Project Report

Peiqi Wang July 20, 2019

Contents

1	Abstract			
2	The Two-Bucket Camera			
	2.1 Notations			
	2.2 Subsampling Mapping			
	2.3 Image Formation			
	2.4 Image Processing Pipeline			
3	Literature Review			
	3.1 Structured Light Coding			
	3.2 Image Priors			
	3.3 Constrained Convex Optimization			
	8.4 Evaluating the Proximal Operator			
4	Methods			
	1.1 A Linear Inverse Problem			
	4.2 Optimization			

1 Abstract

We aim to improve upon low level image processing pipeline for the coded two-bucket camera. Specifically, we aim to jointly upsample, demultiplex, and denoise two-bucket images to produce full resolution images under different illumination conditions for downstream reconstruction tasks.

2 The Two-Bucket Camera

2.1 Notations

The coded two-bucket (C2B) camera is a pixel-wise coded exposure camera that outputs two images in a single exposure.[1] Each pixel in the sensor has two photo-collecting site, i.e. the two *buckets*, as well as a 1-bit writable memory controlling which bucket is actively collecting light. It was shown previously that C2B camera is capable of one-shot 3D reconstruction by solving a simpler image demosaicing and illumination demultiplexing problem instead of a difficult 3D reconstruction problem. We summarize the following notations relevant to discussion

	Notation	Meaning
	F	number of video frames
	P	number of pixels
	S	number of sub-frames
	$_{ m h,w}$	dimension of image
$P \times F \times S$	\mathbf{C}	code tensor
$P \times 1 \times S$	$\widetilde{\mathbf{C}}$	1-frame code tensor that spatially multiplex F frame tensor \mathbf{C}
$F \times S$	${f C}^p$	activity of bucket 0 pixel p cross all frames and sub-frames
$F \times S$	$\overline{{f C}}^p$	activity of bucket 1 pixel p cross all frames and sub-frames
$1 \times S$	\mathbf{c}_f^p	active bucket of pixel p in the sub-frames of frame f
$1 \times L$	9	scene's illumination condition in sub-frame s of every frame
$P \times S$	$\mathbf{C}_f = [\mathbf{c}_1^p; \cdots; \mathbf{c}_F^p]$	activity of bucket activity of all pixels across all sub-frames of f
	$\mathbf{L} = [\mathbf{l}_1; \cdots; \mathbf{l}_S]$	time-varying illumination condition (same for all frames)
$2F \times S$	\mathbf{W}	optimal bucket multiplexing matrix
	\mathbf{t}^p	transport vector at pixel p
$F \times 1$	$\mathbf{i}^p, \hat{\mathbf{i}}^p$	measured two-bucket intensity at pixel p in F frames
$F \times 1$	r,\hat{r}	illumination ratios at pixel p in F frames
$F \times P$	$\mathbf{I} = [\mathbf{i}^1 \cdots \mathbf{i}^P], \hat{\mathbf{I}}$	two-bucket image sequence in F frames
$P \times 2F$	$oldsymbol{I} = [\mathbf{I}^T \; \hat{\mathbf{I}}^T]$	two-bucket image sequence
$P \times 2$	\mathbf{Y}	two-bucket illumination mosaic
$S \times 1$		pixel intensity under S illuminations at pixel p
	$\mathbf{X} = [oldsymbol{i}^1 \cdots oldsymbol{i}^P]^T$	pixel intensity under S illuminations
$2P \times 1$	$\mathbf{y} = vec\left(\mathbf{Y}\right)$	vectorized two-bucket illumination mosaic
$SP \times 1$	$\mathbf{x} = vec\left(\mathbf{X}\right)$	vectorized pixel intensity under S illumiantions
$2P\times 2PF$	В	subsampling linear map
$2P \times SP$	$\mathbf{A} = \mathbf{B}(\mathbf{W} \otimes \mathbf{I}_P)$	illumination multiplexing and subsampling linear map

