

## FORMULA FOR LOGISTIC REGRESSION

1. compute weighted sum

$$\text{weighted sum} = \underset{\theta_0}{\text{bias}} + (\underset{\theta_1}{\text{weight 1}} \times \underset{x_1}{\text{feature 1}}) + (\underset{\theta_2}{\text{weight 2}} \times \underset{x_2}{\text{feature 2}}) + \dots$$

2. apply sigmoid function

$$\text{probability} = 1 \div [1 + e^{-(\text{weighted sum})}]$$

(a)

$$\begin{aligned}\text{weighted sum} &= (-6) + (0.05 \times 40) + (1 \times 3.5) \\ &= -0.5\end{aligned}$$

$$\begin{aligned}\text{probability} &= 1 \div [1 + e^{-(-0.5)}] \\ &= 0.3775 \\ &= 37.75\% \parallel\end{aligned}$$

probability is 37.75%

(b)

find weighted sum:

$$0.5 = 1 \div [1 + e^{-(\text{weighted sum})}]$$

$$0.5 [1 + e^{-(\text{weighted sum})}] = 1$$

$$0.5 e^{-(\text{weighted sum})} = 0.5$$

$$e^{-(\text{weighted sum})} = 1$$

$$\text{weighted sum} = 0$$

find no. of hours using weighted sum formula

$$0 = -6 + (0.05 \times \text{hours}) + (1 \times 3.5)$$

$$\text{hours} = \frac{2.5}{0.05}$$

$$= 50 \parallel$$

Student requires 50 hours