

# **Applied Statistics: R**

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Introduction to R

### **Objectives**

- new graphical methods
- data mangement (import/export)
- functions, debugging, condition handling
- object-oriented programing: S3 and S4 classes
- parallelization of R code
- integration of other programing languages, e.g. C++
- building R packages

#### **Coordination & Examination**

- No Blackboard.
- For lecture notes, code, references, etc. go here: https://github.com/franciscorosales-marticorena/ApplStatsR
- One exam on mid-term week. 20% of your grade.

### **Reading Material**

- Hadley Wickham. Advanced R. The R series. CRC Press, 2015. Available online: http://adv-r.had.co.nz/.
- Owen Jones, Robert Maillardet, and Andrew Robinson. Introduction to scientific programming and simulation using R. Chapman & Hall/CRC, 2009.
- Brian Everitt and Torsten Hothorn. A handbook of statistical analyses using R. Chapman & Hall/CRC, 2006.
- R Data Import/Export manual. Available online: http: //cran.r-project.org/doc/manuals/r-release/R-data.pdf
- Deepayan Sarkar. Lattice: multivariate data visualization with R.
   Use R! Springer, 2008.
- Roger S Bivand, Edzer J Pebesma, and Virgilio Gómez-Rubio.
  Applied spatial data analysis with R, volume 10 of Use R! Springer, 2008.

### Who are you?

- operating system: Linux, Apple, Windows?
- text editor for R: Rstudio, emacs, Vim?
- other programing languages: C, C++, Java, Python, Fortran, Julia?
- compiled already an R package?
- ATEX?

#### **R** Basics

```
help: ?topic, help(topic), args(some function)
assignments: x \leftarrow 5 (recommended), x = 5, 5 \rightarrow x
```

comments: everything that follows #

case sensitive: usage of CAPITAL and small letters matters!

#### **Basic Data Structures**

```
integer: 1,2,301L
double: 1.0, .141, 1.23e-3, NaN, Inf, -Inf
logical: TRUE, FALSE
character: "hello", "I'm a string"
numeric general class for 'numberliness' (integer, double)
complex 1+0i, 1i, 3+5i
missings: NA
```

```
mode(1:10)
                     ## [1] "numeric"
storage.mode(1:10)
                     ## [1]
                            "integer"
mode(pi)
                     ## [1] "numeric"
storage.mode(pi)
                     ## [1] "double"
mode (TRUE)
                     ## [1] "logical"
mode("Hello")
                     ## [1] "character"
### also useful:
str(1:10)
                     ## int [1:10] 1 2 3 4 5 6 7 8 9 10
str(LETTERS)
                     ## chr [1:26]
                                    "A" "B" "C" "D" "E"
```

#### Construction & Coercion

- the constructor for a data type is named like the data type
- vector can be constructed with c()
- coerce to a type xxx by as.xxx()
- when combining different data types, they will be coerced to the most flexible type
- coercion often happens automatically
- check if xxx is a specific type by is.xxx()

```
integer(5)  ## [1] 0 0 0 0 0 0
double(0)  ## numeric(0)
str(c("a",1))  ## chr [1:2] "a" "1"
x <- c(FALSE, FALSE, TRUE)
as.numeric(x)  ## [1] 0 0 1
# Total number of TRUEs
sum(x)  ## [1] 1</pre>
```

### NA, NaN and NULL

In R, there three ways to represent "nothing", but the reason for the missingness of the information can be distinguished:

NA	missing sample values, impossible coercion,
NaN	undefined results in math. operation (e.g. $log(-1)$ , 1/0)
NULL	null pointer, i.e. pointer in empty/undefined memory

```
c(3, NA) ## [1] 3 NA
c(3, O/O) ## [1] 3 NaN
c(3, NULL) ## [1] 3
max(3, NA) ## [1] NA
```

### Inifinity

Some mathematical operations can be performed with Inf and -Inf:

```
max(3, Inf)
## [1] Inf

min(3, Inf)
## [1] 3

c(Inf + Inf, (-Inf) * Inf, Inf - Inf)
## [1] Inf -Inf NaN
```

