Algoritmos e Estruturas de Dados III

Aula 3.3 intercalação por substituição

Prof. Hayala Curto 2022



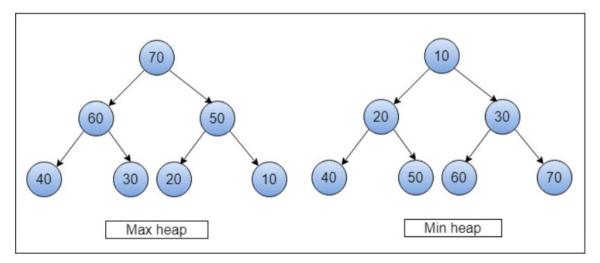
Estratégia 2 Intercalação por Substituição



Intercalação com seleção por substituição

A segunda estratégia de otimização é de gerar segmentos ordenados maiores na fase de distribuição

Requer o uso de uma fila de prioridades, como um heap.

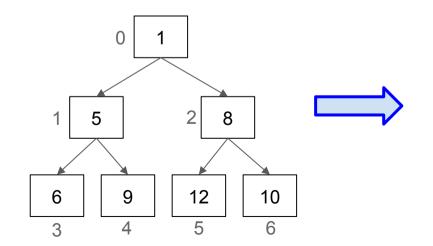


Intercalação com seleção por substituição

0	1	2	3	4	5	6
1	5	8	6	9	12	10

Operações:

- Inserir novo elemento (na raiz e afundá-lo)
- Remover a raiz (colocar o último elemento lá e afundá-lo)



$$filhoesquerdo(i) = i * 2 + 1$$

$$filhodireito(i) = i * 2 + 2$$

$$pai(i) = int((i-1)/2)$$

Intercalação com seleção por substituição

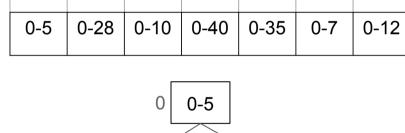
Arquivo a ser ordenado:

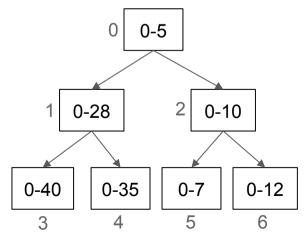
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

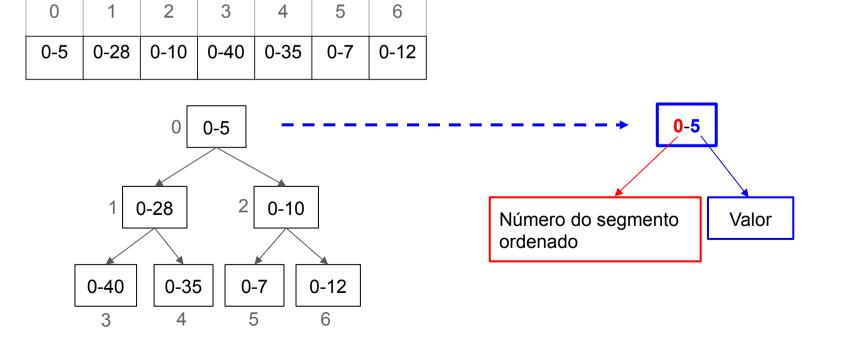
Passo 1: Preenchimento do heap

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

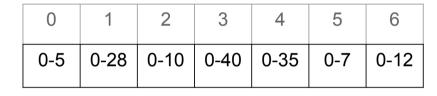


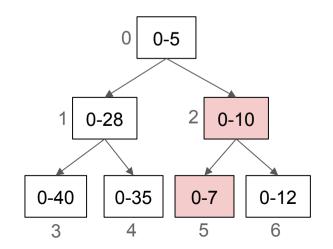


0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



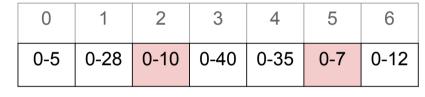
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

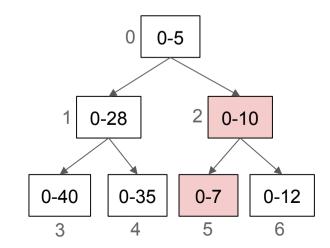




Passo 2: Organização do Heap

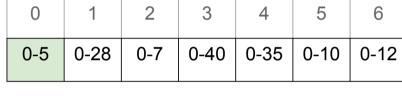
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



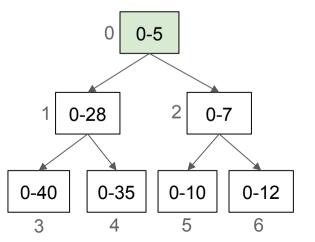


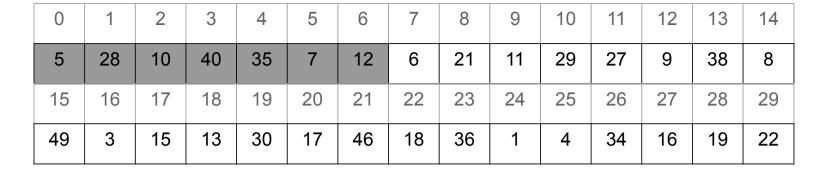
Da posição (n-1)/2, que representa o primeiro pai, até a posição 0, afundar cada elemento.

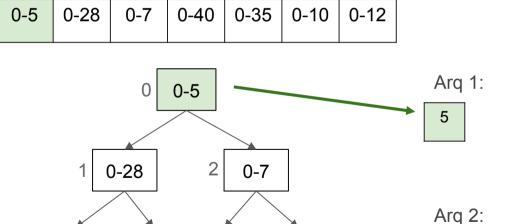
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



Heap organizado: Retira o menor elemento! Saídas:







0-10

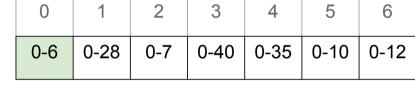
0-12

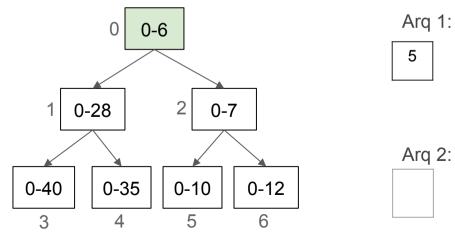
0-35

0-40

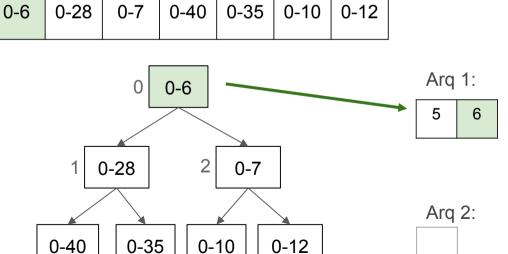
Heap organizado: Retira o menor elemento! Saídas:





