

A farmer with a wolf, a goat, and a cabbage must cross a river by boat. The boat can carry only the farmer and a single item. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage. How can they cross the river without anything being eaten?  
[https://en.m.wikipedia.org/wiki/Wolf,\\_goat\\_and\\_cabbage\\_problem](https://en.m.wikipedia.org/wiki/Wolf,_goat_and_cabbage_problem)

– This spec taught me the difference between CHOICE and with:  
[https://groups.google.com/g/tlapus/c/QJAulqYgC0E/m/Cm2PPJBDCQAJ](https://groups.google.com/g/tlaplus/c/QJAulqYgC0E/m/Cm2PPJBDCQAJ)  
 > CHOOSE is definitely a confusing operator, many people have problems with it including myself.  
 > The idea is that CHOOSE always picks the same value, it does not represent arbitrary values.  
 > If you're trying to say “sub can be any element of *ClaimsData*”, then the “there exists”  
 > operator (existential quantification) is what you're looking for, *i.e.*  
 >  $\exists \text{ sub} \in \text{ClaimsData: SomePredicate}(\text{sub})$

And: > What if multiple values satisfy CHOOSE ? In this case the only requirement is that the result is deterministic: the engine must always return the same value, no matter what. In practice this means that *TLC* will always choose the lowest value that matches the set.  
<https://learntla.com/core/operators.html>  $\neq$  choose

CHOOSE has to be deterministic but in my previous implementation (in last commit) I was trying to use CHOOSE to pick any element in subset of side such that removing that item from side would have left it in a valid state. Because I was using CHOOSE, tlc was always picking the same value leading to a very small possible state transitions and a lot of headache to me.

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MODULE *wolf\_goat\_cabbage*

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LOCAL INSTANCE *TLC*  
 LOCAL INSTANCE *FiniteSets*  
 LOCAL INSTANCE *Integers*

*WOLF*  $\triangleq$  “Wolf”  
*GOAT*  $\triangleq$  “Goat”  
*CABBAGE*  $\triangleq$  “Cabbage”  
*FinalResult*  $\triangleq$  {*WOLF*, *GOAT*, *CABBAGE*}  
*InvalidStates*  $\triangleq$  {{*CABBAGE*, *GOAT*}, {*WOLF*, *GOAT*}}  
*baitinv*  $\triangleq$  TRUE  
*baitinv*  $\triangleq$  *TLCGet*(“level”) < 14

**--algorithm** *wolf\_goat\_cabbage*{

**variables** *side\_start* = *FinalResult*, *side\_end* = {};

**define** {  
   *IsValidState*(*side*)  $\triangleq$   $\neg(\text{side} \in \text{InvalidStates})$   
   *Inv*  $\triangleq$  *side\_end*  $\neq$  *FinalResult*  
     this operator is used select an item  
     from side such that removing this item  
     will leave “side” in a valid state.  
   *ValidSubsets*(*side*)  $\triangleq$  {*s*  $\in$  SUBSET (*side*) : *IsValidState*(*side\_start* \ *s*)  $\wedge$  *Cardinality*(*s*) = 1}  
}

**macro** *PickFrom*( *side*, *other\_side\_is\_valid* ) {  
   **await**  $\wedge$  *transport* = {}  
      $\wedge$  *side*  $\neq$  {}  $\wedge$  *other\_side\_is\_valid* ;

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        choose an item such that this side is left valid:
with (  $item \in ValidSubsets(side)$  ) {
         $transport := item$ ;
         $side := side \setminus transport$ ;
    }
}

macro DropItemTo(  $side$  ) {
    leave an item to  $side\_start$  side. If needed to avoid conflicts, load the other item.
    await  $transport \neq \{\}$ ;
     $side := side \cup transport$ ;
     $transport := \{\}$ ;
}

process (  $Farmer = 1$  )
variable  $transport = \{\}$ ; {
W:
    while ( TRUE ) {
        either {
            pick an item from  $side\_start$  and load it.
             $PickFrom(side\_start, IsValidState(side\_end))$ ;
        } or {
            pick an item from  $side\_end$  and load it.
             $PickFrom(side\_end, IsValidState(side\_start))$ ;
        } or {
             $DropItemTo(side\_start)$ ;
        } or {
             $DropItemTo(side\_end)$ ;
        } ;
    }
}

}

BEGIN TRANSLATION ( $chksum(pcal) = "7c28162a" \wedge chksum(tla) = "b19f62f8"$ )
VARIABLES  $side\_start, side\_end$ 

define statement
 $IsValidState(side) \triangleq \neg(side \in InvalidStates)$ 
 $Inv \triangleq side\_end \neq FinalResult$ 

 $ValidSubsets(side) \triangleq \{s \in SUBSET(side) : IsValidState(side\_start \setminus s) \wedge Cardinality(s) = 1\}$ 

VARIABLE  $transport$ 

vars  $\triangleq \langle side\_start, side\_end, transport \rangle$ 

ProcSet  $\triangleq \{1\}$ 

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$$\begin{aligned}
Init &\triangleq \text{Global variables} \\
&\wedge \text{side\_start} = \text{FinalResult} \\
&\wedge \text{side\_end} = \{\} \\
&\text{Process Farmer} \\
&\wedge \text{transport} = \{\} \\
Farmer &\triangleq \vee \wedge \wedge \text{transport} = \{\} \\
&\quad \wedge \text{side\_start} \neq \{\} \wedge (\text{IsValidState}(\text{side\_end})) \\
&\quad \wedge \exists \text{item} \in \text{ValidSubsets}(\text{side\_start}) : \\
&\quad \quad \wedge \text{transport}' = \text{item} \\
&\quad \quad \wedge \text{side\_start}' = \text{side\_start} \setminus \text{transport}' \\
&\quad \wedge \text{UNCHANGED side\_end} \\
&\vee \wedge \wedge \text{transport} = \{\} \\
&\quad \wedge \text{side\_end} \neq \{\} \wedge (\text{IsValidState}(\text{side\_start})) \\
&\quad \wedge \exists \text{item} \in \text{ValidSubsets}(\text{side\_end}) : \\
&\quad \quad \wedge \text{transport}' = \text{item} \\
&\quad \quad \wedge \text{side\_end}' = \text{side\_end} \setminus \text{transport}' \\
&\quad \wedge \text{UNCHANGED side\_start} \\
&\vee \wedge \text{transport} \neq \{\} \\
&\quad \wedge \text{side\_start}' = (\text{side\_start} \cup \text{transport}) \\
&\quad \wedge \text{transport}' = \{\} \\
&\quad \wedge \text{UNCHANGED side\_end} \\
&\vee \wedge \text{transport} \neq \{\} \\
&\quad \wedge \text{side\_end}' = (\text{side\_end} \cup \text{transport}) \\
&\quad \wedge \text{transport}' = \{\} \\
&\quad \wedge \text{UNCHANGED side\_start} \\
Next &\triangleq \text{Farmer} \\
Spec &\triangleq \wedge Init \wedge \Box [Next]_{vars} \\
&\quad \wedge \text{WF}_{vars}(Next) \\
&\quad \wedge \text{WF}_{vars}(Farmer) \\
&\text{END TRANSLATION} \\
TypeOk &\triangleq \wedge \forall el \in \text{side\_start} : el \in \{WOLF, GOAT, CABBAGE\} \\
&\quad \wedge \forall el \in \text{side\_end} : el \in \{WOLF, GOAT, CABBAGE\} \\
&\quad \wedge \forall el \in \text{transport} : el \in \{WOLF, GOAT, CABBAGE\}
\end{aligned}$$


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