### **Complex Data Types**

complex data structures in R can be organized by their dimensionality and if all their contents are of the same type, or not:

object	homogeneous	heterogeneous	dimension
1d	atomic vector	list	length()
2d	matrix	data frame	<pre>dim()</pre>
nd	array		dim()

a data.frame is a matrix, in which not every column has to have the same data type, and a list, in which each element has the same length

```
x <- matrix(1, nrow = 5, ncol = 2)
is.matrix(x)  ## [1] TRUE
as.vector(x)  ## [1] 1 1 1 1 1 1 1 1 1 1
x <- list(a = "Hallo", b = 1:10, pi = pi)</pre>
```

#### **Attributes**

All objects can have arbitrary additional attributes, used to store metadata about the object.

- can be thought of as a named list (with unique names); other frequently encountered attributes: "dimnames", "names", "class" (!)
- a can be accessed all at once (as a list) with attributes(), or individually with attr().
- arrays are simply vectors with a "dim"-attribute.
- factor is a vector with attribute levels
- as.xxx() functions delete all attributes including dimensionality

#### **Attributes**

#### Example 1.1

```
x \leftarrow matrix(1:10, ncol = 5)
attributes(x)
                              ## $dim
                              ## [1] 2 5
rownames(x) <- c("Eins", "Zwei")
attributes(x)
                              ## $dim
                              ## [1] 2 5
                              ## $dimnames
                              ## $dimnames[[1]]
                              ## [1] "Eins" "Zwei"
                              ## $dimnames[[2]]
                              ## NULL
                              ## [1] "1" "2" "3" "4" "5"...
as.character(x)
attributes(as.character(x)) ## NULL
```

### Subsetting

- There are three subsetting operators: [, [[, and \$
- the three types of subsetting:
  - Positive integers return elements at the specified positions.
  - Logical vectors select elements where the corresponding logical value is TRUE; application of logical expressions.
  - character vectors to return elements with matching names.
- important differences in behaviour of different objects (e.g., vectors, lists, factors, matrices, and data frames).
- More advanced subsetting, in particular in combination with complex logical expressions, can be done using the functions subset() and which().
- There are also two additional subsetting operators that are needed for S4 objects: @ (equivalent to \$), and slot() (equivalent to [[).
- The default drop=TRUE simplifies the data type of the result.

#### **Atomic Vectors**

Use "["-operator and number, logical vector or name of the element you want to pull out.

```
x \leftarrow c(2.1, 4.2, 3.3, 5.4)
x[c(3, 1)]  ## [1] 3.3 2.1
x[-c(3, 1)]  ## [1] 4.2 5.4
x[c(TRUE, TRUE, FALSE, FALSE)] ## [1] 2.1 4.2

(y <- setNames(x, letters[1:4])) ## a b c d
## 2.1 4.2 3.3 5.4
y[c("d", "c", "a")] ## d c a
## 5.4 3.3 2.1
```

### **Matrices & Arrays**

Subsetting matrices and arrays with "["-operator like vectors, while the dimension is separated by comma:

```
x <- matrix(1:10, ncol=2)
colnames(x) <- c("Eins", "Zwei")

x[1:2,]  # results a matrix
x[,"Zwei"]  # results a vector
x[,"Zwei", drop=FALSE] # results a matrix
x[-3,]  # everything, but not third row</pre>
```

#### Lists

Subsetting lists with "["-operator returns always a list, while [[, and \$ pull out elements of the list:

```
x <- list(a = "Hallo", b = 1:10, pi = pi)

x$a  # first element of the list
x[['a']]
x[[1]]
x[1]  # list with one element
x[2:3]  # list with two elements
x[[2:3]]  # wrong result</pre>
```