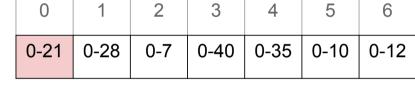


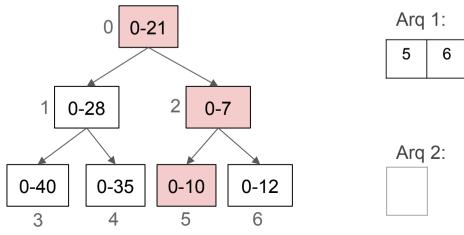


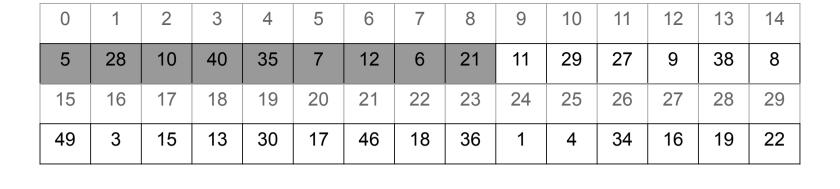


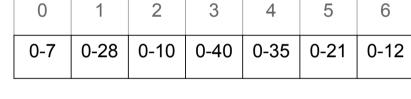
Heap organizado: Retira o menor elemento! Saídas:

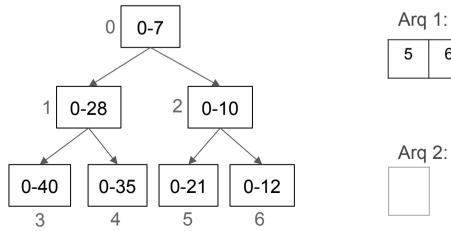


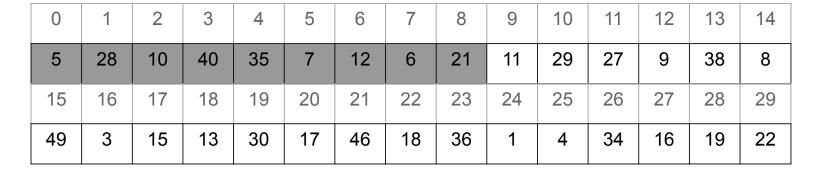


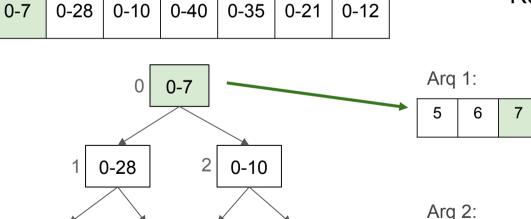




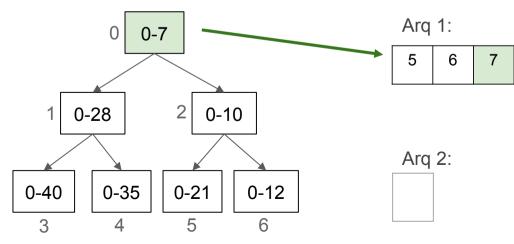


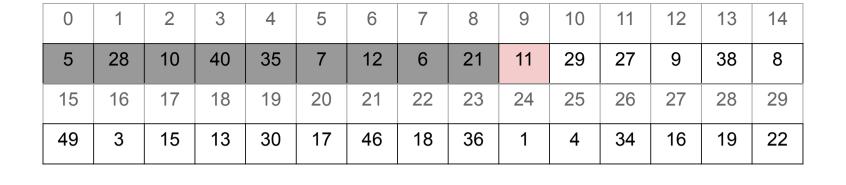


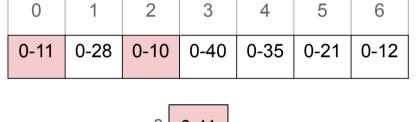


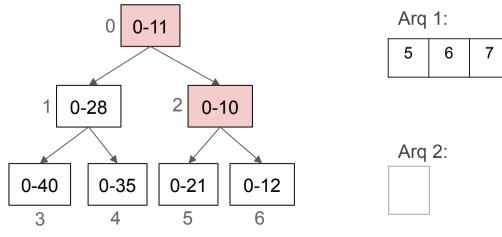


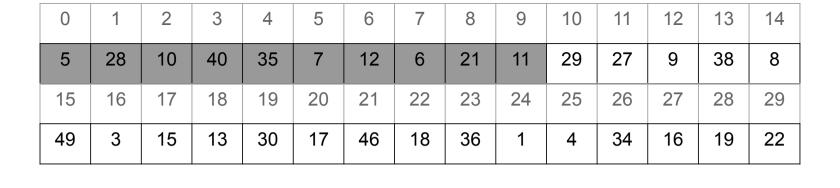
Heap organizado: Retira o menor elemento! Saídas:

