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# **Pattern Discovery: Basic Concepts**

# Pattern Discovery: Basic Concepts

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- ❑ What Is Pattern Discovery? Why Is It Important?
- ❑ Basic Concepts: Frequent Patterns and Association Rules
- ❑ Compressed Representation: Closed Patterns and Max-Patterns



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# **What Is Pattern Discovery? Why Is It Important?**

# What Is Pattern Discovery?

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## ❑ What are patterns?

- ❑ **Patterns**: A set of items, subsequences, or substructures that occur frequently together (or strongly correlated) in a data set
- ❑ Patterns represent **intrinsic** and **important properties** of datasets

## ❑ **Pattern discovery**: Uncovering patterns from massive data sets

## ❑ Motivation examples:

- ❑ What products were often purchased together?
- ❑ What are the subsequent purchases after buying an iPad?
- ❑ What code segments likely contain copy-and-paste bugs?
- ❑ What word sequences likely form phrases in this corpus?

# Pattern Discovery: Why Is It Important?

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- ❑ Finding **inherent regularities** in a data set
- ❑ **Foundation** for many essential data mining tasks
  - ❑ Association, correlation, and causality analysis
  - ❑ Mining sequential, structural (e.g., sub-graph) patterns
  - ❑ Pattern analysis in spatiotemporal, multimedia, time-series, and stream data
  - ❑ Classification: Discriminative pattern-based analysis
  - ❑ Cluster analysis: Pattern-based subspace clustering
- ❑ Broad applications
  - ❑ Market basket analysis, cross-marketing, catalog design, sale campaign analysis, Web log analysis, biological sequence analysis



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# Basic Concepts: Frequent Patterns and Association Rules

# Basic Concepts: k-Itemsets and Their Supports

□ **Itemset**: A set of one or more items

□ **k-itemset**:  $X = \{x_1, \dots, x_k\}$

□ Ex. {Beer, Nuts, Diaper} is a 3-itemset

□ **(absolute) support (count)** of X,  $\text{sup}\{X\}$ :  
Frequency or the number of occurrences  
of an itemset X

□ Ex.  $\text{sup}\{\text{Beer}\} = 3$

□ Ex.  $\text{sup}\{\text{Diaper}\} = 4$

□ Ex.  $\text{sup}\{\text{Beer}, \text{Diaper}\} = 3$

□ Ex.  $\text{sup}\{\text{Beer}, \text{Eggs}\} = 1$

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

□ **(relative) support**,  $s\{X\}$ : The fraction of  
transactions that contains X (i.e., the  
**probability** that a transaction contains X)

□ Ex.  $s\{\text{Beer}\} = 3/5 = 60\%$

□ Ex.  $s\{\text{Diaper}\} = 4/5 = 80\%$

□ Ex.  $s\{\text{Beer}, \text{Eggs}\} = 1/5 = 20\%$

# Basic Concepts: Frequent Itemsets (Patterns)

- An itemset (or a pattern)  $X$  is *frequent* if the support of  $X$  is no less than a *minsup* threshold  $\sigma$
- Let  $\sigma = 50\%$  ( $\sigma$ : *minsup* threshold)  
For the given 5-transaction dataset
  - All the frequent 1-itemsets:
    - Beer: 3/5 (60%); Nuts: 3/5 (60%)
    - Diaper: 4/5 (80%); Eggs: 3/5 (60%)
  - All the frequent 2-itemsets:
    - {Beer, Diaper}: 3/5 (60%)
  - All the frequent 3-itemsets?
    - None



Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

- Why do these itemsets (shown on the left) form the complete set of frequent  $k$ -itemsets (patterns) for any  $k$ ?
- **Observation:** We may need an efficient method to mine a complete set of frequent patterns



# From Frequent Itemsets to Association Rules

- Comparing with itemsets, rules can be more telling

- Ex.  $\text{Diaper} \rightarrow \text{Beer}$

- Buying diapers may likely lead to buying beers*

- How strong is this rule? (support, confidence)

- Measuring association rules:  $X \rightarrow Y (s, c)$

- Both  $X$  and  $Y$  are itemsets

- Support**,  $s$ : The probability that a transaction contains  $X \cup Y$

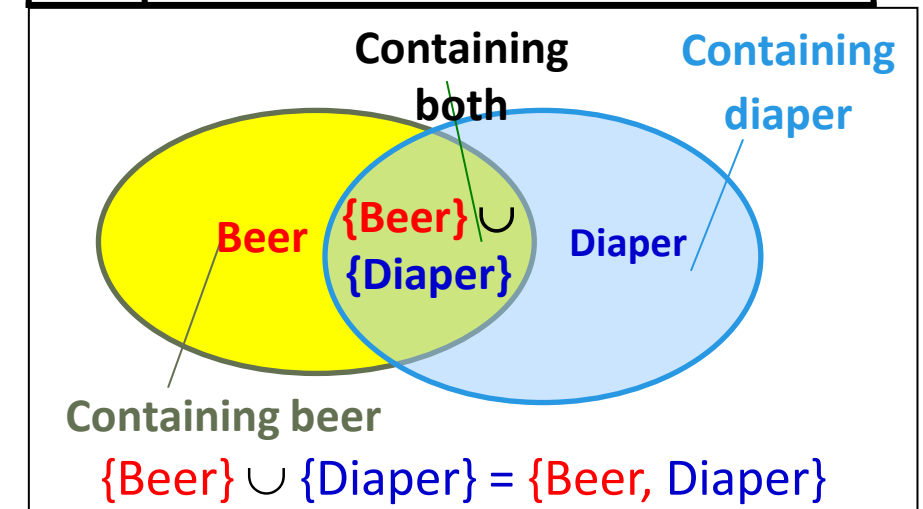
- Ex.  $s\{\text{Diaper}, \text{Beer}\} = 3/5 = 0.6$  (i.e., 60%)

- Confidence**,  $c$ : The *conditional probability* that a transaction containing  $X$  also contains  $Y$

- Calculation:  $c = \text{sup}(X \cup Y) / \text{sup}(X)$

- Ex.  $c = \text{sup}\{\text{Diaper}, \text{Beer}\} / \text{sup}\{\text{Diaper}\} = 3/4 = 0.75$

Tid	Items bought
10	Beer, Nuts, Diaper
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Note:  $X \cup Y$ : the union of two itemsets  
■ The set contains both  $X$  and  $Y$

# Mining Frequent Itemsets and Association Rules

## □ Association rule mining

- Given two thresholds: *minsup*, *minconf*
- Find **all** of the rules,  $X \rightarrow Y$  (*s*, *c*)
  - such that,  $s \geq \text{minsup}$  and  $c \geq \text{minconf}$


## □ Let *minsup* = 50%

- Freq. 1-itemsets: Beer: 3, Nuts: 3, Diaper: 4, Eggs: 3
- Freq. 2-itemsets: {Beer, Diaper}: 3

## □ Let *minconf* = 50%

- $\text{Beer} \rightarrow \text{Diaper}$  (60%, 100%)
- $\text{Diaper} \rightarrow \text{Beer}$  (60%, 75%)

(Q: Are these all rules?)



Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

## □ Observations:

- Mining association rules and mining frequent patterns are very close problems
- Scalable methods are needed for mining large datasets



# **+ + Compressed Representation: Closed Patterns and Max- Patterns**



# Challenge: There Are Too Many Frequent Patterns!

- A long pattern contains a combinatorial number of sub-patterns
- How many frequent itemsets does the following TDB<sub>1</sub> contain?

□ TDB<sub>1</sub>:      T<sub>1</sub>: {a<sub>1</sub>, ..., a<sub>50</sub>}; T<sub>2</sub>: {a<sub>1</sub>, ..., a<sub>100</sub>}

□ Assuming (absolute) *minsup* = 1

□ Let's have a try

1-itemsets: {a<sub>1</sub>}: 2, {a<sub>2</sub>}: 2, ..., {a<sub>50</sub>}: 2, {a<sub>51</sub>}: 1, ..., {a<sub>100</sub>}: 1,

2-itemsets: {a<sub>1</sub>, a<sub>2</sub>}: 2, ..., {a<sub>1</sub>, a<sub>50</sub>}: 2, {a<sub>1</sub>, a<sub>51</sub>}: 1 ..., ..., {a<sub>99</sub>, a<sub>100</sub>}: 1,

..., ..., ..., ...

99-itemsets: {a<sub>1</sub>, a<sub>2</sub>, ..., a<sub>99</sub>}: 1, ..., {a<sub>2</sub>, a<sub>3</sub>, ..., a<sub>100</sub>}: 1

100-itemset: {a<sub>1</sub>, a<sub>2</sub>, ..., a<sub>100</sub>}: 1

- The total number of frequent itemsets:

$$\binom{100}{1} + \binom{100}{2} + \binom{100}{3} + \cdots + \binom{100}{100} = 2^{100} - 1$$

A too huge set for any  
one to compute or store!



# Expressing Patterns in Compressed Form: Closed Patterns

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- How to handle such a challenge?
- Solution 1: **Closed patterns**: A pattern (itemset)  $X$  is **closed** if  $X$  is *frequent*, and there exists *no super-pattern*  $Y \supset X$ , with the same support as  $X$ 
  - Let Transaction DB  $TDB_1$ :  $T_1: \{a_1, \dots, a_{50}\}$ ;  $T_2: \{a_1, \dots, a_{100}\}$
  - Suppose  $minsup = 1$ . How many closed patterns does  $TDB_1$  contain?
    - Two:  $P_1: \{\{a_1, \dots, a_{50}\}: 2\}$ ;  $P_2: \{\{a_1, \dots, a_{100}\}: 1\}$
- **Closed pattern** is a **lossless compression** of frequent patterns
  - Reduces the # of patterns but does not lose the support information!
  - You will still be able to say:  $\{\{a_2, \dots, a_{40}\}: 2\}$ ,  $\{\{a_5, a_{51}\}: 1\}$

# Expressing Patterns in Compressed Form: Max-Patterns

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- ❑ Solution 2: **Max-patterns**: A pattern  $X$  is a **max-pattern** if  $X$  is frequent and there exists no frequent super-pattern  $Y \supset X$
- ❑ Difference from close-patterns?
  - ❑ Do not care the real support of the sub-patterns of a max-pattern
  - ❑ Let Transaction DB  $TDB_1$ :  $T_1: \{a_1, \dots, a_{50}\}$ ;  $T_2: \{a_1, \dots, a_{100}\}$
  - ❑ Suppose  $minsup = 1$ . How many max-patterns does  $TDB_1$  contain?
    - ❑ One:  $P: \{\{a_1, \dots, a_{100}\}: 1\}$
- ❑ **Max-pattern** is a **lossy compression**!
  - ❑ We only know  $\{a_1, \dots, a_{40}\}$  is frequent
  - ❑ But we do not know the real support of  $\{a_1, \dots, a_{40}\}$ , ..., any more!
- ❑ Thus in many applications, mining close-patterns is more desirable than mining max-patterns



The background of the slide is a complex, abstract composition. It features a grid of small, light-colored plus signs (+) overlaid on a dark, reddish-brown background. A large, white, irregular banner shape is positioned in the center, containing the word "Summary". The banner has a subtle gradient and is surrounded by various geometric patterns, including a network of thin, reddish lines and clusters of small, colorful dots (green, blue, yellow) in the upper and lower sections. On the left side, there is a vertical strip of a lighter, textured area with some orange and brown tones. The overall aesthetic is modern and technical.

# Summary

# Summary: Pattern Discovery: Basic Concepts

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- ❑ What Is Pattern Discovery? Why Is It Important?
- ❑ Basic Concepts: Frequent Patterns and Association Rules
- ❑ Compressed Representation: Closed Patterns and Max-Patterns

# Recommended Readings

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- ❑ R. Agrawal, T. Imielinski, and A. Swami, “Mining association rules between sets of items in large databases”, in Proc. of SIGMOD'93
- ❑ R. J. Bayardo, “Efficiently mining long patterns from databases”, in Proc. of SIGMOD'98
- ❑ N. Pasquier, Y. Bastide, R. Taouil, and L. Lakhal, “Discovering frequent closed itemsets for association rules”, in Proc. of ICDT'99
- ❑ J. Han, H. Cheng, D. Xin, and X. Yan, “Frequent Pattern Mining: Current Status and Future Directions”, Data Mining and Knowledge Discovery, 15(1): 55-86, 2007