Illumination ratios are albedo quasi-invariant, a property which can be exploited for downstream processing

$$r = \frac{\mathbf{i}^p[f]}{\mathbf{i}^p[f] + \hat{\mathbf{i}}^p[f]} \qquad \hat{r} = \frac{\hat{\mathbf{i}}^p[f]}{\mathbf{i}^p[f] + \hat{\mathbf{i}}^p[f]}$$

2.2 Subsampling Mapping

Let $\mathbf{S} \in \{1, 2, \dots, F\}^P$ be a vector specifying how the one-frame code tensor $\widetilde{\mathbf{C}}$ is constructed, i.e.

$$\tilde{\mathbf{c}}_1^p := \mathbf{c}_{\mathbf{S}_n}^p$$

for all pixels p. We can view \mathbf{S} as a mask to construct a Subsampling linear map that maps vectorized two-bucket image sequences \mathbf{I} to the vectorized illumination mosaics \mathbf{Y} . In particular, let $\mathbf{B}' \in \mathbb{R}^{P \times PF}$ and $\mathbf{B} \in \mathbb{R}^{2P \times 2PF}$ be defined as follows

$$\begin{split} \mathbf{B}' &= \begin{bmatrix} \mathbf{diag} \mathbb{1}_{\{1\}}(\mathbf{S}) & \mathbf{diag} \mathbb{1}_{\{2\}}(\mathbf{S}) & \cdots & \mathbf{diag} \mathbb{1}_{\{F\}}(\mathbf{S}) \end{bmatrix} \\ \mathbf{B} &= \mathbf{I}_2 \otimes \mathbf{B}' = \begin{bmatrix} \mathbf{B}' & \mathbf{0} \\ \mathbf{0} & \mathbf{B}' \end{bmatrix} \end{split}$$

Then we have the following relation between I and Y,

$$vec(\mathbf{Y}) = \mathbf{B}vec(\mathbf{I})$$
 (1)

We are motivated to think of an analogue where it is common place to perform spatial subsampling. In RGB color imaging, bayer mosaics trade spatial resolution for spectral resolution (R,G,B colors). We can find an analogous one-frame code tensor which generate illuination mosaics that trade spatial resolution for temporal resolution $(1, 2, \dots, F \text{ frames})$. As an example in case of F = 3 and P = 4, the corresponding \mathbf{S} , when reshaped to dimension of a 2×2 image, and single image subsampling linear map \mathbf{B}' are simply

$$\mathbf{S} = \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix}$$

2.3 Image Formation

Per-pixel image formation model is

$$egin{bmatrix} egin{bmatrix} \mathbf{i}^p \ \hat{\mathbf{i}}^p \end{bmatrix} = egin{bmatrix} \mathbf{C}^p \ \mathbf{C}^p \end{bmatrix} egin{bmatrix} \mathbf{l}_1 \mathbf{t}^p \ \vdots \ \mathbf{l}_S \mathbf{t}^p \end{bmatrix} = egin{bmatrix} \mathbf{C}^p \ \mathbf{C}^p \end{bmatrix} m{i}^p$$

If bucket activity is same for all pixels and we use the optimal bucket multiplexing matrix W, then

$$I = XW^T$$
 (2)

2.4 Image Processing Pipeline

The reconstruction pipeline is as follows

- 1. Use $\widetilde{\mathbf{C}}$ for bucket activities and capture the two-bucket image \mathbf{Y}
- 2. upsample the images to full resolution images I
- 3. demultiplex I to obtain S full resolution images X as a least squares solution to a (2)
- 4. use X to solve for disparity and albedo

Step 2 and 3 are critical to downstream reconstructions. When S = 3, S = 4 and **S** being analogous to bayer mask, we can upsample the images using standard demosaicing algorithms. However, it is not immediately obvious to extend demosaicing methods to support arbitrary **S**, or more specifically, for scenarios where the spatial subsampling scheme is not bayer and when number of frames is not 3.