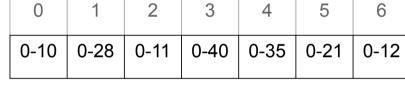


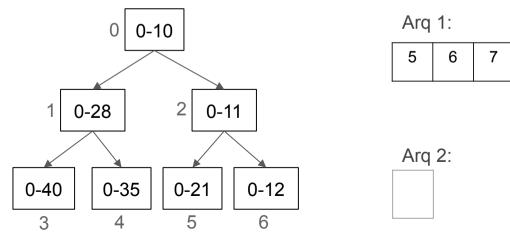




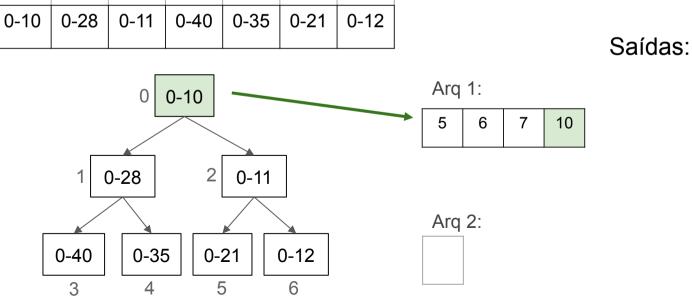


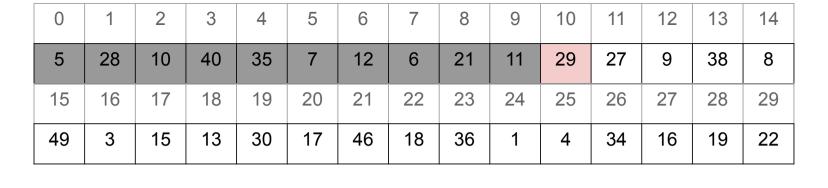


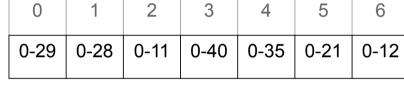


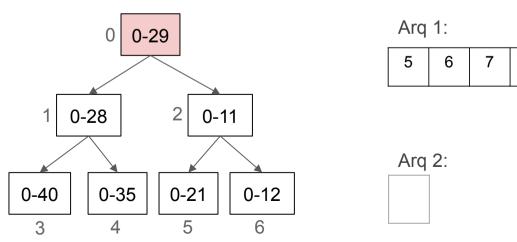






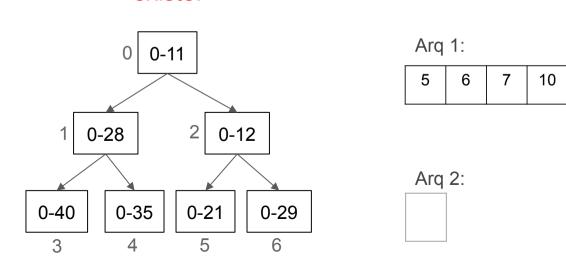




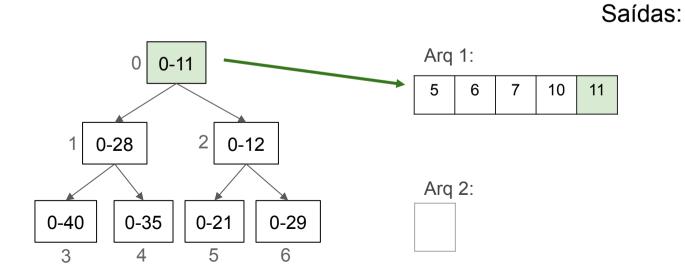


0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

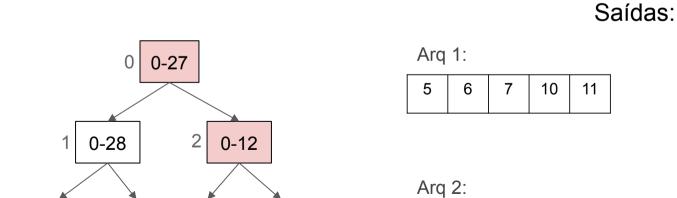
Estou retirando o vetor, mas ele existe!











0-29

6

0-40

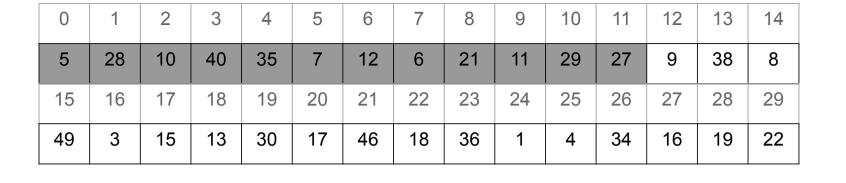
3

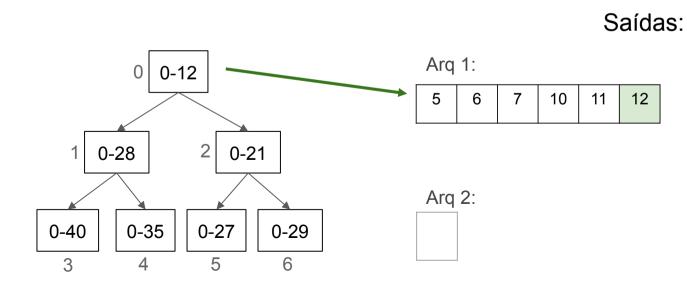
0-35

4

0-21

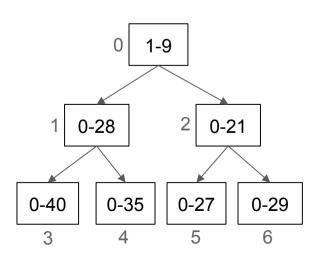
5











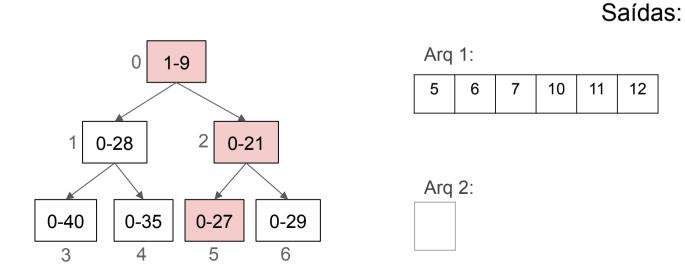


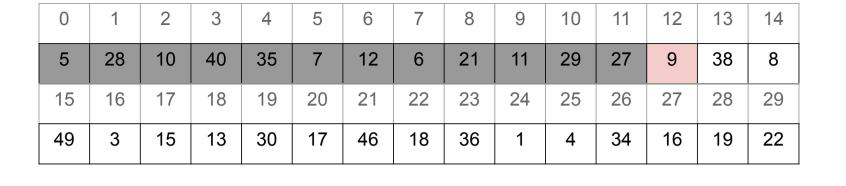
5 6 7 10 11 12

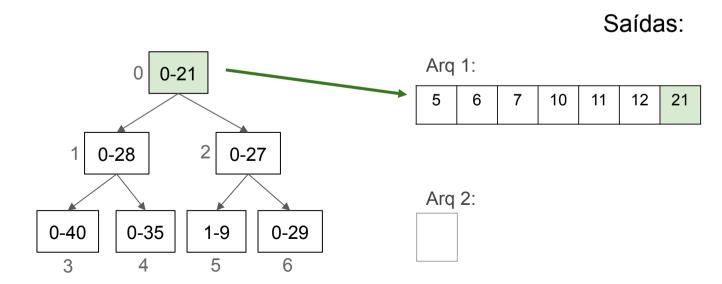
9 < 12

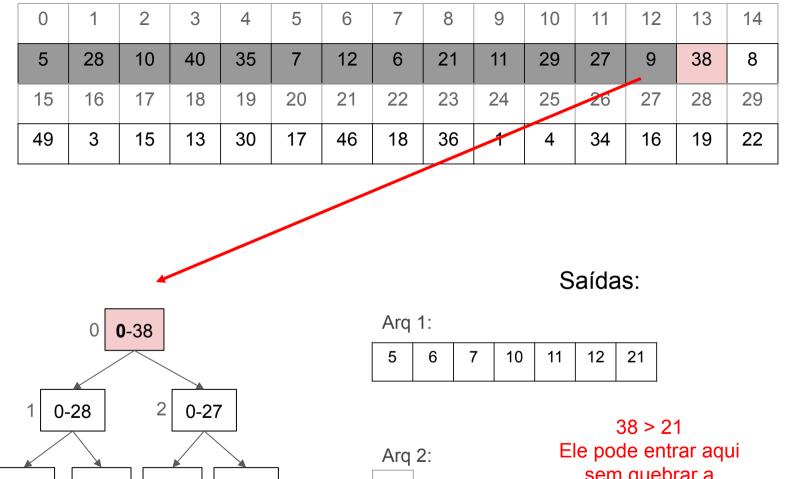
Arq 2: Se ele entrar aqui, o segmento ordenado é finalizado





