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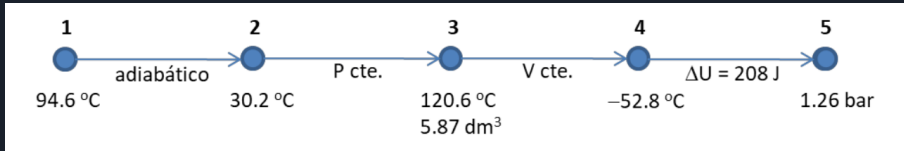
9 de janeiro de 2023

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# I – Teste 2019.2.1

# Questão 1



Considere que submete 1 mol de um gás perfeito ( $C_V = R 5/2$ ) ao processo reversível representado.

Q1 a)

Calcule o trabalho posto em jogo no percurso 2→3.

$$\begin{aligned} W_{(30.2 \rightarrow 120.6)^{\circ}\text{C} P_{\text{cnt}}} &= \int_{Vol_1}^{Vol_2} P_{\text{ext}} dVol = P_{\text{ext}} \int_{Vol_1}^{Vol_2} dVol = P_{\text{ext}} \Delta Vol \Big|_{Vol_1}^{Vol_2} = \\ &= P_{\text{ext}} (Vol_2 - Vol_1) = P_{\text{ext}} \left( \frac{n R T_2}{P_2} - \frac{n R T_1}{P_1} \right) = n R (T_2 - T_1) = \\ &= (1) (8.314) ((120.6 + 273.15) - (30.2 + 273.15)) \cong 751.627 \end{aligned}$$

## Q1 b)

Calcule o trabalho e o calor postos em jogo no percurso 3→4.

(i)

$$W$$

$$W_{vol_{cnt}} = 0$$

(ii)

$$Q$$

$$\begin{aligned} Q_{vol_{cnt}, (120.6 \rightarrow -52.8)^\circ\text{C}} &= \int_{T_3}^{T_4} n C_v \, dT = n C_v \int_{T_3}^{T_4} dT = n C_v \Delta T \Big|_{T_3}^{T_4} = \\ &= (1) (8.314 * 5/2) ((-52.8 + 273.15) - (120.6 + 273.15)) \cong -3.604 \text{ E3} \end{aligned}$$

## Q1 c)

Calcule a pressão do gás no estado 1.

$$\begin{aligned}
 P_1 &= \frac{n R T_1}{vol_1} = \frac{n R T_1}{vol_1} = \frac{n R T_1}{vol_2 \sqrt[3]{P_2/P_1}} = \frac{n R T_1}{\left(\frac{n R T_2}{P_2}\right) (P_3/P_1)^{C_v/C_P}} = \\
 &= \frac{T_1}{T_2 P_3^{-1} (P_3/P_1)^{5/7}} = \frac{T_1 P_1^{5/7}}{T_2 P_3^{5/7-1}} \Rightarrow P_1 = \left( \frac{T_1}{T_2 \left(\frac{n R T_3}{vol_3}\right)^{5/7-1}} \right)^{1/(1-5/7)} = \\
 &= \left( \frac{T_1}{T_2} \right)^{1/(1-5/7)} \frac{n R T_3}{vol_3} = \left( \frac{94.6 + 273.15}{30.2 + 273.15} \right)^{7/2} \frac{(1) (8.314) (120.6 + 273.15)}{5.87 \text{ E } -6} \cong \\
 &\cong 1.094 \text{ E}9
 \end{aligned}$$

# Q1 d)

Calcule  $\Delta S_{viz}$  para o percurso 4→5.