3 Literature Review

3.1 Structured Light Coding

The study of optimal structured light coding started with [2]. The authors draw inspirations from communication theory, where the projector projects unique temporal codes, received at each image plane through a noisy channel and subsequently decoded. Let there be K patterns and L code words, we want to encode $x \in [1:L]$, the indices of vertical light planes, using some encoding sceheme $f:[1:L] \to \mathbb{R}^K$ such that nearest neighbor decoding $\hat{x} = \arg\min_{x \in [1:L]} f(x) - y$ of a noisy observation $y \in \mathbb{R}^K$ minimizes the probability of depth estimation error.

minimize_f
$$\mathbb{E}_{x,y}\left[(x-\hat{x})^2\right]$$

3.2 Image Priors

The choice of regularization has been an important research topic in image processing. Handcrafted priors have been successful in a number of different image recovery tasks. For example, we can choose to enforce task-specific priors: (1) the sparsity of \mathbf{x} with ℓ -1 norm in image deblurring [3] (2) total variation in image denoising [4] (3) cross-channel correlation in color image demosaicing [5] (4) dark channel prior in image dehazing [6], etc. More exhotically, randomly initialized neural network can inject inductive bias to the optimization and act as image priors. [7]

In addition to hand-crafted priors, there has been interest in algorithm induced priors. Alternating direction method of multipliers (ADMM) is a common convex optimization method for inverse problem where the objective function is separable with respect to the *data term* and the *regularizer*. Each primal update involves an evaluation of a proximal operator, which can be interpreted as performing denoising on some iterate. [8, 9, 10] proposed plug-and-play priors where the choice of regularization is implicitly specified by the denoiser used. [11] proposed an explicit laplacian-based expression for the regularizer and generalizes the method to a number of different iterative optimization algorithms.

The convergence of plug-and-play ADMM is studied by a number of papers. [12] showed fixed point convergence of plug-and-play ADMM. [11] showed convergence of the algorithm under some mild conditions of the denoiser, which are satisfied by some state of the art denoisers like *Block-matching and 3D filtering*

(BM3D) [13] and Trainable Nonlienar Reaction Diffusion (TNRD) [14]. Most recently, [15] established convergence given that the denoising network satisfy certain Lipschitz condition.

Some proposed to learn proximal operator from data. [16] used a CNN denoiser [17]. Instead of substituting the proximal operator with a denoiser, [18] learns a projection mapping to the space of natural images by training a single neural network and showed impressive results on a number of different linear inverse problems.

3.3 Constrained Convex Optimization

Alternating Method of Multipliers (ADMM) is an efficient convex optimization algorithm for minimizing the sum of nonsmooth convex separable functions subject to a set of linear equality constraints. It combines the advantage of dual decomposition, where we can solve subproblems at each iteration, and that of method of multipliers, where optimization over augmented lagrangian relaxes strict convexity condition for the objective. [19] Specifically, we are interested in solving the following constrained convex optimization problem

$$\begin{array}{ll}
\underset{\mathbf{x}_{1}, \cdots, \mathbf{x}_{N}}{\text{minimize}} & \sum_{i=1}^{N} f_{i}(\mathbf{x}_{i}) \\
\text{subject to} & (\mathbf{x}_{1}, \cdots, \mathbf{x}_{N}) \in \mathcal{C}
\end{array} \tag{3}$$

where $\mathbf{x}_i \in \mathbb{R}^{n_i}$, $f_i : \mathbb{R}^n \to (-\infty, \infty)$ are closed proper convex functions for $i = 1, \dots, N$, and \mathcal{C} is an affine set of the form

$$\mathcal{C} = \{ \mathbf{x} \in \mathbb{R}^{\sum_i n_i} \mid A\mathbf{x} = \mathbf{b} \}$$

which has an equivalent ADMM form [19],

minimize
$$f(\mathbf{x}) + I_{\mathcal{C}}(\mathbf{z})$$

subject to $\mathbf{x} - \mathbf{z} = 0$ (4)

