

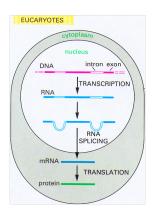


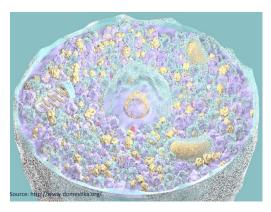
Statistical Methods for Quantitative MS-Based Proteomics:

1. Identification & False discovery rate

Lieven Clement

Proteomics Data Analysis Shortcourse

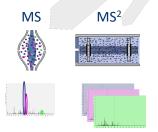






Challenges in Label Free MS-based Quantitative Proteomics



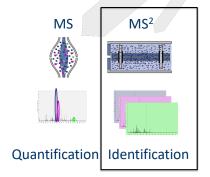


Quantification Identification



Challenges in Label Free MS-based Quantitative Proteomics







Identification

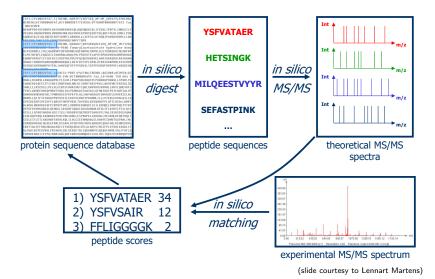
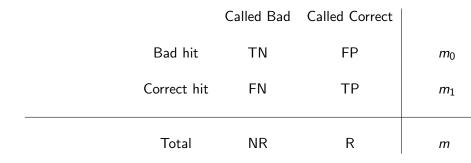


Table of Outcomes



- TN: number of true negatives
- FP: number of false positives
- FN: number of false negatives
- TP: number of true positives
- NR: number of non-rejections, R: number of rejections



Table of Outcomes

		Called Bad	Called Correct	
Unobservable	Bad hit	TN	FP	m_0
	Correct hit	FN	TP	m_1
Observable	Total	NR	R	m

 $FDP = \frac{FP}{FP+TP}$. But is unknown! (FDP: false discovery proportion)

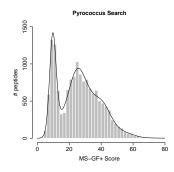


Table of Outcomes

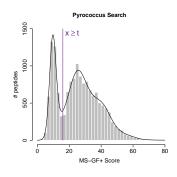
		Called Bad	Called Correct	
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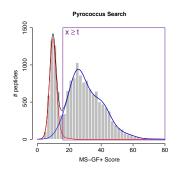
$$FDR = E \left[\frac{FP}{FP+TP} \right]$$
. (FDR: false discovery rate)





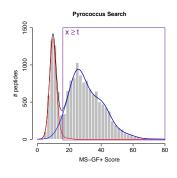






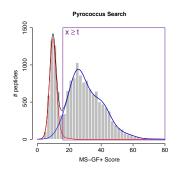
$$f(x) = \pi_0 f_0(x) + (1 - \pi_0) f_1(x)$$





$$f(x) = \pi_0 f_0(x) + (1 - \pi_0) f_1(x)$$

$$FDR(t) = E\left[\frac{FP}{FP+TP}\right]$$

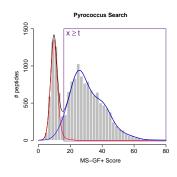


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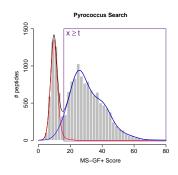
$$FDR(t) = \frac{mP[FP]P[x \ge t|FP]}{mP[x > t]}$$





Score threshold t? $f(x) = \pi_0 f_0(x) + (1 - \pi_0) f_1(x)$ $FDR(t) = E\left[\frac{FP}{FP + TP}\right]$ $FDR(t) = \frac{mP[FP]P[x \ge t|FP]}{mP[x > t]}$

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$$f(x) = \pi_0 f_0(x) + (1 - \pi_0) f_1(x)$$

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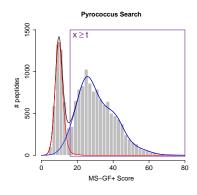
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$$P_{\cdot}[x \ge t] = \int_{t}^{\infty} f_{\cdot}(x) dx$$



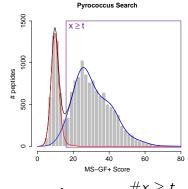
How to estimate FDR?



$$FDR(t) = E\left[\frac{FP}{FP+TP}\right]$$
$$= \frac{\pi_0 P_0[x \ge t]}{P[x \ge t]}$$

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How to estimate FDR?



