## **EC315 Summary (3):**

# **Topics in Microeconomics With Cross Section Econometrics**

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EC315: Topics in Microeconomics With Cross Section Econometrics

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### **EC315: Topics in Microeconomics With Cross Section Econometrics Topic Summary**

#### **Topics:**

- 1) Exam Summary
- 2) Game Theory (Externalities & Consequences)
- 3) Topics in Public Economics (Government Role & Functions)
- 4) Cross-Section Economics (Theory & Real World)

#### **Cross-Section Econometrics**

#### 1: Descriptive Statistics

#### 1.1: Variables

Nume	rical:
	Continuous: infinite possible values (on real line or in an interval)
	<u>Discrete</u> : set value (number of values it can take on are finite (countable))
Catego	orical:
	Ordinal: ordered and means something
	Regular: ordered but means nothing
Relati	onships:
	Correlation ≠ Causation
	Associated: roughly connected
	Independent: not connected
	<u>Dependent</u> : depends on another
1.2: D	ata Collection
	Sample: group you're analysing
	Population: entire group of something
Sampl	ing Bias:
	Non-Responsive: only fraction respond
	Voluntary Response: people feel too strong
	<u>Convenience</u> : more accessible – easier to answer
Explai	natory & Response Variables:
	Observations: rather than asking questions
	Experiment: man-made situations

1.3: E	xamining Data
	Scatterplot: allows to identify relationship (e.g. Linear, Pos/Neg)
	$\circ$ x-axis: explanatory variable
	<ul> <li>y-axis: response variable</li> </ul>
	Dot Plot: shows volume at ends of sample scale
	Return Distribution Moments:
	○ 1: Mean
	o 2: Variance
	o 3: Skewness
	o 4: Kurtosis
1.3.1:	Mean
	Most common value (useful for predicting values etc. such as stock)
	Influenced by outliers so can be skewed inaccurately
	Population Mean: $\mu = \frac{\Sigma x}{T}$ ; Sample Mean: $\overline{x} = \frac{\Sigma x}{n}$
1.3.2:	Median
	Value in the middle of the dataset
	Splits 50%'ile (Quartile 2)
	o Q1: 25%, Q2: 50%; Q3: 75%
	○ <u>Interquartile Range</u> : Q1 – Q3
	Use here where we don't want outliers' influence (e.g. employee salary. Mean
	misleads due to the CEO's etc. salary)
1.3.3:	Standard Deviation
	σ
	How far deviated from the mean, is the data
	Same units as data
	"how many std.devs does the data lie from the mean"
	,

#### 1.3.4: Variance

 $\Box \quad \sigma^2$   $\Box \quad \text{The squere of the standard of } \sigma^2$ 

☐ The square of the standard deviation – to fairly weight (e.g. discard negatives)

☐ Therefore, weights higher deviations more

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	$cov_{Rx,Ry} = \sigma_x \sigma_y \rho$ Uses same units as the data – variance of members of the data set relative to others
1.3.6:	Correlation & Correlation Matrix
	$ ho = rac{cov_{Rx,Ry}}{\sigma_{x},\sigma_{y}}$
	Where $[\rho = 1]$ : Perfect Positive Correlation (Together) Where $[\rho = -1]$ : Perfect Negative Correlation (Apart) Where $[\rho = 0]$ : No Correlation To what degree the data moves together A <u>Correlation Matrix</u> maps all individual values with movement relative to all others in a relative <b>N</b> by <b>N</b> matrix
1.3.7:	Skewness
	The degree of asymmetry around the mean
	Symmetric: assume mean is centre
	○ {mean $\approx$ median}; {skewness $\approx$ 0}
	<u>Left Skewness</u> : $\{Skewness < 0\}$ ; tail to the left
	<ul><li>{mean &gt; median}; Positive Distribution</li></ul>
	Right Skewness: {Skewness > 0}; tail to the right
	<ul><li>{mean &lt; median}; Negative Distribution</li></ul>
1.3.8:	Kurtosis
	<u>Leptokurtic</u> : <b>Positive Kurtosis</b> ; above Normal Distribution w/ skinny tails  o {Excess Kurtosis < 0}
	Platykurtic: Negative Kurtosis; below Normal Distribution w/ fat tails
	○ {Excess Kurtosis > 0}
	Mesokurtic: Normal Distribution
	○ {Excess Kurtosis = 0}
	Excess Kurtosis: How peaked the data is relative to the Normal Distribution
	• Excess Kurtosis = $\{k-3\}$
	o Generally, EK of 1 is significant
	Measure of the peak of data; likelihood of extreme values  The higher the value of Kurtosia, the more likely you have outliers.
	The higher the value of Kurtosis, the more likely you have outliers
1.3.9:	Modality
	<u>Unimodal</u> : 1 Peak
	Multimodal: > 2 Peaks
	<u>Uniform</u> : No Peaks (outcomes have equal probabilities)