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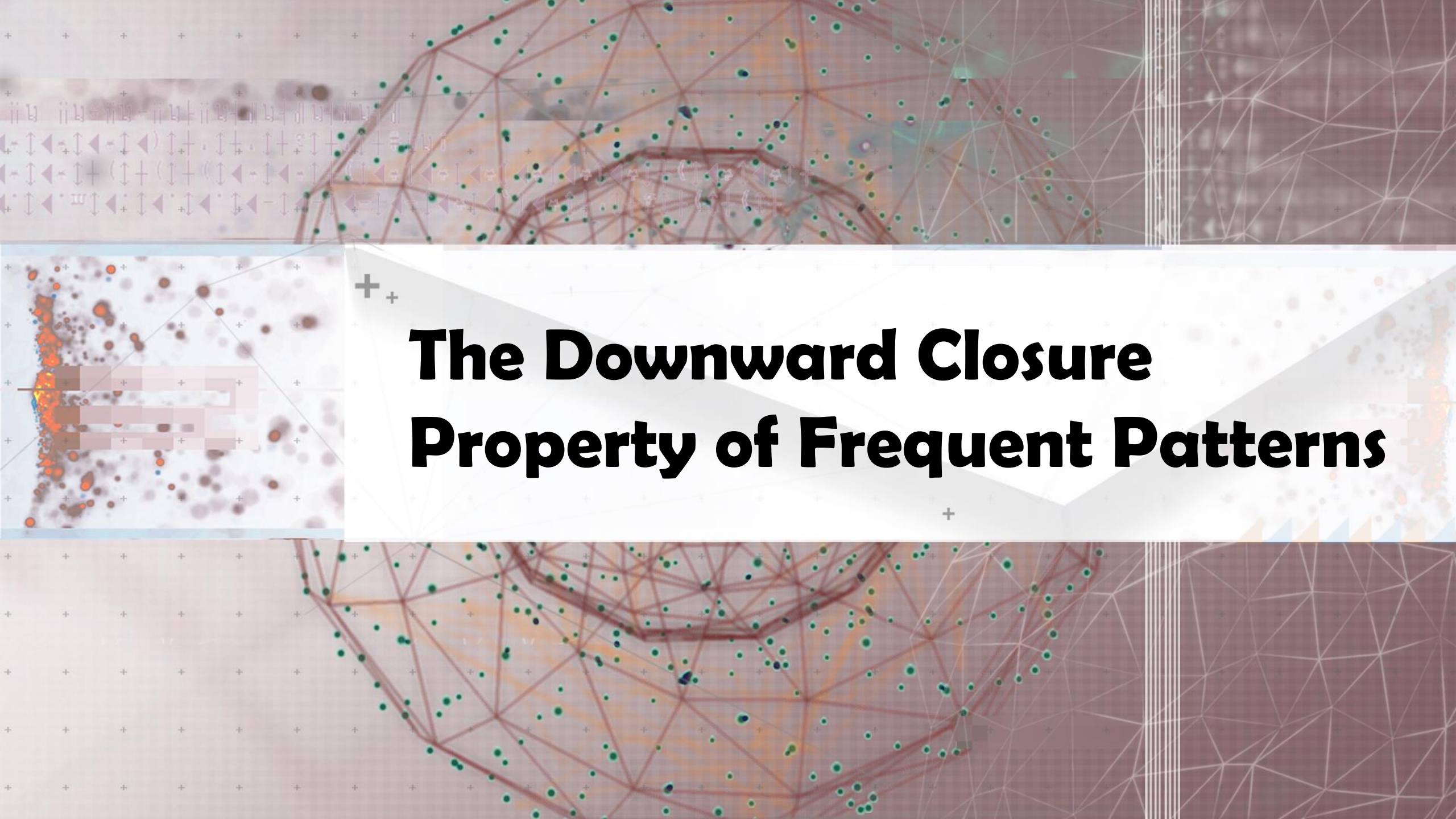
# Efficient Pattern Mining Methods

# Efficient Pattern Mining Methods

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- ❑ The Downward Closure Property of Frequent Patterns
- ❑ The Apriori Algorithm
- ❑ Extensions or Improvements of Apriori
- ❑ Mining Frequent Patterns by Exploring Vertical Data Format
- ❑ FPGrowth: A Frequent Pattern-Growth Approach
- ❑ Mining Closed Patterns




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# The Downward Closure Property of Frequent Patterns



# The Downward Closure Property of Frequent Patterns

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- ❑ Observation: From  $TDB_1: T_1: \{a_1, \dots, a_{50}\}; T_2: \{a_1, \dots, a_{100}\}$ 
  - ❑ We get a frequent itemset:  $\{a_1, \dots, a_{50}\}$
  - ❑ Also, its subsets are all frequent:  $\{a_1\}, \{a_2\}, \dots, \{a_{50}\}, \{a_1, a_2\}, \dots, \{a_1, \dots, a_{49}\}, \dots$
  - ❑ There must be some hidden relationships among frequent patterns!
- ❑ The **downward closure (also called “Apriori”)** property of frequent patterns
  - ❑ If  **$\{\text{beer, diaper, nuts}\}$**  is frequent, so is  **$\{\text{beer, diaper}\}$**
  - ❑ Every transaction containing  $\{\text{beer, diaper, nuts}\}$  also contains  $\{\text{beer, diaper}\}$
  - ❑ Apriori: Any subset of a frequent itemset must be frequent
- ❑ Efficient mining methodology
  - ❑ If **any subset of an itemset  $S$**  is infrequent, then there is no chance for  $S$  to be frequent—why do we even have to consider  $S$ !?  A sharp knife for pruning!

# Apriori Pruning and Scalable Mining Methods

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- ❑ Apriori pruning principle: If there is any itemset which is infrequent, its superset should not even be generated! (Agrawal & Srikant @VLDB'94, Mannila, et al. @ KDD' 94)
- ❑ Scalable mining Methods: Three major approaches
  - ❑ Level-wise, join-based approach: Apriori (Agrawal & Srikant@VLDB'94)
  - ❑ Vertical data format approach: Eclat (Zaki, Parthasarathy, Ogihara, Li @KDD'97)
  - ❑ Frequent pattern projection and growth: FPgrowth (Han, Pei, Yin @SIGMOD'00)

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# The Apriori Algorithm

# Apriori: A Candidate Generation & Test Approach

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- ❑ Outline of Apriori (level-wise, candidate generation and test)
  - ❑ Initially, scan DB once to get frequent 1-itemset
  - ❑ Repeat
    - ❑ Generate length-(k+1) candidate itemsets from length-k frequent itemsets
    - ❑ Test the candidates against DB to find frequent (k+1)-itemsets
    - ❑ Set  $k := k + 1$
  - ❑ Until no frequent or candidate set can be generated
  - ❑ Return all the frequent itemsets derived



# The Apriori Algorithm (Pseudo-Code)

---

$C_k$ : Candidate itemset of size  $k$

$F_k$ : Frequent itemset of size  $k$

$K := 1$ ;

$F_k := \{\text{frequent items}\}$ ; // frequent 1-itemset

**While** ( $F_k \neq \emptyset$ ) **do** { // when  $F_k$  is non-empty

$C_{k+1} := \text{candidates generated from } F_k$ ; // candidate generation

    Derive  $F_{k+1}$  by counting candidates in  $C_{k+1}$  with respect to  $TDB$  at minsup;