where $f(\mathbf{x}) = \sum_{i=1}^{N} f_i(\mathbf{x}_i)$. The scaled form of ADMM for (4) is

$$\mathbf{x}_{i}^{k+1} = \underset{\mathbf{x}_{i}}{\operatorname{arg min}} \left(f_{i}(\mathbf{x}_{i}) + \frac{\rho}{2} \left\| \mathbf{x}_{i} - (\mathbf{z}_{i}^{k} - \mathbf{u}_{i}^{k}) \right\|_{2}^{2} \right) = \mathbf{prox}_{(1/\rho)f_{i}}(\mathbf{z}_{i}^{k} - \mathbf{u}_{i}^{k})$$

$$\mathbf{z}^{k+1} = \underset{\mathbf{z}}{\operatorname{arg min}} \left(\mathbf{I}_{\mathcal{C}}(\mathbf{z}) + \frac{\rho}{2} \left\| \mathbf{z} - (\mathbf{x}^{k+1} + \mathbf{u}^{k}) \right\|_{2}^{2} \right) = \mathbf{prox}_{(1/\rho)\mathbf{I}_{\mathcal{C}}}(\mathbf{x}^{k+1} + \mathbf{u}^{k})$$

$$\mathbf{u}^{k+1} = \mathbf{u}^{k} + \mathbf{x}^{k+1} - \mathbf{z}^{k+1}$$

 \mathbf{u}^k is the scaled dual variable. $\rho > 0$ is the augmented lagrangian parameter. $\mathbf{prox}_{\lambda f} : \mathbb{R}^n \to \mathbb{R}^n$ is the proximal operator of λf , $\lambda > 0$,

$$\mathbf{prox}_{\lambda f}(\mathbf{v}) = \operatorname*{arg\ min}_{\mathbf{x}} \left(f(\mathbf{x}) + \frac{1}{2\lambda} \|\mathbf{x} - \mathbf{v}\|_{2}^{2} \right)$$

3.4 Evaluating the Proximal Operator

Evaluating the proximal operator involves solving a convex optimization problem. We will show how we can compute the proximal operators relevant to our methods. (See section 6 of [20])

1. The proximal operator of an indicator function onto a convex set \mathcal{C} is simply the projection onto \mathcal{C} .

$$\mathbf{prox}_{(1/\rho)I_{\mathcal{C}}}(\mathbf{x}^{k+1} + \mathbf{u}^k) = \prod_{\mathcal{C}}(\mathbf{x}^{k+1} + \mathbf{u}^k)$$

When C is affine, there is an analytic expression for the projection

$$\prod_{\mathcal{C}}(\mathbf{v}) = \mathbf{v} - A^{\dagger}(A\mathbf{v} - \mathbf{b})
= \mathbf{v} - A^{T}(A^{T}A)^{-1}(A\mathbf{v} - \mathbf{b})$$
 (if $A \in \mathbb{R}^{m \times n}$ has $m < n$ and full rank)

2. Let f be ℓ -2 norm of an affine function,

$$f(x) = ||A\mathbf{x} - \mathbf{y}||_2^2 = \mathbf{x}^T A^T A \mathbf{x} - 2\mathbf{y}^T A \mathbf{x} + \mathbf{y}^T \mathbf{y}$$

Then proximal operator of $(1/\rho)f$ has a closed form expression

$$\mathbf{prox}_{(1/\rho)f}(\mathbf{v}) = \mathbf{prox}_{(2/\rho)(1/2)f} = (I + \frac{2}{\rho}A^TA)^{-1}(\mathbf{v} + \frac{2}{\rho}A^T\mathbf{y})$$

which can be solved efficiently with conjugate gradient, as $(I + \frac{2}{\rho}A^TA) > 0$. If ρ is fixed throughout, we can use Cholesky factorization to factor $(I + (2/\rho)A^TA)$ in $\mathcal{O}(n^3)$. Any subsequent computation of the inverse would only cost $\mathcal{O}(mn)$.

