Physics

SECTION-A

31. Which of the following Maxwell's equations is valid for time varying conditions but not valid for static conditions :

(1) $\oint \vec{B}.\vec{dl} = \mu_0 I$ (2) $\oint \vec{E}.\vec{dl} = 0$

(3) $\oint \vec{E}.\vec{dl} = -\frac{\partial \phi_B}{\partial t}$ (4) $\oint \vec{D}.\vec{dA} = Q$

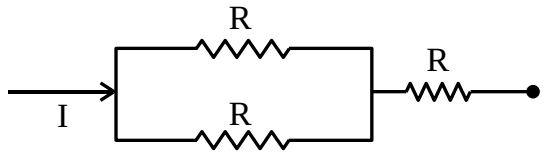
Official Ans. by NTA (3)

Ans. (3)

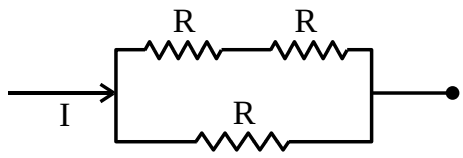
32. Different combination of 3 resistors of equal resistance R are shown in the figures.

The increasing order for power dissipation is:

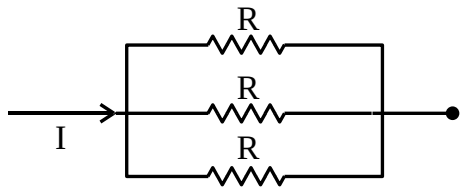
(A)



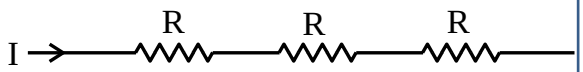
(B)



(C)



(D)



(1) $P_A < P_B < P_C < P_D$

(2) $P_C < P_D < P_A < P_B$

(3) $P_B < P_C < P_D < P_A$

(4) $P_C < P_B < P_A < P_D$

Official Ans. by NTA (4)

Ans. (4)

33. A vessel of depth 'd' is half filled with oil of refractive index n_1 and the other half is filled with water of refractive index n_2. The apparent depth of this vessel when viewed from above will be-

(1) $\frac{d\, n_1 n_2}{(n_1 + n_2)}$

(2) $\frac{d(n_1 + n_2)}{2n_1 n_2}$

(3) $\frac{d\, n_1 n_2}{2(n_1 + n_2)}$

(4) $\frac{2d(n_1 + n_2)}{n_1 n_2}$

Official Ans. by NTA (2)

Ans. (2)

34. The source of time varying magnetic field may be

(A) a permanent magnet

(B) an electric field changing linearly with time

(C) direct current

(D) a decelerating charge particle

(E) an antenna fed with a digital signal

Choose the correct answer from the options given below:

(1) (D) only

(2) (C) and (E) only

(3) (A) only

(4) (B) and (D) only

Official Ans. by NTA (1)

Ans. (1)

35. Two trains 'A' and 'B' of length 'l' and '$4l$' are travelling into a tunnel of length 'L' in parallel tracks from opposite directions with velocities 108 km/h and 72 km/h, respectively. If train 'A' takes 35s less time than train 'B' to cross the tunnel then, length 'L' of tunnel is:(Given L = 60 l)

(1) 1200 m

(2) 2700 m

(3) 1800 m

(4) 900 m

Official Ans. by NTA (3)

Ans. (3)

36. The ratio of powers of two motors is $\frac{3\sqrt{x}}{\sqrt{x}+1}$, that are capable of raising 300 kg water in 5 minutes and 50 kg water in 2 minutes respectively from a well of 100 m deep. The value of x will be

(1) 2

(2) 4

(3) 2.4

(4) 16

Official Ans. by NTA (4)

Ans. (4)

37. A planet having mass 9 Me and radius $4R_e$, where Me and Re are mass and radius of earth respectively, has escape velocity in km/s given by:

(Given escape velocity on earth

$V_e = 11.2\times10^3$ m/s)

(1) 67.2

(2) 16.8

(3) 33.6

(4) 11.2

Official Ans. by NTA (2)

Ans. (2)

38. The difference between threshold wavelengths for two metal surfaces A and B having work function $\phi_A = 9$eV and $\phi_B = 4.5$eV in nm is:

(Given, hc = 1242 eV nm)

(1) 264

(2) 138

(3) 276

(4) 540

Official Ans. by NTA (2)

Ans. (2)

39. A bullet 10 g leaves the barrel of gun with a velocity of 600 m/s. If the barrel of gun is 50 cm long and mass of gun is 3 kg, then value of impulse supplied to the gun will be :

(1) 12 Ns (2) 6 Ns

(3) 36 Ns (4) 3 Ns

Official Ans. by NTA (2)

Ans. (2)

40. Two charges each of magnitude 0.01 C and separated by a distance of 0.4 mm constitute an electric dipole. If the dipole is placed in an uniform electric field $'\vec{E}'$ of 10 dyne/C making 30^0 angle with $\vec{E}$, the magnitude of torque acting on dipole is :

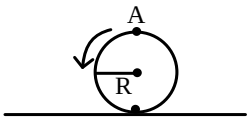
(1) 4.0×10^{-10} Nm (2) 2.0×10^{-10} Nm

(3) 1.0×10^{-8} Nm (4) 1.5×10^{-9} Nm

Official Ans. by NTA (2)

Ans. (2)

