

# Implementation documentation

## Queue

Implemented methods: enqueue, dequeue, peek, clear, isEmpty, size, toLinkedList

All methods for this data structure only perform simple value assignments, some of them with if-checks. That way all Queue's actions are done in constant time and with constant memory. enqueue() creates a new object, which still requires constant memory. toLinkedList() method is an exception, as its time and memory requirement is  $O(n)$ , where  $n$  is amount of elements in the Queue. Besides the elements, queue only needs to store a constant amount of variables. So, overall, memory requirement for the Queue is  $O(n)$ .

## LinkedList

Implemented methods: add, clear, isEmpty, reset, hasNext, getNext, size

All methods for this data structure only perform simple value assignments, some of them with if-checks. That way all LinkedList's actions are done in constant time and with constant memory. add() creates a new object, which still requires constant memory. Besides the elements, LinkedList only needs to store a constant amount of variables. So, overall, memory requirement for the LinkedList is  $O(n)$  where  $n$  is amount of elements in the LinkedList.

## Tree

Implemented methods: add, remove, getMin, clear, isEmpty, contains, size, toLinkedList

Implemented tree is self-balancing using the red-black principle. Implementation mimics the guidelines presented in the Wikipedia article: [http://en.wikipedia.org/wiki/Red-black\\_tree](http://en.wikipedia.org/wiki/Red-black_tree)

**add:** First, tree finds a suitable placement for the new element. In worst case scenario, the placement in question may be found at the bottom of the

tree. Because tree's height is below  $2 * \log(n)$  ( $n$  = amount of elements), finding the placement requires  $O(\log(n))$  time. After that several tree balancing techniques are used depending on a specific scenario. Most techniques require constant time, however one scenario requires to iterate the balancing techniques for added node's parent. Balancing on addition requires  $O(\log(n))$ . Overall, time requirement is  $O(\log(n))$ . Memory requirement is constant.

**remove:** Deleted element first must be found, which requires  $O(\log(n))$  time. Some balancing techniques are performed in constant time, others iterate upwards, requiring  $O(\log(n))$  time. Overall, time requirement is  $O(\log(n))$ . Memory requirement is constant.

**contains:** Required element may be a leaf of the tree, in which case finding it requires  $O(\log(n))$  time. Same time is required, if tree doesn't contain given element. Overall, time requirement is  $O(\log(n))$ . Memory requirement is constant.

**toLinkedList:** All elements are traversed breadth first using the queue. Each element is processed once, so required time is  $O(n)$ . Elements need to be stored in queue and the LinkedList, which the method will return. Overall memory requirement is  $O(n)$

getMin, clear, isEmpty and size perform at constant time and memory. Besides the elements, LinkedList only needs to store a constant amount of variables, making overall memory requirement  $O(n)$ .

Tree can be extended to act as a map that holds key-value pairs. Overall memory requirement is not changed in  $O$ -notation.

**get:** finds the key element and returns its value. Time requirement  $O(\log(n))$ , memory requirement constant.

**put:** Calls contains method. If element is contained, elements value is changed. If not, add is called to add a new element to the tree. Time requirement  $O(\log(n))$ , memory requirement constant.