#### 1.4: Types of Economic Data

- Time Series: observations of the same unit, different points in time
  - o  $P_t$  for t = 1, 2, ..., T
  - o E.g. monthly profits of a firm between 1999 to 2008
- ☐ <u>Cross Section</u>: observations of different units, same time period
  - o  $P_i$  for i = 1, 2, ..., N
  - o E.g. profits of 256 companies over August 2008
- ☐ <u>Panels</u>: several units, varying time (e.g. company, country...)
  - $\circ P_{i,t} \text{ for } \begin{cases} i = 1, 2, \dots, N \\ t = 1, 2, \dots, T \end{cases}$
  - o E.g. profits of 256 companies in the financial sector from 1999 to 2008

#### ☐ General Notation:

- o  $X_i$  for i = 1, 2, ..., n; otherwise:  $X_1, X_2, ..., X_n$
- $\circ$  Representing n observations of X

#### 2: Regression Analysis

#### 2.1: Introduction

- ☐ How variation in one variable effects variation in the other
- ☐ Make expectations based on regression projections
- ☐ <u>Step 1</u>: Determine correlation for relationship
- ☐ Step 2: Is the relationship statistically significant?

#### 2.2: Graphing

- ☐ Must find the **best fit** line to identify <u>Correlation</u> & <u>Relationship</u>
  - o Recall: perfect positive, perfect negative, no correlation
  - o This will be seen through the **gradient** of the slope
- ☐ Recall: Correlation ≠ Causation
  - O With no causation however, there can still be a variable in common. Call it k as it's unknown and outside the Explanatory and Response variables (x and y)
  - $\circ$  E.g. hot weather (k) causes ice cream sales (x) and seaside deaths (y)
- $\Box$  x axis: Explanatory Variable
- □ y axis: Response Variable

#### **2.3:** The Line

- - $\circ$  y is the dependent variable (what effects y?)
  - $\circ$  x is the explanatory variable (does it affect y?)
  - o  $\alpha$  y-intercept (level of y when x = 0)
  - o  $\beta$  slope of the line (severity of the relationship)
- ☐ Everyone has one of these lines (variables values will change), we want to aggregate:
  - $\circ \quad \widehat{y}_i = \widehat{\alpha} + \widehat{\beta} x_i$
  - $\circ \quad \{\text{Alternatively: } \widehat{y}_i = \widehat{\beta}_0 + \widehat{\beta}_1 x \}$ 
    - Recall: *i* represents *N* individuals
    - Recall:  $\hat{k}$  (hat) represents estimation
  - $\circ \quad \text{Recall: } \boldsymbol{\beta} = \frac{\Delta y}{\Delta x} = \frac{\partial y}{\partial x}$ 
    - "For each (+) unit on the x axis, expect the y value to change by  $\beta$ "