$$\begin{aligned}
 \Delta S_{viz} &= -\Delta S = -\left(\int n C_V \frac{dT}{T} + n R \ln \frac{V_5}{V_4}\right) = -\int_{T_4}^{T_5} n C_V \frac{dT}{T} - n R \ln \frac{V_f}{V_i} = \\
 &= -n C_v \ln \frac{T_5}{T_4} - n R \ln \frac{(n R T_5/P_5)}{V_4} = \\
 &= -n C_v \ln \left(\frac{\frac{\Delta U}{n C_v} + T_4}{T_4}\right) - n R \ln \frac{n R \left(\frac{\Delta U}{n C_v} + T_4\right)}{V_4 P_5} = \\
 &= -n C_v \ln \left(\frac{\Delta U}{n C_v T_4} + 1\right) - n R \ln \frac{R \left(\frac{\Delta U}{C_v} + T_4\right)}{V_4 P_5} = \\
 &= -(1)(8.314 * 5/2) \ln \left(\frac{208}{(1)(8.314 * 5/2)(-52.8 + 273.15)} + 1\right) + \\
 &\quad - (1)(8.314) \ln \frac{(8.314) \left(\frac{208}{8.314*5/2} + (-52.8 + 273.15)\right)}{(5.87 \text{ E } -3)(1.26 \text{ E } 5)} \cong -8.8
 \end{aligned}$$

**Nota:** N aguento mais esses calculos, fazer com variáveis intermediárias é menos preciso porem mais fácil

## Q2 a)

Calcule a variação de energia interna associada à passagem da água gasosa, a 138.9°C e 1.01 bar, a água sólida, a 0°C e 1.01 bar.

$$\begin{aligned}
 \Delta U_{\text{H}_2\text{O}(\text{g}) \rightarrow (\text{s}), (138.9 \rightarrow 0)^\circ\text{C}, 1.01\text{bar}} & \stackrel{P_{\text{cnt}}}{=} \Delta H - P \Delta V = \\
 & = \left( \begin{array}{l} \Delta H_{\text{H}_2\text{O}(\text{s}), (138.9 \rightarrow 100)^\circ\text{C}} \\ + \Delta H_{\text{H}_2\text{O}(\text{s}) \rightarrow (\text{l}), 100^\circ\text{C}} \\ + \Delta H_{\text{H}_2\text{O}(\text{l}), (100 \rightarrow 0)^\circ\text{C}} \\ + \Delta H_{\text{H}_2\text{O}(\text{l}) \rightarrow (\text{s}), 0^\circ\text{C}} \end{array} \right) - P(V_f - V_i) = \\
 & = \left( \begin{array}{l} n C_{p,(\text{g})}((100 + 273.15) - (138.9 + 273.15)) \\ + n(-\Delta H_{\text{vap}}) \\ + n C_{p,(\text{l})}((0 + 273.15) - (100 + 273.15)) \\ + n(-\Delta H_{\text{fus}}) \end{array} \right) - P \left( \frac{n}{M} \rho_{(\text{s})} - \frac{n R T_i}{P_i} \right) = \\
 & = n \left( \begin{array}{l} C_{p,(\text{g})}(100 - 138.9) \\ + (-\Delta H_{\text{vap}}) \\ + C_{p,(\text{l})}(-100) \\ + (-\Delta H_{\text{fus}}) \end{array} \right) - n \left( \frac{P \rho_{(\text{s})}}{M} - R T_i \right) \cong \\
 & \cong n \left( \begin{array}{l} (36)(100 - 138.9) \\ + (-40.7 \text{ E } 3) \\ + (75)(-100) \\ + (-6.01 \text{ E } 3) \end{array} \right) - n \left( \frac{1.01 \text{ E } 5 * 18}{0.92 \text{ E } 6} - 8.314(138.9 + 273.15) \right) \cong \\
 & \cong (n) - 52.186 \text{ E } 3
 \end{aligned}$$



Q2 b)

Calcule o trabalho máximo associado à transformação da alínea anterior.

