# **Mechatronische Netzwerke**

# **Eigenschaften eines Transformators**

# Impedanztransformation (Kettenmatrix)

Transformator in Kettenform (A-Matrix)

$$\begin{bmatrix} Y_1 \\ I_{X1} \end{bmatrix} = \begin{bmatrix} A_{11} & 0 \\ 0 & A_{22} \end{bmatrix} \cdot \begin{bmatrix} Y_2 \\ I_{X2} \end{bmatrix}$$

reziproker Wandler (|A| = 1)

$$A_{22}\!=\!{A_{11}}^{-1}$$

Impedanztransformation (allgemein)

$$Z_1 = \frac{A_{11}}{A_{22}} \cdot Z_2$$

Widerstand R

$$Z_2 = R_2$$

$$Z_1 \!=\! \frac{A_{11}}{A_{22}} \!\cdot\! R_2 \!=\! R_1$$

Transformationsbeziehung (R)

$$R_1 = \frac{A_{11}}{A_{22}} \cdot R_2$$

Induktivität L

$$Z_2 = 1\mathrm{i} \boldsymbol{\cdot} \omega \boldsymbol{\cdot} L_2$$

$$Z_1 = \frac{A_{11}}{A_{22}} \cdot 1i \cdot \omega \cdot L_2 = 1i \cdot \omega \cdot L_1$$

Transformationsbeziehung (L)

$$L_1 = \frac{A_{11}}{A_{22}} \cdot L_2$$

Kapazität C

$$Z_2 = \frac{1}{1 \mathbf{i} \cdot \omega \cdot C_2}$$

$$Z_1 = \frac{A_{11}}{A_{22}} \cdot \frac{1}{1 \cdot \omega \cdot C_2} = \frac{1}{1 \cdot \omega \cdot C_1}$$

Transformationsbeziehung (C)

$$C_1 = \frac{A_{22}}{A_{11}} \cdot C_2$$

Reihenschaltung

$$Z_2 = Z_{21} + Z_{22}$$

$$Z_1 = \frac{A_{11}}{A_{22}} \cdot Z_2 = \frac{A_{11}}{A_{22}} \cdot Z_{21} + \frac{A_{11}}{A_{22}} \cdot Z_{22} = Z_{11} + Z_{22}$$

Transformationsbeziehung (Z)

$$Z_{11} = \frac{A_{22}}{A_{11}} \cdot Z_{21}$$
  $Z_{12} = \frac{A_{22}}{A_{11}} \cdot Z_{22}$ 

## **Parallelschaltung**

$$\boldsymbol{Y}_2 = \boldsymbol{Y}_{21} + \boldsymbol{Y}_{22}$$

$$Z_1 = \frac{A_{11}}{A_{22}} \cdot \frac{1}{Y_2} = \frac{A_{11}}{A_{22}} \cdot \frac{1}{Y_{21} + Y_{22}}$$

$$\frac{1}{Y_1} = \frac{A_{11}}{A_{22}} \cdot \frac{1}{Y_{21} + Y_{22}} = \frac{1}{Y_{11} + Y_{12}}$$

$$\frac{A_{22} \cdot Y_{21} + A_{22} \cdot Y_{22}}{A_{11}} = Y_{11} + Y_{12}$$

Transformationsbeziehung (Z)

$$Z_{11} = \frac{A_{11}}{A_{22}} \cdot Z_{21}$$
  $Z_{12} = \frac{A_{11}}{A_{22}} \cdot Z_{22}$ 

# aktive Bauelemente

$$\begin{bmatrix} Y_1 \\ I_{X1} \end{bmatrix} = \begin{bmatrix} A_{11} & 0 \\ 0 & A_{22} \end{bmatrix} \cdot \begin{bmatrix} Y_2 \\ -I_{X2} \end{bmatrix}$$

Transformationsbeziehungen

$$\boldsymbol{Y}_1 \!=\! \boldsymbol{A}_{11} \! \cdot \! \boldsymbol{Y}_2$$

$$I_{X1} = -A_{22} \cdot I_{X2}$$

## Impedanztransformation (Hybridmatrix)

Transformator in Hybridform (H-Matrix)

$$\begin{bmatrix} Y_1 \\ I_{X2} \end{bmatrix} = \begin{bmatrix} 0 & H_{12} \\ H_{21} & 0 \end{bmatrix} \cdot \begin{bmatrix} I_{X1} \\ Y_2 \end{bmatrix}$$

reziproker Wandler

$$H_{12}$$
 =  $-H_{21}$ 

Impedanztransformation (allgemein)

$$Z_1 = -H_{12} \boldsymbol{\cdot} H_{21} \boldsymbol{\cdot} Z_2$$

### **Widerstand R**

$$Z_2 = R_2$$

Transformationsbeziehung (R)

$$R_1 = -H_{12} \cdot H_{21} \cdot R_2$$

## Induktivität L

$$Z_2 = 1\mathbf{i} \cdot \omega \cdot L_2$$

Transformationsbeziehung (L)

$$L_1 = -H_{12} \boldsymbol{\cdot} H_{21} \boldsymbol{\cdot} L_2$$

# Kapazität C

$$Z_2 = \frac{1}{1 \mathbf{i} \cdot \boldsymbol{\omega} \cdot \boldsymbol{C}_2}$$

Transformationsbeziehung (C)

$$C_1\!=\!\frac{-1}{H_{12}\!\cdot\!H_{21}}\!\cdot\!C_2$$

# Reihenschaltung

$$Z_2 = Z_{21} + Z_{22}$$

Transformationsbeziehung (Z)

$$Z_{11} = \frac{-1}{H_{12} \cdot H_{21}} \cdot Z_{21}$$

$$Z_{12}\!=\!\frac{-1}{H_{12}\!\cdot\! H_{21}}\!\cdot\! Z_{22}$$



# **Parallelschaltung**

$$\boldsymbol{Y}_2 = \boldsymbol{Y}_{21} + \boldsymbol{Y}_{22}$$

Transformationsbeziehung (Z)

$$Z_{11} = -H_{12} \boldsymbol{\cdot} H_{21} \boldsymbol{\cdot} Z_{21}$$

$$Z_{12} = -H_{12} \cdot H_{21} \cdot Z_{22}$$

## aktive Bauelemente

$$\begin{bmatrix} Y_1 \\ I_{X2} \end{bmatrix} = \begin{bmatrix} 0 & H_{12} \\ H_{21} & 0 \end{bmatrix} \cdot \begin{bmatrix} I_{X1} \\ Y_2 \end{bmatrix}$$

Transformationsbeziehungen

$$Y_1 = H_{12} \cdot Y_2$$

$$I_{X1} \!=\! \frac{1}{H_{21}} \! \cdot \! I_{X2}$$