#### 2.4: Residuals

	Calculating error of the line: distance between actual observations and the <b>best fit</b> line
	Error term: $e$ or $u$ w/ subscript of $i$
	$e_i = y_i - \widehat{y}_i$
	$\circ  \{\text{Alternatively: } \boldsymbol{u_i} = \boldsymbol{y_i} - \boldsymbol{\hat{y}_i} \}$
	Each individual will have a predicted $\hat{y}_i$ on the best fit line, directly above or below
	their real $y_i$
	Choose line which reduces <u>Aggregated Error</u> across all observations
	O This is such that the sum of $e^2$ is minimised:
	We want to minimise the amount of errors:
	$\circ$ "Finding $\hat{\boldsymbol{\alpha}}$ and $\hat{\boldsymbol{\beta}}$ which reduces the number of squared residuals"
	• Where here, and elsewhere: $\widehat{\alpha} = \widehat{\beta}_0$ ; $\widehat{\beta} = \widehat{\beta}_1$
	Reducing the sum of squared residuals
	• Hence, reducing $\sum_{i=1}^{N} e_i^2$
2.5: In	acluding Multiple Explanatory Variables
	Fitting a <u>Hyperplane</u> :
	$\circ \min_{\beta_{0},\beta_{1},\dots,\beta_{k}} \sum_{i=1}^{N} e_{i}^{2} \equiv \min_{\beta_{0},\beta_{1},\dots,\beta_{k}} \sum_{i=1}^{N} (y_{i} - \widehat{\beta}_{0} - \sum_{k=1}^{k} \beta_{k} x_{k,i})^{2}$
	This means that $\beta_0, \beta_1,, \beta_k$ are all the explanatory variables
	Here (in supplementary slideshow): $u_i = e_i$
2.6: C	onditions & Assumptions
	Assume to be <u>Linear</u> (not quadratic etc.)
	Assume Nearly Normal distribution (closest to line as possible: {Exp. Error $\approx 0$ })
2.7: R	<sup>2</sup> Value:
	The square of the Correlation Coefficient $\{0 < R^2 < 1\}$
	% of variability in dependent variable $(y)$ attributed to explanatory variable $(x)$
	R <sup>2</sup> increases when you increase <u>Explanatory Variables</u> (doesn't mean better model)
	o Hence, don't use if <u>Multiple Regression</u> ; use <u>Adjusted R<sup>2</sup></u>
	o Interpret in the same way
2.8: P	-Value:
	3(***): Certain at 99% (1% <u>Significance Level</u> ; P-Value < 0.01)
	2(**): Certain at 95% (5% <u>Significance Level</u> ; 0.01 < P-Value < 0.05)
	1(*): Certain at 90% (10% <u>Significance Level</u> ; P-Value < 0.10)
	(No Stars): Insignificant (Statistically Insignificant; 0.10 < P-Value)

#### 3: Multiple Regression & Goodness of Fit

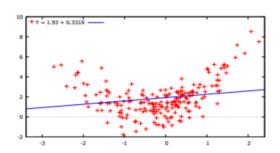
- 1) This simply adds more **Explanatory Variables**
- 2) Explore the extent to which the model explains the data (R<sup>2</sup>)

#### 3.1: 'Aggregation' & Adding More Explanatories

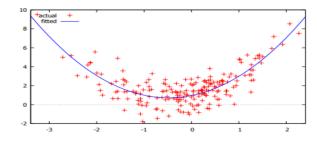
- $\Box$  Expand:  $y = \alpha + \beta x$
- $\Box$  For Explanatories: 1 to k
- □ Note that it may not always be linear (<u>Hyperplane</u>)
  - Not all variables have linear relationships
  - o Concavity/Convexity etc.

#### 3.2: Nonlinearity

- □ Non-linear data can be captured in a linear model
- ☐ E.g. the Concave
- ☐ Hence, linear model does a poor job of explaining the data



- ☐ This can be fixed with <u>Polynomial Models</u>
- $\Box \quad \text{Hence: } Y_i = \alpha = \beta_1 X_i + \beta_2 X_i^2 + \dots + \beta_k X_i^k + u_i$ 
  - Constant remains ( $\alpha$  or  $\beta_0$ )
  - Error term remains  $(u_i)$
- $\Box$  Thus, keep adding <u>Polynomial Terms</u> ( $x^2$  values) until the model best fits the spread
- ☐ Hence:



#### 3.3: Dummy Variables

- ☐ <u>Dummy Variables</u> do not have values
- ☐ They are <u>Categorical</u>: e.g. Male/Female or Retired/Employed
  - O You expect one group to show different levels of y for any x
  - o They're purely binary {1 or 0}
    - 1: Observation comes from the group of 'interest'
    - 0: Null response thus, otherwise
- $\square$  Modify Regression:  $Y_i = \alpha = \beta_1 X_i + \tau D_i + u_i$ 
  - Where:  $\tau$  = Coefficient of Dummy Variable
  - o If:  $D_i = 0$ ;  $Y_i = \alpha = \beta_1 X_i + u_i$  (Male (Null) in e.g.)
  - o If:  $D_i = 1$ ;  $Y_i = \alpha = \beta_1 X_i + \tau + u_i$  (Female in e.g.)
    - Hence, intercept alters

