

# Real-Time High Quality Rendering

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## Lecture 10: Real-Time Physically-Based Materials (surface models)



# Announcements

- Correction: 2/3 contents covered after today's lecture!
- GAMES202 homework late submission is open now!
- GAMES101 graders
  - Now we have a few applications for graders!
  - Will soon reach out to get started!
- GAMES101 now has 599K views on Bilibili!

# Last Lecture

- Real-Time Global Illumination (screen space cont.)
  - Screen Space Directional Occlusion (SSDO)
  - Screen Space Reflection (SSR)
- Real-Time Physically-Based Materials

# Today

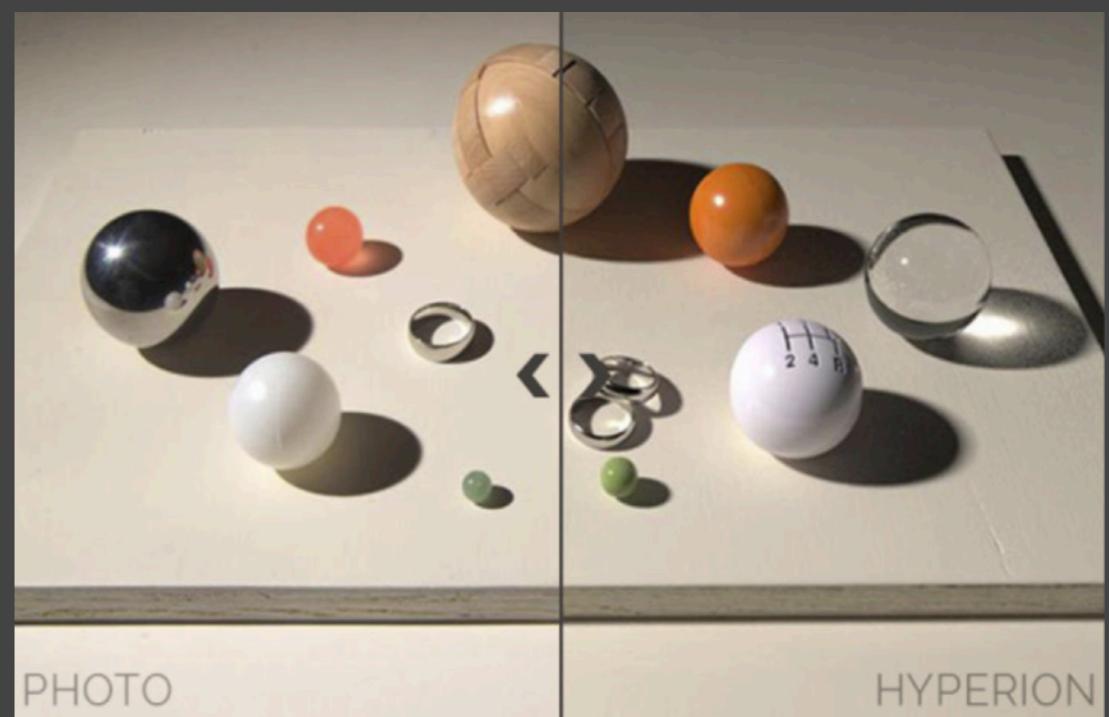
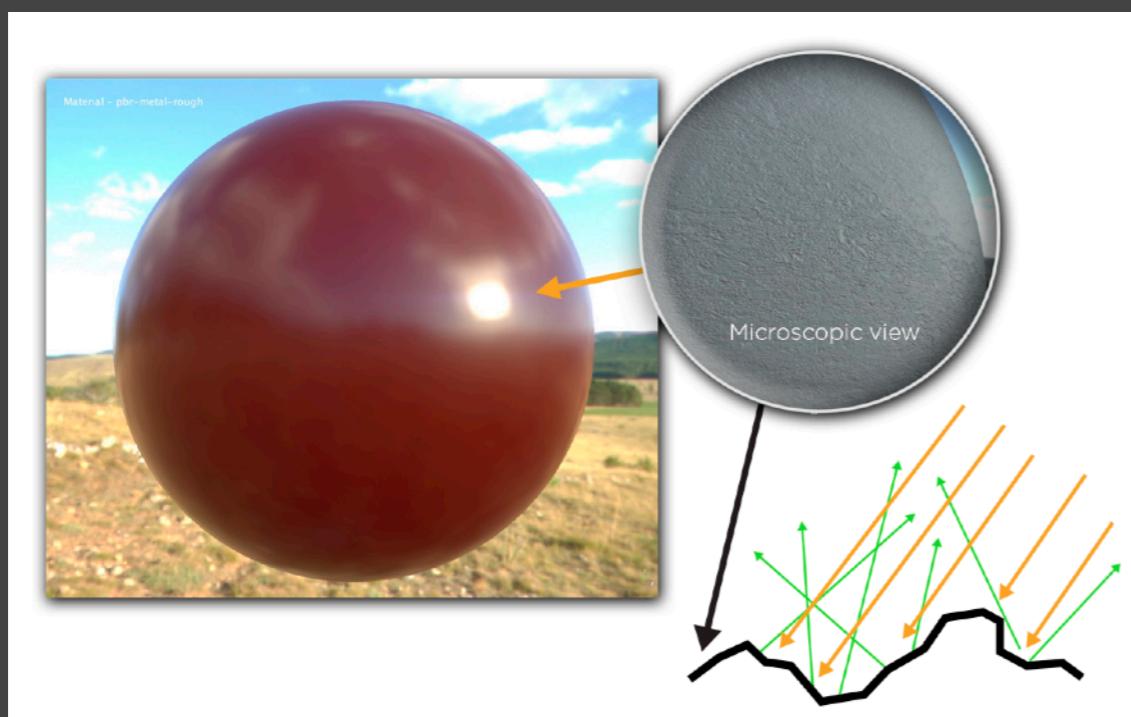
- Real-Time Physically-Based Materials
  - Microfacet BRDF
  - Disney principled BRDF
- Shading with microfacet BRDFs under polygonal lighting
  - Linearly Transformed Cosines (LTC)

# PBR and PBR Materials

- Physically-Based Rendering (PBR)
  - Everything in rendering should be physically based
  - Materials, lighting, camera, light transport, etc.
  - Not just materials, but usually referred to as materials :)
- PBR materials in RTR
  - The RTR community is much behind the offline community
  - “PB” in RTR is usually not actually physically based :)

# PBR Materials in RTR

- PBR materials in RTR
  - **For surfaces**, mostly just microfacet models (used wrong so not PBR) and Disney principled BRDFs (artist friendly but still not PBR)



# PBR Materials in RTR

- PBR materials in RTR
  - **For surfaces**, mostly just microfacet models and Disney principled BRDFs
  - **For volumes**, mostly focused on fast and approximate single scattering and multiple scattering (for cloud, hair, skin, etc.)



[Lara Croft from the Tomb Raider series]

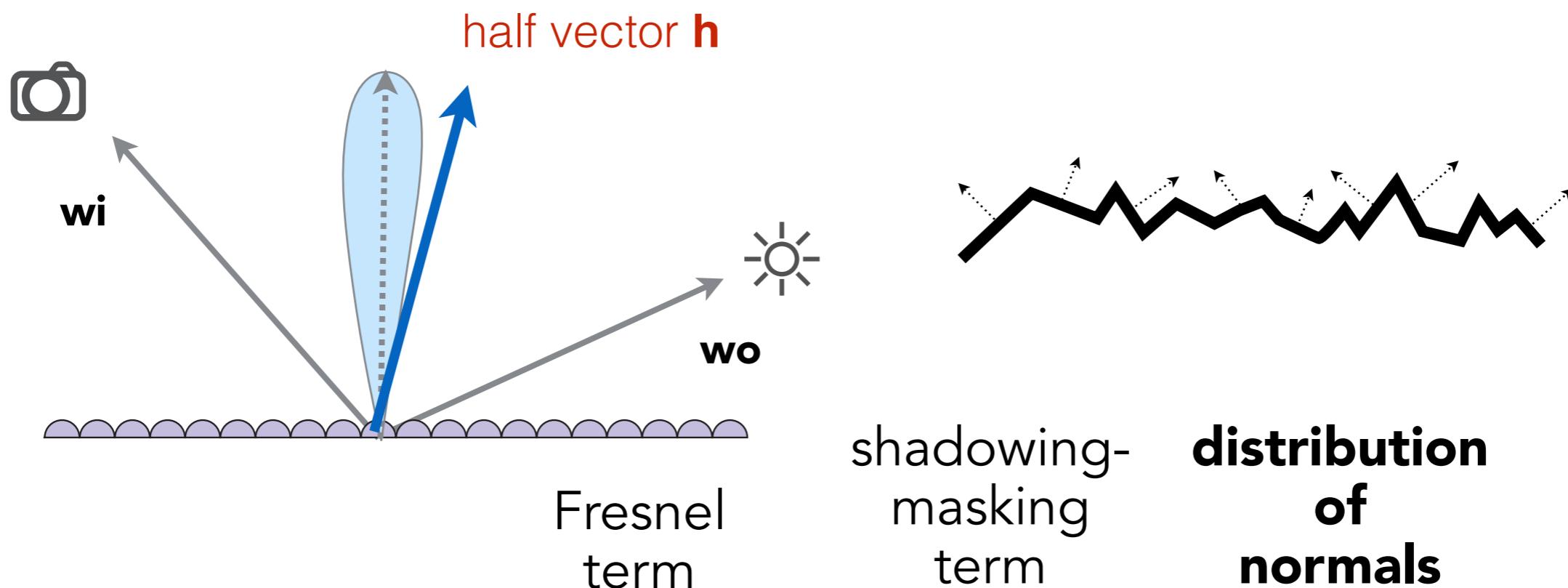
# PBR Materials in RTR

- PBR materials in RTR
  - **For surfaces**, mostly just microfacet models (used wrong so not PBR) and Disney principled BRDFs (artist friendly but still not PBR)
  - **For volumes**, mostly focused on fast and approximate single scattering and multiple scattering (for cloud, hair, skin, etc.)
  - Usually not much new theory, but a lot of implementation hacks\*
  - Still, performance (speed) is the key factor to consider