41. A disc is rolling without slipping on a surface. The radius of the disc is R. At t = 0, the top most point on the disc is A as shown in figure. When the disc completes half of its rotation, the displacement of point A from its initial position is



(1) $R\sqrt{(\pi^2+4)}$ (2) $R\sqrt{(\pi^2+1)}$

(3) 2 R (4) $2R\sqrt{(1+4\pi^2)}$

Official Ans. by NTA (1)

Ans. (1)

42. Match List – I with List – II

List - I (Layer of atmosphere)	**List – II (Approximate height over earth's surface)**
(A) F_1 - Layer	(I) 10 km
(B) D – Layer	(II) 170 – 190 km
(C) Troposphere	(III) 100 km
(D) E-layer	(IV) 65 – 75 km

Choose the correct answer from the options given below:

(1) A – III, B – IV, C – I, D – II

(2) A – II, B – IV, C – III, D – I

(3) A – II, B – I, C – IV, D – III

(4) A – II, B – IV, C – I, D – III

Official Ans. by NTA (4)

Ans. (4)

43. The rms speed of oxygen molecule in a vessel at particular temperature is $\left(1+\frac{5}{x}\right)^{\frac{1}{2}}\upsilon$, where υ is the average speed of the molecule. The value of x will be:(Take $\pi=\frac{22}{7}$)

(1) 28
(2) 27
(3) 8
(4) 4

Official Ans. by NTA (1)

Ans. (1)

44. A body of mass (5 ± 0.5) kg is moving with a velocity of (20 ± 0.4) m/s. Its kinetic energy will be

(1) (1000 ± 140)J

(2) (1000 ± 0.14)J

(3) (500 ± 0.14)J

(4) (500 ± 140)J

Official Ans. by NTA (1)

Ans. (1)

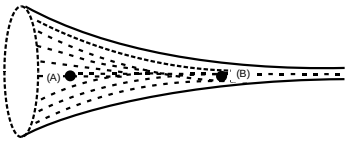
45. Two bodies are having kinetic energies in the ratio 16 : 9. If they have same linear momentum, the ratio of their masses respectively is :

(1) 4 : 3 (2) 3 : 4
(3) 16 : 9 (4) 9 : 16

Official Ans. by NTA (4)

Ans. (4)

46.



The figure shows a liquid of given density flowing steadily in horizontal tube of varying cross-section. Cross sectional areas at A is 1.5 cm^2, and B is 25 mm^2, if the speed of liquid at B is 60 cm/s then $(P_A - P_B)$ is :
(Given P_A and P_B are liquid pressures at A and B points.
Density $\rho=1000\ kg\ m^{-3}$
A and B are on the axis of tube

(1) 175 Pa
(2) 27 Pa
(3) 135 Pa
(4) 36 Pa

Official Ans. by NTA (1)

Ans. (1)

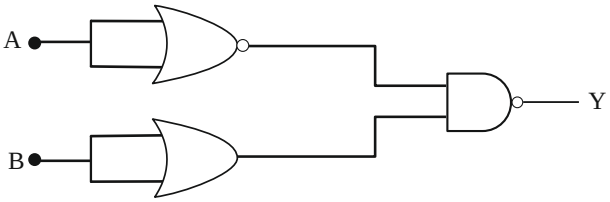
47. Under isothermal condition, the pressure of a gas is given by $P=aV^{-3}$, where a is a constant and V is the volume of the gas. The bulk modulus at constant temperature is equal to

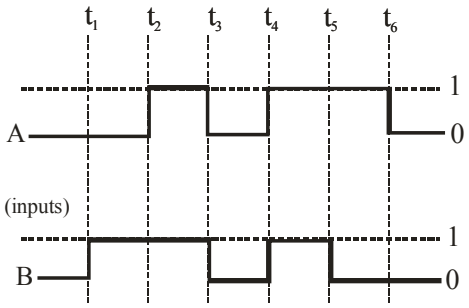
(1) $\frac{P}{2}$ (2) 3 P
(3) 2 P (4) P

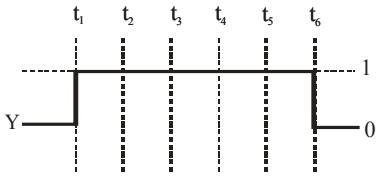
Official Ans. by NTA (2)

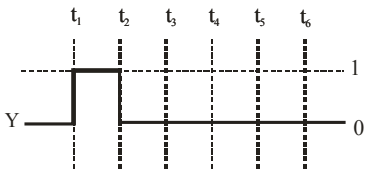
Ans. (2)

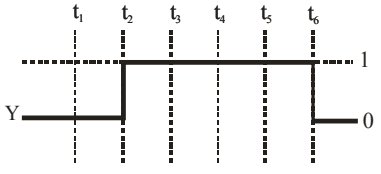
48. For the following circuit and given inputs A and B, choose the correct option for output 'Y'

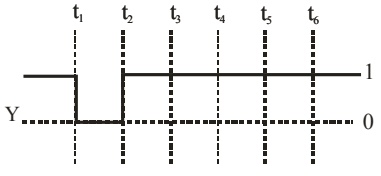




(1)


(2)


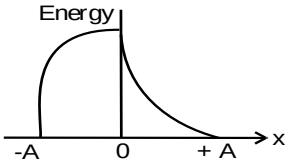
(3)


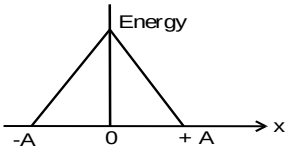
(4)


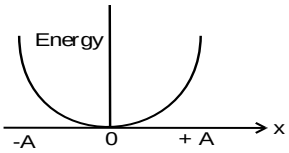
Official Ans. by NTA (4)

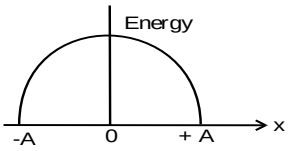
Ans. (4)

49. Which graph represents the difference between total energy and potential energy of a particle executing SHM Vs it's distance from mean position?