3. Let $f(\mathbf{x}) = ||\mathbf{x}||_1$, then the proximal operator of $(\lambda/\rho)f$ is

$$\mathbf{prox}_{(\lambda/\rho)f}(\mathbf{v}) = \mathcal{S}_{\lambda/\rho}(\mathbf{v})$$

where S is element-wise soft shrinkage operator

$$(S_{\kappa}(\mathbf{v}))_i = (1 - \kappa/|\mathbf{v}_i|)_+ \mathbf{v}_i \qquad \mathbf{x}_+ = \max(\mathbf{x}, 0)$$

4. Let $f(\mathbf{x}) = (1/2)\mathbf{x}^T(\mathbf{x} - \mathcal{D}(\mathbf{x}))$ for some denoiser \mathcal{D} , the explicit regularizer in RED.[11]. We use one fixed point iteration evaluate the approximate proximal operator for λf . Specifically, we want to evaluate

$$\mathbf{prox}_{(\lambda/\rho)f}(\mathbf{v}) = \arg\min_{\mathbf{x}} \frac{\lambda}{2} \mathbf{x}^{T} (\mathbf{x} - \mathcal{D}(\mathbf{x})) + \frac{\rho}{2} \|\mathbf{x} - \mathbf{v}\|_{2}^{2}$$

Setting the gradient to zero, we arrive at the fixed point iteration

$$\mathbf{x}^{(k)} \leftarrow \frac{1}{\rho + \lambda} (\lambda \mathcal{D}(\mathbf{x}^{(k-1)}) + \rho \mathbf{v})$$

If we only iterate once, then

$$\mathbf{prox}_{(\lambda/\rho)f}(\mathbf{v}) = \frac{1}{\rho + \lambda} (\lambda \mathcal{D}(\mathbf{x}^{(0)}) + \rho \mathbf{v})$$

for some initialization value $\mathbf{x}^{(0)}$

4 Methods

4.1 A Linear Inverse Problem

We consider the problem of recovering full resolution images **X** under S illuminations from a two-bucket image **Y** as an linear inverse problem. Let $\mathbf{A} \in \mathbb{R}^{2P \times SP}$ represent a linear map that illumination multiplexes and subsamples **X**,

$$\mathbf{A} = \mathbf{B}(\mathbf{W} \otimes \mathbf{I}_P)$$

where $\mathbf{I}_P \in \mathbb{R}^{P \times P}$ is identity. From (1) and (2), there exists a linear relationship between \mathbf{x} and \mathbf{y} ,

$$\mathbf{y} = \mathbf{B}vec\left(\mathbf{I}\right) = \mathbf{B}vec\left(\mathbf{X}\mathbf{W}^{T}\right) = \mathbf{B}(\mathbf{W} \otimes \mathbf{I}_{P})vec\left(\mathbf{X}\right) = \mathbf{A}\mathbf{x}$$
 (5)

Note (5) is an underdetermined system. Given 2 images, we want to recover S images - the larger the number of subframes, the harder the recovery becomes. This asks for stronger prior knowledge of the underlying distribution of \mathbf{x} to restrict search space for solutions as S increases. Jointly upsample and demultiplex enforces a prior knowledge of image formation. Instead of treating upsampling (recover 2F images \mathbf{I} from 2 images \mathbf{Y}) and demultiplexing (recover S images \mathbf{X} from 2F images \mathbf{I}) as distinct steps, we aim to recover \mathbf{X} directy from \mathbf{Y} , in a single step, by solving the following unconstrained optimization problem,

minimize
$$\|\mathbf{A}\mathbf{x} - \mathbf{y}\|_2^2 + \lambda \rho(\mathbf{x})$$
 (6)

where $\rho: \mathbb{R}^{SP} \to \mathbb{R}$ are regularizers for \mathbf{x} , the optimization variable. The problem (6) has a bayesian interpretation. Specifically, the ℓ -2 norm can be interpreted as a log-likelihood *data term* that captures the following probablistic relationship between recovered image \mathbf{x} and observation \mathbf{y} ,