# Recap: Microfacet BRDF

# Microfacet BRDF

- What kind of microfacets reflect  $w_i$  to  $w_o$ ?  
(hint: microfacets are mirrors)



$$f(\mathbf{i}, \mathbf{o}) = \frac{\mathbf{F}(\mathbf{i}, \mathbf{h})\mathbf{G}(\mathbf{i}, \mathbf{o}, \mathbf{h})\mathbf{D}(\mathbf{h})}{4(n, \mathbf{i})(n, \mathbf{o})}$$

# The Fresnel Term

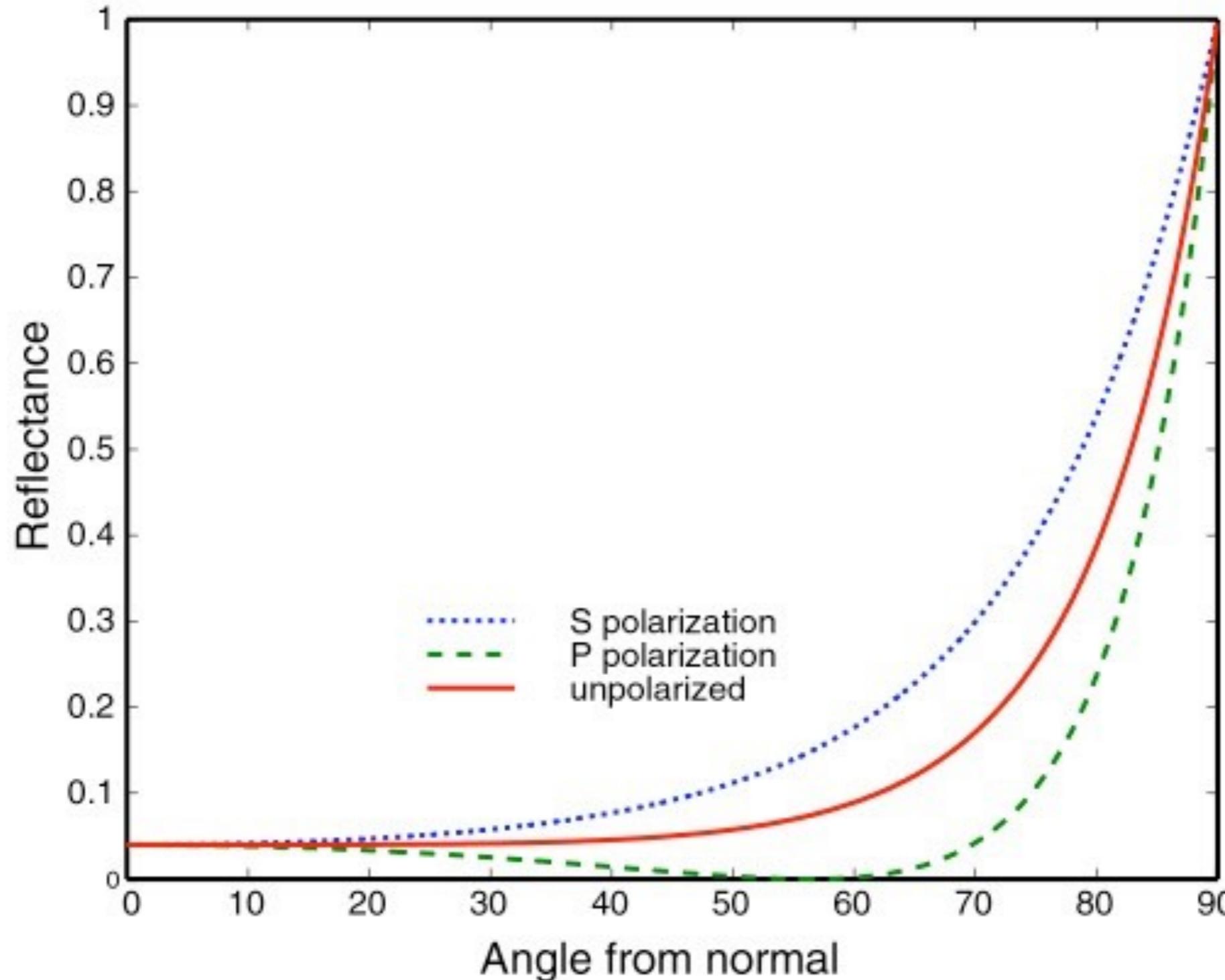
Reflectance depends on incident angle (and polarization of light)



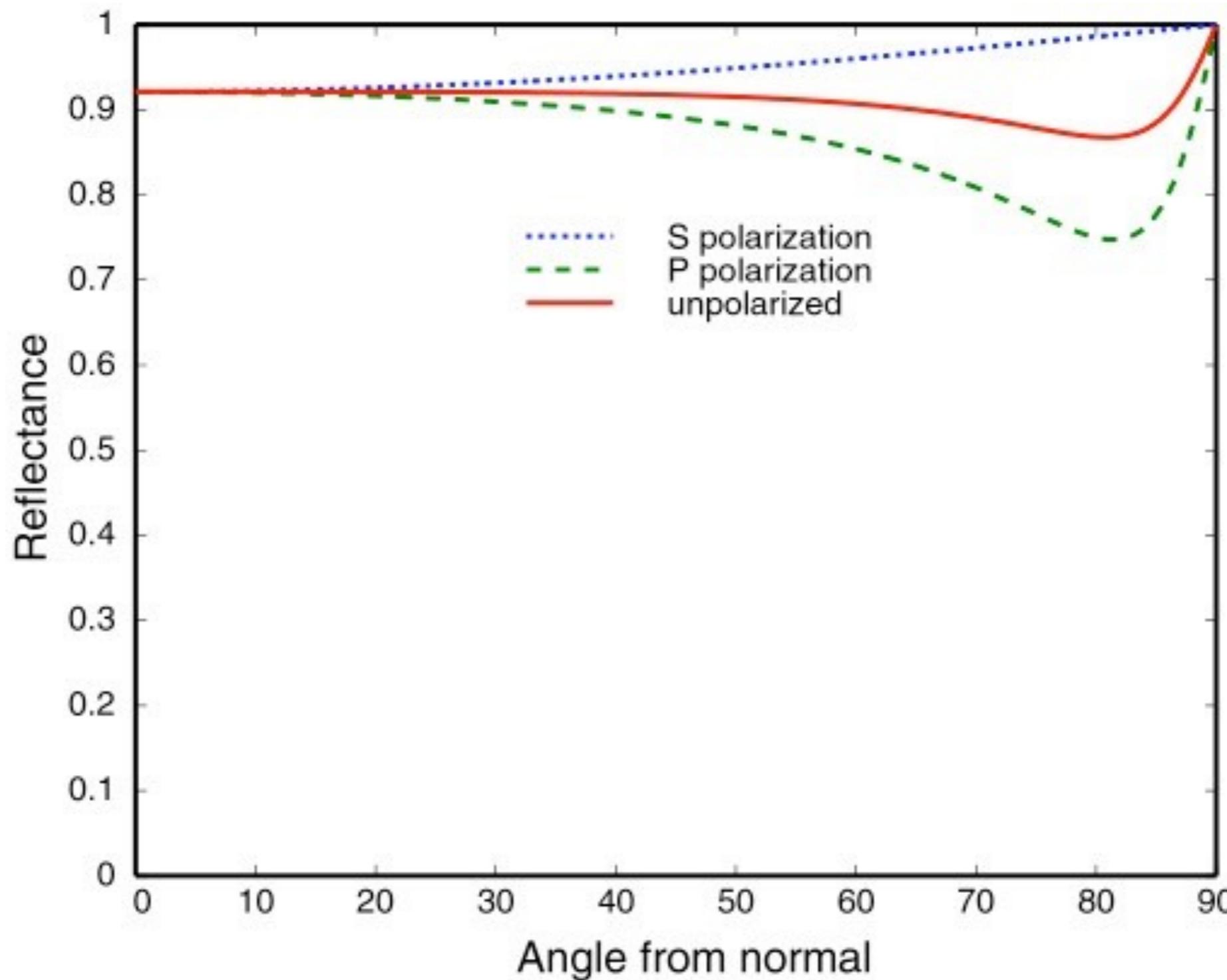
This example: reflectance increases with grazing angle

[Lafortune et al. 1997]

# Fresnel Term (Dielectric, $\eta = 1.5$ )



# Fresnel Term (Conductor)



# Fresnel Term — Formulae

Accurate: need to consider polarization

$$R_s = \left| \frac{n_1 \cos \theta_i - n_2 \cos \theta_t}{n_1 \cos \theta_i + n_2 \cos \theta_t} \right|^2 = \left| \frac{n_1 \cos \theta_i - n_2 \sqrt{1 - \left( \frac{n_1}{n_2} \sin \theta_i \right)^2}}{n_1 \cos \theta_i + n_2 \sqrt{1 - \left( \frac{n_1}{n_2} \sin \theta_i \right)^2}} \right|^2,$$
$$R_p = \left| \frac{n_1 \cos \theta_t - n_2 \cos \theta_i}{n_1 \cos \theta_t + n_2 \cos \theta_i} \right|^2 = \left| \frac{n_1 \sqrt{1 - \left( \frac{n_1}{n_2} \sin \theta_i \right)^2} - n_2 \cos \theta_i}{n_1 \sqrt{1 - \left( \frac{n_1}{n_2} \sin \theta_i \right)^2} + n_2 \cos \theta_i} \right|^2.$$