#### 3.4: Changes in Slope

- ☐ E.g. expenditure patters may be at two extremes
- $\Box$  Take a <u>Dummy Variable</u> with criteria to identify all people who spend > 2000
  - $\circ$  1: Spend > 2000 (e.g.)
  - o 0: Spend < 2000 (e.g.)
- □ Thus: Dummy Variable for  $X \ge x$ 
  - o If:  $X \ge x$  then 1
  - o If: X < x then 0
- $\square$  Modify Regression:  $Y_i = \alpha = \beta_1 X_i + \beta_2 (X_i \cdot D_i(x)) + u_i$ 
  - Where:  $D_i(x) = Dummy Variable$
  - $\quad \text{o} \quad \text{If: } D_i(x) = 0; Y_i = \alpha = \beta_1 X_i + u_i$
  - o If:  $D_i(x) = 1$ ;  $Y_i = \alpha = \beta_1 X_i + \beta_2 X_i + u_i$ 
    - Hence, intercept alters

#### 3.5: Interpretation

- ☐ Simple Regression: If the Explanatory Variable changes by 1 unit, how much does the Reliant Variable change?
  - o  $\beta_i$  is the marginal effect of x on y
- ☐ Multiple Regression: If the <u>Explanatory Variable</u> changes by 1 unit, how much does the <u>Reliant Variable</u> change, given all other <u>Explanatory Variables</u> are constant work your way along all of the Beta values holding each other constant
  - $\circ$   $\beta_i$  is the marginal effect of  $X_i$  on Y

3.6: H	ypothesis Testing
	Null Hypothesis $\mathbf{H_0}$ : $R^2 = 0$ ; $X$ doesn't have any explanatory power for $Y$ Alternative Hypothesis $\mathbf{H_1}$ : $R^2 \neq 0$ ; Reject Null in favour of Alternative
3.7: M	<b>Sulticollinearity</b>
	When two variables have a high correlation (close to 1 or -1) The model struggles to understand which one is actually explaining <i>Y</i> Run a Multicollinearity test for the Matrix Drop a highly correlated variable
3.8: C	hoosing Explanatory Variables
,	Use hypothesis testing  Test for significance and omit insignificant ones  o If significant and omitted, Omitted Variables Bias
3.9: C	hoosing Models
	Schwartz Information Criterion Akaike Information Criterion Hannan-Quinn Information Criterion

☐ Pick one

□ Compare across models□ Select the lowest value

#### 4: Theory

	Probability Theory & relationship to Econometrics
	o Expected Values
	o <u>Variance</u>
	<ul> <li><u>Probability</u> <u>Distribution</u> (Density Functions)</li> </ul>
	Problem: taking several <u>Samples</u> from the same population means estimates will
	change from sample to sample so not represent the Population correctly
	If we only have one sample: how significant are the estimates to the <u>Population</u> ?
l.1: E	experiments & Events
	"An outcome unknown in advance"
	Possible outcomes (realisations) of experiments: Events
	o i.e. predict positive relationship
	Set of all possible outcomes: <u>Sample Space</u>
	Variables of Experiments & Events are:
	Recall: <u>Discrete</u> : set value (number of values it can take on are finite (countable))
	<ul> <li>Depends on scale of variability (e.g. Happy? Rate: 0-M&amp;S)</li> </ul>
	o If counter-intuitive (e.g. Happy? Rate M&S-0) cant interpret like Continuous
	Recall: Continuous: infinite possible values (on real line or in an interval)
1.2: R	andom Variables & Probability
	A variable through which we don't know the outcome (e.g. <b>Y</b> on a regression)
	Probability reflects likelihood of an event
	o E.g. just knowing what income is doesn't allow to you know expenditure
	■ Income = 1000; Consumption <b>not</b> > 1000
	o E.g. Probability of A occurring denoted:
	$\circ$ $Pr(A)$
	Example:
	o Dice, probability of rolling any six options: <b>Constant</b> <u>Probability</u>
	o Sample Space: {1,2,3,4,5,6}
	o The <u>Discrete Random Variable</u> (A): {1,2,3,4,5,6}
	<ul> <li>Same probability of rolling any face</li> </ul>
	• Hence, Probabilities: $Pr(A = 1) = Pr(A = 2) = \cdots = [A = 1/6]$
	o Realisation of random variable is value which actually arises
	o <u>Independence</u> : events A and B are <u>Independent</u> so:
	Pr(A) = Pr(B) = Pr(A, B)
	O Conditional: event A may be Conditional upon B so:

■ Probability of A occurring given B occurs

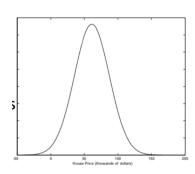
With Continuous Random Variables use notation: p(A|B); p(A,B); p(B)

#### 4.3: Probability in Regression

- ☐ Regression provides description of the probable values of the dependent variable
- ☐ Hence, we use <u>Probability Density Functions</u> (p.d.f.)
  - o Used with Continuous Normal Variables
  - Probabilities are the number under the Normal Distribution function

#### **■** Example:

0



- Tells you which plausible values that y can take given the set x value
- At the highest point, we see the most plausible values
- ☐ The shape of the distribution depends on the Mean and the Variance
- □ "Y has a Normal Probability Density Function"
  - $\circ$  Mean =  $\mu$
  - Variance =  $\sigma^2$
  - $o Normal p.d.f. = y \sim N(\mu, \sigma^2)$
- Recall House Price Example:
  - o  $\mu = 61.153$  (Mean value of a house of lot size > 5000)
  - o  $\sigma^2 = 683.812$  (Not really any intuitive value)
- ☐ Defined areas under the <u>p.d.f.</u> curve are the <u>Probabilities</u>
- □ "Probability of price being between 60k and 100k":

$$\circ N(\mu,\sigma^2)$$

$$\circ = \Pr(\min \le k \le \max)$$

$$\circ = \Pr(60 \le Y \le 100)$$

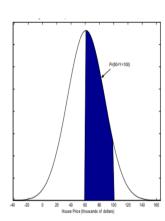
$$\circ = \Pr\left(\frac{60-\mu}{\sigma} \le \frac{Y-\mu}{\sigma} \le \frac{100-\mu}{\sigma}\right)$$

$$\begin{array}{ll} \circ & = Pr\left(\frac{60-\mu}{\sigma} \leq \frac{Y-\mu}{\sigma} \leq \frac{100-\mu}{\sigma}\right) \\ \circ & = Pr\left(\frac{60-61.153}{\sqrt{683.812}} \leq \frac{Y-61.153}{\sqrt{683.812}} \leq \frac{100-61.153}{\sqrt{683.812}}\right) \end{array}$$

$$\circ = Pr(0 \le Z \le 0.04) \to 0.016$$

$$\circ = Pr(0 \le Z \le 1.49) \to 0.4319$$

o \* These are the two independent areas \*



- 0 -----
- $\circ$  (+ Together) = **0**.4479 : 45%

#### 4.4: Other Distributions

#### 4.4.1: Chi-Distribution

- ☐ Distribution depending on the <u>Degrees of Freedom</u> (accounts for number of observations and variables)
  - $\circ$  Higher the better  $\rightarrow$  more flexibility
  - Denoted by df
  - Skewness decreases with the raising <u>Degrees of Freedom</u>
- □ Not bell-shaped like <u>Normal Distribution</u>
  - $\circ$  Only for the positive values of  $\boldsymbol{x}$

#### 4.4.1: t-Distribution

- $\square$  How we calculate the <u>p-Value</u>
- ☐ Shows how significant values are
- □ Symmetric
- ☐ Compare from (Critical Value) -1.96 to 1.96
  - o If 0 sits in the centre, Normally Distributed
- "If **t-Value** is > **Critical Value**, explanatory variables are statistically significant"

#### 4.5: Assumptions of a Regression (OLS) \*\*GROUP PROJECT\*\* 2 & 3

- 1)  $E(u_i) = 0$  Mean Expect dependent variable to lie on the best fit
- 2)  $var(u_i) = E(u_i^2) = \sigma^2$  all observations should have constant errors
  - Homoscedasticity: constant errors
  - o Heteroscedasticity: non constant errors (must adjust model)
- 3)  $cov(u_i, u_i) = 0$  for  $i \neq j$  Expecting observations to be uncorrelated
  - o If two explanatory variables have high collinearity, omit one (run corr. matrix)
- 4) Expect errors are normally distributed (not a lot of outliers)
- 5) Explanatories are fixed

