

**C-3.40**

$$c_1 \log(f(n)) \leq \log_b f(n) \leq c_2 \log(f(n))$$

$$(c_1 \log(f(n)) \leq \frac{\log f(n)}{\log b} \leq c_2 \log(f(n))) \log(b)$$

$$\log(f(n)) \leq \frac{\log f(n)}{\log b} \leq c_2 \log(f(n))$$

**C-3.50**

- a) Use two for/while loops
- b) Store the value of  $x^i$ , multiply it by x after each loop, and update.
- c)  $O(n)$

**R-3.17**

$(n+1)^5 \leq c \cdot n^5$  when  $c > 1$  and  $n \geq n_0 = 1$  so  $(n+1)^5$  is  $O(n^5)$

**C-4.20**

```
def foo(S, k):
    if len(S) <= 1:
        return S
    h = S[0]
    if h <= k:
        return [h] + foo(S[1:], k)
    else:
        return foo(S[1:], k) + [h]
```

The runtime is  $O(n)$ .

**C-4.10**

```
def foo(n, c=-1):
    if n==0:
        return c
    return foo(int(n/2), c+1)
```