$$y = Ax + e$$

where **e** is the noise random variable, usually assumed to be Gaussian. The regularizer can be then interpreted as *prior* knowledge on the distribution of **x**. The data term is continuous and fully differentiable in all of \mathbb{R}^n . Therefore, tractability of (6) usually depends on how well behaved ρ is. If ρ is convex but possibly non-smooth, e.g. $\rho(\mathbf{x}) = ||\mathbf{x}||_1$, the problem can be efficiently solved with standard convex optimization methods like proximal gradients with guaranteed convergence and global optimality.[3] More realistic priors, i.e. regularizers that more precisely capture the prior knowledge of image distributions, might potentially make (6) a much harder problem that compromises convergence and optimality properties.[7]

We first note that the illumination ratios are albedo quasi-invariant, and therefore smooth within object boundaries. Therefore, total variation regularization on illuination ratio images could be particularly effective. To avoid extra notations, we use \mathbf{x}, \mathbf{y} as the corresponding illumination ratios that we want to reconstruct. Additionally, we adapt algorithm in [11] for imposing algorithm induced priors with state-of-the-art denoisers. In summary, we want to optimize the following constrained problem with a set of affine constraints,

minimize
$$\|\mathbf{A}\mathbf{x}_1 - \mathbf{y}\|_2^2 + \frac{\lambda_2}{2}\mathbf{x}_2^T(\mathbf{x}_2 - \mathcal{D}(\mathbf{x}_2)) + \lambda_3 \|\mathbf{x}_3\|_1$$

subject to $\mathbf{x}_1 - \mathbf{x}_2 = 0$
 $\mathbf{G}\mathbf{x}_1 - \mathbf{x}_3 = 0$

where $\mathbf{x}_1, \mathbf{x}_2 \in \mathbb{R}^{SP}$, $\mathbf{x}_3 \in \mathbb{R}^{2SP}$. $\lambda_2, \lambda_3 > 0$ are weights to the regularizers. $\mathbf{G} \in \mathbb{R}^{2SP \times SP}$ is the discrete image gradient for S images

$$\mathbf{G} = egin{bmatrix} \mathbf{I}_S \otimes \mathbf{G}_x \ \mathbf{I}_S \otimes \mathbf{G}_y \end{bmatrix}$$

where $\mathbf{G}_x, \mathbf{G}_y \in \mathbb{R}^{P \times P}$ are the discrete image gradients for a single image computed using forward difference. We can gather constraints into a single linear system

$$\mathbf{H}\mathbf{x} = 0 \quad \text{where} \quad \mathbf{H} = \begin{bmatrix} \mathbf{I}_{SP} & -\mathbf{I}_{SP} & 0 \\ \mathbf{G} & 0 & -\mathbf{I}_{SP} \end{bmatrix} \quad \mathbf{x} = \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \\ \mathbf{x}_3 \end{bmatrix}$$

and arrive at an equivalent optimization problem

minimize
$$f_1(\mathbf{x}_1) + \lambda_2 f_2(\mathbf{x}_2) + \lambda_3 f_3(\mathbf{x}_3)$$

subject to $(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) \in \mathcal{C}$ (7)

where $C = \{ \mathbf{x} \in \mathbb{R}^{4SP} \mid \mathbf{H}\mathbf{x} = 0 \}$ and

$$f_1(\mathbf{x}_1) = \|\mathbf{A}\mathbf{x}_1 - \mathbf{y}\|_2^2$$

$$f_2(\mathbf{x}_2) = \frac{1}{2}\mathbf{x}_2^T(\mathbf{x}_2 - \mathcal{D}(\mathbf{x}_2))$$

