)(bab + bbb)(aba + abb + bbb)$

This one is particularly tough and I have implemented it partially. If any of you is able to crack it, you can email me with the solution so that I can update it here!

Language 1. The language of all strings over $\{a, b\}$ such that the as and bs are strictly alternating.

Examples of strings in the language: ϵ , a, b, ab, ba, aba, bab, abab, baba

Examples of strings not in the language: bb, aa, abba

Answer: $(ab)^*(a|e)|(ba)^*(b|e)$

Language 2. The language of all strings over $\{a, b\}$ that begin with “aba” and end with “bb”.

Examples of strings in the language: ababb, ababb, ababbb, ababbababb

Examples of strings not in the language: ϵ , aba, abab, abb

Answer: $aba(a|b)^*bb$

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Language 3. The language of all strings over $\{a, b\}$ such that the as always occur in groups of 2 or more.

Examples of strings in the language: ϵ , b, bbbb, aa, aaa, aabaaabbaa, bbaabaaabaabaaa

Examples of strings not in the language: a, aba, abba, aabaaaaba

Answer: $(b|(aaa^*))^*$

Language 4. The language of all strings over $\{a, b, c\}$ which start with “a” and which do not contain the substring “cb”. (Note that this one is challenging as a regular expression.)

Examples of strings in the language: a, ab, abc, ac, acc, accab

Examples of strings not in the language: ϵ , b, c, acb, abbabcba

Answer: $a(a|b|cc^*a)^*(cc^*|e)$

Language 5. The language of all strings over $\{a, b\}$ such that the number of as is even and the number of bs is odd. (Note that this one is challenging as a regular expression.)

Examples of strings in the language: b, aab, baa, aba, aaaba, aababab

Examples of strings not in the language: ϵ , aa, abba, abbbabab

Answer: $(aa|bb|abba|baab|abab|baba)^*(aba|b)(aa|bb|abba|baab|abab|baba)^*$

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Input Set is 0 and 1 For the questions below:

Q) 0 or 11 or 101

A) $0 | 11 | 101$

Q) only 0s

A) 0^*

Q) all binary strings

A) $(0|1)^*$

Q) all binary strings except empty string

A) $(0|1)(0|1)^*$

Q) begins with 1, ends with 1

A) $1 | (0|1)^*1$

Q) ends with 00

A) $(0|1)^*00$

Q) contains at least three 1s

A) $(0|1)^*1(0|1)^*1(0|1)^*1$

Q) contains at least three consecutive 1s

A) $(0|1)^*111(0|1)^*$

Q) contains the substring 110

A) $(0|1)^*110(0|1)^*$

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Q) doesn't contain the substring 110

A) $(0|10)^*1^*$

Q) contains at least two 0s but not consecutive 0s

A) $(1^*011^*(0+011^*))^*$

Q) has at least 3 characters, and the third character is 0

A) $(0|1)(0|1)0(0|1)^*$

Q) number of 0s is a multiple of 3

A) $1^*|(1^*01^*01^*01^*)^*$

Q) starts and ends with the same character

A) $1(0|1)^*1|0(0|1)^*0$

Q) odd length

A) $(0|1)((0|1)(0|1))^*$

Q) starts with 0 and has odd length, or starts with 1 and has even length

A) $0((0|1)(0|1))^*|1(0|1)((0|1)(0|1))^*$

Q) length is at least 1 and at most 3

A) $(0|1)|(0|1)(0|1)|(0|1)(0|1)(0|1)$

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