$k := k + 1$

}

**return**  $\cup_k F_k$  // return  $F_k$  generated at each level

# The Apriori Algorithm—An Example

Database TDB

Tid	Items
10	A, C, D
20	B, C, E
30	A, B, C, E
40	B, E

minsup = 2

$C_1$

1<sup>st</sup> scan

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

$F_1$

Itemset	sup
{A}	2
{B}	3
{C}	3
{E}	3

$F_2$

Itemset	sup
{A, C}	2
{B, C}	2
{B, E}	3
{C, E}	2

$C_2$

Itemset	sup
{A, B}	1
{A, C}	2
{A, E}	1
{B, C}	2
{B, E}	3
{C, E}	2

2<sup>nd</sup> scan

$C_2$

Itemset
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}

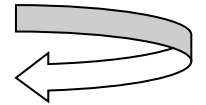
$C_3$

Itemset
{B, C, E}

3<sup>rd</sup> scan

$F_3$

Itemset	sup
{B, C, E}	2



# Apriori: Implementation Tricks

## □ How to generate candidates?

□ Step 1: self-joining  $F_k$

□ Step 2: pruning

## □ Example of candidate-generation

□  $F_3 = \{abc, abd, acd, ace, bcd\}$

□ Self-joining:  $F_3 * F_3$

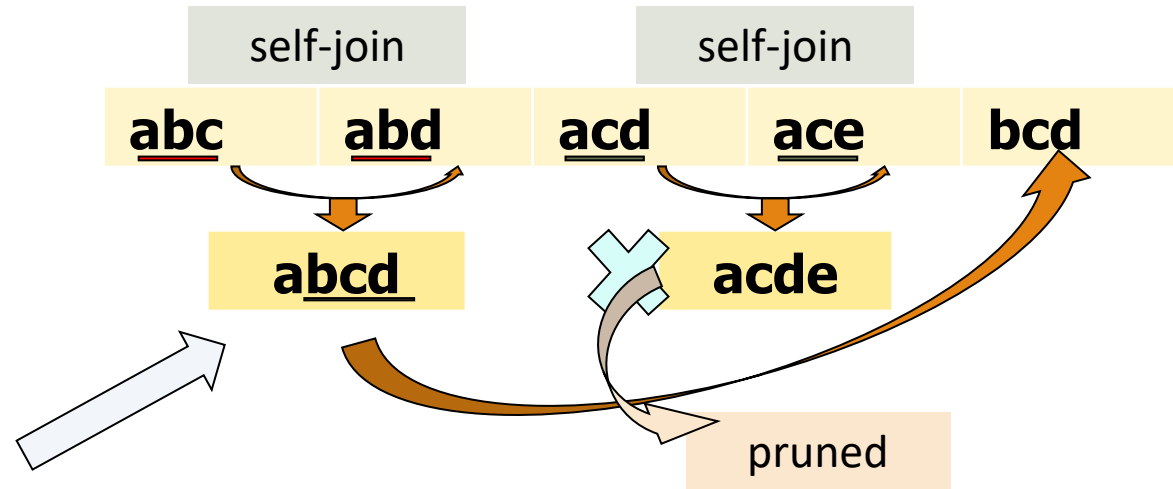
□  $abcd$  from  $abc$  and  $abd$

□  $acde$  from  $acd$  and  $ace$

□ Pruning:

□  $acde$  is removed because  $ade$  is not in  $F_3$

□  $C_4 = \{abcd\}$



# Candidate Generation: An SQL Implementation

- Suppose the items in  $F_{k-1}$  are listed in an order

- Step 1: self-joining  $F_{k-1}$   
insert into  $C_k$

select  $p.item_1, p.item_2, \dots, p.item_{k-1}, q.item_{k-1}$

from  $F_{k-1}$  as  $p, F_{k-1}$  as  $q$

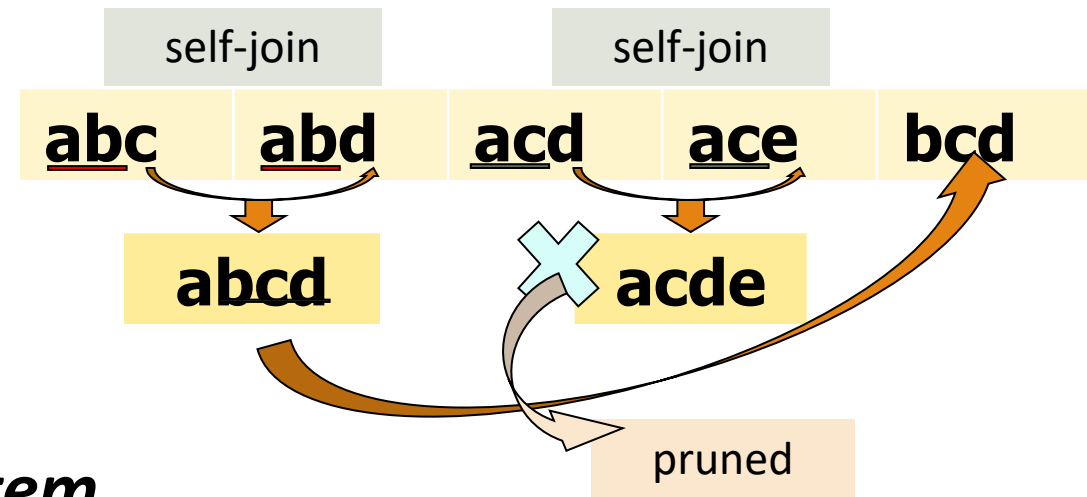
where  $p.item_1 = q.item_1, \dots, p.item_{k-2} = q.item_{k-2}, p.item_{k-1} < q.item_{k-1}$

- Step 2: pruning

for all *itemsets*  $c$  in  $C_k$  do

for all  $(k-1)$ -subsets  $s$  of  $c$  do

if ( $s$  is not in  $F_{k-1}$ ) then delete  $c$  from  $C_k$





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# **Extensions or Improvements of Apriori**

# Apriori: Improvements and Alternatives

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- ❑ Reduce passes of transaction database scans

- ❑ Partitioning (e.g., Savasere, et al., 1995)

- ❑ Dynamic itemset counting (Brin, et al., 1997)




To be discussed in subsequent slides

- ❑ Shrink the number of candidates

- ❑ Hashing (e.g., DHP: Park, et al., 1995)

- ❑ Pruning by support lower bounding (e.g., Bayardo 1998)

- ❑ Sampling (e.g., Toivonen, 1996)