(1) 

(2) 

(3) 

(4) 

Official Ans. by NTA (4)

Ans. (4)

50. $\underset{92}{\overset{238}{A}} \rightarrow \underset{90}{\overset{234}{B}} + \underset{2}{\overset{4}{D}} + Q$

In the given nuclear reaction, the approximate amount of energy released will be :

[Given, mass of $\underset{92}{\overset{238}{A}} = 238.05079 \times 931.5\ MeV/c^2$,

mass of $\underset{90}{\overset{234}{B}} = 234.04363 \times 931.5\ MeV/c^2$,

mass of $\underset{2}{\overset{4}{D}} = 4.00260 \times 931.5\ MeV/c^2$]

(1) 3.82 MeV (2) 5.9 MeV

(3) 2.12 MeV (4) 4.25 MeV

Official Ans. by NTA (4)

Ans. (4)

Section - B

51. The elastic potential energy stored in a steel wire of length 20 m stretched through 2 cm is 80 J. The cross sectional area of the wire is_____ mm^2. (Given, $y = 2.0 \times 10^{11}\ Nm^{-2}$)

Official Ans. by NTA (40)

Ans. (40)

52. A potential V_0 is applied across a uniform wire of resistance R. The power dissipation is P_1. The wire is then cut into two equal halves and a potential of V_0 is applied across the length of each half. The total power dissipation across two wires is P_2. The ratio $P_2 : P_1$ is $\sqrt{x}:1$. The value of x is _____.

Official Ans. by NTA (16)

Ans. (16)

53. At a given point of time the value of displacement of a simple harmonic oscillator is given as $y = A\cos(30^0)$. If amplitude is 40 cm and kinetic energy at that time is 200 J, the value of force constant is $1.0 \times 10^x\ Nm^{-1}$. The value of x is _____.

Official Ans. by NTA (4)

Ans. (4)

54. When a resistance of 5Ω is shunted with a moving coil galvanometer, it shows a full scale deflection for a current of 250 mA, however when $1050\,\Omega$ resistance is connected with it in series, it gives full scale deflection for 25 volt. The resistance of galvanometer is _____ Ω.

Official Ans. by NTA (50)

Ans. (50)

55. The radius of 2^{nd} orbit of He^+ of Bohr's model is r_1 and that of fourth orbit of Be^{3+} is represented as r_2. Now the ratio $\frac{r_2}{r_1}$ is x : 1. The value of x is _____

Official Ans. by NTA (2)

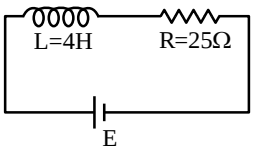
Ans. (2)

56. A thin infinite sheet charge and an infinite line charge of respective charge densities $+\sigma$ and $+\lambda$ are placed parallel at 5 m distance from each other. Points 'P' and 'Q' are at $\frac{3}{\pi}$ m and $\frac{4}{\pi}$ m perpendicular distance from line charge towards sheet charge, respectively. 'E_P' and 'E_Q' are the magnitudes of resultant electric field intensities at point 'P' and 'Q', respectively. If $\frac{E_P}{E_Q}=\frac{4}{a}$ for $2|\sigma|=|\lambda|$. Then the value of a is _____.

Official Ans. by NTA (6)

Ans. (6)

57. In the given figure, an inductor and a resistor are connected in series with a battery of emf E volt. $\frac{E^a}{2b}$ J/s represents the maximum rate at which the energy is stored in the magnetic field (inductor). The numerical value of $\frac{b}{a}$ will be _____



Official Ans. by NTA (25)

Ans. (25)

58. A fish rising vertically upward with a uniform velocity of 8 ms^{-1}, observes that a bird is diving vertically downward towards the fish with the velocity of 12 ms^{-1}. If the refractive index of water is $\frac{4}{3}$, then the actual velocity of the diving bird to pick the fish, will be _____ ms^{-1}.

Official Ans. by NTA (3)

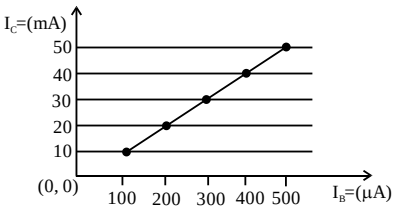
Ans. (3)

59. A solid sphere is rolling on a horizontal plane without slipping. If the ratio of angular momentum about axis of rotation of the sphere to the total energy of moving sphere is $\pi : 22$ then, the value of its angular speed will be _____ rad/s.

Official Ans. by NTA (4)

Ans. (4)

60. From the given transfer characteristic of a transistor in CE configuration, the value of power gain of this configuration is 10^x, for R_B = 10 kΩ, and R_C = 1 kΩ. The value of x is _____.