$$f_3(\mathbf{x}_3) = \|\mathbf{x}_3\|_1$$

4.2 Optimization

As shown previously, the scaled form ADMM for solving (7) is given by

$$\begin{split} \mathbf{x}_{1}^{k+1} &= \mathbf{prox}_{(1/\rho)f_{1}}(\mathbf{z}_{1}^{k} - \mathbf{u}_{1}^{k}) = (I + \frac{2}{\rho}A^{T}A)^{-1}(\mathbf{z}_{1}^{k} - \mathbf{u}_{1}^{k} + \frac{2}{\rho}A^{T}y) \\ \mathbf{x}_{2}^{k+1} &= \mathbf{prox}_{(\lambda_{2}/\rho)f_{2}}(\mathbf{z}_{2}^{k} - \mathbf{u}_{2}^{k}) = \frac{1}{\lambda_{2} + \rho}(\lambda_{2}\mathcal{D}(\mathbf{x}_{2}^{k}) + \rho(\mathbf{z}_{2}^{k} - \mathbf{u}_{2}^{k})) \\ \mathbf{x}_{3}^{k+1} &= \mathbf{prox}_{(\lambda_{3}/\rho)f_{3}}(\mathbf{z}_{3}^{k} - \mathbf{u}_{3}^{k}) = \mathcal{S}_{\lambda_{3}/\rho}(\mathbf{z}_{3}^{k} - \mathbf{u}_{3}^{k}) \\ \mathbf{z}^{k+1} &= \mathbf{prox}_{(1/\rho)I_{C}}(\mathbf{x}^{k+1} + \mathbf{u}^{k}) = (I - \mathbf{H}^{\dagger}\mathbf{H})(\mathbf{x}^{k+1} + \mathbf{u}^{k}) \\ \mathbf{u}^{k+1} &= \mathbf{u}^{k} + \mathbf{x}^{k+1} - \mathbf{z}^{k+1} \end{split}$$