$$\begin{aligned}
 \max W &= \Delta A = \Delta U - \Delta(TS) = \Delta U - (T_f S_f - T_i S_i) = \Delta U - T_f S_f + T_i S_i = \\
 &= \Delta U - T_f (S_{(l),25^\circ\text{C},1\text{bar}} + \Delta S_{((l),25^\circ\text{C},1\text{bar}) \rightarrow f}) + \\
 &+ T_i (S_{(l),25^\circ\text{C},1\text{bar}} + \Delta S_{((l),25^\circ\text{C},1\text{bar}) \rightarrow i}) = \\
 &= \Delta U - T_f \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \Delta S_{((l),25^\circ\text{C},1\text{bar}) \rightarrow f} \end{array} \right) + T_i \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \Delta S_{((l),25^\circ\text{C},1\text{bar}) \rightarrow i} \end{array} \right) = \\
 &= \Delta U - T_f \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \Delta S_{(l),(25 \rightarrow 0)^\circ\text{C}} \\ + \Delta S_{(l \rightarrow s),0^\circ\text{C}} \end{array} \right) + T_i \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \Delta S_{(l),(25 \rightarrow 100)^\circ\text{C}} \\ + \Delta S_{(l \rightarrow g),100^\circ\text{C}} \\ + \Delta S_{(g),(100 \rightarrow 138.9)^\circ\text{C}} \end{array} \right) = \\
 &\stackrel{P_{\text{cnt}}}{=} \Delta U - T_f \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \int C_{p,(l)} \frac{dT}{T} \\ + (-\Delta H_{fus})/T \end{array} \right) + T_i \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + \int C_{p,(l)} \frac{dT}{T} \\ + \Delta H_{vap}/T \\ + \int C_{p,(g)} \frac{dT}{T} \end{array} \right) = \\
 &= \Delta U - T_f \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + C_{p,(l)} \ln \frac{0 + 273.15}{25 + 273.15} \\ + (-\Delta H_{fus})/T \end{array} \right) + T_i \left( \begin{array}{c} S_{(l),25^\circ\text{C},1\text{bar}} \\ + C_{p,(l)} \ln \frac{100 + 273.15}{25 + 273.15} \\ + \Delta H_{vap}/T \\ + C_{p,(g)} \ln \frac{138.9 + 273.15}{100 + 273.15} \end{array} \right) \cong
 \end{aligned}$$

Q2 c)

Em que medida a 3a lei da Termodinâmica complementa o sentido da 2a lei?

# I – Teste 2022.2.1

# Questão 1

Considere que tem 1 mol de um gás perfeito ( $C_V = 5/2R$ ). Na figura estão representados estados deste gás (1, 2, 3 e 4) e transições reversíveis entre eles.  $P_1 = 4.0 \text{ bar}$ ,  $T_1 = 293.15 \text{ K}$ ,  $T_4 = 197.27 \text{ K}$ , as transições  $2 \rightarrow 3$  e  $4 \rightarrow 1$  são adiabáticas, o calor envolvido na transição  $1 \rightarrow 2$  é de  $5466 \text{ J}$ , e o calor envolvido na transição  $3 \rightarrow 4$  é de  $-4100 \text{ J}$ .

- $n = 1 \text{ mol}$

- $T_1 = 293.15 \text{ K}$

- $4 \rightarrow 1$ : Adiabática

- $C_V = 5/2R$

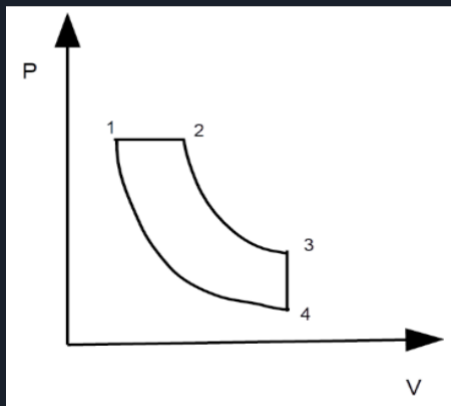
- $T_4 = 197.27 \text{ K}$

- $\Delta H_{1 \rightarrow 2} = +5466 \text{ J}$

- $P_1 = 4.0 \text{ bar}$

- $2 \rightarrow 3$ : Adiabática

- $\Delta H_{3 \rightarrow 4} = -4100 \text{ J}$



Q1 a)