## Graph building with tracing

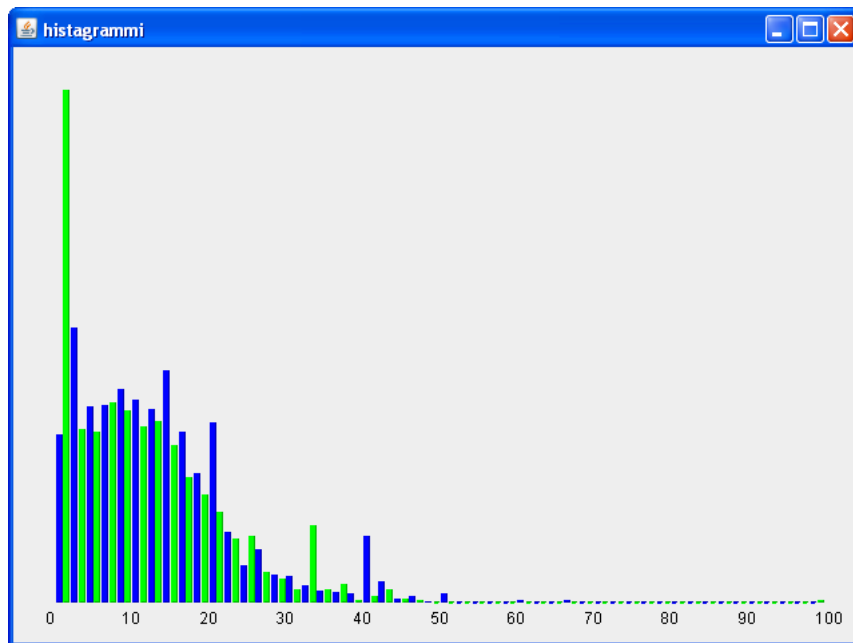
Tracing algorithm was largely underestimated in the requirements documen-

tation. Algorithm's rough progression:

1. Choose a vertex  $v$  from which point of view other vertices are traced.
2. Choose another point  $p$ . Store the direction and distance from  $v$  to  $p$ . Also store direction and distance from  $v$  to  $p.\text{right}$ , assuming that  $p$  is a part of a polygon and thus has a connection with a left and right neighbour, all of which are a part of the same polygon. This data can be represented as a sector of two directions.
3. Repeat 2 for every point in the field. Sectors are stored in a heap, where a sector with the smallest left direction value is placed on top of the heap. Time requirement:  $O(p \cdot \log(p))$  Memory requirement:  $O(p)$ , where  $p$  is amount of geometry points.
4. Go through the sectors and remove redundant and overlapping sectors. Each stored sector is pulled from the heap (Time:  $O(p \cdot \log(p))$ ) and stored in a tree (Time:  $O(p \cdot \log(p))$ ), where sectors closest to the  $v$  are stored as a left child. Using this technique, amount of stored sectors is reduced significantly, where sector amount is  $s$  and  $s \leq p$ . Memory requirement:  $O(p)$ .
5. All vertices are checked whether they are obstructed by any sector. Time requirement:  $O(r \cdot s)$ , where  $r$  is amount of points with reflex angles (which is less than or equals  $p$ ) and  $s$  is amount of usable sectors (also less than  $p$ ). Memory requirement:  $O(q)$ , where  $q$  is amount of points that are unobstructed to the  $v$ . That way  $q \leq p$ .
6. Repeat this for every  $v$  in the field.

Overall time requirement:  $O(v \cdot ((p \cdot \log(p)) + (r \cdot s)))$ , where  $v$  is amount of all vertices in the field, regardless if they are part of some polygon. That way  $p \leq v$ , also we have established that  $r \leq p$  and  $s \leq p$ . So, in worst case scenario, we could argue that the time to rebuild the graph is:  $O(v \cdot (p \cdot \log(p) + p^2)) = O(v^2 \cdot \log(v) + v^3)$ . In current implementation, it is fair to assume that  $v = p$ , because with currently implemented tools user can only place two vertices, which are not a part of any polygon. To assume that  $r = p$  is a bit of a stretch, however that will happen if user decides to have all of the polygons to be reflex. The interesting bit is studying the relation between  $s$  and  $p$ .

Because  $s \leq p$ , we can represent the relation as:  $s = c \cdot p$ , where  $c \geq 0$  and  $c \leq 1$ . This histogram shows the value of  $c$  retrieved by empirical means.



This data was collected from 55672 occurrences. X-axis represents the value of  $c$  (in percents), and height of a column shows how many occurrences fit the particular value interval. We can see that  $c$  hardly reaches above 0.5 and has a distinct peak at  $[0.1, 0.2]$ . This suggests that equating  $s$  with  $p$  isn't entirely fair. Now time requirement looks like:  $O(p^2 * (\log(p) + c))$   
Memory requirement:  $O(p)$ . At any stage of the algorithm no more than  $p$  amount of memory allocation is required.