



How to generate knots?

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not valid (no cross terms)

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$$\mathbb{P}(X, \tilde{X}) = \frac{1}{Z} \exp \left( \sum_{i \sim j} X_i X_j \right) \frac{1}{Z'(X)} \exp \left( \sum_{i \sim j} \tilde{X}_i \tilde{X}_j + X_i \tilde{X}_j + \tilde{X}_i X_j \right)$$