

Aufgabe 1

$$t_1 = \sigma(\sigma(x_1, \alpha), \sigma(\gamma(x_3), x_3))$$

$$t_2 = \sigma(\sigma(\gamma(x_2), \alpha), \sigma(x_2, x_3))$$

Aufgabe 1

$$\left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\}$$

Aufgabe 1

$$\begin{array}{l} \left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\} \\ \text{Dekomp.} \\ \Rightarrow \left\{ \begin{pmatrix} \sigma(x_1, \alpha) \\ \sigma(\gamma(x_2), \alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3), x_3) \\ \sigma(x_2, x_3) \end{pmatrix} \right\} \end{array}$$

Aufgabe 1

$$\begin{aligned} & \left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} \sigma(x_1, \alpha) \\ \sigma(\gamma(x_2), \alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3), x_3) \\ \sigma(x_2, x_3) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix}, \begin{pmatrix} x_3 \\ x_3 \end{pmatrix} \right\} \end{aligned}$$

Aufgabe 1

$$\begin{aligned} & \left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} \sigma(x_1, \alpha) \\ \sigma(\gamma(x_2), \alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3), x_3) \\ \sigma(x_2, x_3) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix}, \begin{pmatrix} x_3 \\ x_3 \end{pmatrix} \right\} \\ \text{Elim.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \end{aligned}$$

Aufgabe 1

$$\begin{aligned} & \left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} \sigma(x_1, \alpha) \\ \sigma(\gamma(x_2), \alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3), x_3) \\ \sigma(x_2, x_3) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix}, \begin{pmatrix} x_3 \\ x_3 \end{pmatrix} \right\} \\ \text{Elim.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \end{aligned}$$

Aufgabe 1

$$\begin{aligned} & \left\{ \begin{pmatrix} \sigma(\sigma(x_1, \alpha), & \sigma(\gamma(x_3), x_3)) \\ \sigma(\sigma(\gamma(x_2), \alpha), & \sigma(x_2, x_3)) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} \sigma(x_1, \alpha) \\ \sigma(\gamma(x_2), \alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3), x_3) \\ \sigma(x_2, x_3) \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix}, \begin{pmatrix} x_3 \\ x_3 \end{pmatrix} \right\} \\ \text{Elim.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \\ \text{Dekomp.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \\ \text{Vert.} \Rightarrow & \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \end{aligned}$$

Aufgabe 1 (cont.)

$$\left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\}$$

Aufgabe 1 (cont.)

$$\begin{array}{c} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \\ \text{Subst.} \\ \Rightarrow \left\{ \begin{pmatrix} x_1 \\ \gamma(\gamma(x_3)) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \end{array}$$

Aufgabe 1 (cont.)

$$\begin{array}{c} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \\ \text{Subst.} \\ \Rightarrow \left\{ \begin{pmatrix} x_1 \\ \gamma(\gamma(x_3)) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \end{array}$$

$$x_1 \mapsto \gamma(\gamma(x_3))$$

$$x_2 \mapsto \gamma(x_3)$$

$$x_3 \mapsto x_3$$

Aufgabe 1 (cont.)

$$\begin{array}{c} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \\ \text{Subst.} \\ \Rightarrow \left\{ \begin{pmatrix} x_1 \\ \gamma(\gamma(x_3)) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \end{array}$$

$$x_1 \mapsto \gamma(\gamma(x_3))$$

$$x_2 \mapsto \gamma(x_3)$$

$$x_3 \mapsto x_3$$

Zwei weitere Unifikatoren:

$$x_1 \mapsto \gamma(\gamma(\alpha))$$

$$x_2 \mapsto \gamma(\alpha)$$

$$x_3 \mapsto \alpha$$

$$x_1 \mapsto \gamma(\gamma(\sigma(\alpha, \alpha)))$$

$$x_2 \mapsto \gamma(\sigma(\alpha, \alpha))$$

$$x_3 \mapsto \sigma(\alpha, \alpha)$$