To be discussed in subsequent slides

- ❑ Exploring special data structures

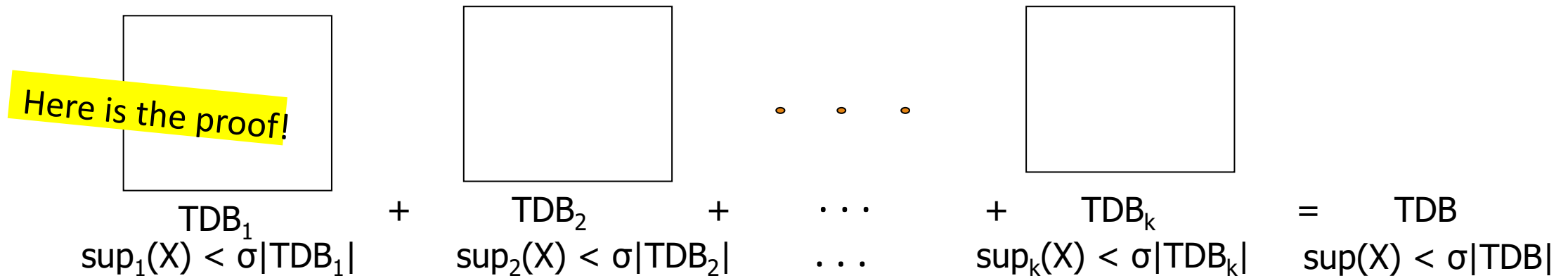
- ❑ Tree projection (Agarwal, et al., 2001)

- ❑ H-miner (Pei, et al., 2001)

- ❑ Hypercube decomposition (e.g., LCM: Uno, et al., 2004)

# Partitioning: Scan Database Only Twice

- Theorem: *Any itemset that is potentially frequent in TDB must be frequent in at least one of the partitions of TDB*



- Method: Scan DB twice (A. Savasere, E. Omiecinski and S. Navathe, *VLDB'95*)
  - Scan 1: Partition database so that each partition can fit in main memory (why?)
    - Mine local frequent patterns in this partition
  - Scan 2: Consolidate global frequent patterns
    - Find global frequent itemset candidates (those frequent in at least one partition)
    - Find the true frequency of those candidates, by scanning  $\text{TDB}_i$  one more time

# Direct Hashing and Pruning (DHP)

- ❑ DHP (Direct Hashing and Pruning): (J. Park, M. Chen, and P. Yu, SIGMOD'95)
- ❑ Hashing: Different itemsets may have the same hash value:  $v = \text{hash}(\text{itemset})$
- ❑ 1<sup>st</sup> scan: When counting the 1-itemset, hash 2-itemset to calculate the bucket count
- ❑ Observation: A  $k$ -itemset cannot be frequent if its corresponding hashing bucket count is below the *minsup* threshold

- ❑ Example: At the 1<sup>st</sup> scan of TDB, count 1-itemset, and

Itemsets	Count
{ab, ad, ce}	35
{bd, be, de}	298
.....	...
{yz, qs, wt}	58

**Hash Table**

- ❑ Hash 2-itemsets in the transaction to its bucket

- ❑ {ab, ad, ce}

- ❑ {bd, be, de}

- ❑ ...

- ❑ At the end of the first scan,

- ❑ if  $\text{minsup} = 80$ , remove *ab, ad, ce*, since  $\text{count}\{ab, ad, ce\} < 80$



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# **Mining Frequent Patterns by Exploring Vertical Data Format**

# Exploring Vertical Data Format: ECLAT

- ❑ ECLAT (Equivalence Class Transformation): A depth-first search algorithm using set intersection [Zaki et al. @KDD'97]
- ❑ Tid-List: List of transaction-ids containing an itemset
- ❑ Vertical format:  $t(e) = \{T_{10}, T_{20}, T_{30}\}$ ;  $t(a) = \{T_{10}, T_{20}\}$ ;  $t(ae) = \{T_{10}, T_{20}\}$
- ❑ Properties of Tid-Lists
  - ❑  $t(X) = t(Y)$ : X and Y always happen together (e.g.,  $t(ac) = t(d)$ )
  - ❑  $t(X) \subset t(Y)$ : transaction having X always has Y (e.g.,  $t(ac) \subset t(ce)$ )
- ❑ Deriving frequent patterns based on vertical intersections
- ❑ Using **diffset** to accelerate mining
  - ❑ Only keep track of differences of tids
  - ❑  $t(e) = \{T_{10}, T_{20}, T_{30}\}$ ,  $t(ce) = \{T_{10}, T_{30}\} \rightarrow \text{Diffset}(ce, e) = \{T_{20}\}$

A transaction DB in Horizontal Data Format

Tid	Itemset
10	a, c, d, e
20	a, b, e
30	b, c, e

The transaction DB in Vertical Data Format

Item	TidList
a	10, 20
b	20, 30
c	10, 30
d	10
e	10, 20, 30



The background of the slide is a complex, abstract composition. It features a network graph with numerous nodes and edges, rendered in a reddish-brown hue. Overlaid on this are various geometric patterns, including a grid of small plus signs and a series of horizontal lines with arrows pointing left. A large, light-colored, angular shape, resembling a stylized letter 'A' or a folded piece of paper, is positioned behind the main title. In the bottom left corner, there is a small inset image showing a cluster of orange and brown dots, with a horizontal bar chart overlaid on it.

# **FPGrowth: A Pattern Growth Approach**

# Why Mining Frequent Patterns by Pattern Growth?

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- ❑ Apriori: A *breadth-first search* mining algorithm
  - ❑ First find the complete set of frequent  $k$ -itemsets
  - ❑ Then derive frequent  $(k+1)$ -itemset candidates
  - ❑ Scan DB again to find true frequent  $(k+1)$ -itemsets
- ❑ Motivation for a different mining methodology
  - ❑ Can we develop a *depth-first search* mining algorithm?
  - ❑ For a frequent itemset  $p$ , can subsequent search be confined to only those transactions that containing  $p$ ?
- ❑ Such thinking leads to a frequent pattern growth approach:
  - ❑ FPGrowth (J. Han, J. Pei, Y. Yin, “Mining Frequent Patterns without Candidate Generation,” SIGMOD 2000)

# Example: Construct FP-tree from a Transaction DB

TID	Items in the Transaction	Ordered, frequent itemlist
100	{f, a, c, d, g, i, m, p}	f, c, a, m, p
200	{a, b, c, f, l, m, o}	f, c, a, b, m
300	{b, f, h, j, o, w}	f, b
400	{b, c, k, s, p}	c, b, p
500	{a, f, c, e, l, p, m, n}	f, c, a, m, p

After inserting the 1<sup>st</sup> frequent Itemlist: "f, c, a, m, p"

1. Scan DB once, find single item frequent pattern:

Let min\_support = 3

f:4, a:3, c:4, b:3, m:3, p:3

2. Sort frequent items in frequency descending order, f-list

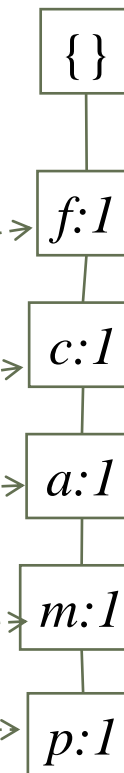
F-list = f-c-a-b-m-p

3. Scan DB again, construct FP-tree

- The frequent itemlist of each transaction is inserted as a branch, with shared sub-branches merged, counts accumulated