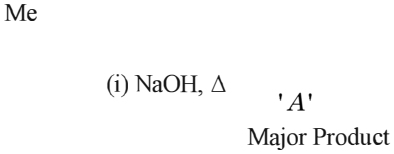
Official Ans. by NTA (3)

Ans. (3)

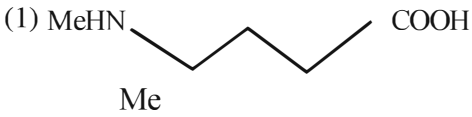
Chemistry

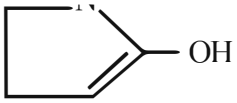
SECTION-A

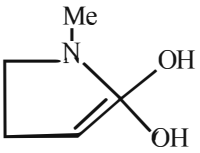
61. In the reaction given below

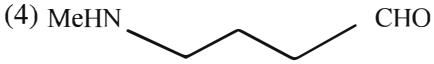


'A' is

(1) 

(2) 

(3) 

(4) 

Official Ans. by NTA (1)

Ans. (1)

62. Given below are two statements:

Statement-I Permutit process is more efficient compared to the synthetic resin method for the softening of water.

Statement-II: Synthetic resin method results in the formation of soluble sodium salts.

In the light of the above statements, choose the most appropriate answer from the options given below:

(1) Both the Statements I and II are correct

(2) Statement I is correct but Statement II is incorrect

(3) Statement I is incorrect but Statement II is correct

(4) Both the Statements I and II are incorrect

Official Ans. by NTA (4)

Ans. (4)

63. The mismatched combinations are

A. Chlorophyll - Co

B. Water hardness - EDTA

C. Photography - $\left[Ag(CN)_2\right]^-$

D. Wilkinson catalyst - $\left[(Ph_3P)_3\ RhCl\right]$

E. Chelating ligand – D - Penicillamine

Choose the correct answer from the options given below:

(1) A and C Only

(2) A and E Only

(3) D and E Only

(4) A, C and E Only

Official Ans. by NTA (1)

Ans. (1)

64. In which of the following processes, the bond order increases and paramagnetic character changes to diamagnetic one?

(1) $O_2 \rightarrow O_2^{2-}$

(2) $NO \rightarrow NO^+$

(3) $N_2 \rightarrow N_2^+$

(4) $O_2 \rightarrow O_2^+$

Official Ans. by NTA (2)

Ans. (2)

65. The incorrect statement from the following for borazine is:

(1) It has electronic delocalization

(2) It contains banana bonds.

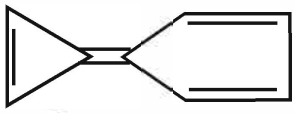
(3) It can react with water.

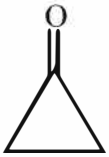
(4) It is a cyclic compound.

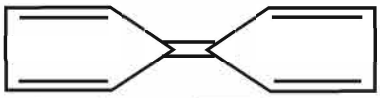
Official Ans. by NTA (3)

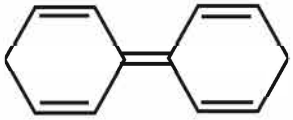
Ans. (2)

66. Among the following compounds, the one which shows highest dipole moment is

(1) 

(2) 

(3) 

(4) 

Official Ans. by NTA (1)

Ans. (1)

67. Match the following

Column –A		Column-B	
a	Nylon 6	**I**	Natural Rubber
b	Vulcanized Rubber	**II**	Cross Linked
c	cis-1,4-polyisoprene	**III**	Caprolactam
d	Polychloroprene	**IV**	Neoprene

Choose the correct answer from option given below:

(1) a → IV,b-III, c → II,d → I

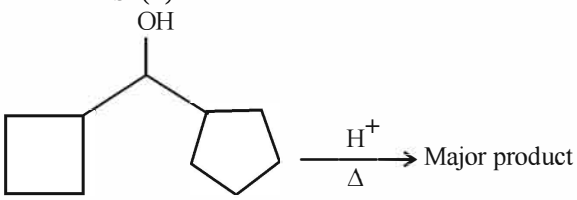
(2) a → III, b → IV, c → I,d → II

(3) a → II, b → III, c → IV, d → I

(4) a → III, b → II, c → I, d → IV

Official Ans. by NTA (4)

Ans. (4)

68. 

In the above reaction. Left hand side and right hand side rings are named as 'A' and 'B' respectively. They undergo ring expansion. The correct statement for this process is:

(1) Finally both rings will become six membered each.

(2) Finally both rings will become five membered each.

(3) Only 'A' will become 6 membered.

(4) Ring expansion can go upto seven membered rings

Official Ans. by NTA (1)

Ans. (1)

69. The radical which mainly causes ozone depletion in the presence of UV radiations is:

(1) $CH_3^{\bullet}$

(2) $NO^{\bullet}$

(3) $Cl^{\bullet}$

(4) $\dot{O}H$

Official Ans. by NTA (3)

Ans. (3)

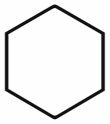
70. In the following reaction 'X' is

$$CH_3(CH_2)_4CH_3 \xrightarrow[HCl,\,\Delta]{Anhy.AlCl_3} \underset{\text{major product}}{'X}$$

(1) $CH_3(CH_2)_4CH_2Cl$

(2) $Cl-CH_2-(CH_2)_4-CH_2-Cl$

(3) $CH_3\underset{\displaystyle CH_3}{\underset{|}{CH}}-(CH_2)_2CH_3$

(4) 