Calcule  $T_2$

$$\int_1^2 n C_P dT = n (C_V + R) \Delta T = \Delta H_{1 \rightarrow 2} = Q_{1 \rightarrow 2} \implies$$

$$\implies T_2 = T_1 + \frac{Q_{1 \rightarrow 2}}{n (C_V + R)} \cong 293.15 + \frac{5466}{1 * 3.5 * 8.31} \cong 480.98$$

## Q1 b)

Calcole  $T_3$  e  $V_3$

(i)  $T_3$

$$\int_{3 \rightarrow 4} n C_V dT = n (C_P + R) (T_4 - T_3) = Q_{3 \rightarrow 4} \implies$$

$$\implies T_3 = T_4 - \frac{Q_{3 \rightarrow 4}}{n (C_V)} \cong 197.27 - \frac{-4100}{1 * 2.5 * 8.31} \cong 394.52$$

(ii)  $V_3$

$$P_3 V_3^\gamma = \left( \frac{n R T_3}{V_3} \right) V_3^{C_P/C_V} = n R T_3 V_3^{1.4-1} = n R T_3 V_3^{0.4} \stackrel{2 \rightarrow 3}{\underset{\text{adiab. rev.}}{=}}$$

$$= P_2 V_2^\gamma = P_1 \left( \frac{n R T_2}{P_2} \right)^{1.4} = \frac{n^{1.4} R^{1.4} T_2^{1.4}}{P_1^{1.4-1}} \implies$$

$$\implies V_3 = \left( \frac{n^{0.4} R^{0.4} T_2^{1.4}}{P_1^{0.4} T_3} \right)^{1/0.4} = \frac{n R T_2^{3.5}}{P_1 T_3^{2.5}} \cong \frac{1 * 8.31 * (480.98)^{3.5}}{4.0 * 10^5 * (394.52)^{2.5}} \cong 16.41 \text{ E-3}$$

Q1 c)

Calcule  $W_{4 \rightarrow 1}$

$$\begin{aligned} W_{4 \rightarrow 1} + Q_{4 \rightarrow 1} &= W_{4 \rightarrow 1} = \Delta U_{4 \rightarrow 1} = \int_4^1 n C_V dT = n C_V \Delta T \cong \\ &\cong 1 * 2.5 * 8.31(293.15 - 197.27) \cong 1.99 \text{ E3} \end{aligned}$$

Q1 d)

Calcule  $\Delta S_{viz}$  no processo  $1 \rightarrow 4 \rightarrow 3$ . (se não resolveu b, considere  $T_3 = 400 \text{ K}$ )

$$\begin{aligned}\Delta S_{viz,1 \rightarrow 4 \rightarrow 3} &= -\Delta S_{1 \rightarrow 3} = -\left(\int_1^3 n C_P \, dT/T + n R \ln(P_1/P_3)\right) = \\ &= -n 3.5 R \ln(T_3/T_1) - n R \ln \frac{P_1}{\left(\frac{n R T_3}{V_3}\right)} = -n R \left(3.5 \ln(T_3/T_1) + \ln \frac{P_1}{\left(\frac{n R T_3}{V_3}\right)}\right) \cong \\ &\cong 8.31 \left(-3.5 \ln \left(\frac{394.52}{283.15}\right) - \ln \frac{4.0 * 10^5}{\left(\frac{8.31 * 394.52}{16.41 \text{ E-}3}\right)}\right) \cong -15.42\end{aligned}$$



Q1 e)

Imagine uma transição isotérmica reversível (realizada a  $T_4$ ) entre o estado 4 e um estado 5, com  $W_{4 \rightarrow 5} = -3986 \text{ J}$ . Calcule  $V_5$ . (se não resolveu b, considere  $T_3 = 400 \text{ K}$  e  $V_3 = 15.0 \text{ dm}^3$ )

$$\begin{aligned} -n R T_4 \ln(V_5/V_4) &= W_{4 \rightarrow 5} \implies V_5 = V_4 \exp\left(-\frac{W_{4 \rightarrow 5}}{n R T_4}\right) \cong \\ &\cong 16.41 \text{ E-3} * \exp\left(-\frac{-3986}{1 * 8.31 * 197.27}\right) \cong 186.42 \text{ E-3} \end{aligned}$$

## Q1 f)

(i)

Imagine uma forma de levar o gás de 1 a 3 de forma irreversível. Represente graficamente essa transição, bem como o trabalho associado.