$$\hat{P}[x \ge t] = \frac{\#x \ge t}{m} \implies$$

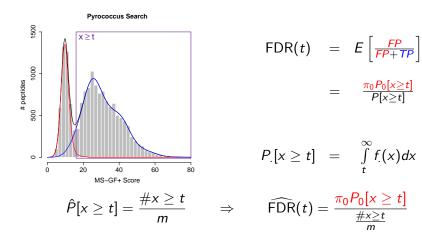
$$FDR(t) = E\left[\frac{FP}{FP+TP}\right]$$
$$= \frac{\pi_0 P_0[x \ge t]}{P[x \ge t]}$$

$$P_{\cdot}[x \geq t] = \int_{t}^{\infty} f_{\cdot}(x) dx$$

$$\widehat{\mathsf{FDR}}(t) = \frac{\pi_0 P_0[x \ge t]}{\frac{\#x \ge t}{m}}$$

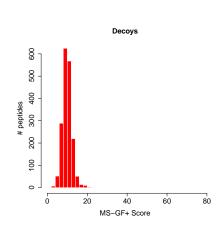


How to estimate FDR?

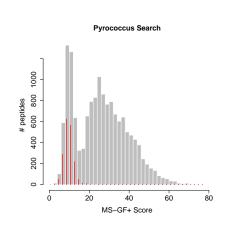


How to characterize $f_0(t)$ and π_0 in proteomics?

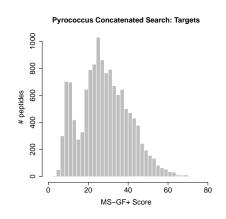




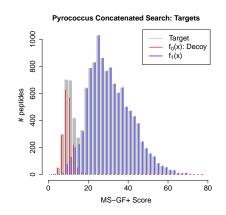
- Search against decoy database to generate representative bad hits
- Reversed databases are popular



- Search against decoy database to generate representative bad hits
- Reversed databases are popular
- Concatenated search



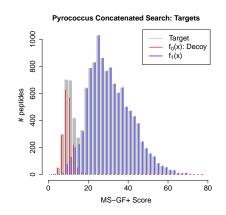
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- Assumption: bad hits has equal probability to map on target and decoy

$$\hat{\pi}_0 = rac{\# extit{decoys}}{\# extit{targets}}$$



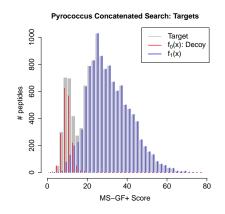


- Search against decoy database to generate representative bad hits
- Reversed databases are popular
- Concatenated search
- Assumption: bad hits has equal probability to map on target and decoy

$$\hat{\pi}_0 = \frac{\# decoys}{\# targets}$$

• Score cuttoff: $FDR(x) = E \left[\frac{FP}{FP+TP} \right]$

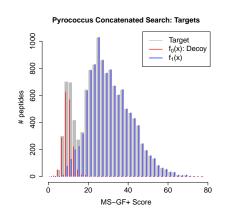




• Competitive Target - decoy:

$$\widehat{\mathsf{FDR}}(x) = \frac{\#\mathsf{decoys}|X \ge x}{\#\mathsf{targets}|X \ge x}$$





• Competitive Target - decoy:

$$\widehat{\mathsf{FDR}}(x) = \frac{\# decoys | X \ge x}{\# targets | X \ge x}$$

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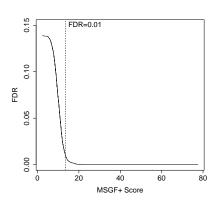
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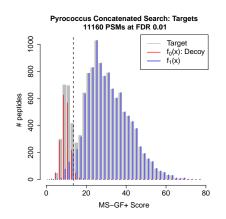


• Competitive Target - decoy:

$$\widehat{\mathsf{FDR}}(x) = \frac{\# decoys | X \ge x}{\# targets | X \ge x}$$

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$$\frac{\# decoys}{\# decoys}$$



Competitive Target - decoy:

$$\widehat{\mathsf{FDR}}(x) = \frac{\# decoys}{\# targets} \frac{X \ge x}{X \ge x}$$

$$\widehat{\mathsf{FDR}}(x) = \frac{\# decoys}{\# targets} \frac{\# decoys}{\# targets} \frac{X \ge x}{\# decoys}$$

$$\frac{\# decoys}{\# targets} \frac{\# decoys}{\# targets} \frac{X \ge x}{\# targets}$$

$$\widehat{\mathsf{FDR}}(x) = \hat{\pi}_0 \frac{\hat{P}_0[X \ge x]}{\hat{P}[X > x]}$$

Assess TDA assumptions

We have to evaluate that

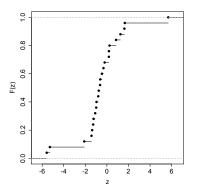
• The decoys are good simulations of the bad target hits: compare distributions $F_0(x)$ with F(x)

$$F_0(x) = \int_{-\infty}^t f_0(x) dx \quad \leftrightarrow \quad F(x) = \int_{-\infty}^t f(x) dx$$

- $\hat{\pi}_0 = \frac{\#decoys}{\#targets}$ is a good estimator for π_0 .
- We will use Probability-Probability-plots (PP-plot) for this purpose.