#### **Data Frames**

Data frames possess the characteristics of both lists and matrices: if you subset with a single vector, they behave like lists; if you subset with two vectors, they behave like matrices.

```
iris[1:10,]  # data frame with 10 rows
iris[,1]  # numerical
iris$Sepal.Length  # the name
iris$Sepal.Length  # Oops! what happened?
iris[,"Sepal.Length"]  # again first column
iris[,"Sepal.Length"]  # Error: undefined columns selected
iris[,1, drop=FALSE]  # data frame with one column
```

#### Flow Control

- conditional evaluation: if, else, ifelse
- loops: for, while, repeat, switch

#### basic vocabulary:

```
if, &&, || (short circuiting)
for, while, repeat
next, break
switch
ifelse
```

### if/else Conditions

```
if (<test>) {
    <expression1>
} else {
    <expression2>
}
```

- else block is optional
- <test> has to result in a value that can be converted to a logical value
- only the first element of <test> is used, otherwise a warning is triggered
- for the evaluation of more than one statement use &, | or all() and any()
- can be nested

### for Loop

In each interation, <var> is set to the next element of <vector> and <expression> is evaluated.

```
for (<var> in <vector>) {
  <expression>
sum <- 0
for(i in 1 : length(x)) {
  sum <- sum + x[i]</pre>
sum <- 0
for(x_value in x) { ## more efficient
  sum <- sum + x_value
```

Use seq\_along(x) instead of 1:length(x)

### while Loop

As long <test> is TRUE the <expression> is evaluated.

```
while(<test>) {
  <expression>
E.g., the sum until the first NA:
sum < -0
i <- 1
while((i <= length(x)) && !is.na(x[i])) {
  sum <- sum + x[i]</pre>
i <- i + 1 }
```

Be aware of infinite loops!

#### next & break

- next jumps to the next iteration in for or while loops
- break terminates for or while loops.

```
x \leftarrow c(1, 1, 1, NA, 2)
sum <- 0
for(val in x) {
  if(is.na(val)) break
  sum <- sum + val
x \leftarrow c(1, 1, 1, NA, 2)
sum <- 0
for(val in x) {
  if(is.na(val)) next
  sum <- sum + val
```

### Style Example: Bad

```
 fWLM <-function(y,X_mat,w) \{T0 <-t(X_mat)\%*\%diag(w)\%*\%X_mat \\ t <-system.time(\{t_1 <-solve(T0)\%*\%t(X_mat)\%*\%(w*y); \\ t2 <-X_mat\%*\%t_1\}) \\ return(list(beta=t_1,hat=t2,stddev=sqrt(sum(w*(t2-y)^2))/(length(y)-ncol(X_mat)), wts=w,t=t[[3]])) \}
```

### Style Example: Good

```
fit_weighted_lm <- function(response, design, weights) {</pre>
  n_obs <- length(response)</pre>
  n_coef <- ncol(design)</pre>
  time_start <- Sys.time()</pre>
  wcrossprod_design <- crossprod(design * weights, design)</pre>
  weighted_response <- weights * response</pre>
  coef <- solve(wcrossprod_design, t(design) %*% weighted_response)</pre>
  time <- Sys.time() - time_start</pre>
  fitted <- design %*% coef
  residuals <- response - fitted
  weighted_rss <- sum(weights * residuals^2)</pre>
  sd_resid <- sqrt(weighted_rss / (n_obs - n_coef))</pre>
  list(coef = coef,
      fitted = fitted,
      sd_resid = sd_resid,
      weights = weights,
      time = time)
```

#### **Notation & Names**

■ find meaningful file names; if files need to be run in sequence, prefix them with numbers.

```
0-download.R
```

- avoid uppercase
- use an underscore to separate words within a name
- use nouns for variable names and verbs for function names

### **Notation & Names**

■ strive for names that are concise and meaningful (this is not easy!).

avoid using names of existing functions and variables.

```
# Bad
T <- FALSE
c <- 10
t <- temporal_variable
mean <- function(x) sum(x)</pre>
```