(ii)

O coeficiente de Joule-Thomson do  $H_2$  é negativo. Que consequências, em termos da 1ª Lei da Termodinâmica, poderão existir no desenho de um motor de combustão, quando o  $H_2$  passa através da válvula de saída do depósito a 200K, num processo a entalpia constante?

## Questão 2

- $C_{p,L} = 255.7 \text{ J K}^{-1} \text{ mol}^{-1}$

- $C_{p,G} = 239.0 \text{ J K}^{-1} \text{ mol}^{-1}$

- $\Delta H_{vap,(125.6^\circ\text{C}, 1.01 \text{ bar})} = 41.53 \text{ kJ mol}^{-1}$

- $\alpha_{p,liq} \approx 1.4 * 10^{-3} \text{ K}^{-1}$

- $\rho_{liq} = 0.703 \text{ g cm}^{-3}$

- $M_{(n-octano)} = 114.23 \text{ g mol}^{-1}$

## Q2 a)

Calcule  $\Delta H$  e  $\Delta G$  associados à passagem de 200 g de n-octano do estado (125.6 °C, gás, 0.5 bar) ao estado (125.6 °C, líquido, 100 bar)

(i)

$$\begin{aligned}
 \Delta H &= \\
 &= \left( \begin{array}{c} \Delta H_{gas,(0.5 \rightarrow 1.01) \text{ bar}} \\ + \Delta H_{(gas \rightarrow liq), 1.01 \text{ bar}} \\ + \Delta H_{liq, (1.01 \rightarrow 100) \text{ bar}} \end{array} \right) = \\
 &= \left( \begin{array}{c} 0 \text{ (gas perfeito)} \\ + n \Delta H_{vap} \\ + \int_{P_0}^{P_1} v (1 - \alpha_p T) dP \end{array} \right) = \\
 &= \left( \begin{array}{c} (m/M) \Delta H_{vap} \\ + (m/\rho) (1 - \alpha_p T) (P_1 - P_0) \end{array} \right) = \\
 &= \left( \begin{array}{c} (200/114.23) * 41.53 * 10^3 \\ + \frac{200 * 10^{-3}}{0.703 * 10^3} * (1 - (1.4 * 10^{-3}) * (125.6 + 273.15)) * (100 - 1.01) * 10^5 \end{array} \right) \cong \\
 &\cong 73.96 \text{ EJ}
 \end{aligned}$$

(ii)

$$\begin{aligned}
 \Delta G &= \\
 &= \left( \begin{array}{c} \Delta G_{gas,(0.5 \rightarrow 1.01) \text{ bar}} \\ + \Delta G_{(gas \rightarrow liq), 1.01 \text{ bar}} \\ + \Delta G_{liq, (1.01 \rightarrow 100) \text{ bar}} \end{array} \right) = \\
 &= \left( \begin{array}{c} \int_{P_0}^{P_1} V dP \\ + 0 \\ + \int_{P_1}^{P_2} V dP \end{array} \right) = \\
 &= \left( \begin{array}{c} \int_{P_0}^{P_1} \frac{n R T}{P} dP \\ + V \int_{P_1}^{P_2} dp \text{ (vol liq constante em } \Delta P) \end{array} \right) = \\
 &= \left( \begin{array}{c} (m/M) R T \ln(P_1/P_0) \\ + (m/\rho) (P_2 - P_1) \end{array} \right) = \\
 &= \left( \begin{array}{c} (200/114.23) * 8.31 * (125.6 + 273.15) * \ln(1.01/0.5) \\ + \frac{200 * 10^{-3}}{0.703 * 10^3} * (100 - 1.01) * 10^5 \end{array} \right) \cong \\
 &\cong 6897.53
 \end{aligned}$$