Official Ans. by NTA (3)

Ans. (3)

71. 2-Methyl propyl bromide reacts with $C_2H_5O^-$ and gives 'A' whereas on reaction with C_2H_5OH it gives 'B'. The mechanism followed in these reactions and the products 'A' and 'B' respectively are:

(1) S_N2. A = iso-butyl ethyl ether; S_N1, B= tert-butyl ethyl ether

(2) S_N1, A = tert-butyl ethyl ether; S_N1, B = 2-butyl ethyl ether

(3) S_N1, A = tert-butyl ethyl ether; S_N2, B = iso-butyl ethyl ether

(4) S_N2, A =2-butyl ethyl ether; S_N2, B= iso-butyl ethyl ether

Official Ans. by NTA (1)

Ans. (1)

72. D- (+)- Glyceraldehyde $\xrightarrow[\text{(ii) } H_2O/H^+]{\text{(i) HCN}}$ $\xrightarrow{\text{(iii) } HNO_3}$

The products formed in the above reaction are

(1) Two optically active products

(2) One optically active and one meso product

(3) One optically inactive and one meso product.

(4) Two optically inactive products

Official Ans. by NTA (2)

Ans. (2)

73. Which one of the following is most likely a mismatch?

(1) Zinc- Liquation

(2) Titanium – van Arkel method

(3) Nickel – Mond process

(4) Copper - Electrolysis

Official Ans. by NTA (1)

Ans. (1)

74. ClF_5 at room temperature is a:

(1) Colourless gas with trigonal bipyramidal geometry.

(2) Colourless gas with square pyramidal geometry

(3) Colourless liquid with square pyramidal geometry

(4) Colourless liquid with trigonal bipyramidal geometry.

Official Ans. by NTA (3)
Ans. (3)

75. $Be(OH)_2$ react with $Sr(OH)_2$ to yield an ionic salt. Choose the incorrect option related to this reaction from the following:

(1) Be is tetrahedrally coordinated in the ionic salt.

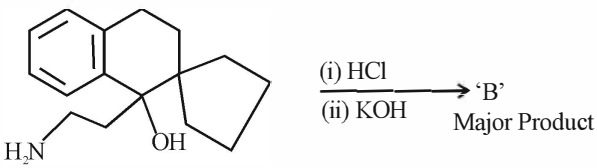
(2) The reaction is an example of acid - base neutralization reaction.

(3) Both Sr and Be elements are present in the ionic salt.

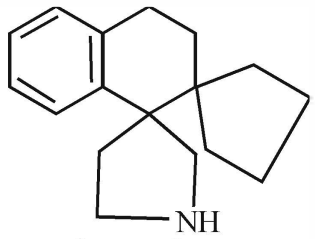
(4) The elements Be is present in the cationic part of the ionic salt.

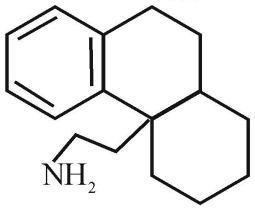
Official Ans. by NTA (4)
Ans. (4)

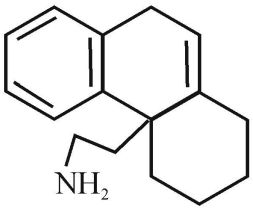
76. In the reaction given below

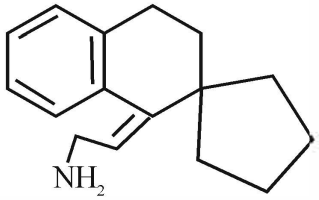


'B' is:

(1)


(2)


(3)


(4)


Official Ans. by NTA (3)
Ans. (3)

77. Which of the following statements are **not** correct?

A. The electron gain enthalpy of F is more negative than that of Cl

B. Ionization enthalpy decreases in a group of periodic table

C. The electronegativity of an atom depends upon the atoms bonded to it.

D. Al_2O_3 and NO are examples of amphoteric oxides.

Choose the most appropriate answer from the options given below:

(1) A, B, C, and D

(2) A, C and D Only

(3) B and D Only

(4) A, B and D Only

Official Ans. by NTA (2)

Ans. (A&D, Bonus)

78. The energy of an electron in the first Bohr orbit of hydrogen atom is $-2.18\times10^{-18}J$. Its energy in the third Bohr orbit is_____.

(1) $\frac{1}{27}$ of this value

(2) One third of this value

(3) Three times of this value

(4) $\frac{1}{9}$ th of this value

Official Ans. by NTA (4)

Ans. (4)

79. What happens when a lyophilic sol is added to a lyophobic sol?

(1) Lyophilic sol is dispersed in lyophobic sol.

(2) Film of lyophobic sol is formed over lyophilic sol.

(3) Lyophobic sol is coagulated

(4) Film of lyophilic sol is formed over lyophobic sol.

Official Ans. by NTA (4)

Ans. (4)

80. The pair of lanthanides in which both elements have high third –ionization energy is:

(1) Eu, Gd

(2) Eu, Yb

(3) Lu, Yb

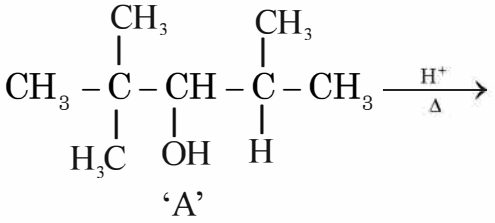
(4) Dy, Gd

Official Ans. by NTA (2)

Ans. (2)

SECTION-B

81. For the given reaction



'A'

The total number of possible products formed by tertiary carbocation of A is _____.