Header Table

Item	Frequency	header
f	4	
c	4	
a	3	
b	3	
m	3	
p	3	





# Example: Construct FP-tree from a Transaction DB

TID	Items in the Transaction	Ordered, frequent itemlist
100	{f, a, c, d, g, i, m, p}	f, c, a, m, p
200	{a, b, c, f, l, m, o}	f, c, a, b, m
300	{b, f, h, j, o, w}	f, b
400	{b, c, k, s, p}	c, b, p
500	{a, f, c, e, l, p, m, n}	f, c, a, m, p

After inserting the 2<sup>nd</sup> frequent itemlist "f, c, a, b, m"

1. Scan DB once, find single item frequent pattern:

Let min\_support = 3

f:4, a:3, c:4, b:3, m:3, p:3

2. Sort frequent items in frequency descending order, f-list

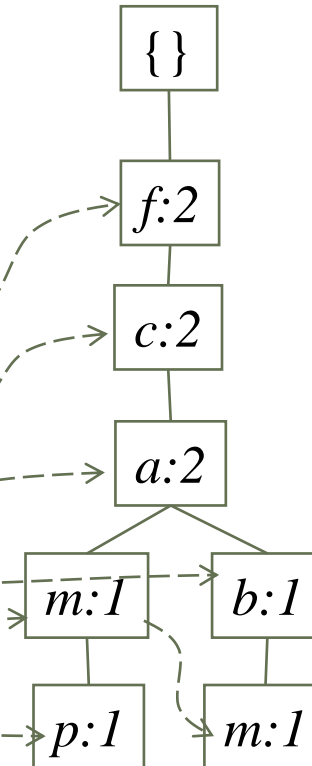
F-list = f-c-a-b-m-p

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p	3	



# Example: Construct FP-tree from a Transaction DB

TID	Items in the Transaction	Ordered, frequent itemlist
100	{f, a, c, d, g, i, m, p}	f, c, a, m, p
200	{a, b, c, f, l, m, o}	f, c, a, b, m
300	{b, f, h, j, o, w}	f, b
400	{b, c, k, s, p}	c, b, p
500	{a, f, c, e, l, p, m, n}	f, c, a, m, p

1. Scan DB once, find single item frequent pattern:

Let min\_support = 3

f:4, a:3, c:4, b:3, m:3, p:3

2. Sort frequent items in frequency descending order, f-list

F-list = f-c-a-b-m-p

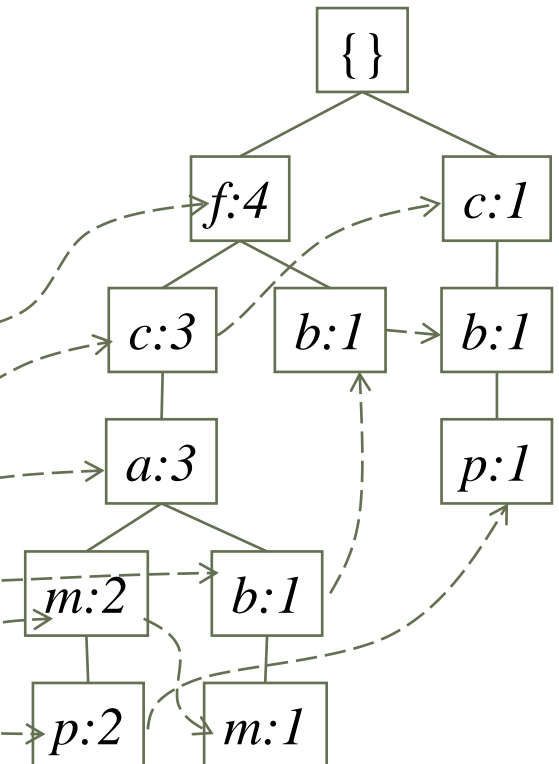
3. Scan DB again, construct FP-tree

- The frequent itemlist of each transaction is inserted as a branch, with shared sub-branches merged, counts accumulated

Header Table

Item	Frequency	header
f	4	
c	4	
a	3	
b	3	
m	3	
p	3	

After inserting all the frequent itemlists

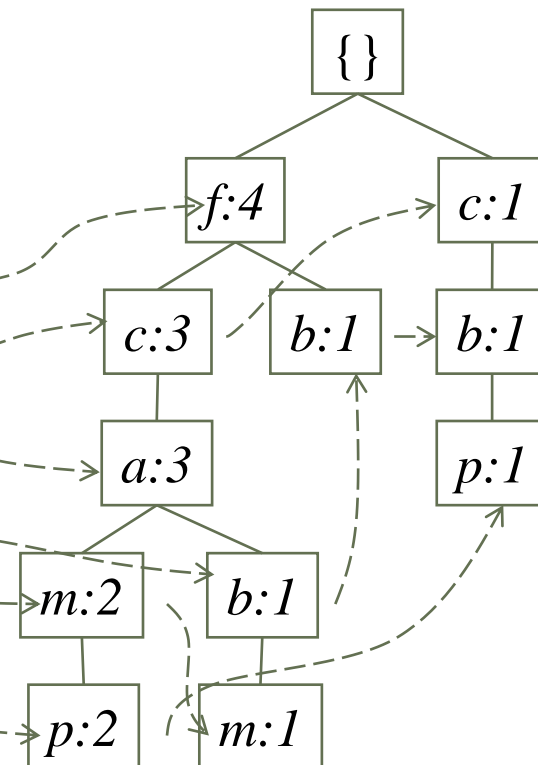


# Mining FP-Tree: Divide and Conquer Based on Patterns and Data

- Pattern mining can be partitioned according to current patterns
  - Patterns containing  $p$ :  $p$ 's conditional database:  $fcam:2, cb:1$ 
    - $p$ 's conditional database (i.e., the database under the condition that  $p$  exists):
      - *transformed prefix paths* of item  $p$
  - Patterns having  $m$  but no  $p$ :  $m$ 's conditional database:  $fca:2, fcab:1$
  - ..... .....