$$R_{\text{eff}} = \frac{1}{2} (R_s + R_p).$$

Approximate: Schlick's approximation

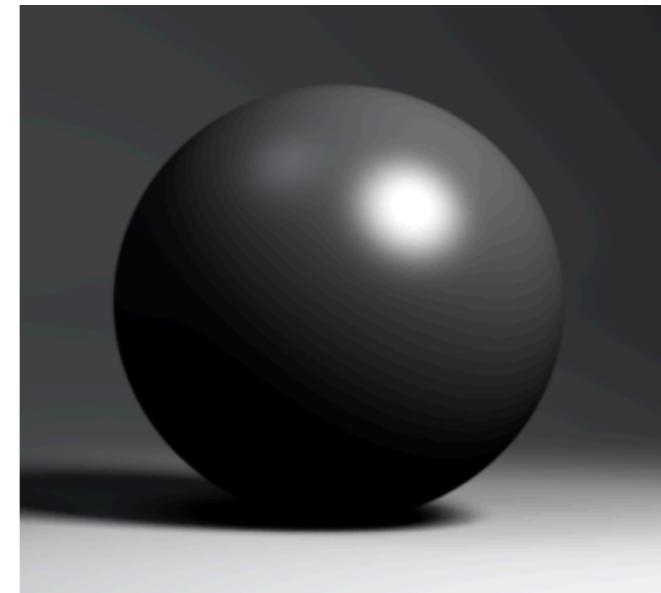
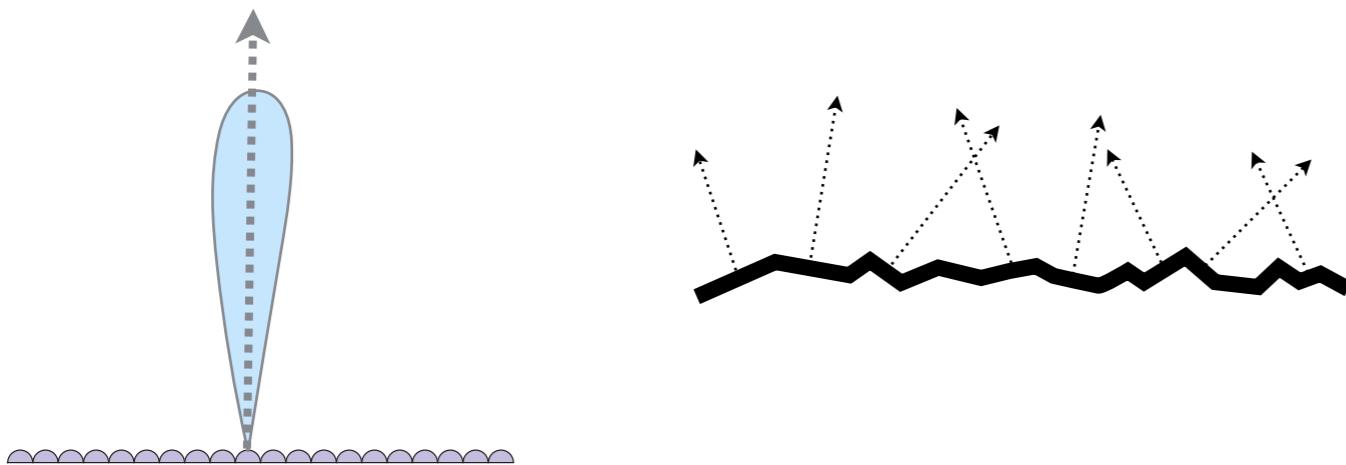
$$R(\theta) = R_0 + (1 - R_0)(1 - \cos \theta)^5$$

$$R_0 = \left( \frac{n_1 - n_2}{n_1 + n_2} \right)^2$$

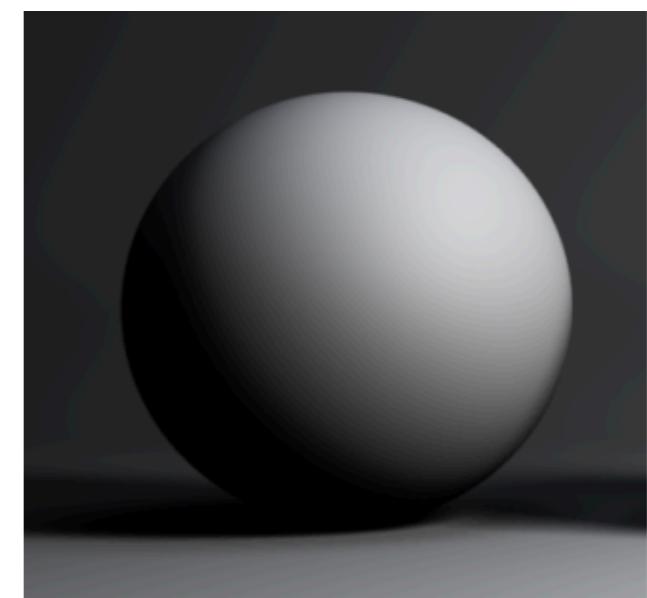
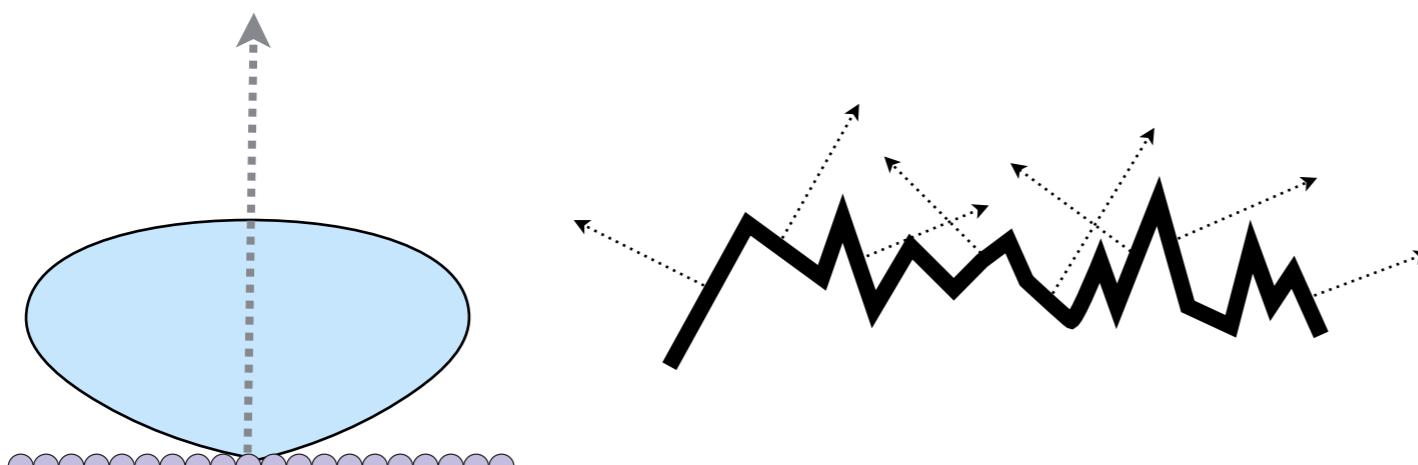
# Normal Distribution Function (NDF)

- Key: the **distribution** of microfacets' normals

- Concentrated  $\iff$  glossy

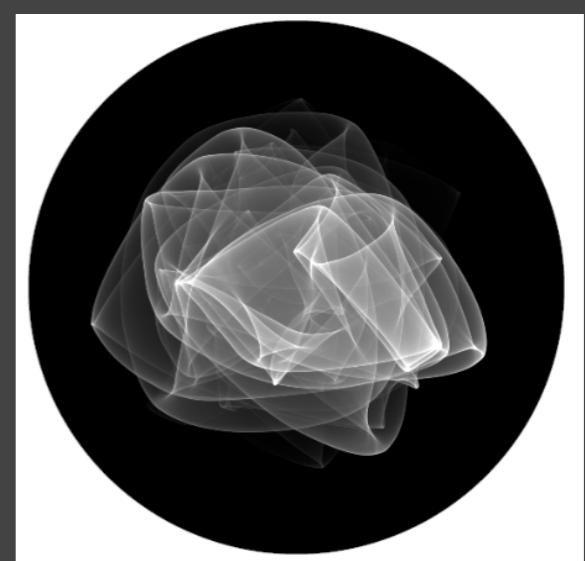
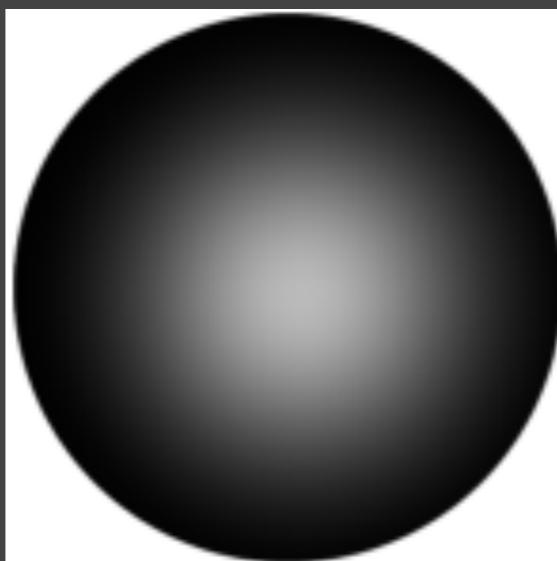
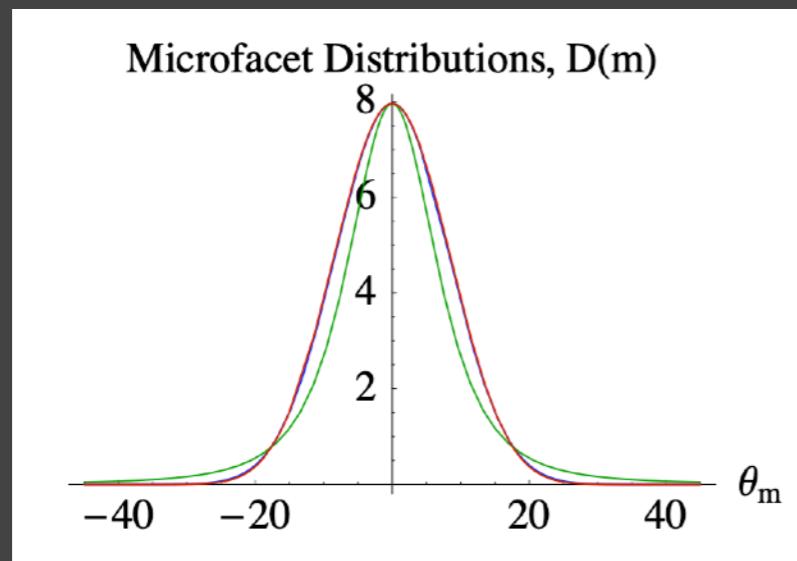