#### **Rough Notes on Interpretation \*\*TEST\*\*:**

Don't interpret constant
Four explanatory variables follow below, for each:
Dummies (oneAdult, ownsHouse)
<ul> <li>If you are not included in the criteria: 0</li> </ul>

- o If you are included in the criteria: 0

#### 1) **P-Vale**: is it significant?

 $\circ$  Here, {P < 0.01 @ 0.0001} so "Statistically Significant at explaining the dependant variable at the 1% Significance Level"

#### 2) Coefficients:

- o As significant, look at coefficients. Don't analyse if statistically insignificant
- o If Positive Corr. (Converse): as explanatory increases, reliant increases
- o If Negative Corr. (Inverse): as explanatory increases, reliant decreases

#### ☐ Examples:

- o A One Adult Household is significant at 1% significance level and spends £96.63 less (-96.6313)
- o A higher managerial occupied man is significant at 1% and spends %55.88 more

#### 3) Bottom (only interested in a few)

- o **Mean Dependent**: for interest
- $\circ$  **R**<sup>2</sup> or: goodness of fit (% of variability in y which can be explained by x)
  - E.g. 52% of the variability in expenditure can be explained by the dependent variables
  - But! Use adjusted as there are multiple explanatory variables

Model 1: OLS, using observations 1-5144 Dependent variable: P550tpr

	Coefficient	Std. Er	ror	t-ratio	p-value	
const	200.942	8.333	05	24.11	< 0.0001	***
P344pr	0.468970	0.0110	996	42.25	< 0.0001	***
ownsHouse	4.55590	6.416	97	0.7100	0.4778	
oneAdult	-96.6313	7.061	04	-13.69	< 0.0001	***
DA094r_1	55.8807	7.265	78	7.691	< 0.0001	***
Mean dependent var	479.	7584	S.D.	dependent var	292	2.3652
Sum squared resid	2.11	e+08	S.E.	of regression	202	2.6383
R-squared	0.51	9986	Adju	sted R-squared	0.5	19613
F(4, 5139)	1391	.736	P-val	ue(F)	0.0	00000
Log-likelihood	-3461	8.48	Akail	ke criterion	692	246.95
Schwarz criterion	6927	9.68	Hann	an-Quinn	692	258.41

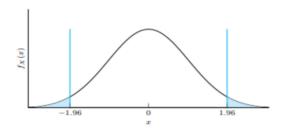
#### **5:** Hypothesis Testing

#### **5.1:** What is a Hypothesis

- 1) t-test
- 2) f-test
- 3) RESET Test
- □ Suppose  $\hat{\beta} = 0.47$  (estimated coefficient); is that significantly different from 0.5?
- $\Box$  We must know distribution/density function of  $\hat{\alpha} \& \hat{\beta}$
- ☐ There are two Hypotheses (e.g. yes/no)
- ☐ We want to test if this variable is significant or insignificant
- □ **H**<sub>0</sub>: Null Hypothesis ( $\beta = 0$ )
  - o Unable to reject Null Hypothesis
  - o "explanatory variable is insignificant in explanation of dependent variable"
  - o If p-value > 0.1: Unable to reject
- $\Box$  **H**<sub>A</sub>: Alternative Hypothesis ( $\beta \neq 0$ )
  - o Reject Null Hypothesis
  - o "explanatory variable is significant in explanation of dependent variable"
  - o If p-value < 0.1: Reject in favour of alternative
- ☐ Type I Error: Reject Null when it's in fact true
- ☐ Type II Error: Fail to Reject Null when it is in fact false
- □ \*\*As long as p-value < 0.1, these won't occur\*\*

#### 5.2: t-test

#### 5.2.1: t-ratio



- $\Box$  If Null Hypothesis Failed Rejection:  $\hat{t}$  close to 0
- □ If Null Hypothesis Rejected:  $\hat{t} < -1.96$  or  $\hat{t} > 1.96$

