

UNIVERSITY OF STRATHCLYDE  
DEPARTMENT OF MATHEMATICS & STATISTICS

MM104: Statistics and Data Presentation Semester 2  
MM107: Statistics and Data Presentation

FORMULA SHEET

One sample Z-test

$$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

Two sample Z test

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

One sample t-test

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}, \quad s = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

Two sample t-test

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{s^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}, \quad s^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

Effect size for a two sample t-test

$$ES = \frac{|\bar{x}_1 - \bar{x}_2|}{\sqrt{\left( \frac{s_1^2 + s_2^2}{2} \right)}}$$

$\chi^2$  test for association (independence) test statistic

$$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$$

$$\begin{aligned} S_{xx} &= \sum x_i^2 - \frac{(\sum x_i)^2}{n} \\ S_{yy} &= \sum y_i^2 - \frac{(\sum y_i)^2}{n} \\ S_{xy} &= \sum x_i y_i - \frac{\sum x_i \sum y_i}{n} \end{aligned}$$

$$R^2 = \frac{S_{xy}^2}{S_{xx} S_{yy}}$$