- Spread  $\iff$  diffuse



# Normal Distribution Function (NDF)

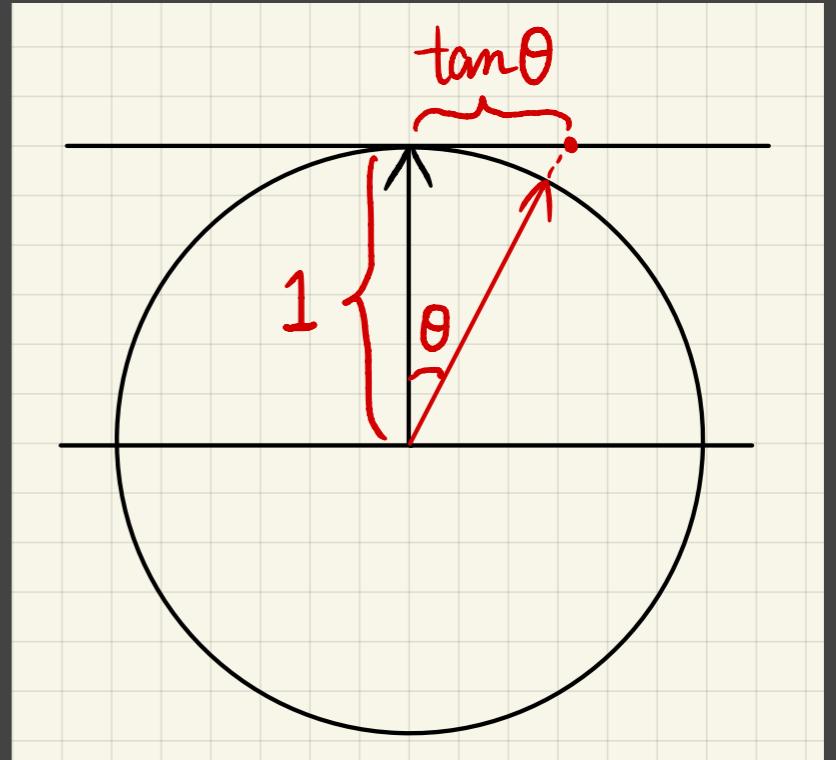
- The Normal Distribution Function (NDF)
  - Note: has nothing to do with the normal distribution in stats
  - Various models to describe it
    - Beckmann, GGX, etc.
    - Detailed models [Yan 2014, 2016, 2018, ...]



# Normal Distribution Function (NDF)

- Beckmann NDF
  - Similar to a Gaussian
  - But defined on the **slope space**

$$D(h) = \frac{e^{-\frac{\tan^2 \theta_h}{\alpha^2}}}{\pi \alpha^2 \cos^4 \theta_h}$$

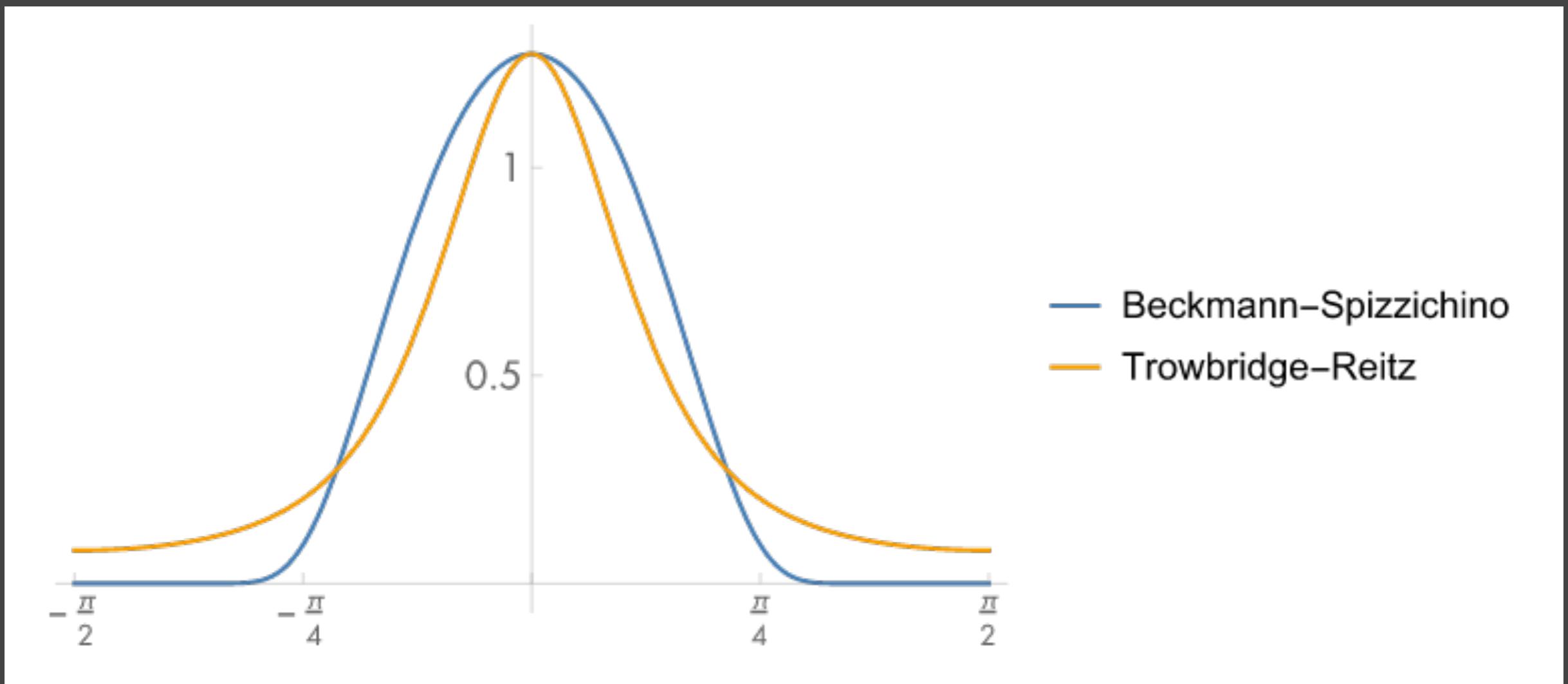


$\alpha$ : roughness of the surface (the smaller, the more like mirror/specular)

$\theta_h$ : angle between half vector  $h$  and normal  $n$

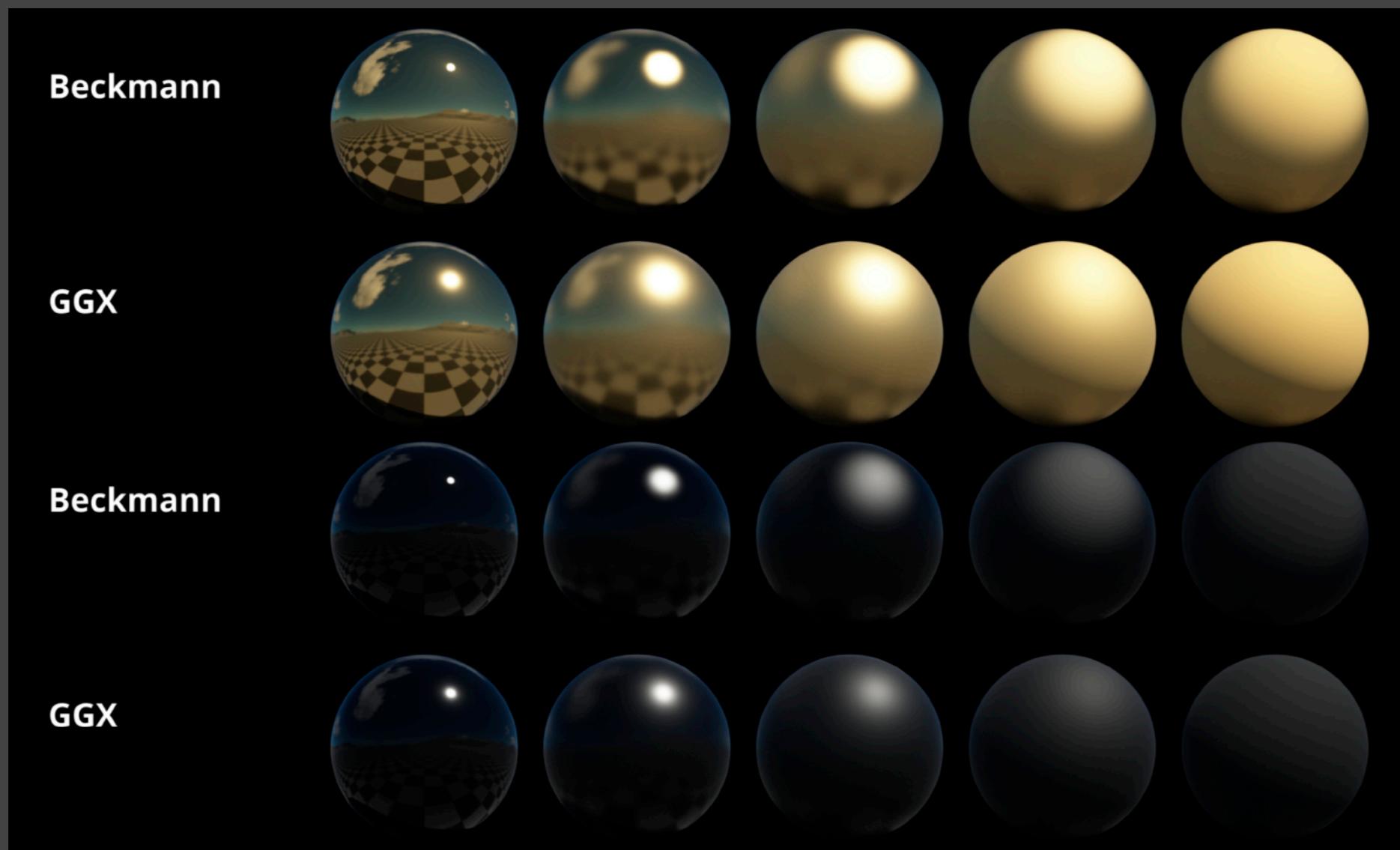
# Normal Distribution Function (NDF)

- GGX (or Trowbridge-Reitz) [Walter et al. 2007]
  - Typical characteristic: long tail!