**min\_support = 3**

Item	Frequency	Header
f	4	
c	4	
a	3	
b	3	
m	3	
p	3	



**Conditional database of each pattern**

<u>Item</u>	<u>Conditional database</u>
<i>c</i>	<i>f:3</i>
<i>a</i>	<i>fc:3</i>
<i>b</i>	<i>fca:1, f:1, c:1</i>
<i>m</i>	<i>fca:2, fcab:1</i>
<i>p</i>	<i>fcam:2, cb:1</i>

# Mine Each Conditional Database Recursively

min\_support = 3

## Conditional Data Bases

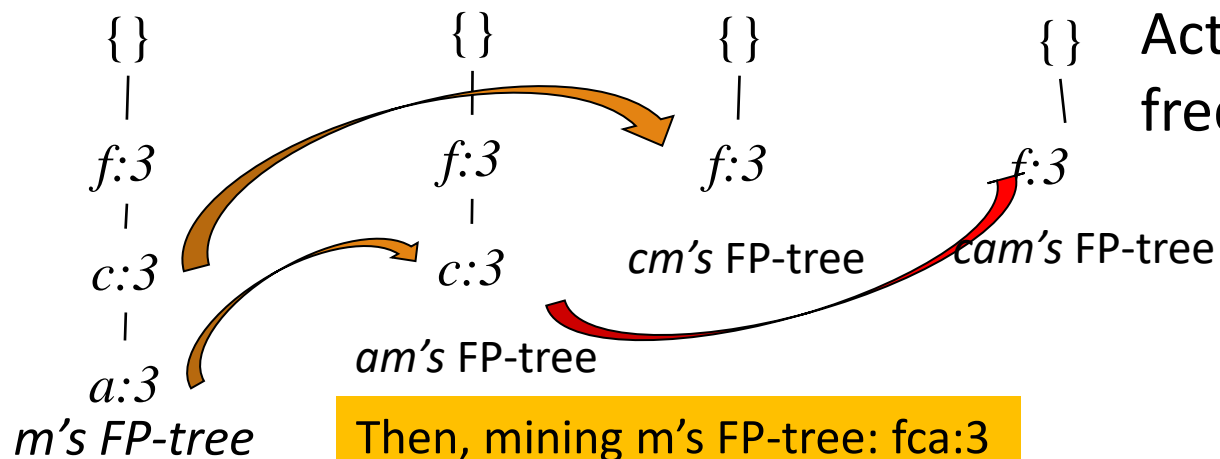
<i>item</i>	<i>cond. data base</i>
<i>c</i>	<i>f:3</i>
<i>a</i>	<i>fc:3</i>
<i>b</i>	<i>fca:1, f:1, c:1</i>
<i>m</i>	<i>fca:2, fcab:1</i>
<i>p</i>	<i>fcam:2, cb:1</i>

- For each conditional database
  - Mine single-item patterns
  - Construct its FP-tree & mine it

*p*'s conditional DB: *fcam:2, cb:1* → *c: 3*

*m*'s conditional DB: *fca:2, fcab:1* → *fca: 3*

*b*'s conditional DB: *fca:1, f:1, c:1* →  $\phi$



Actually, for single branch FP-tree, all the frequent patterns can be generated in one shot

*m: 3*

*fm: 3, cm: 3, am: 3*

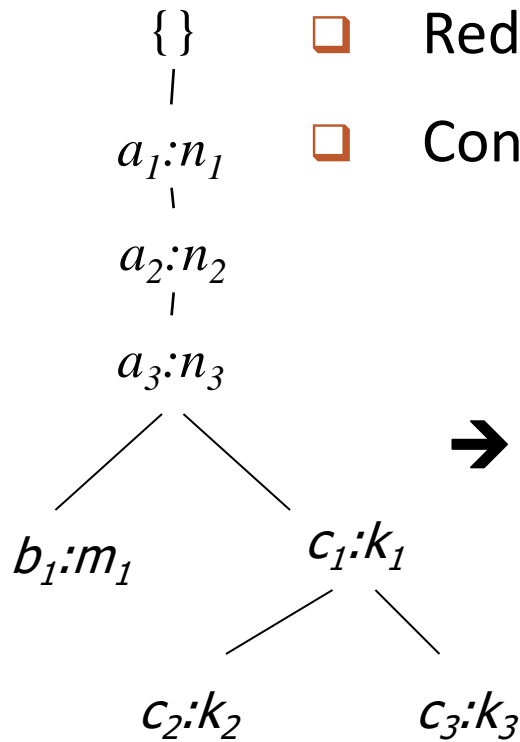
*fcm: 3, fam:3, cam: 3*

*fcam: 3*



# A Special Case: Single Prefix Path in FP-tree

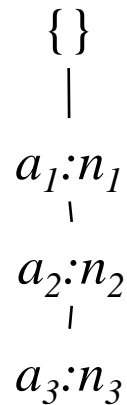
- Suppose a (conditional) FP-tree  $T$  has a shared single prefix-path  $P$
- Mining can be decomposed into two parts



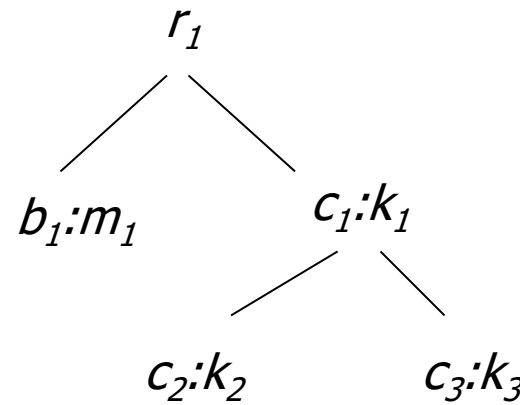
- Reduction of the single prefix path into one node
- Concatenation of the mining results of the two parts



$r_1 =$



+



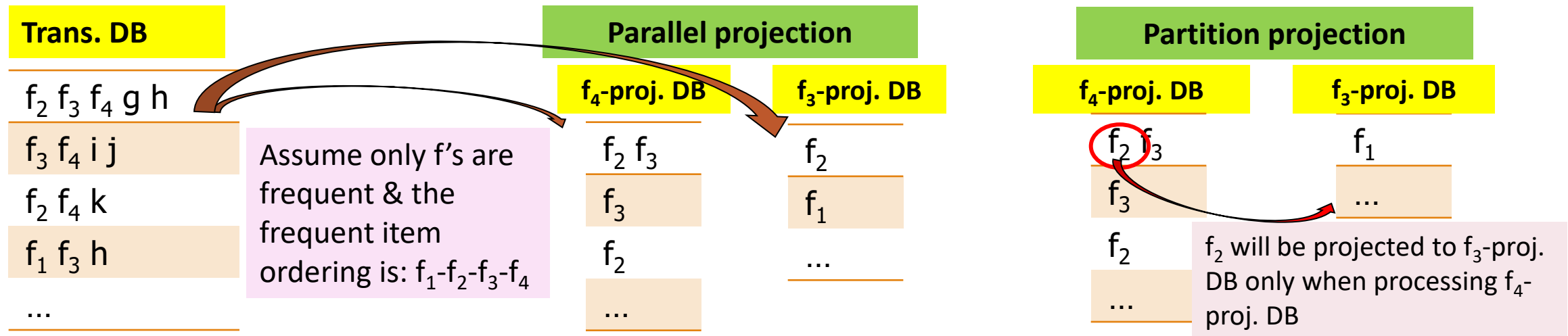
# FPGrowth: Mining Frequent Patterns by Pattern Growth