Official Ans. by NTA (4)

Ans. (5)

82. Solution of 12 g of non – electrolyte (A) prepared by dissolving it in 1000 mL of water exerts the same osmotic pressure as that of 0.05 M glucose solution at the same temperature. The empirical formula of A is CH_2O. The molecular mass of A is _____ g. (Nearest integer)

Official Ans. by NTA (240)

Ans. (240)

83. 25.0 mL of 0.050 M $Ba(NO_3)_2$ is mixed with 25.0 mL of 0.020 M NaF. K_{sp} of BaF_2 is 0.5×10^{-6} at 298 K. The ratio of $\left[Ba^{2+}\right]\left[F^-\right]^2$ and K_{sp} is _____ (Nearest integer)

Official Ans. by NTA (5)

Ans. (5)

84. $A_2 + B_2 \rightarrow 2AB.\ \Delta H_f^0 = -200\ kJmol^{-1}$

AB, A_2 and B_2 are diatomic molecule. If the bond enthalpies of A_2, B_2 and AB are in the ratio 1:0.5:1, then the bond enthalpy of A_2 is _____ $kJmol^{-1}$ (Nearest integer)

Official Ans. by NTA (400)

Ans. (800)

85. An organic compound gives 0.220 g of CO_2 and 0.126 g of H_2O on complete combustion. If the % of carbon is 24 then the % hydrogen is _____ $\times10^{-1}$. (Nearest integer)

Official Ans. by NTA (56)

Ans. (56)

86. 20 mL of calcium hydroxide was consumed when it was reacted with 10 mL of unknown solution of H_2SO_4. Also 20 mL standard solution of 0.5 M HCl containing 2 drops of phenolphthalein was titrated with calcium hydroxide the mixture showed pink colour when burette displayed the value of 35.5 mL whereas the burette showed 25.5 mL initially. The concentration of H_2SO_4 is _____ M (Nearest integer)

Official Ans. by NTA (1)

Ans. (1)

87. A certain quantity of real gas occupies a volume of 0.15 dm^3 at 100 atm and 500 K when its compressibility factor is 1.07. Its volume at 300 atm and 300K (When its compressibility factor is 1.4) is _____ $\times 10^{-4} dm^3$ (Nearest integer)

Official Ans. by NTA (392)

Ans. (392)

88. $t_{87.5}$ is the time required for the reaction to undergo 87.5% completion and t_{50} is the time required for the reaction to undergo 50% completion. The relation between $t_{87.5}$ and t_{50} for a first order reaction is $t_{87.5} = x \times t_{50}$

The value of x is_____ (Nearest integer)

Official Ans. by NTA (3)

Ans. (3)

89. $KMnO_4$ is titrated with ferrous ammonium sulphate hexahydrate in presence of dilute H_2SO_4. Number of water molecules produced for 2 molecules of $KMnO_4$ is _____.

Official Ans. by NTA (68)

Ans. (68)

90. A metal surface of 100 cm^2 area has to be coated with nickel layer of thickness 0.001mm. A current of 2A was passed through a solution of $Ni(NO_3)_2$ for 'x' seconds to coat the desired layer. The value of x is _____ (Nearest integer)

(ρ_{Ni} (density of Nickel) is 10 gmL^{-1}, Molar mass of Nickel is 60 $gmol^{-1}$ F = 96500 C mol^{-1})

Official Ans. by NTA (161)

Ans. (161)

Mathematics

SECTION-A

1. $\int_0^{\infty} \frac{6}{e^{3x}+6e^{2x}+11e^{x}+6}dx$

(1) $\log_e\left(\frac{512}{81}\right)$

(2) $\log_e\left(\frac{32}{27}\right)$

(3) $\log_e\left(\frac{256}{81}\right)$

(4) $\log_e\left(\frac{64}{27}\right)$

Official Ans. by NTA (2)

Ans. (2)

2. $\max\limits_{0\le x\le\pi}\left\{x-2\sin x\cos x+\frac{1}{3}\sin 3x\right\}=$

(1) $\frac{5\pi+2+3\sqrt{3}}{6}$

(2) $\frac{\pi+2-3\sqrt{3}}{6}$

(3) π

(4) 0

Official Ans. by NTA (1)

Ans. (1)

3. The set of all $a\in\mathbb{R}$ for which the equation $x|x-1|+|x+2|+a=0$ has exactly one real root is :

(1) $(-6,-3)$

(2) $(-\infty,\infty)$

(3) $(-6,\infty)$

(4) $(-\infty,-3)$

Official Ans. by NTA (2)

Allen Ans. (2)

4. The negation of the statement

$\big((A\wedge(B\vee C))\Rightarrow(A\vee B)\big)\Rightarrow A$ is

(1) equivalent to $\sim A$

(2) equivalent to $\sim C$

(3) equivalent to $B\vee\sim C$

(4) a fallacy

Official Ans. by NTA (1)

Ans. (1)

