## How to generate knockoffs?

 $\mathbb{P}(X) = \frac{1}{2} \exp \left[ \sum_{i=1}^{n} X_{i} X_{j} \right], X \sim \{-1,1\}^{p}$ 

 $\mathbb{P}(X, \tilde{X}) = \frac{1}{Z} \exp \left[ \sum_{i=1}^{N} X_i X_j \right] \frac{1}{Z'(X)} \exp \left[ \sum_{i=1}^{N} \tilde{X}_i \tilde{X}_j + X_i \tilde{X}_j + \tilde{X}_i X_j \right]$ 

## Z' is a function of X!

## How to generate knockoffs?

$$\mathbb{P}(X) = \frac{1}{Z} \exp\left(\sum_{i \sim j} X_i X_j\right), X \sim \{-1, 1\}^p$$

$$\mathbb{P}(X, \tilde{X}) = \frac{1}{Z} \exp\left(\sum_{i \sim j} X_i X_j\right) \frac{1}{Z'(X)} \exp\left(\sum_{i \sim j} \tilde{X}_i \tilde{X}_j + X_i \tilde{X}_j + \tilde{X}_i X_j\right)$$

Z' is a function of X!

## Solved cases

**Old Knockoff Factory**