# Normal Distribution Function (NDF)

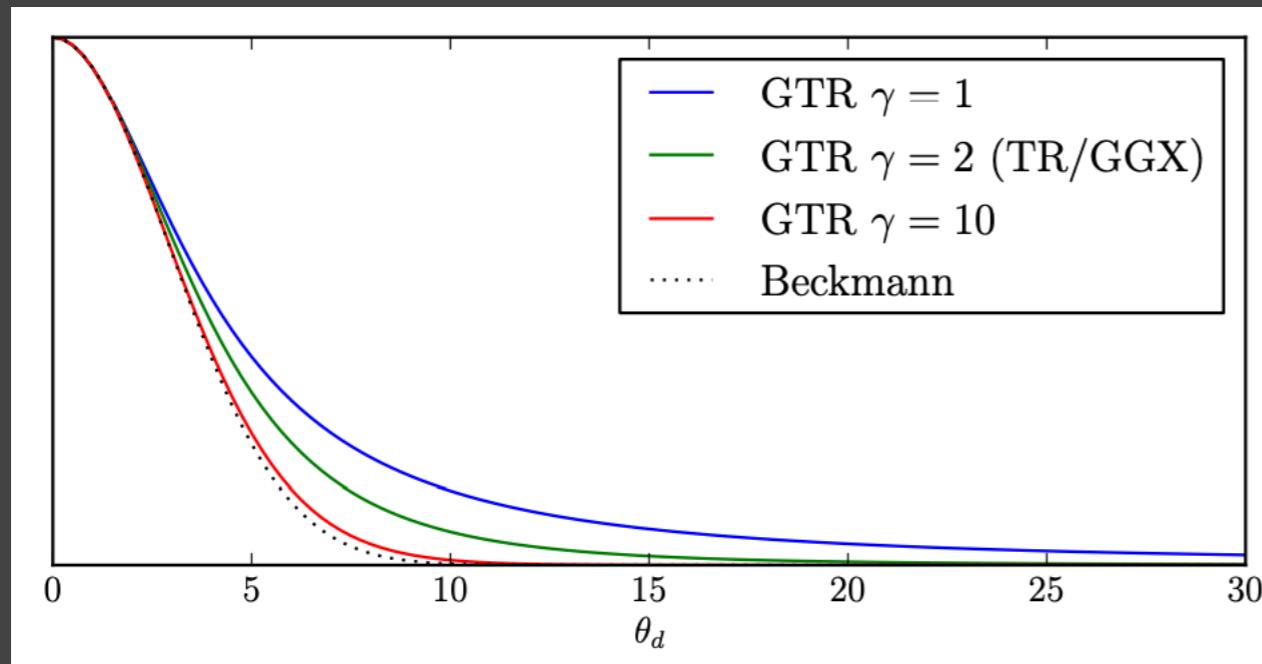
- Comparison: Beckmann vs. GGX



<https://planetside.co.uk/news/terragen-4-5-release/>

# Normal Distribution Function (NDF)

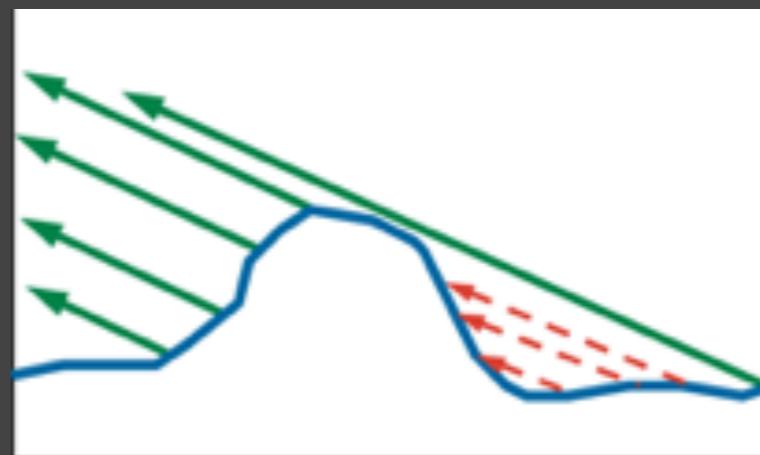
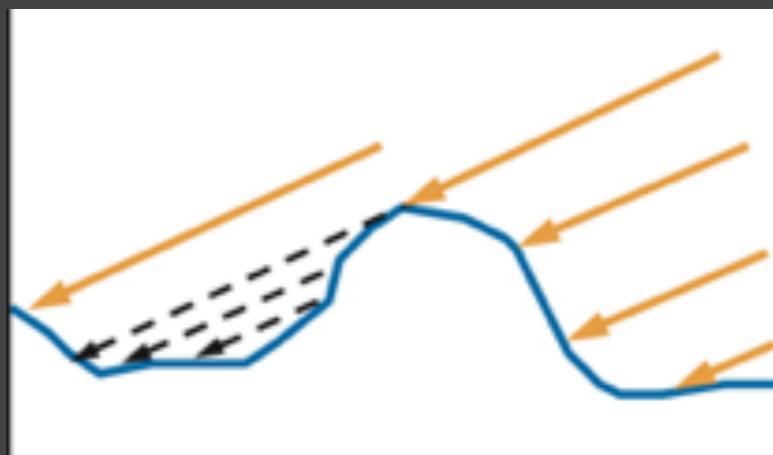
- Extending GGX [by Brent Burley from WDAS]
  - GTR (Generalized Trowbridge-Reitz)
  - Even longer tails



# Shadowing-Masking Term

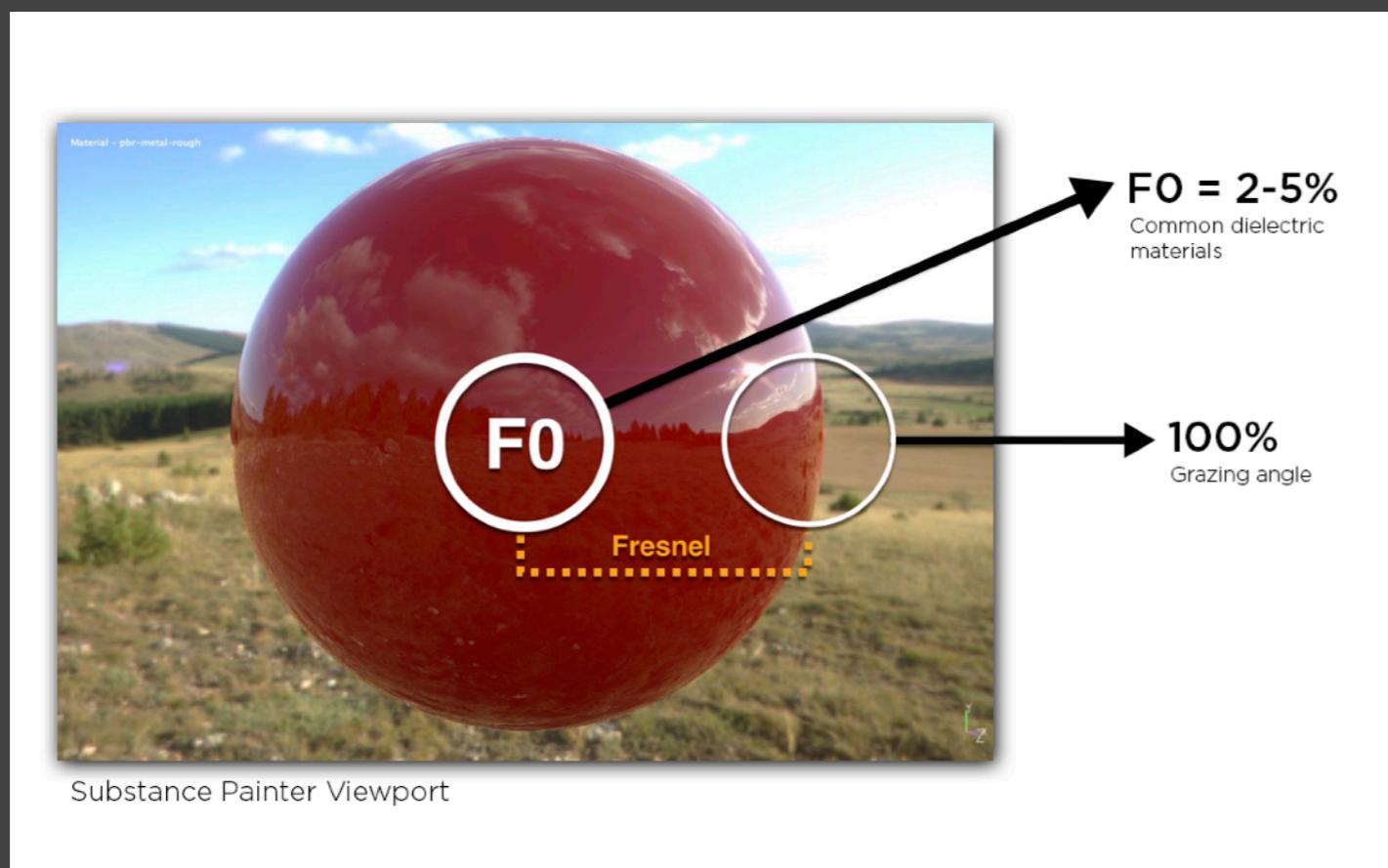
- Or, the geometry term  $G$ 
  - Account for self-occlusion of microfacets
  - Shadowing – light, masking – eye
  - Provide darkening esp. around grazing angles

$$f(i, o) = \frac{F(i, h)G(i, o, h)D(h)}{4(n, i)(n, o)}$$



# Shadowing-Masking Term

- Why is it important?
  - Suppose no G term, what will happen when the incident / outgoing is from grazing angle?