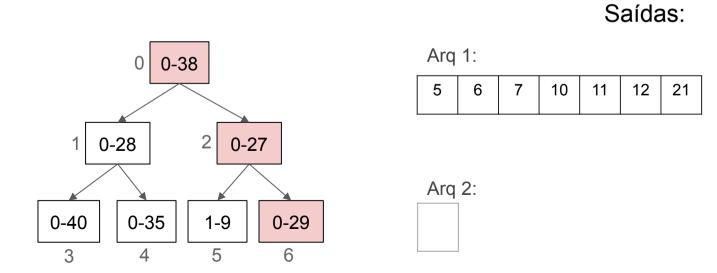


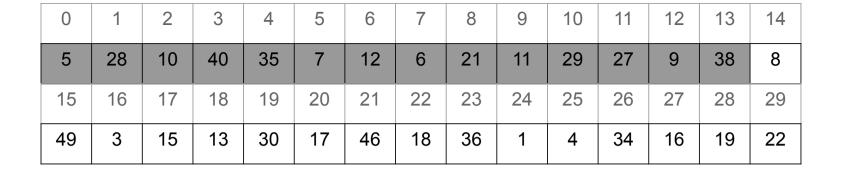


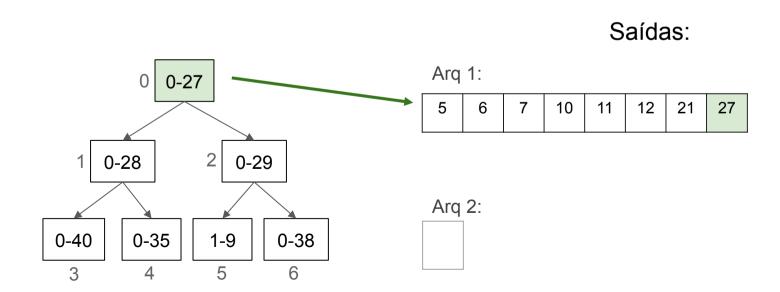


sem quebrar a 0-40 0-35 1-9 0-29 ordenação do segmento 3 4 5 6

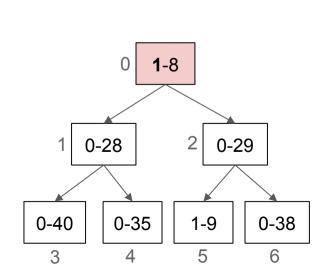






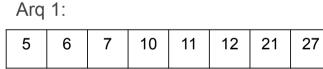




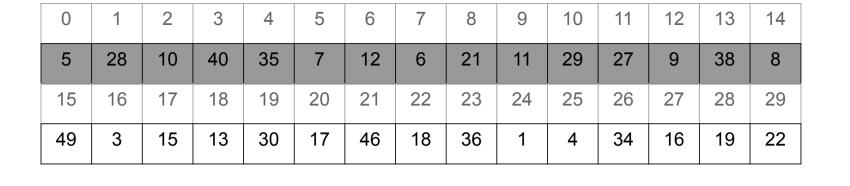


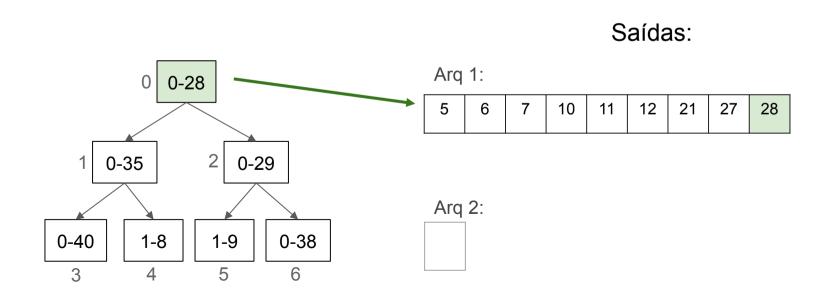


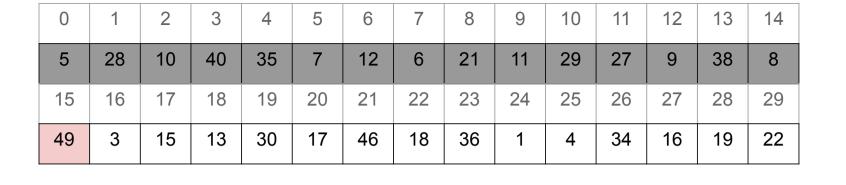
Arq 2:

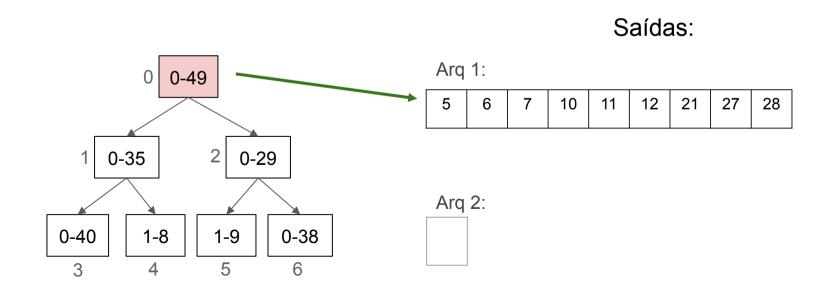


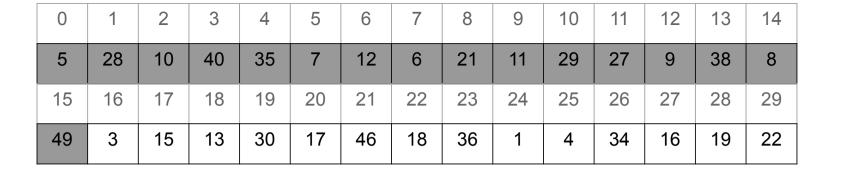
8 < 27 Se ele entrar aqui, o segmento ordenado é finalizado

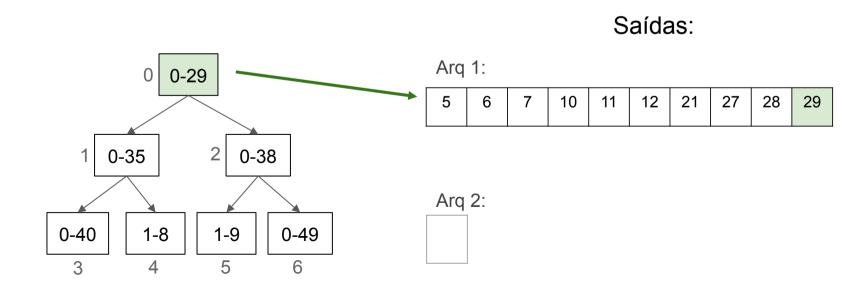


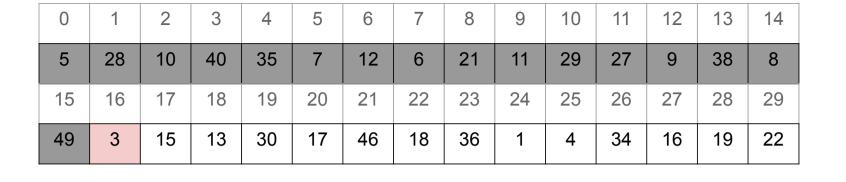


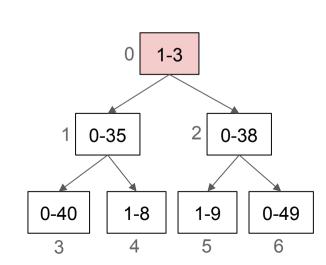












Arq 1:





Arq 2:







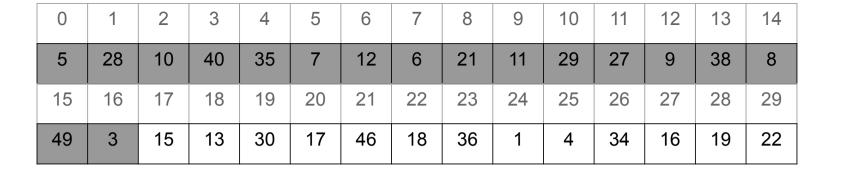


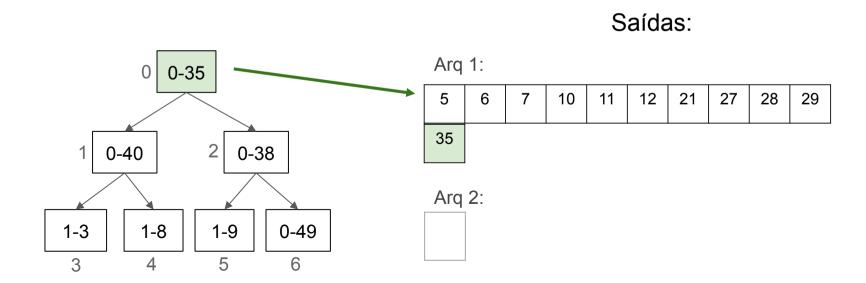


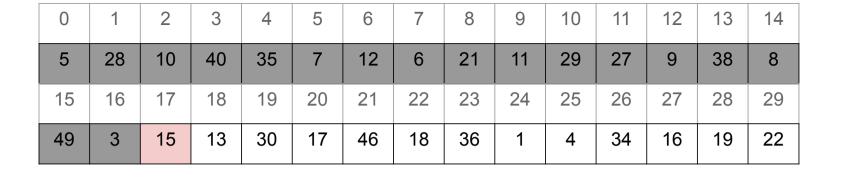


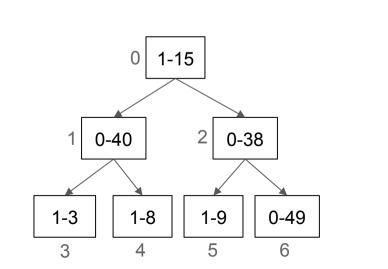


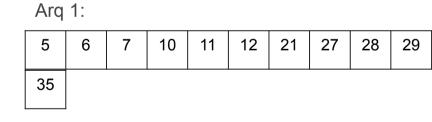






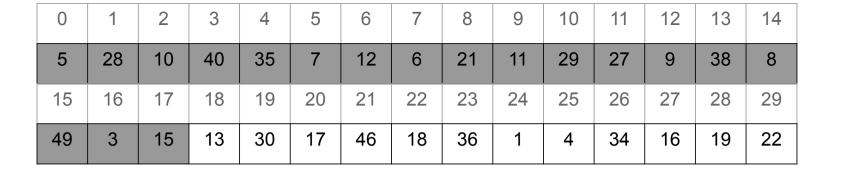


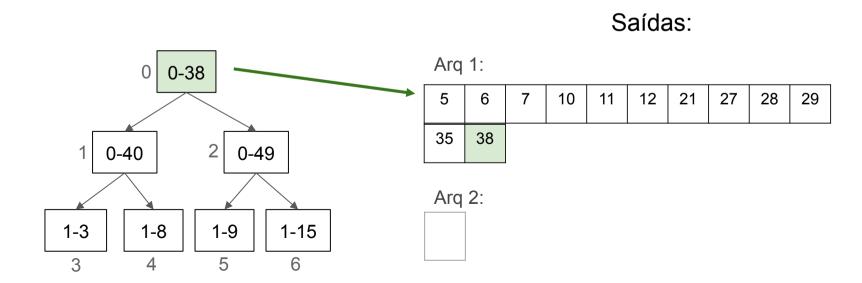


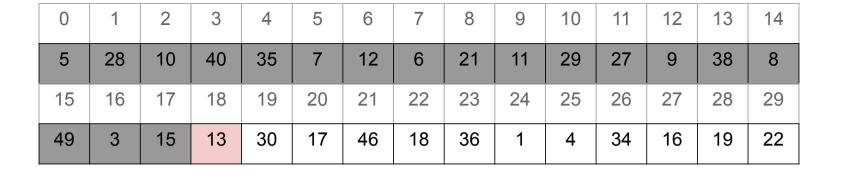


Saídas:

Arq 2:









1-13

2

1-9

5

0

1-8

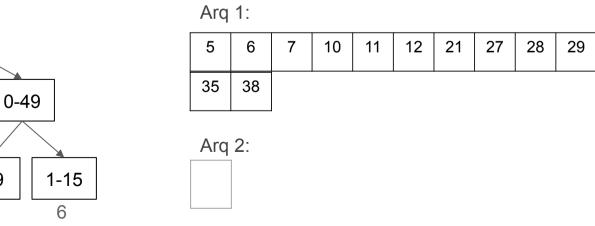
4

0-40

1

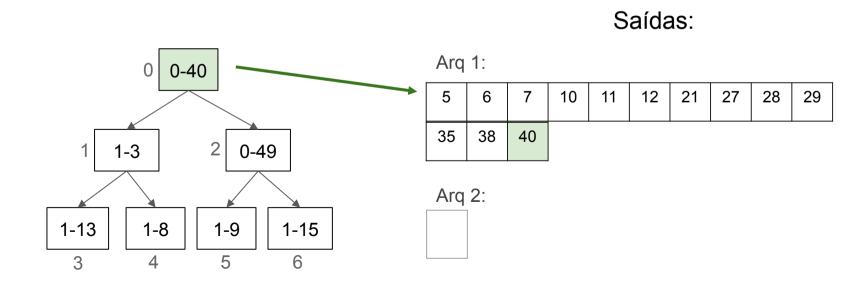
1-3

3



Saídas:









1-30

1-9

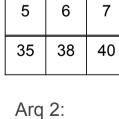
0-49

1-15

1-8

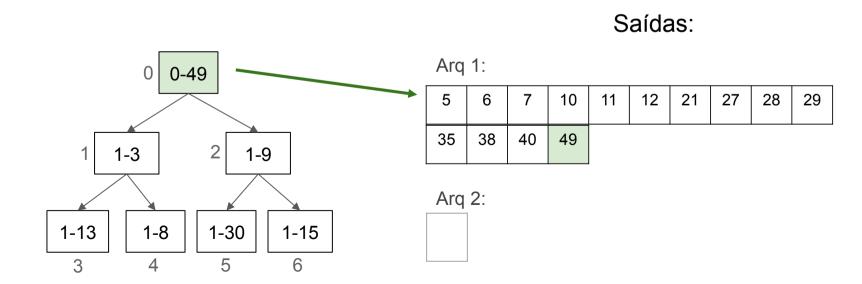
1-3

1-13



Saídas:







. .