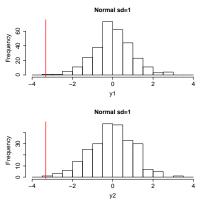


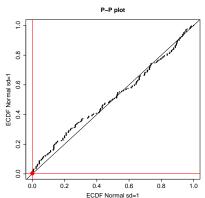
- To make PP-plots we need estimates for $F_0(x)$ and F(x).
- The empirical cumulative distribution (ECDF) is used for that purpose



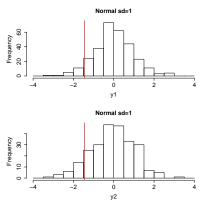
$$\hat{F}_0(x) = \frac{\#decoys|X \le x}{\#decoys}, \quad \hat{F}(x) = \frac{\#targets|X \le x}{\#targets}$$

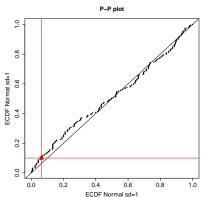




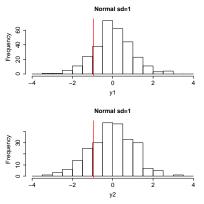


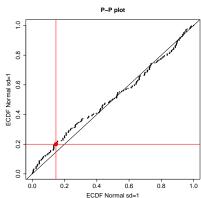




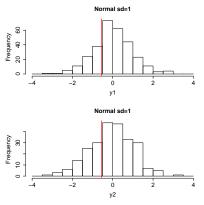


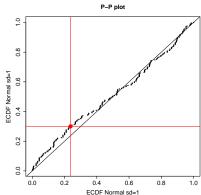




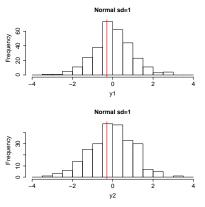


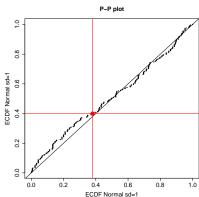


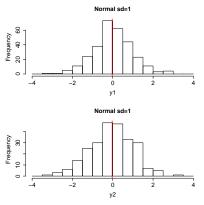


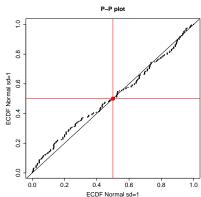


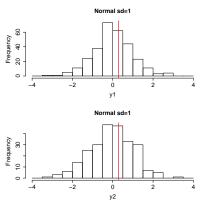


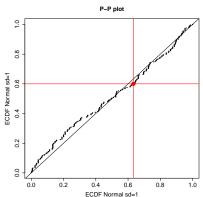


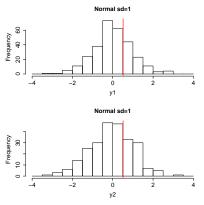


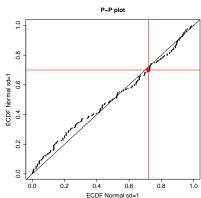


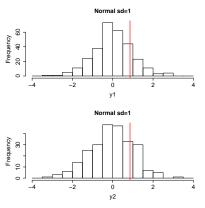


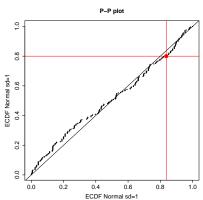


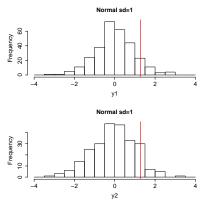


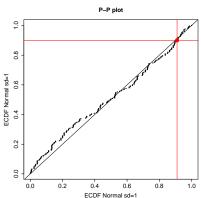


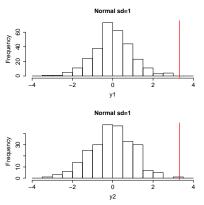


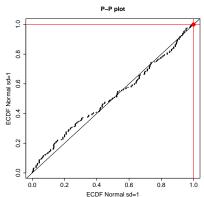


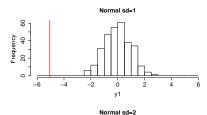


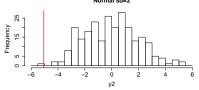


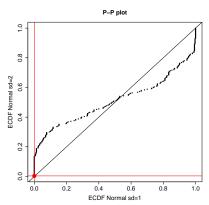




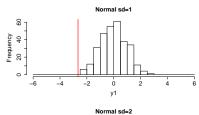


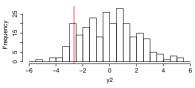


