

# EB – 12 Homogeneous Reactions

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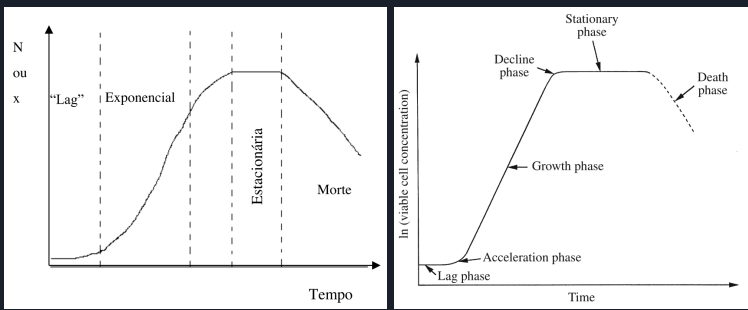
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## 12.8 Bioreactor Kinetics

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# 12.8.1 Batch Growth

When cells are grown in batch culture, **several phases** of cell growth are observed. The different phases of growth are more **readily distinguished** when the **logarithm of viable cell concentration is plotted against time**



Phase	Specific growth rate	Description
Lag	$\mu \approx 0$	Cells adapting to new environment
Acceleration	$\mu < \mu_{\max}$	Cell population starts growing
Growth	$\mu \approx \mu_{\max}$	Growth achieve maximum rate
Decline	$\mu < \mu_{\max}$	Culture reaches limitant in nutrients or build-up of products
Stationary	$\mu = 0$	Cell death and birth equalize
Death	$\mu < 0$	Cells dying faster than they can multiply

Growth rate:  $r_X = \frac{dx}{dt} = \mu x$

## Growth rate

The cell growth rate ( $r_X$ ) measures the change in volumetric concentration of viable cells (unit ( $x$ ) = g/m<sup>3</sup>)

$$r_X = \frac{dx}{dt} = \mu x \implies \Delta \ln x = \mu t \quad (12.1)$$

$\dim x = \text{M/L}^3; \quad \dim \mu = \text{T}^{-1}$

**Doubling time  $t_d$**  Cell growth rates are often expressed in terms of the time it takes to duplicate the population.

$$x = 2 x_0 : t = t_d = \frac{\log 2}{\mu} \quad (12.2)$$

$$t_d \implies \Delta \ln x = \ln \frac{x}{x_0} = \ln \frac{2 x_0}{x_0} = \ln 2 = \mu t_d$$

## 12.8.2 Balanced Growth

In an environment favourable for growth, cells regulate their metabolism and adjust the rates of various internal reactions so that a condition of balanced growth occurs. During balanced growth, **the composition of the biomass remains constant**. For the biomass composition to remain constant during growth, the specific rate of production of each component in the culture must be equal to the cell specific growth rate  $\mu$ .

In most cultures, balanced growth occurs at the same time as exponential growth.

$$r_P = \mu p \quad (12.3)$$

Another point is that the cell consumption is also constant

$$\frac{dx}{dt} = r_X$$

### 12.8.3 Effect of Substrate Concentration

During the growth and decline phases of batch culture, the specific growth rate of the cells depends on the concentration of nutrientes in the medium.

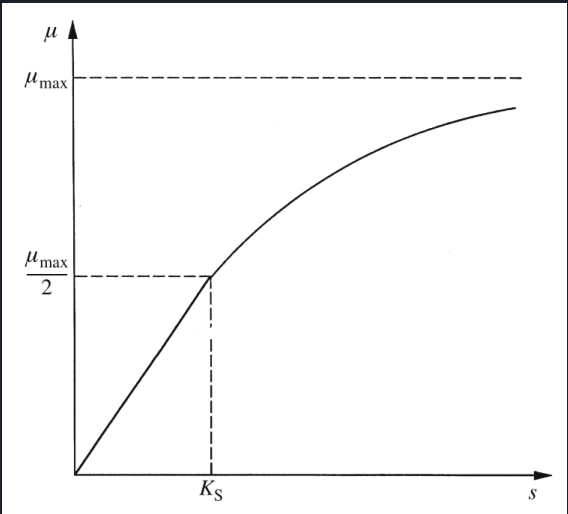
Often a single substrate exerts a dominant influence on the rate of growth; this component is know as the growth-rate-limiting substrate (S).

During balanced growth, the specific growth rate is related to the concentration of the growth limiting substrate by a homologue of the Michaelis–Menten expression, the Monod equation:

$$\mu = \frac{\mu_{\max} s}{K_S + s} = \frac{\mu_{\max}}{1 + K_S/s}$$

$\dim s = \frac{\text{M (S)}}{\text{L}^3}$

(12.4)



#### Rate behavious based on concentration of substrate

if  $\mu$  is dependent on the substrate concentration as indicated by the Monod equation, how can  $\mu$  remain constant during the growth phase? Typical values for the substrate constant ( $K_S$ ) are very small in order of mg/L for carbonhydrate substrates and  $\mu\text{g/L}$  for other compounds such as aminoacids.