5.2.2: p-v	alues
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	p-value is the probability that, under $H_0$ , the test value is at least as large as $\hat{t}$
	If probability (Significance Level) > p-value: Fail to Reject Null
	If probability (Significance Level) < p-value: Reject Null in favour of Alternative
	T
	Example:
	$\hat{t}=2$ ; show: $P(t\geq 2)=0.022$ (Significance Level) @ defined p-value
	o If p-value = $0.05$ : Reject as $0.022 < 0.05$
	o If p-value = 0.01: Fail to Reject as $0.022 > 0.01$
5.3: f-1	test
	A joint test for the whole regression: $H_0$ : $R^2 = 0$
	Must reject in favour of the Alternative Hypothesis
	Observe f-ratio: like t-ratio but for regression as a whole
	Observe p-value: in the same way as the individual p-values
	This is tested against the 5% level
	o If p-value < 0.05: Reject Null so some significance
	<ul> <li>If p-value &gt; 0.05: Fail to Reject Null</li> </ul>
	If single regression: p-value (f-test) = p-value (t-test)
5.4: R	ESET Testing
	Is your model well specified (do not needing logs or polynomials)
	Hypothetically adds gamma coefficients to hypothetical log and polynomial values
	Hence: $H_0$ : $Gamma = Gamma_2 = 0$
5.4.1:	RESET in Gretl
	After the Regression;
	Tests;
	Ramsay's RESET;
	Squares and Cubes;
	Don't Interpret Coefficients;
	F-test for Gamma Polynomials;
	P-value at Bottom;
	Use 5% level;
	If p-value < 0.05: model mis-specified (needs extra like polynomials and logs etc.)
	If p-value > 0.05: model well-specified (does not need polynomials etc.)
	Opposite of what we conclude about p-values in general
	If mis-specified: try logs and polynomials

#### **6: Instrumental Variables**

	Drop assumption that explanatory variables are fixed, they aren't
	Random explanatories don't cause problems unless correlated with the error ( <i>u</i> )  Don't use OLS (Ordinary Least Squares), use alternative IV (Instrumental Variables)
ш	estimator 2SLS (Two Stage Least Squares)
	This incorporates everything that the model doesn't include (unknown)
	coefficients where variable correlated with $u$ )
	o E.g. all else when your using income to explain consumption (age etc.)
П	Example:
	• Earnings: dependent; Schooling: explanatory; Error: <i>u</i>
	o $y = \beta x + u$ ; where u captures all explanation not done by schooling (which is
	usually higher with people of <b>higher ability</b> ) $\rightarrow$ E.g. ability can also effect
	o If error value is high: "high un-associated explanation"
	<ul> <li>Endogeneity: "factors within the model causing x to increase so changes in x are also associated with changes in u"</li> </ul>
	$\circ$ What would x have been if not measures with error u, as x is higher than it
	should be as correlated to $u. \rightarrow 2SLS$
6.1: In	troducing Instrumental Variables
	Solution to the above problem
	z = Instrumental Variable
	Isolates movement in $x$ which is uncorrelated to the error $u$ (e.g. ability)
	Hence, coefficient will no longer be inflated
	Endogenous: variables correlated with error term u
	Exogenous: variables uncorrelated with error term $u$
6.2: V	ariation of x
	2 Parts: one is correlated with <i>u</i> and second is uncorrelated with <i>u</i>
	Isolate the uncorrelated with <i>u</i>
	The uncorrelated parts are included in 1 to N z values for each explanatory
	An IV only influences y through an explanatory, it wouldn't hold up as an explanatory itself
	$\circ$ E.g. ability effects schooling (x) but not directly income (y)
6.3: In	strumental Variable Satisfactions
	z is correlated with (Endogenous) $x$
	z is uncorrelated with $y (z \rightarrow x \rightarrow y; \mathbf{not} z \rightarrow y)$