References

- [1] Mian Wei et al. "Coded Two-Bucket Cameras for Computer Vision". en. In: Computer Vision ECCV 2018. Ed. by Vittorio Ferrari et al. Vol. 11207. Cham: Springer International Publishing, 2018, pp. 55–73. ISBN: 978-3-030-01218-2 978-3-030-01219-9. DOI: 10.1007/978-3-030-01219-9_4.
- [2] E. Horn and N. Kiryati. "Toward optimal structured light patterns". In: *Proceedings. International Conference on Recent Advances in 3-D Digital Imaging and Modeling (Cat. No.97TB100134)*. Proceedings. International Conference on Recent Advances in 3-D Digital Imaging and Modeling (Cat. No.97TB100134). ISSN: null. May 1997, pp. 28–35. DOI: 10.1109/IM.1997.603845.
- [3] A. Beck and M. Teboulle. "A Fast Iterative Shrinkage-Thresholding Algorithm with Application to Wavelet-Based Image Deblurring". In: 2009 IEEE International Conference on Acoustics, Speech and Signal Processing. Apr. 2009, pp. 693–696. DOI: 10.1109/ICASSP.2009.4959678.
- [4] Antoni Buades, Bartomeu Coll, and Jean-Michel Morel. "Nonlocal Image and Movie Denoising". en. In: International Journal of Computer Vision 76.2 (Feb. 2008), pp. 123–139. ISSN: 1573-1405. DOI: 10.1007/s11263-007-0052-1.
- [5] H. S. Malvar, Li-wei He, and R. Cutler. "High-Quality Linear Interpolation for Demosaicing of Bayer-Patterned Color Images". In: 2004 IEEE International Conference on Acoustics, Speech, and Signal Processing. Vol. 3. May 2004, pp. iii-485. DOI: 10.1109/ICASSP.2004.1326587.
- [6] Raanan Fattal. "Single Image Dehazing". In: ACM SIGGRAPH 2008 Papers. SIGGRAPH '08. New York, NY, USA: ACM, 2008, 72:1–72:9. ISBN: 978-1-4503-0112-1. DOI: 10.1145/1399504.1360671.
- [7] Dmitry Ulyanov, Andrea Vedaldi, and Victor Lempitsky. "Deep Image Prior". In: arXiv:1711.10925 [cs, stat] (Nov. 2017). arXiv: 1711.10925 [cs, stat].
- [8] S. V. Venkatakrishnan, C. A. Bouman, and B. Wohlberg. "Plug-and-Play Priors for Model Based Reconstruction". In: 2013 IEEE Global Conference on Signal and Information Processing. Dec. 2013, pp. 945–948. DOI: 10.1109/GlobalSIP.2013.6737048.
- [9] Felix Heide et al. "FlexISP: A Flexible Camera Image Processing Framework". In: *ACM Trans. Graph.* 33.6 (Nov. 2014), 231:1–231:13. ISSN: 0730-0301. DOI: 10.1145/2661229.2661260.
- [10] Stanley H. Chan. "Algorithm-Induced Prior for Image Restoration". In: ArXiv abs/1602.00715 (2016). arXiv: 1602.00715.
- [11] Yaniv Romano, Michael Elad, and Peyman Milanfar. "The Little Engine That Could: Regularization by Denoising (RED)". In: arXiv:1611.02862 [cs] (Nov. 2016). arXiv: 1611.02862 [cs].
- [12] Stanley H. Chan, Xiran Wang, and Omar A. Elgendy. "Plug-and-Play ADMM for Image Restoration: Fixed Point Convergence and Applications". In: arXiv:1605.01710 [cs] (May 2016). arXiv: 1605.01710 [cs].
- [13] K. Dabov et al. "Image Denoising by Sparse 3-D Transform-Domain Collaborative Filtering". In: *IEEE Transactions on Image Processing* 16.8 (Aug. 2007), pp. 2080–2095. ISSN: 1057-7149. DOI: 10.1109/TIP.2007.901238.
- [14] Yunjin Chen and Thomas Pock. "Trainable Nonlinear Reaction Diffusion: A Flexible Framework for Fast and Effective Image Restoration". In: *IEEE Transactions on Pattern Analysis and Machine Intelligence* 39.6 (June 2017), pp. 1256–1272. ISSN: 0162-8828, 2160-9292. DOI: 10.1109/TPAMI. 2016.2596743. arXiv: 1508.02848.
- [15] Ernest Ryu et al. "Plug-and-Play Methods Provably Converge with Properly Trained Denoisers". en. In: *International Conference on Machine Learning*. May 2019, pp. 5546–5557.

- [16] Tim Meinhardt et al. "Learning Proximal Operators: Using Denoising Networks for Regularizing Inverse Imaging Problems". In: arXiv:1704.03488 [cs] (Apr. 2017). arXiv: 1704.03488 [cs].
- [17] K. Zhang et al. "Beyond a Gaussian Denoiser: Residual Learning of Deep CNN for Image Denoising". In: IEEE Transactions on Image Processing 26.7 (July 2017), pp. 3142–3155. ISSN: 1057-7149. DOI: 10.1109/TIP.2017.2662206.
- [18] J. H. Rick Chang et al. "One Network to Solve Them All Solving Linear Inverse Problems Using Deep Projection Models". en. In: 2017 IEEE International Conference on Computer Vision (ICCV). Venice: IEEE, Oct. 2017, pp. 5889–5898. ISBN: 978-1-5386-1032-9. DOI: 10.1109/ICCV.2017.627.
- [19] Stephen Boyd et al. "Distributed Optimization and Statistical Learning via the Alternating Direction Method of Multipliers". In: Found. Trends Mach. Learn. 3.1 (Jan. 2011), pp. 1–122. ISSN: 1935-8237. DOI: 10.1561/2200000016.
- [20] Neal Parikh and Stephen Boyd. "Proximal Algorithms". In: Found. Trends Optim. 1.3 (Jan. 2014), pp. 127–239. ISSN: 2167-3888. DOI: 10.1561/2400000003.