5. The distance of the point $(-1,2,3)$ from the plane $\vec{r}.(\hat{i}-2\hat{j}+3\hat{k})=10$ parallel to the line of the shortest distance between the lines $\vec{r}=(\hat{i}-\hat{j})+\lambda(2\hat{i}+\hat{k})$ and $\vec{r}=(2\hat{i}-\hat{j})+\mu(\hat{i}-\hat{j}+\hat{k})$ is :

(1) 3 6

(2) $3\sqrt{5}$

(3) $2\sqrt{6}$

(4) $2\sqrt{5}$

Official Ans. by NTA (3)

Ans. (3)

6. A coin is biased so that the head is 3 times as likely to occur as tail. This coin is tossed until a head or three tails occur. If X denotes the number of tosses of the coin, then the mean of X is

(1) $\frac{21}{16}$

(2) $\frac{81}{64}$

(3) $\frac{15}{16}$

(4) $\frac{37}{16}$

Official Ans. by NTA (1)

Ans. (1)

7. For the system of linear equations

$2x+4y+2az=b$

$x+2y+3z=4$

$2x-5y+2z=8$

which of the following is **NOT** correct ?

(1) It has infinitely many solutions if a =3, b = 6

(2) It has unique solution if a = b = 6

(3) It has unique solution if a = b = 8

(4) It has infinitely many solution if a = 3, b = 8

Official Ans. by NTA (1)

Ans. (1)

8. For the differentiable function $f:\mathbb{R}-\{0\}\to\mathbb{R}$, let $3f(x)+2f\left(\frac{1}{x}\right)=\frac{1}{x}-10$, then $\left|f(3)+f'\left(\frac{1}{4}\right)\right|$ is equal to

(1) 7

(2) $\frac{33}{5}$

(3) $\frac{29}{5}$

(4) 13

Official Ans. by NTA (4)

Ans. (4)

9. Let the tangent and normal at the point $(3\sqrt{3},1)$ on the ellipse $\frac{x^2}{36}+\frac{y^2}{4}=1$ meet the y-axis at the points A and B respectively. Let the circle C be drawn taking AB as a diameter and the line $x=2\sqrt{5}$ intersect C at the points P and Q. If the tangents at the points P and Q on the circle intersect at the point (α,β), then $\alpha^2-\beta^2$ is equal to

(1) $\frac{314}{5}$

(2) $\frac{304}{5}$

(3) 60

(4) 61

Official Ans. by NTA (2)

Ans. (2)

10. The area of the region enclosed by the curve $f(x)=\max\{\sin x,\cos x\}$, $-\pi\le x\le\pi$ and the x–axis is

(1) $2(\sqrt{2}+1)$

(2) $2\sqrt{2}(\sqrt{2}+1)$

(3) $4(\sqrt{2})$

(4) 4

Official Ans. by NTA (4)

Ans. (4)

11. The number of symmetric matrices of order 3, with all the entries from the set {0, 1, 2, 3, 4, 5, 6, 7, 8, 9}, is :

(1) 6^{10}

(2) 9^{10}

(3) 10^9

(4) 10^6

Official Ans. by NTA (4)

Ans. (4)

12. Among :

(S1) : $\lim\limits_{n\to\infty}\frac{1}{n^2}(2+4+6+.....+2n)=1$

(S2) : $\lim\limits_{n\to\infty}\frac{1}{n^{16}}(1^{15}+2^{15}+3^{15}+.....+n^{15})=\frac{1}{16}$

(1) Both (S1) and (S2) are true

(2) Both (S1) and (S2) are false

(3) Only (S2) is true

(4) Only (S1) is true

Official Ans. by NTA (1)

Ans. (1)

13. Let PQ be a focal chord of the parabola $y^2=36x$ of length 100, making an acute angle with the positive x-axis. Let the ordinate of P be positive and M be the point on the line segment PQ such that PM:MQ=3:1. Then which of the following points does NOT lie on the line passing through M and perpendicular to the line PQ?

(1) $(-3,43)$

(2) $(-6,45)$

(3) $(3,33)$

(4) (6, 29)

Official Ans. by NTA (1)

Ans. (1)

14. For $x\in\mathbb{R}$, two real valued functions f(x) and g(x) are such that, $g(x)=\sqrt{x}+1$ and $fog(x)=x+3\sqrt{x}$. Then f(0) is equal to

(1) 1

(2) –3

(3) 5

(4) 0

Official Ans. by NTA (3)

Ans. (3) or Bonus

15. Fractional part of the number $\frac{4^{2022}}{15}$ is equal to

(1) $\frac{4}{15}$

(2) $\frac{1}{15}$

(3) $\frac{14}{15}$

(4) $\frac{8}{15}$

Official Ans. by NTA (2)

Ans. (2)

16. Let $\vec{a}=\hat{i}+4\hat{j}+2\hat{k}, \vec{b}=3\hat{i}-2\hat{j}+7\hat{k}$ and $\vec{c}=2\hat{i}-\hat{j}+4\hat{k}$. If a vector $\vec{d}$ satisfies $\vec{d}\times\vec{b}=\vec{c}\times\vec{b}$ and $\vec{d}.\vec{a}=24$, then $|\vec{d}|^2$ is equal to

(1) 413
(2) 423
(3) 323
(4) 313

Official Ans. by NTA (1)

Ans. (1)

17. Let $B=\begin{bmatrix}1 & 3 & \alpha\\ 1 & 2 & 3\\ \alpha & \alpha & 4\end{bmatrix}, \alpha>2$ be the adjoint of a matrix A and $|A| = 2$, then $[\alpha\ -2\alpha\ \alpha]B\begin{bmatrix}\alpha\\ -2\alpha\\ \alpha\end{bmatrix}$ is equal to :-