6.4: Two Stage Least Squares (2SLS)		
	y: Dependent Variable	
	$x_{lk}$ : Endogenous Variables	
	$w_{1k}$ : Exogenous Variables	
	$z_{lk}$ : Instrumental Variables	
	"For every x you expect to be <u>Endogenous</u> , you require an <u>Instrumental Variable</u> "	
1)	Regress $x$ on $z_{Ik}$ values for $x_{Ik}$ and obtain <b>predicted</b> values: $\hat{x}$	
2)	Regress y on $w_{Ik}$ (don't need <u>Instrumental Variables</u> )	
3)	Look for high correlation between <u>Instrumental Variables</u> and <u>Explanatory Variables</u>	
6.5: Testing for Endogeneity		
	"Hausman Test"	
	H <sub>0</sub> : Explanatory Variable uncorrelated with error term	
	<ul> <li>Fail to Reject: use OLS</li> </ul>	
	o Reject: use <u>Instrumental Variables</u> for 2SLS	
	p-value > 0.05 Means no <b>Endogeneity</b> problem (Fail to Reject)	
	p-value < 0.05 Means <b>Endogeneity</b> problem (Reject)	
	Like RESET Test	
6.5.1: Strength of Instruments		
	High Correlation with (Endogenous) <i>x</i> : Strong Instrument – use <b>2SLS</b>	
	Low Correlation with (Endogenous) x: Weak Instrument – might as well use <b>OLS</b>	
	Relevant?	
	<ul> <li>R<sup>2</sup> shows this integrity</li> </ul>	
	o f-test shows validity of the set of instruments as a whole (like OLS)	

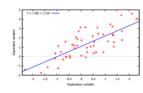
#### 7: Robust Estimation

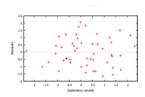
- ☐ Characteristics:
  - o Heteroscedasticity (as opposed to Homoscedasticity)
  - Cross-Sectional Correlation
- ☐ As possible results show:
  - o Affect reliability of hypothesis tests
  - Don't introduce significant bias in estimates
- ☐ Recall:
  - $\circ$   $var(u) = \sigma^2$
  - All regression errors have equal variance

#### 7.1: Heteroscedasticity & Homoscedasticity

- ☐ <u>Heteroscedastic</u>: Non-Constant Error Variance
- ☐ Homoscedastic: Constant Error Variance
  - $\circ$   $var(u) = \sigma^2$

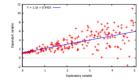
#### **□** Example:

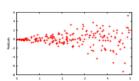




o Hence, <u>Homoscedastic</u> (no pattern)

#### ☐ Example:





- o Hence, <u>Heteroscedastic</u> (pattern)
- OLS regression (left) does good job when income is low but lacks explanatory value as income increases
- E.g.: when income increases, expenditure may only increase a little and savings may take place instead

# 7.1.1: Homoscedasticity □ var(u) = σ² □ House price dataset: ○ Dependent variable: house price ○ Explanatory variables: bedrooms, bathrooms etc. □ u measures whether a house is under or over-priced relative to similar houses □ Homoscedasticity doesn't say all errors are same for every house but, that they're from the same distribution ○ "Magnitudes of under or over-pricing tend to be the same for all kinds of

#### 7.1.2: Heteroscedasticity

houses"

 $\Box$   $var(u) = \sigma^2 \omega_i^2$ 

 $\circ$  For: i = 1,...,N; i denotes that variance of the error can be different for each observation

#### ☐ Implications:

- 1) Least squares estimates are unbiased and/or inefficient
- 2) Variances and covariances need reconstrained
- 3) t-tests and f-tests lose validity so don't represent good p-values

#### 7.2: Test for Heteroscedasticity in Gretl

Solving problem (3)
Making standard errors 'robust

#### **☐** White Test

- o Using 'White', 'Robust', 'Heteroscedasticity Consistent (HC)' standard errors
- New t-ratios, p-values
- o If <u>Heteroscedasticity</u> is not present, OLS fine (**BLUE**)
- o If <u>Heteroscedasticity</u> is present, use robust std. errors (**HCE**)
- o H<sub>0</sub>: <u>Homoscedastic</u> Constant Error Variance
- o H<sub>A</sub>: Heteroscedastic Non-Constant Error Variance
- o p-value < 0.05: Reject Null Hypothesis (Reject Homoscedasticity)
- o p-value > 0.05: Fail to Reject Null Hypothesis (Accept <u>Homoscedasticity</u>)
- o In response to Heteroscedasticity, tick Robust Standard Errors
- 1) Run Model
- 2) Use White Test
- 3) Analyse p-value
- 4) Tick Robust Standard Errors in OLS Window

#### 7.3: Cross-Sectional Dependence

	Samples are completed in 'clusters'
	Clusters from different classes, clusters from different countries, different firms etc.
	Data can therefore be highly <u>Correlated</u> due to similar traits
П	Use Cluster Robust Standard Errors