1-17

2

1-30

5

1-9

1-15

6

0

1-8

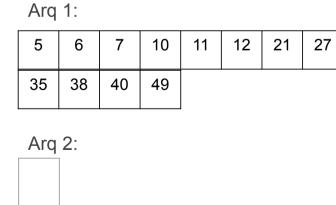
4

1-3

1

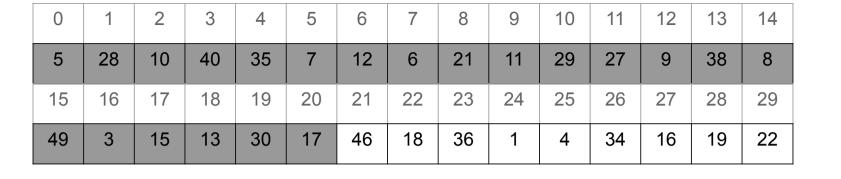
1-13

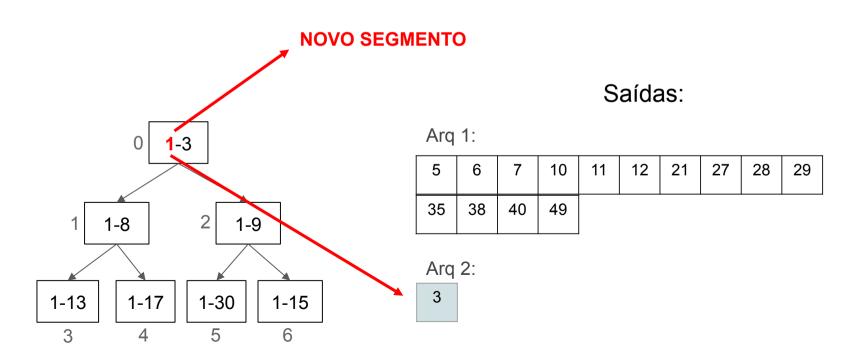
3



Saídas:

28









0

1-17

4

1-8

1

1-13

3

1-46

2

1-30

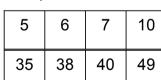
5

1-9

1-15

6

Arq 1:



Saídas:

12

21

27

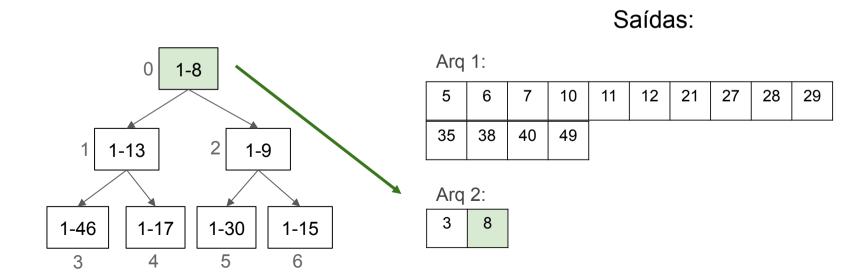
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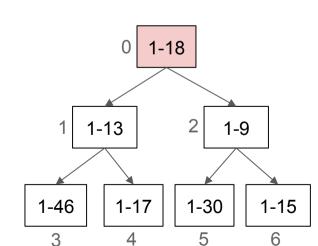
11

Arq 2:











5	6	7	10	
35	38	40	49	

Saídas:

12

21

27

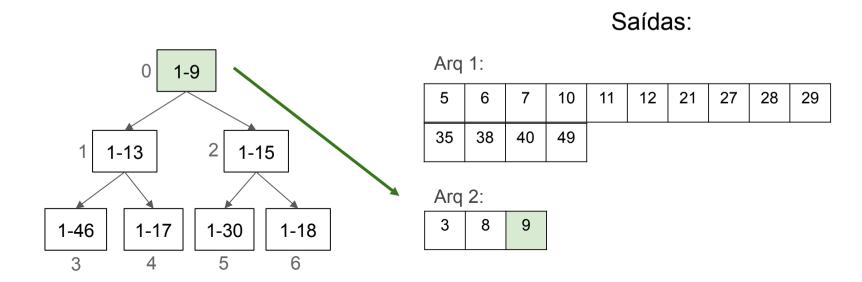
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29

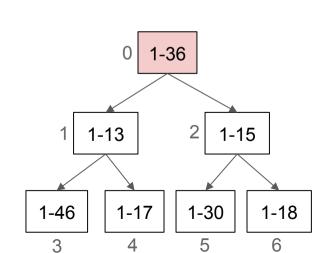
11

Arq 2:











5	6	7	10
35	38	40	49

Saídas:

12

21

27

28

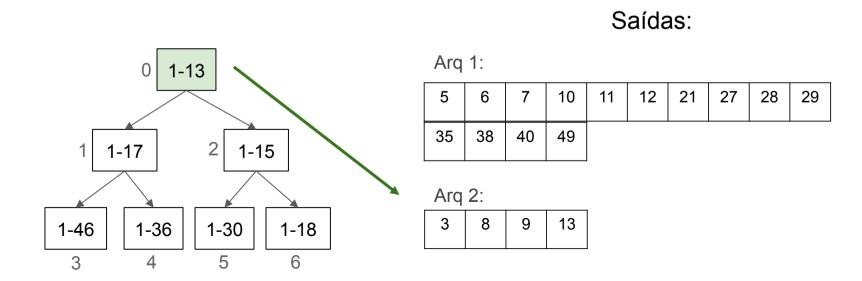
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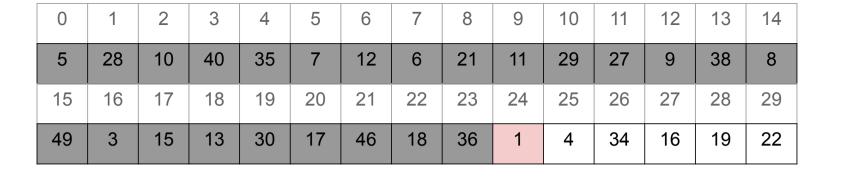
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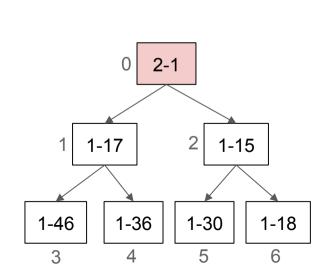
Arq 2:

3 8 9









Ara 1



5	6	7	10	
35	38	40	49	

Saídas:

12

11

21

27

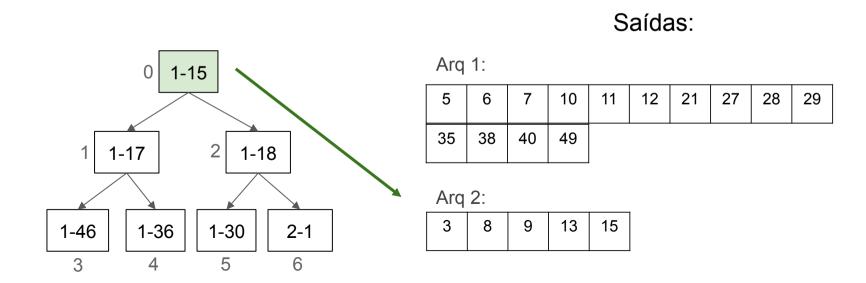
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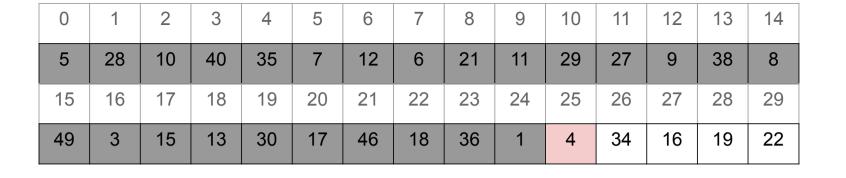
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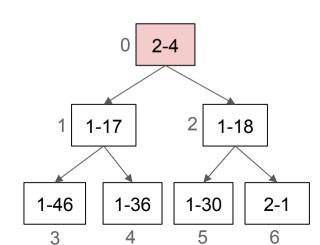
Arq 2:

3 8 9 13







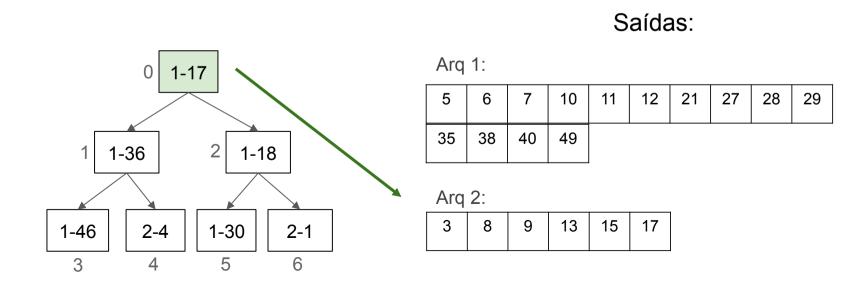




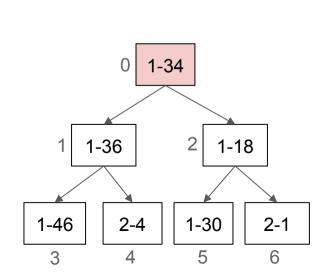
Saídas:

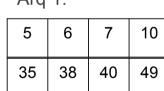
Arq 2:						
3	8	9	13	15		







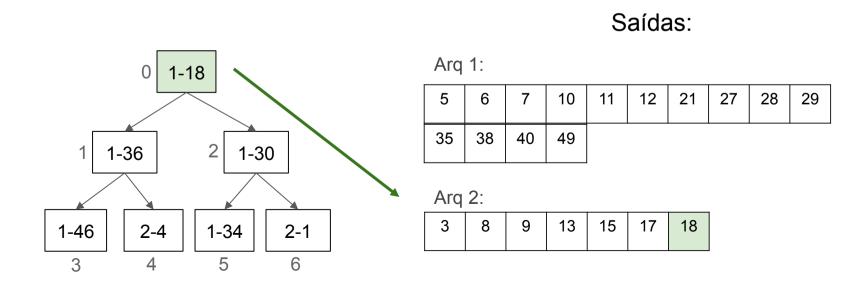




Arq	2:				
3	8	9	13	15	1

Saídas:









0

2-4

4

1-36

1

1-46

3

2-16

2

1-34

5

1-30

2-1

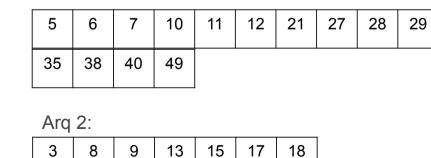
6

Arq 1:

3

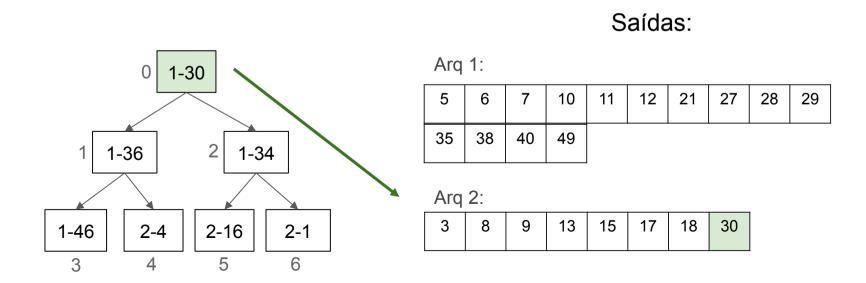
8

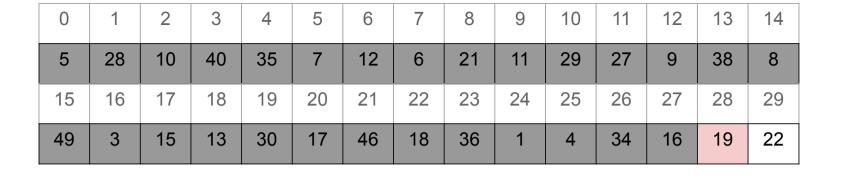
9

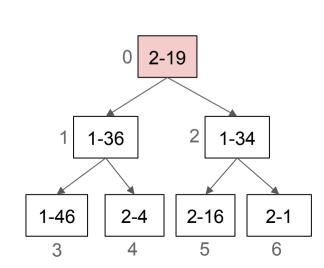


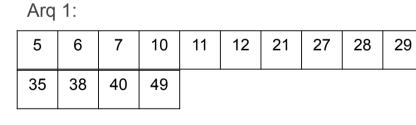
Saídas:







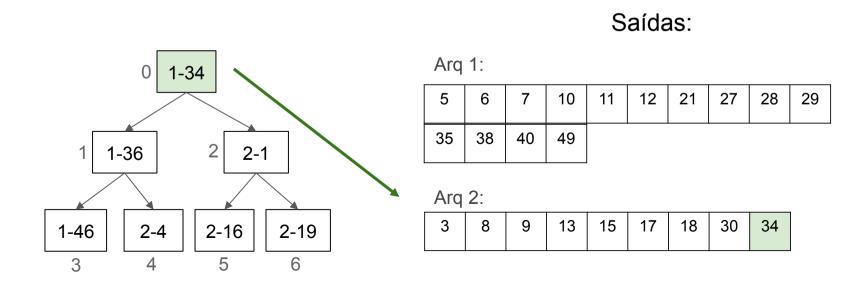




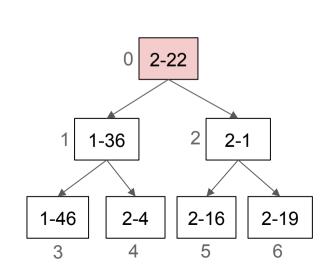
Saídas:

Arq	2:						
3	8	9	13	15	17	18	30









Ara 1



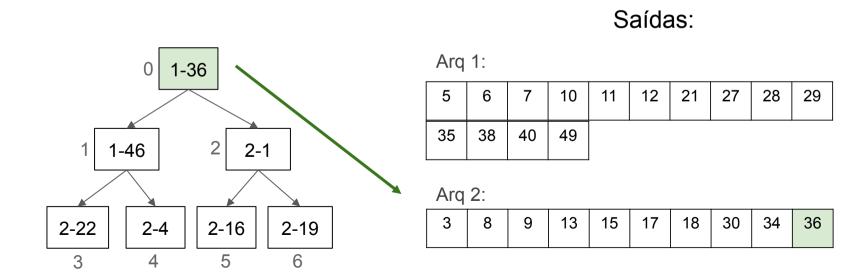
5	6	7	10	
35	38	40	49	

Arq 2:

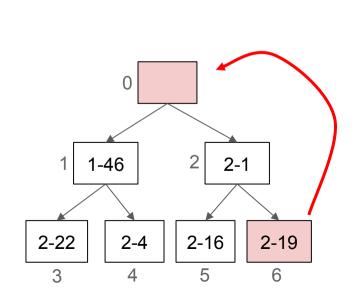
9								
3	8	9	13	15	17	18	30	34
		•	•			•		

Saídas:





0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



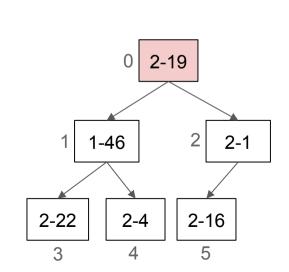
5	6	7	10	
35	38	40	49	

Arq 2:

3	8	9	13	15	17	18	30	34	36

Saídas:





A 4

Arq 1:

5	6	7	10	
35	38	40	49	

Arq 2:

3	8	9	13	15	17	18	30	34	36

11

Saídas:

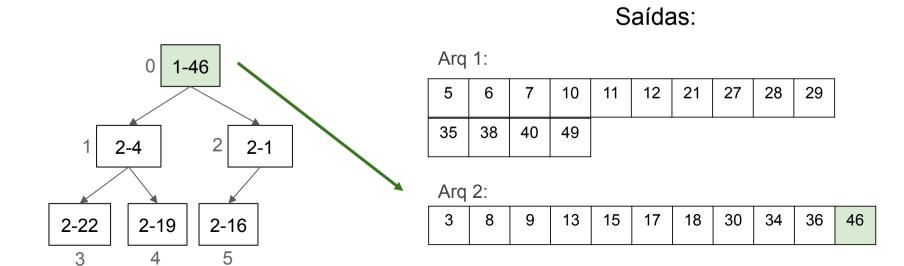
12

21

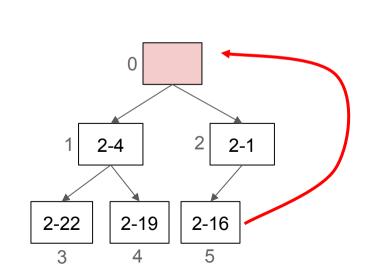
27

28

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



5	6	7	10	11	12	2
35	38	40	49			

Arq 2:

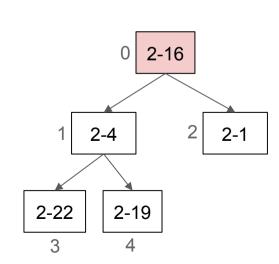
		3	8	9	13	15	17	18	30	34	36	46
--	--	---	---	---	----	----	----	----	----	----	----	----

Saídas:

27

28





A rou



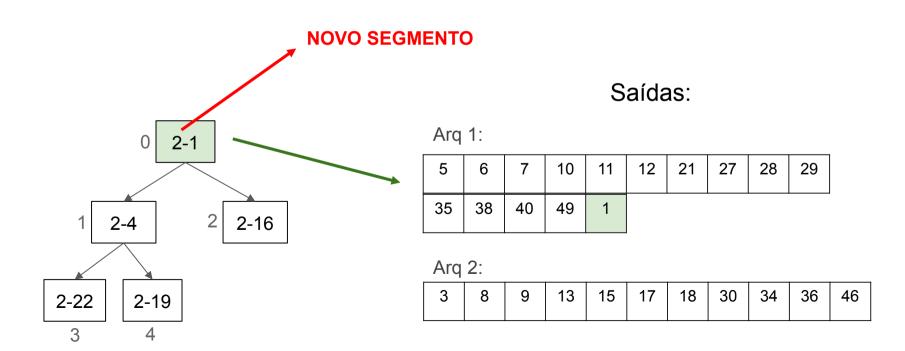
5	6	7	10
35	38	40	49

Arq 2:

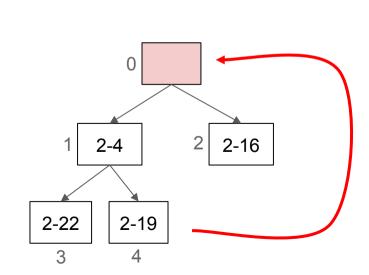
3	8	9	13	15	17	18	30	34	36	46
---	---	---	----	----	----	----	----	----	----	----

Saídas:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22





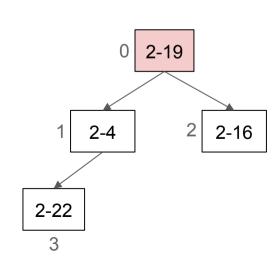
5	6	7	10	11
35	38	40	49	1

Arq 2:

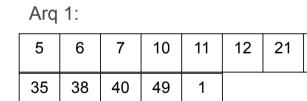
|--|

Saídas:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



. .



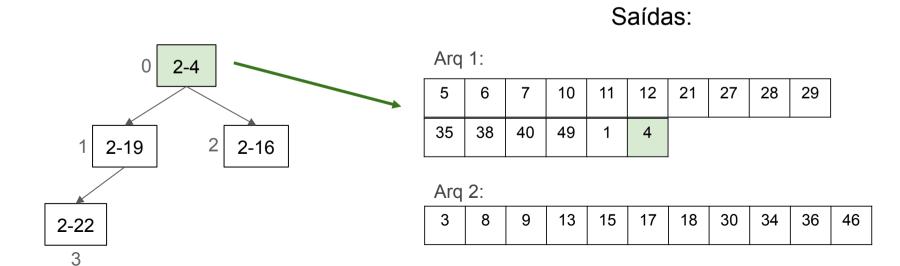
Arq	2:									
3	8	9	13	15	17	18	30	34	36	46

Saídas:

27

28

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

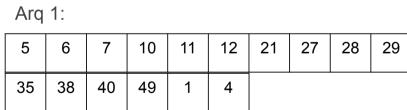


0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

0 2-22

2-19

2-16



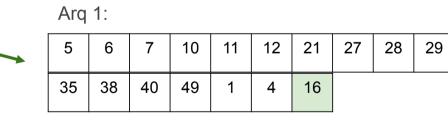
Saídas:

Arq 2:

3 8 9 13 15 17 18 30	34 36	46

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22





Arq 2:

2-16

2-19

2-22

(3	8	9	13	15	17	18	30	34	36	46

Saídas:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

0 2-22

2-19



Saídas:

Arq 2:

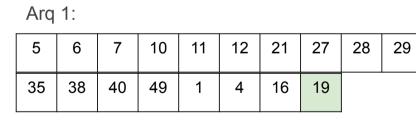
3 8 9 13 15 17 18 30	34 36	46

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



2-19

2-22

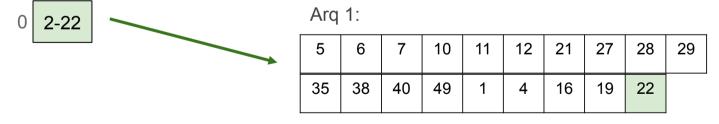


Saídas:

Arq 2:

(3	8	9	13	15	17	18	30	34	36	46

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22



|--|

3	8	9	13	15	17	18	30	34	36	46

Saídas:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
5	28	10	40	35	7	12	6	21	11	29	27	9	38	8
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
49	3	15	13	30	17	46	18	36	1	4	34	16	19	22

Agora é só fazer as intercalações!!!

	Arq	1
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5	6	7	10	11	12	21	27	28	29	
35	38	40	49	1	4	16	19	22		

Saídas:

Arq 2:

3	8	9	13	15	17	18	30	34	36	46

Estratégia 3 Economia de arquivos temporários



Intercalação Balanceada

No exemplo, foram utilizadas 2M fontes para uma intercalaçãode-M-caminhos.

É possível usar apenas M + 1 fitas, a saber:

- Encaminhe todos os blocos para uma única fita de saída.
- Redistribua estes blocos entre as fitas de onde eles foram lidos.

Custo: uma passada a mais em cada intercalação.