## Q2 b)

Calcule  $\Delta S$  e  $\Delta U$  associados à passagem de 200 g de n-octano do estado (50 °C, líquido, 1.01 bar) ao estado (200 °C, gás, 0.5 bar)

(i)

$$\begin{aligned}
 \Delta S &= \\
 &= \left( \begin{array}{l} \Delta S_{liq, 1.01 \text{ bar}, (50 \rightarrow 125.6)^\circ \text{C}} + \\ + \Delta S_{(liq \rightarrow gas), 1.01 \text{ bar}, 125.6^\circ \text{C}} + \\ + \Delta S_{gas, 1.01 \text{ bar}, (125.6 \rightarrow 200)^\circ \text{C}} + \\ + \Delta S_{gas, (1.01 \rightarrow 0.5) \text{ bar}, 200^\circ \text{C}} \end{array} \right) = \\
 &= \left( \begin{array}{l} \int_{T_0}^{T_1} n C_{p, liq} dT/T + 0 + \\ + n \Delta H_{vap}/T_1 + \\ + \int_{T_1}^{T_2} n C_{p, gas} dT/T + 0 + \\ + 0 + n R \int_{P_2}^{P_3} dP/P \end{array} \right) = \\
 &= \left( \begin{array}{l} n C_{p, liq} \ln(T_1/T_0) + \\ + n \Delta H_{vap}/T_1 + \\ + n C_{p, gas} \ln(T_2/T_1) + \\ + n R \ln(P_3/P_2) \end{array} \right) = \\
 &= \left( \begin{array}{l} 255.7 * \ln \left( \frac{125.6 + 273.15}{50 + 273.15} \right) + \\ + 41.53 * 10^3 / (125.6 + 273.15) + \\ + 239.0 * \ln \left( \frac{200 + 273.15}{125.6 + 273.15} \right) + \\ + 8.31 * \ln(0.5/1.01) \end{array} \right) * (200/114.23) \cong \\
 &\cong 337.82
 \end{aligned}$$

(ii)

$$\begin{aligned}
 \Delta U &= \Delta H - \Delta(PV) = \\
 &= \left( \begin{array}{l} \Delta H_{liq, 1.01 \text{ bar}, (50 \rightarrow 125.6)^\circ \text{C}} + \\ + \Delta H_{(liq \rightarrow gas), 1.01 \text{ bar}, 125.6^\circ \text{C}} + \\ + \Delta H_{gas, 1.01 \text{ bar}, (125.6 \rightarrow 200)^\circ \text{C}} + \\ + \Delta H_{gas, (1.01 \rightarrow 0.5) \text{ bar}, 200^\circ \text{C}} \end{array} \right) - \Delta(PV) = \\
 &= \left( \begin{array}{l} \int_{T_0}^{T_1} n C_{P, l} dT + \\ + n \Delta H_{vap} + \\ + \int_{T_1}^{T_2} n C_{P, g} dT + \\ + 0 \end{array} \right) - (P_3 V_3 - P_0 V_0) = \\
 &= \left( \begin{array}{l} n C_{P, l} (T_1 - T_0) + \\ + n \Delta H_{vap} + \\ + n C_{P, g} (T_2 - T_1) \end{array} \right) - P_3 \left( \frac{n R T_3}{P_3} \right) + P_0 (m/\rho_{liq}) = \\
 &= \left( \begin{array}{l} C_{P, l} (T_1 - T_0) + \\ + \Delta H_{vap} + \\ + C_{P, g} (T_2 - T_1) + \\ - R T_3 + \\ + P_0 M/\rho_{liq} \end{array} \right) (m/M) = \\
 &= \left( \begin{array}{l} 255.7 * (125.6 - 50) + \\ + 41.53 * 10^3 + \\ + 239.0 * (200 - 125.6) + \\ - 8.31 * (200 + 273.15) + \\ + 1.01 * 114.23 / (0.703 * 10^6) \end{array} \right) (200/114.23) \cong \\
 &\cong 130\,803.70
 \end{aligned}$$