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- ❑ Essence of frequent pattern growth (FPGrowth) methodology
  - ❑ Find frequent single items and partition the database based on each such single item pattern
  - ❑ Recursively grow frequent patterns by doing the above for each *partitioned database* (also called the pattern's *conditional database*)
  - ❑ To facilitate efficient processing, an efficient data structure, FP-tree, can be constructed
- ❑ Mining becomes
  - ❑ Recursively construct and mine (conditional) FP-trees
  - ❑ Until the resulting FP-tree is empty, or until it contains only one path—single path will generate all the combinations of its sub-paths, each of which is a frequent pattern

# Scaling FP-growth by Item-Based Data Projection

- ❑ What if FP-tree cannot fit in memory?—Do not construct FP-tree
  - ❑ “Project” the database based on frequent single items
  - ❑ Construct & mine FP-tree for each projected DB
- ❑ **Parallel projection** vs. **partition projection**
  - ❑ Parallel projection: Project the DB on each frequent item
    - ❑ Space costly, all partitions can be processed in parallel
  - ❑ Partition projection: Partition the DB in order
    - ❑ Passing the unprocessed parts to subsequent partitions

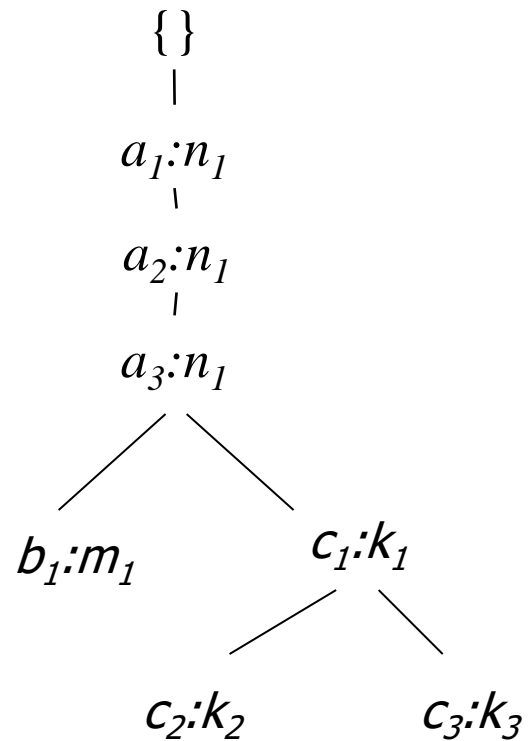


The background of the slide is a complex, abstract composition. It features a dark, reddish-brown base with a network of thin, light-colored lines forming a web-like structure. Scattered throughout are numerous small, colored dots in shades of green, blue, and yellow. A prominent white diagonal band runs from the top-left towards the bottom-right, creating a sense of depth and movement. In the upper-left corner, there is a rectangular inset showing a different data visualization: a grid of small squares with varying shades of orange and red, overlaid with a network of lines and dots. The overall aesthetic is technical and data-driven.

# Mining Closed Patterns



# CLOSET+: Mining Closed Itemsets by Pattern-Growth



- ❑ Efficient, *direct* mining of closed itemsets
- ❑ Intuition:
  - ❑ If an FP-tree contains a single branch as shown left
  - ❑ “a<sub>1</sub>, a<sub>2</sub>, a<sub>3</sub>” should be merged
- ❑ Itemset merging: If Y appears in every occurrence of X, then Y is merged with X
  - ❑ *d*-proj. db: {acef, acf} → *acfd*-proj. db: {e}
  - ❑ Final closed itemset: *acfd*:2
- ❑ There are many other tricks developed
  - ❑ For details, see J. Wang, et al., “CLOSET+: Searching for the Best Strategies for Mining Frequent Closed Itemsets”, KDD'03

TID	Items
1	acdef
2	abe
3	cefg
4	acdf

Let minsupport = 2

a:3, c:3, d:2, e:3, f:3

F-List: a-c-e-f-d

The background of the slide is a complex, abstract composition. It features a central white rectangular area where the word 'Summary' is written. This central area is flanked by two large, light gray triangular shapes that point towards the center. The background is further decorated with a grid of small gray plus signs and a network of thin, intersecting lines in shades of brown and orange. Scattered throughout are small, colorful dots in green, blue, and orange. In the top-left corner, there is a horizontal band with a repeating pattern of small, stylized symbols. In the bottom-left corner, there is a small, square inset image showing a cluster of orange and brown dots on a light background, with a grid of plus signs overlaid on it.

# Summary

# Summary: Efficient Pattern Mining Methods

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- ❑ The Downward Closure Property of Frequent Patterns
- ❑ The Apriori Algorithm
- ❑ Extensions or Improvements of Apriori
- ❑ Mining Frequent Patterns by Exploring Vertical Data Format
- ❑ FPGrowth: A Frequent Pattern-Growth Approach
- ❑ Mining Closed Patterns

# Recommended Readings

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- ❑ R. Agrawal and R. Srikant, “Fast algorithms for mining association rules”, VLDB'94
- ❑ A. Savasere, E. Omiecinski, and S. Navathe, “An efficient algorithm for mining association rules in large databases”, VLDB'95
- ❑ J. S. Park, M. S. Chen, and P. S. Yu, “An effective hash-based algorithm for mining association rules”, SIGMOD'95
- ❑ S. Sarawagi, S. Thomas, and R. Agrawal, “Integrating association rule mining with relational database systems: Alternatives and implications”, SIGMOD'98
- ❑ M. J. Zaki, S. Parthasarathy, M. Ogihara, and W. Li, “Parallel algorithm for discovery of association rules”, Data Mining and Knowledge Discovery, 1997
- ❑ J. Han, J. Pei, and Y. Yin, “Mining frequent patterns without candidate generation”, SIGMOD'00
- ❑ M. J. Zaki and Hsiao, “CHARM: An Efficient Algorithm for Closed Itemset Mining”, SDM'02
- ❑ J. Wang, J. Han, and J. Pei, “CLOSET+: Searching for the Best Strategies for Mining Frequent Closed Itemsets”, KDD'03
- ❑ C. C. Aggarwal, M.A., Bhuiyan, M. A. Hasan, “Frequent Pattern Mining Algorithms: A Survey”, in Aggarwal and Han (eds.): Frequent Pattern Mining, Springer, 2014