$$f(i, o) = \frac{F(i, h)G(i, o, h)D(h)}{4(n, i)(n, o)}$$

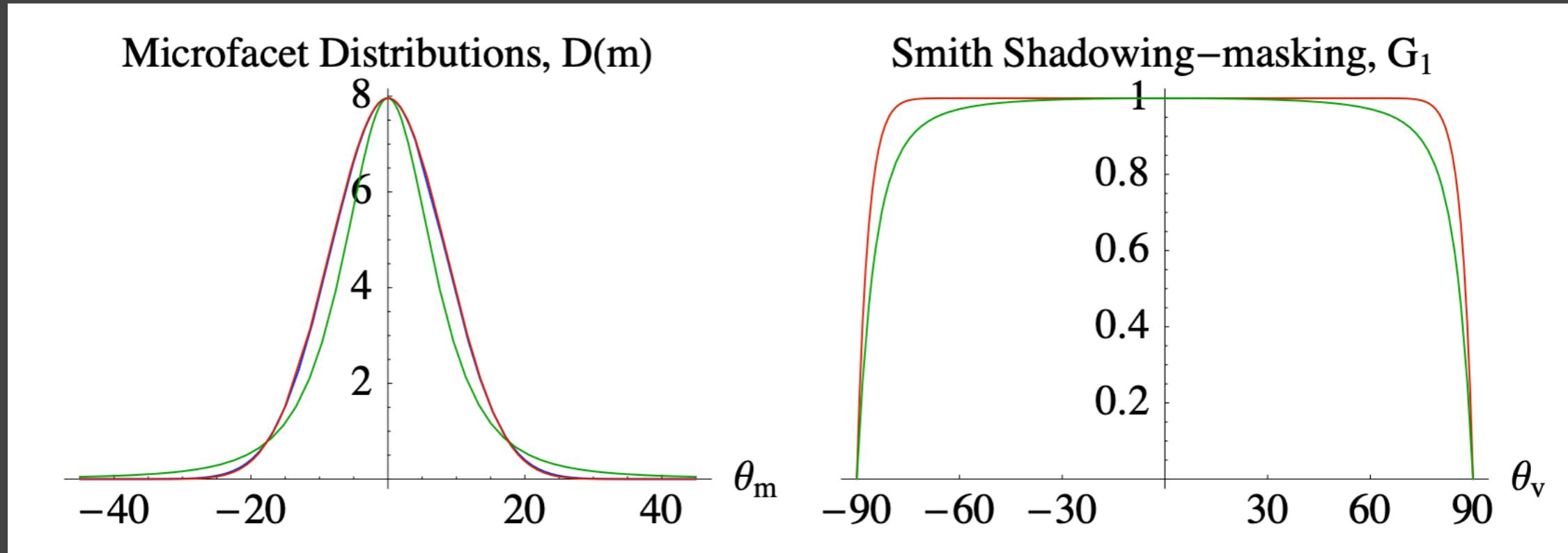


Can be arbitrarily bright around grazing angles!

# Shadowing-Masking Term

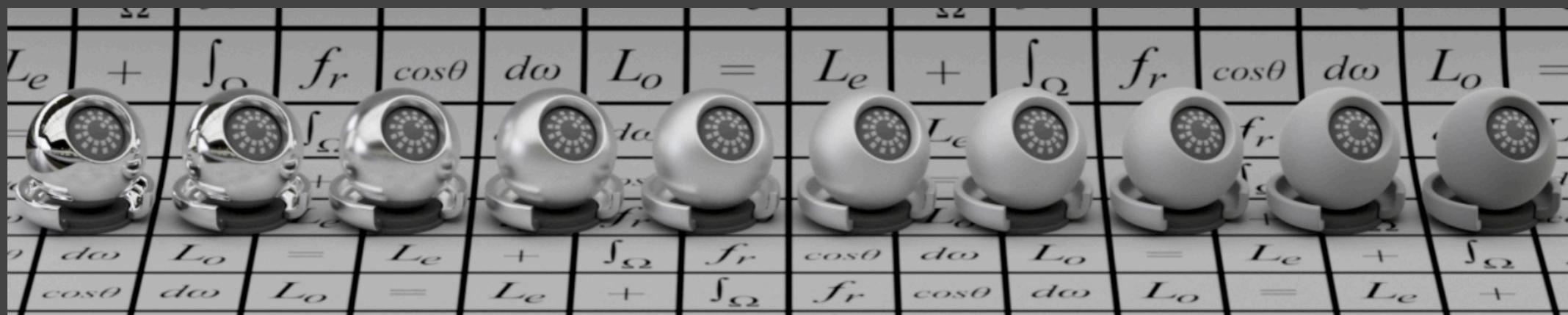
- A commonly used shadowing-masking term
  - The Smith shadowing-masking term
  - Decoupling shadowing and masking

$$G(\mathbf{i}, \mathbf{o}, \mathbf{m}) \approx G_1(\mathbf{i}, \mathbf{m})G_1(\mathbf{o}, \mathbf{m})$$



# Multiple Bounces

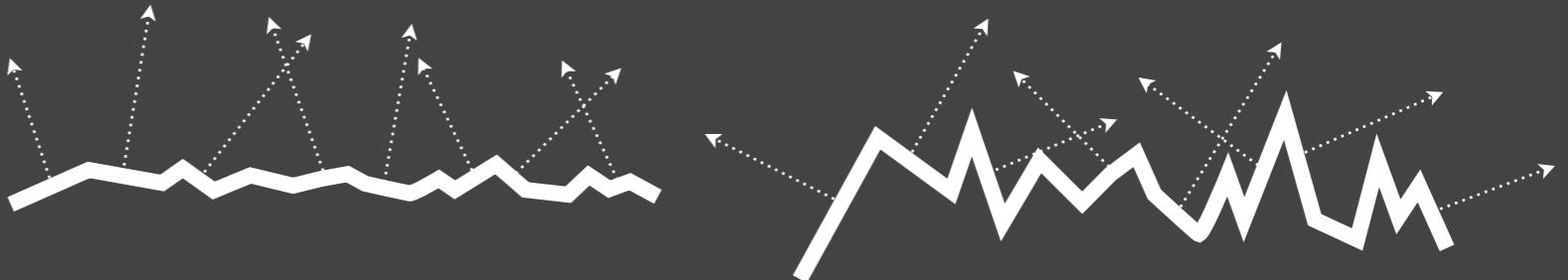
- Missing energy!
    - Especially prominent when roughness is high (why?)



[https://fpsunflower.github.io/ckulla/data/s2017\\_pbs\\_imageworks\\_slides\\_v2.pdf](https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf)

# Multiple Bounces

- Missing energy!



- Adding back the missing energy?
  - Accurate methods exist [Heitz et al. 2016]
  - But can be too slow for RTR
- Basic idea
  - Being occluded == next bounce happening

# The Kulla-Conty Approximation

- What's the overall energy of an outgoing 2D BRDF lobe?

$$E(\mu_o) = \int_0^{2\pi} \int_0^1 f(\mu_o, \mu_i, \phi) \mu_i d\mu_i d\phi$$

Note:  $\mu = \sin \theta$

- Key idea
  - We can design an additional lobe that integrates to  $1 - E(\mu_o)$
  - The outgoing BRDF lobe can be different for different incident dir.
  - Consider reciprocity, it should be\* of the form  
 $c(1 - E(\mu_i))(1 - E(\mu_o))$

# The Kulla-Conty Approximation

- Therefore,

$$f_{\text{ms}}(\mu_o, \mu_i) = \frac{(1 - E(\mu_o))(1 - E(\mu_i))}{\pi(1 - E_{\text{avg}})}, E_{\text{avg}} = 2 \int_0^1 E(\mu) \mu d\mu$$

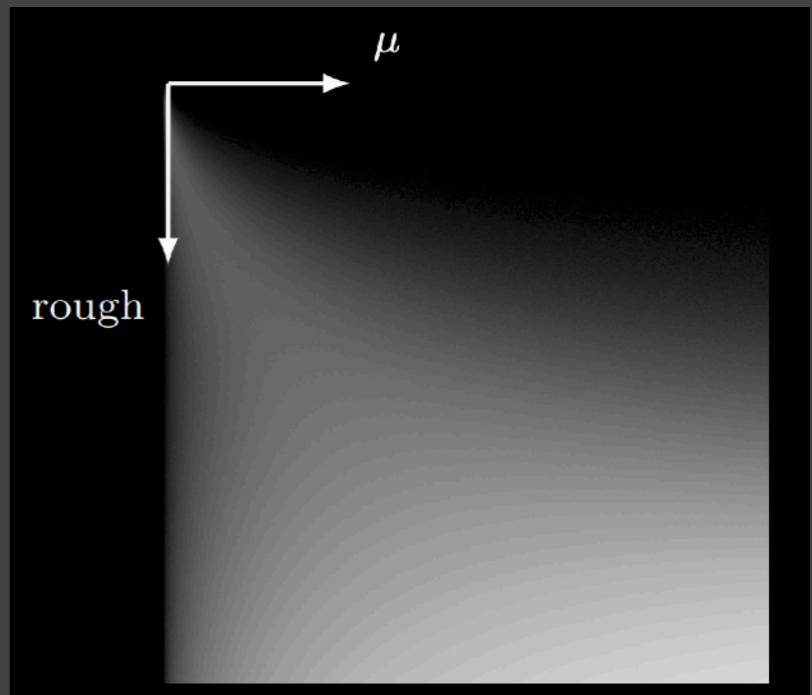
- FYI, validation:

$$\begin{aligned} E_{\text{ms}}(\mu_o) &= \int_0^{2\pi} \int_0^1 f_{\text{ms}}(\mu_o, \mu_i, \phi) \mu_i d\mu_i d\phi \\ &= 2\pi \int_0^1 \frac{(1 - E(\mu_o))(1 - E(\mu_i))}{\pi(1 - E_{\text{avg}})} \mu_i d\mu_i \\ &= 2 \frac{1 - E(\mu_o)}{1 - E_{\text{avg}}} \int_0^1 (1 - E(\mu_i)) \mu_i d\mu_i \\ &= \frac{1 - E(\mu_o)}{1 - E_{\text{avg}}} (1 - E_{\text{avg}}) \\ &= 1 - E(\mu_o) \end{aligned}$$

[https://fpsunflower.github.io/ckulla/data/s2017\\_pbs\\_imageworks\\_slides\\_v2.pdf](https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf)

