

Solving Exam Scheduling Problem Using Graph Coloring

A Final Report

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## I. INTRODUCTION

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## II. DEFINITION OF THE PROBLEM

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## IX. FURTHER DISCUSSION

### A. Genetic Algorithm

The genetic algorithm presented in the paper has some interesting properties. The optimal fitness score is defined to be 0, since that would mean there are no conflicting edges. The authors present two different parent selection and mutation functions in an attempt to converge as quickly as possible. Despite trying to implement those functions, I was unable to reproduce the same benchmarks that were presented in the paper. However, I did try various ideas and with some fine tuning, I managed to get fairly decent performance. One problem that I currently have with it is the execution speed. Python isn't particularly fast, but I also am not familiar enough with the language to be able to optimize it enough. After profiling the code, I found that the bottleneck is from constantly getting the colors of adjacent edges. This also explains why the algorithm struggles with densely connected graphs.

There are some details left out of the paper as well. For example, they talk about parent selection, crossover, mutation and then adding the child to the population. However, they only add one child to the population while also mentioning that the population size should be constant. Therefore, I either need to repeat the process with another child so that I can replace both parents, or leave a parent in the population. I experimented with both. Creating two children made the fitness scores more erratic. This could potentially be beneficial since there is more exploration, but it seemed to converge onto a pattern. I think this would be a more feasible option if there was more randomness in play. The other option I explored was to take the

fittest of the parents and put that parent back into the population. This had the effect of a slow, but steady decrease in the fitness score.

Bad edges are defined as edges between vertices of the same color. The fitness function is calculated by counting the number of bad edges. However, given enough colors and a large enough graph, this is pointless. For example, if I gave the genetic algorithm enough colors for each vertex, then the algorithm would converge in seconds, usually around 12 to 20 generations. However, the color assignment seems like it might be slightly better than trying to randomly assign colors. The result of this would usually be around 500 out of 800 colors. So perhaps an adjustment that can be made is to have a penalty for chromosomes that use a lot of colors. That way the fitness score improves when there are better assignments or there are less colors used or, ideally, both.

Another thing to take into consideration is the initial population. I tried assigning colors at random while also using all of the colors, assigning at random using a subset of colors and assigning all the vertices the same color. The initial assignment with all vertices the same color converged quickly at first, but then peaks. Assigning colors at random with a color for each vertex converges in about 10-20 generations but also uses about 500 colors. Finally, assigning the vertices at random, but only using a subset of the colors behaves similar to assigning them to one color.

I also tried limiting the number of colors that were available to the algorithm. For example, giving the algorithm a set of 50 colors to work with in the exam graph of 800 vertices allows the algorithm to converge to a solution in about 20 generations. Giving it 35 colors makes it converge at around 50 to 200 generations.

Some other variables that I changed were the population size, mutation rate and crossover rate. Changing the population size didn't really help. Having a high mutation rate was good, but I found that 0.8 tends to work best with a crossover rate of 1.0. If the mutation rate was too high, it would often get to a good fitness score, but then get stuck.

Finally, I found that a mutation rate of 0.8 with a crossover rate of 1.0, population size of 50 and between 37-40 colors converges in a reasonable amount of time. However, the genetic algorithm performs poorly on random graphs since I can't really fine tune the parameters. So one of the downfalls of the genetic algorithm is that it sometimes requires fine tuning the parameters for specific examples.

## X. CONCLUSION

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