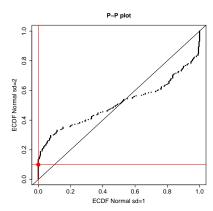




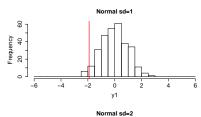


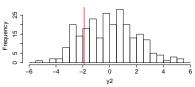


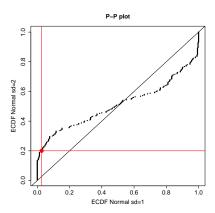




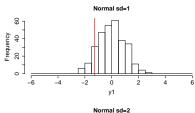


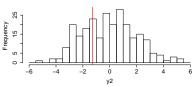


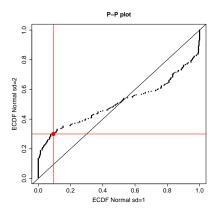




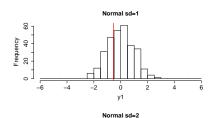


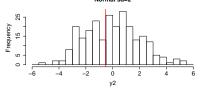


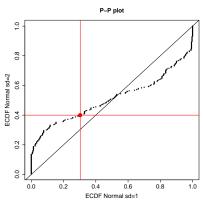




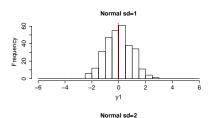


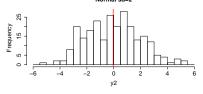


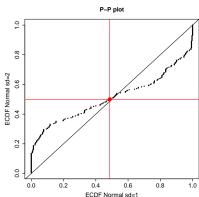




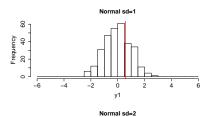


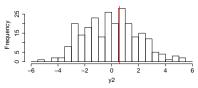


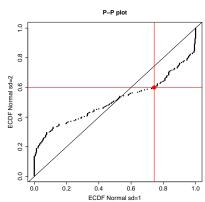




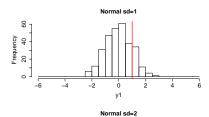


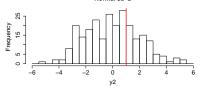


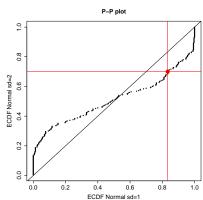




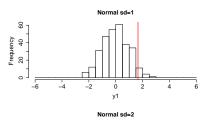


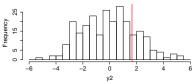


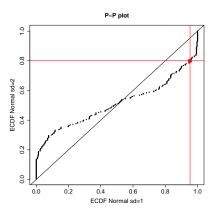




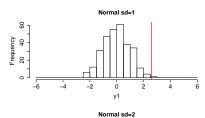


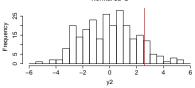


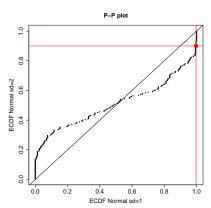




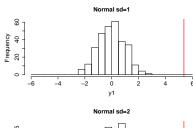


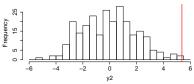


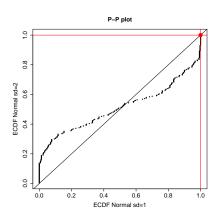




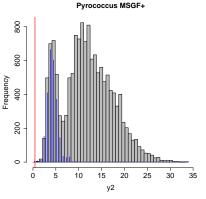


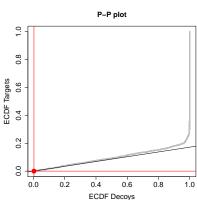




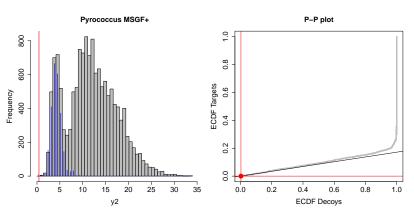












What about $\hat{\pi}_0$?