# The Kulla-Conty Approximation

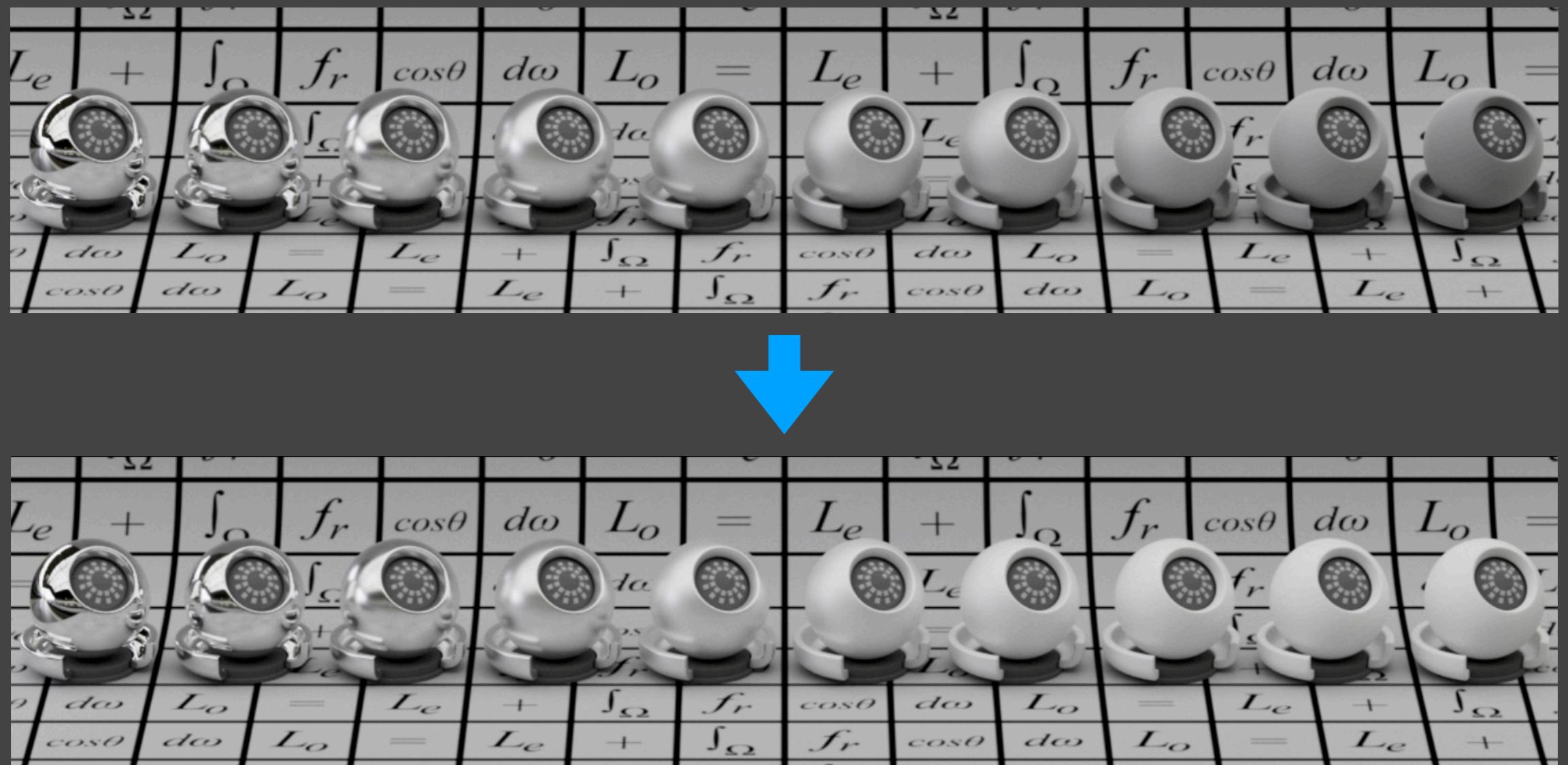
- But neither  $E(\mu)$  nor  $E_{avg} = 2 \int_0^1 E(\mu) \mu \, d\mu$  are analytic
- But we already know what to do!
  - Hint: in split sum, how do we deal with a difficult integral?
  - Precompute / tabulate!
- Dimension / parameters of  $E(\mu)$  and  $E_{avg}$ ?
  - $E(\mu)$ : roughness &  $\mu$  [therefore, a 2D table]
  - $E_{avg}$ : just roughness [therefore, a 1D table]



Precomputed table for  $E(\mu)$

# The Kulla-Conty Approximation

- Results



[https://fpsunflower.github.io/ckulla/data/s2017\\_pbs\\_imageworks\\_slides\\_v2.pdf](https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf)

# The Kulla-Conty Approximation

- What if the BRDF has color?
  - Color == absorption == energy loss (as it should)
  - So we'll just need to compute the overall energy loss
- Define the average Frensel (how much energy is reflected)

$$F_{avg} = \frac{\int_0^1 F(\mu) \mu \, d\mu}{\int_0^1 \mu \, d\mu} = 2 \int_0^1 F(\mu) \mu \, d\mu$$

[Therefore, just  
a number]

- And recall that  $E_{avg}$  is how much energy that you can see  
(i.e., will **NOT** participate in further bounces)

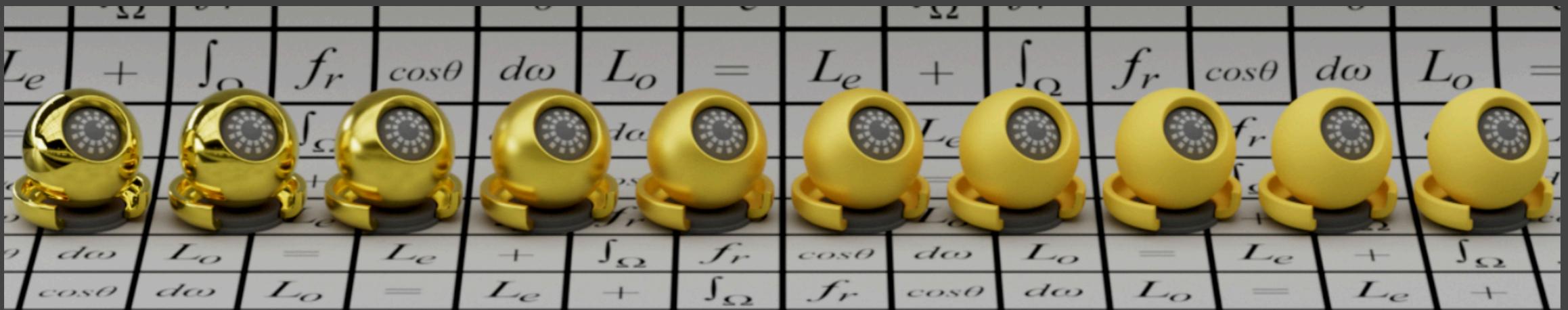
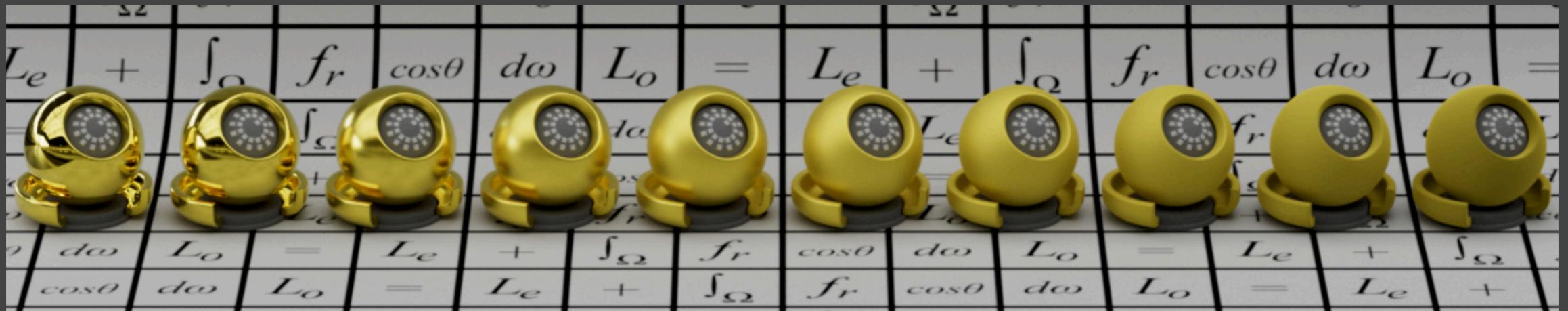
# The Kulla-Conty Approximation

- Therefore, the proportion of energy (color) that
  - You can directly see:  $F_{avg}E_{avg}$
  - After one bounce then be seen:  $F_{avg}(1 - E_{avg}) \cdot F_{avg}E_{avg}$
  - ...
  - After  $k$  bounces then be seen:  $F_{avg}^k(1 - E_{avg})^k \cdot F_{avg}E_{avg}$
- Adding everything up, we have the color term
  - Which will be directly multiplied on the **uncolored additional BRDF**

$$\frac{F_{avg}E_{avg}}{1 - F_{avg}(1 - E_{avg})}$$

# The Kulla-Conty Approximation

- ## • Results



[https://fpsunflower.github.io/ckulla/data/s2017\\_pbs\\_imageworks\\_slides\\_v2.pdf](https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf)

# However, An Undesirable Hack

- Combining a Microfacet BRDF with a **diffuse** lobe
  - Pervasively used in computer vision for material recognition
  - COMPLETELY WRONG
  - COULDN'T BE WORSE
  - I NEVER TAUGHT YOU SO
- Issues
  - Physically incorrect
  - Not energy preserving  
(fixed in Kulla-Conty)  
(can also be fixed in other ways)