(1) 16
(2) 32
(3) -16
(4) 0

Official Ans. by NTA (3)

Ans. (3)

18. Let $s_1, s_2, s_3,\ldots..,s_{10}$ respectively be the sum to 12 terms of 10 A.P.s whose first terms are 1, 2, 3, …. , 10 and the common differences are 1, 3, 5, …. , 19 respectively. Then $\sum_{i=1}^{10} s_i$ is equal to

(1) 7380
(2) 7220
(3) 7360
(4) 7260

Official Ans. by NTA (4)

Ans. (4)

19. Let $y = y_1(x)$ and $y = y_2(x)$ be the solution curves of the differential equation $\frac{dy}{dx}=y+7$ with initial conditions $y_1(0)=0, y_2(0)=1$ respectively. Then the curves $y = y_1(x)$ and $y = y_2(x)$ intersect at

(1) Two points
(2) no point
(3) infinite number of points
(4) one point

Official Ans. by NTA (2)

Ans. (2)

20. Let the equation of plane passing through the line of intersection of the planes $x+2y+az=2$ and $x-y+z=3$ be $5x-11y+bz=6a-1$. For $c\in\mathbb{Z}$, if the distance of this plane from the point $(a,-c,c)$ is $\frac{2}{\sqrt{a}}$, then $\frac{a+b}{c}$ is equal to

(1) -2
(2) 2
(3) -4
(4) 4

Official Ans. by NTA (3)

Ans. (3)

SECTION-B

21. Let α be the constant term in the binomial expansion of $\left(\sqrt{x}-\frac{6}{x^{\frac{3}{2}}}\right)^n$, $n\le 15$. If the sum of the coefficients of the remaining terms in the expansion is 649 and the coefficient of x^{-n} is $\lambda\alpha$, then λ is equal to _____.

Official Ans. by NTA (36)

Ans. (36)

22. If

$$S=\left\{x\in\mathbb{R}:\sin^{-1}\left(\frac{x+1}{\sqrt{x^2+2x+2}}\right)-\sin^{-1}\left(\frac{x}{\sqrt{x^2+1}}\right)=\frac{\pi}{4}\right\},$$

then

$$\sum_{x\in R}\left(\sin\left(\left(x^2+x+5\right)\frac{\pi}{2}\right)-\cos\left(\left(x^2+x+5\right)\pi\right)\right)$$ is equal to _____.

Official Ans. by NTA (4)

Ans. (4)

23. Let $\omega=z\bar{z}+k_1z+k_2iz+\lambda(1+i), k_1, k_2\in\mathbb{R}$. Let $\mathrm{Re}(\omega)=0$ be the circle C of radius 1 in the first quadrant touching the line y =1 and the y-axis. If the curve Im (ω) = 0 intersects C at A and B, then 30 $(AB)^2$ is equal to _____.

Official Ans. by NTA (24)

Ans. (24)

24. Let for $x\in\mathbb{R}, S_0(x)=x$,

$S_k(x)=C_kx+k\int_0^x S_{k-1}(t)dt$, where

$C_0=1, C_k=1-\int_0^1 S_{k-1}(x)dx$, k = 1, 2, 3….. Then $S_2(3)+6C_3$ is equal to _____.

Official Ans. by NTA (18)

Ans. (18)

25. The sum to 20 terms of the series

$2.2^2-3^2+2.4^2-5^2+2.6^2-\ldots\ldots$ is equal to _____.

Official Ans. by NTA (1310)

Ans. (1310)

26. The number of seven digit positive integers formed using the digits 1,2,3 and 4 only and sum of the digits equal to 12 is _____.

Official Ans. by NTA (413)

Ans. (413)

27. Let m_1 and m_2 be the slopes of the tangents drawn from the point P(4,1) to the hyperbola $H:\frac{y^2}{25}-\frac{x^2}{16}=1$. If Q is the point from which the tangents drawn to H have slopes $|m_1|$ and $|m_2|$ and they make positive intercepts α and β on the x-axis, then $\frac{(PQ)^2}{\alpha\beta}$ is equal to _____.

Official Ans. by NTA (8)

Ans. (8)

28. Let the image of the point $\left(\frac{5}{3},\frac{5}{3},\frac{8}{3}\right)$ in the plane $x-2\quad y+z-2=0$ be P. If the distance of the point $Q(6,-2,\alpha), \alpha>0$, from P is 13, then α is equal to _____.

Official Ans. by NTA (15)

Ans. (15)

29. Let $\vec{a}=3\hat{i}+\hat{j}-\hat{k}$ and $\vec{c}=2\hat{i}-3\hat{j}+3\hat{k}$. If $\vec{b}$ is a vector such that $\vec{a}=\vec{b}\times\vec{c}$ and $|\vec{b}|^2=50$, then $|72-|\vec{b}+\vec{c}|^2|$ is equal to _____.

Official Ans. by NTA (66)

Ans. (66)

30. Let the mean of the data

x	1	3	5	7	9
Frequency(f)	4	24	28	α	8

be 5. If m and σ^2 are respectively the mean deviation about the mean and the variance of the data, then $\frac{3\alpha}{m+\sigma^2}$ is equal to _____.

Official Ans. by NTA (8)

Ans. (8)