The behaviour of specific growth rate ( $\mu$ ) with the concentration of substrate in relation to the substrate constant  $K_S$  follows:

Growth	$s \gtrsim K_S 10$	$\implies \mu \approx \mu_{\max}$
Decline Start	$s \in K_S * [10, 1]$	$\implies \mu = \mu_{\max}/(1 + K_S/s)$
Decline	$s \approx K_S$	$\implies \mu \approx \mu_{\max}/2$
Decline End	$s < K_S$	$\implies \mu = \mu_{\max}/(1 + K_S/s)$
Statinoary	$s \ll K_S$	$\implies \mu \approx 0$

Some examples for the substrate constant  $K_S$ :

Microoragnism (genus)	Limiting Substrate	$K_S/(\text{mg/L})$
<i>Saccgaromyces</i>	Glucose	25
<i>Escherichia</i>	Glucose	4.0
	Lactose	20
	Phosphate	1.6
<i>Aspergillus</i>	Glucose	5.0
<i>Candida</i>	Glycerol	4.5
	Oxygen	0.042 $\rightarrow$ 0.45
<i>Pseudomonas</i>	Methanol	0.7
	Methane	0.4
<i>Klebsiella</i>	Carbon dioxide	0.4
	Magnesium	0.56
	Potassium	0.39
	Sulphate	2.7
<i>Hansenula</i>	Methanol	120.0
	Ribose	3.0
<i>Cryptococcus</i>	Thiamine	1.4 E <sup>-7</sup>

#### Limit of Monod equation

The Monod equation is by far the most frequently used expression relating to growth rate to substrate concentration. However, it is **valid only for balanced growth** and should not be applied when growth conditions are changing rapidly. There are also other restrictions; for example, the Monod equations has been found to have limited applicability at **extremely low substrate levels**. **When growth is inhibited by high substrate or product concentrations, extra terms can be added to the Monod equation** to account for these effects. Several other kinetic expressions has been developed for cell growth these provide better correlations for experimental data in certain situations

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# 12.10 Production Kinetics in Cell Culture

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# Rate of Product Formation

$$r_P = q_P x \quad (12.5)$$

$$\dim r_P = \frac{\text{M/L}^3}{\text{T}}; \quad \dim x = \text{M (B)/L}^3; \quad \dim q_P = \frac{1}{\text{T}}$$

$r_P$  is the volumetric rate of production formation

$x$  is the biomass concentration

$q_P$  is the *specific rate of product formation*

## Production rate $q_P$

- can be evaluated at any time during fermentation as the **ratio of the production rate and biomass concentration**.
- Is **not necessarily constant** during batch culture
- We can develop equations for  $q_P$  as a **function of growth rate and other metabolic parameters** (Depending on whether the product is linked to energy metabolism or not)



## 12.10.1 Product Formation Directly Coupled with Energy Metabolism

For products formed using pathways that generate ATP, the **rate of production is related to the cellular energy demand**. Growth is usually the major energy-requiring function of cells; therefore, if production is coupled to energy metabolism, product will be formed whenever there is growth. However, ATP is also required for other activities called *maintenance*. **Maintenance activities are carried out by living cells even in the absence of growth. Products synthesised in energy pathways will be produced whenever maintenance functions are carried out** because ATP is required.

Examples of maintenance:

- Cell motility
- Turnover of cellular components
- Adjustment of membrane potential and internal pH

Kinetic expressions for the rate of product formation must account for growth-associated and maintenance-associated production, as in the following equation

$$r_P = Y_{PX} r_X + m_P x \quad (12.6)$$

$$\dim m_P = \frac{1}{\text{TM (B)}}$$

$r_X$  is the volumetric rate of biomass formation.

$Y_{PX}$  is the theoretical or true yield of product from biomass

$m_P$  is the *specific rate of product formation due to maintenance*

$x$  is the biomass concentration

$$q_P = Y_{PX} \mu + m_P \quad (12.7)$$

Using (12.6), (12.5) and (12.1)

$$q_P = \frac{r_P}{x} = \frac{Y_{PX} r_X + m_P x}{x} = \frac{Y_{PX} (\mu x) + m_P x}{x} = Y_{PX} \mu + m_P$$

## 12.10.3 Product Formation **Not** Coupled with Energy Metabolism

Production not involving energy metabolism is difficult to relate to growth because growth and product synthesis are somewhat dissociated. However, **in some cases**, the rate of formation of nongrowth-associated products is directly proportional to biomass concentration, so that **the production rate defined in (12.5) can be applied with constant  $q_P$** . Sometimes  $q_P$  is a complex function of the growth rate and must be expressed using empirical equations derived from experiment.