# Questions?

# Disney's Principled BRDF

# Why is it needed?

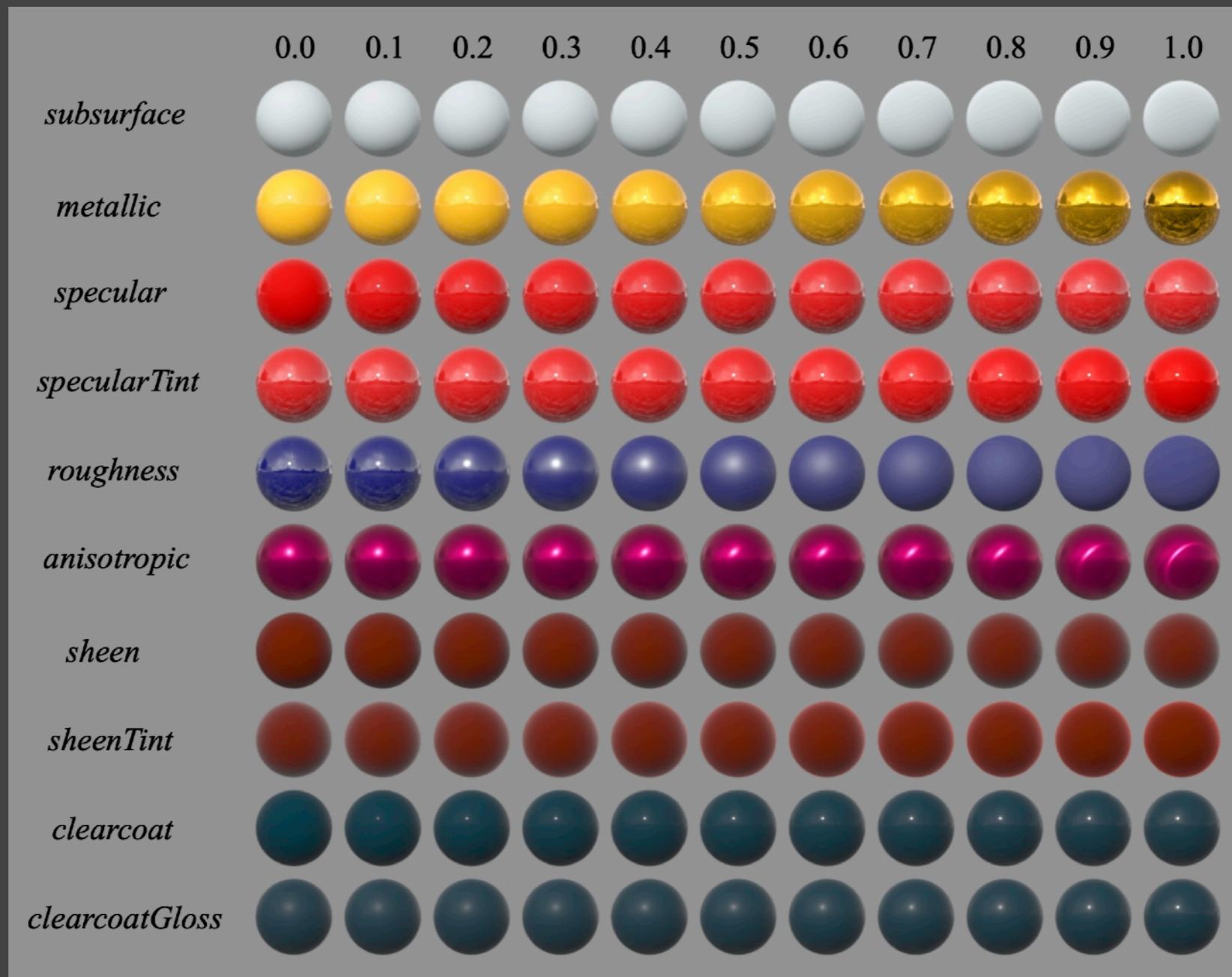
- Motivation
  - No physically-based materials are good at rep. all real materials
    - e.g. lacking diffuse term in most microfacet models
  - Physically-based materials are not artist friendly
    - e.g. “the complex index of refraction  $n_{ik}$ ”
- High level design goal
  - Art directable, not necessarily physically correct
  - But again, referred to as PBR in real-time rendering...

# What is “principled”?

- The BRDF is designed with a few important principles
  - Intuitive rather than physical parameters should be used.
  - There should be as few parameters as possible.
  - Parameters should be zero to one over their plausible range.
  - Parameters should be allowed to be pushed beyond their plausible range where it makes sense.
  - All combinations of parameters should be as robust and plausible as possible.

# How does it work?

- A table showing the effects of **individual** parameters



# Pros and Cons

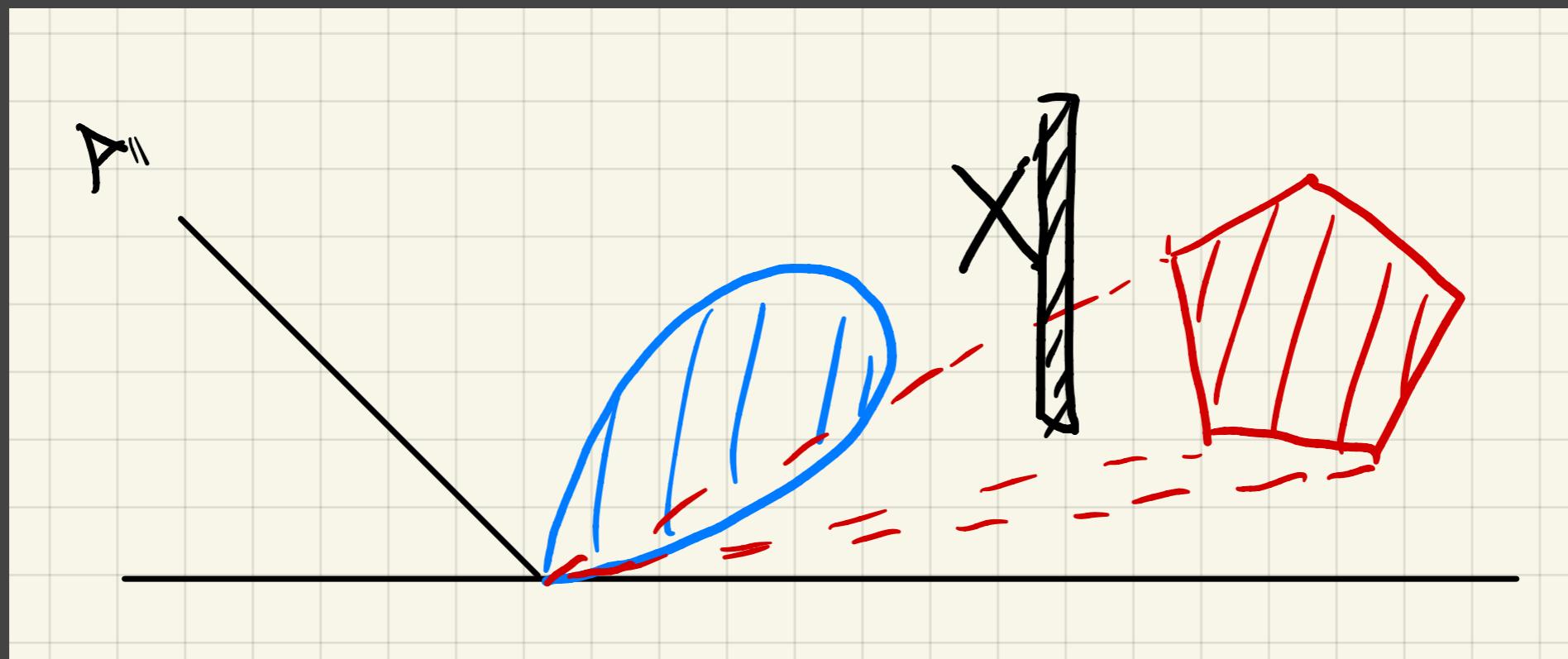
- Easy-to-understand / control
- A wide range of materials in a single model
- Open source implementation is available
- Not physically based
  - But is it a big problem?
  - Academia vs. industry
- Huge parameter space

# Questions?

# Shading Microfacet Models using Linearly Transformed Cosines (LTC)

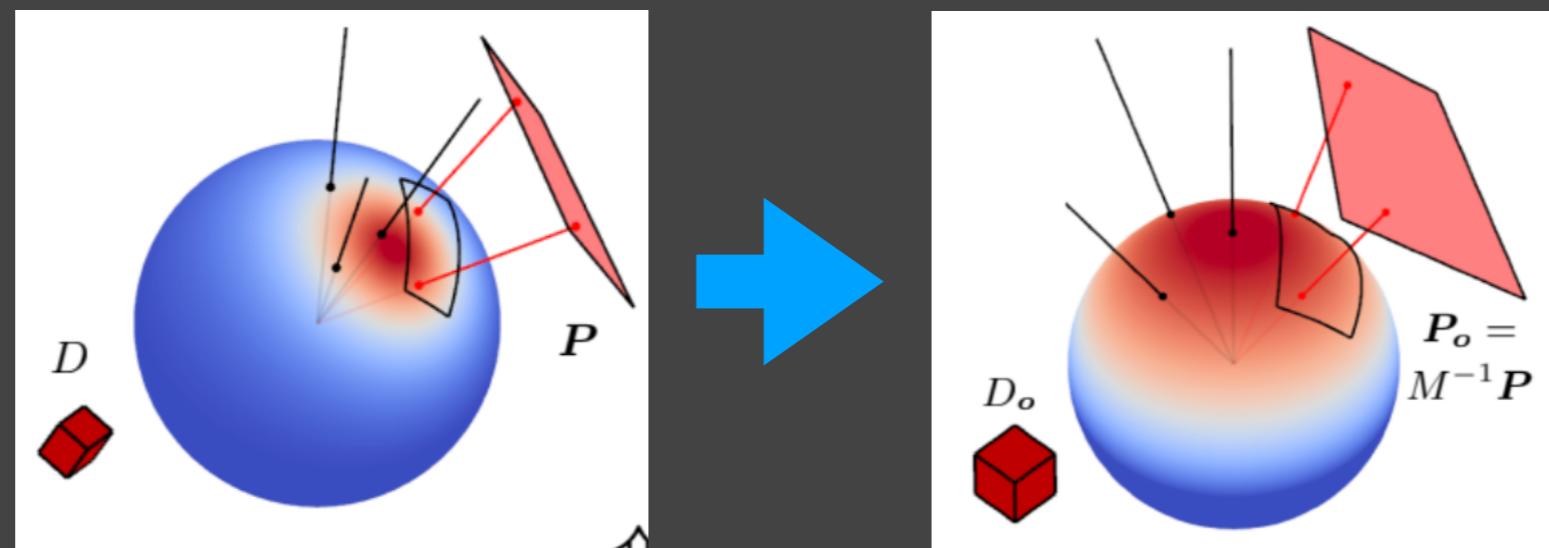
# Linearly Transformed Cosines

- Solves the shading of microfacet models
  - Mainly on GGX, though others are also fine
  - No shadows
  - Under polygon shaped light



# Linearly Transformed Cosines

- Key idea
  - Given the viewing direction, any outgoing 2D BRDF lobe can be transformed to a cosine
  - The shape of the light can also be transformed along
  - Integrating the transformed light on a cosine lobe can be **analytical**



# Next Lecture

- More Real-Time Physically-Based Materials!



<https://www.wired.com/story/cloud-gaming-infrastructure-arms-race/>

Thank you!