### **Formatting**

- strive to limit your code to 80 characters per line.
- when indenting your code, use two spaces. Never use tabs.
- use "<-", not "=", for assignment
- place spaces around all infix operators (=, +, -, <-, etc.), before parentheses, and after comma (just like in regular English)

```
# Good
average <- mean(feet / 12 + inches, na.rm = TRUE)</pre>
# Bad
average <- mean (feet/12+inches, na.rm=TRUE)
# Good
if (debug) do(x)
plot(x, y)
# Bad
if (debug)do(x)
plot (x, y)
```

### **Formatting**

an opening (or closing) curly brace should always be followed by a new line, unless it's followed by else.

```
if (y == 0) {
  log(x)
} else {
  y^x
}
```

■ use commented lines of - and = to break up your file into chunks.

```
# Load data ------
# Plot data ------
```

formatR::tidy\_source() cleans up and does some automatic formatting such as consistent indent

# Advanced Graphics

#### **Motivation**

- creating interest and attention of the reader
- essential meaning can be visualized at a glance
- comprehensive picture of a problem gives more complete and balanced understanding
- the human visual system is very powerful in detecting patterns: outliers, diagnose models, search for perhaps unexpected phenomena

### **Graphical Devices**

- A graphical device can be thought as a paper on which you can draw with different pens and colours, but nothing can be deleted.
- It can be opened more than one device, but there is only one active.
- There is no difference no matter which device is used.
- Typical steps to produce a graphic is:
  - 1 start device, e.g. pdf('testgraphics.pdf')
  - 2 generate graphic, e.g. plot(1:10)
  - 3 close device: dev.off()
- If no device is open, using a high-level graphics function will cause a device to be opened.

### **Graphical Devices**

The following graphics devices are currently available:

- pdf(): write PDF graphics commands to a file; can be handy for distribution to cooperation partners, integration in PDFLATEX, or viewing many graphics
- postscript(): writes PostScript graphics commands to a file
- bitmap(): bitmap pseudo-device via 'Ghostscript' (if available).

Interactive plotting with GUI:

- x11(): The graphics device for the X11 windowing system
- png(): compressed Bitmap, without loss
- jpeg(): compressed Bitmap with information loss, optimized for pictures with many color shades

For more info see ?Devices.

## **High-level Plots**

 $High-level\ functions\ generate/initialize\ a\ graphic,\ e.g.:$ 

plot()	depend of context
barplot()	Barplot
boxplot()	Boxplot
coplot ()	Conditioning plots
contour()	Contour line plot
curve()	Plotting functions
dotchart()	Dot Plots
hist()	Histogram
image()	Countour Plot (3. Dim. as color)
mosaicplot()	Mosaicplots (categorial data)
pairs()	Scatterplot matrix
persp()	perspective surface
qqplot()	QQ-Plot

## **High-level Plots**

Many Functions can be applied to different object types. They react in a "intelligent" way, so that a meaningful graphic specifically for the given object can be found.

```
plot(trees)  ## scatterplotmatrix
plot(Volume ~ Girth, data=trees) ## scatterplot

tree.lm <- lm(Volume ~ Girth, data = trees)
abline(tree.lm)  ## regression line
plot(tree.lm)  ## residual/diagnostic plots
boxplot(trees)  ## boxplots
qqnorm(trees$Volume) ## quantile plot</pre>
```

- for nicer graphics, the par graphical parameters can be adapted
- some graphical parameters can be adjusted in high-level functions
- for help check ?plot, ?plot.default, or more comprehensive ?par

Some graphical parameters can can be set in high-level functions like plot(). For example:

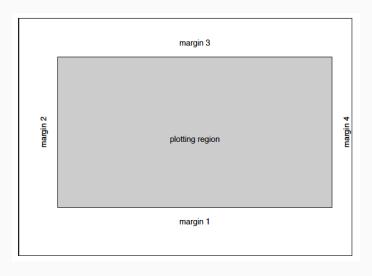
axes	should the axes be plotted?
col	color
log	logarithmic scale
main, sub	title and subtitle
pch	symbol for points
type	type (I=line, p=point, b=both, n=none)
xlab, ylab	x-/y-axis label xlim, ylim
xlim, ylim	x-/y-axis range

The most commonly used arguments in par():

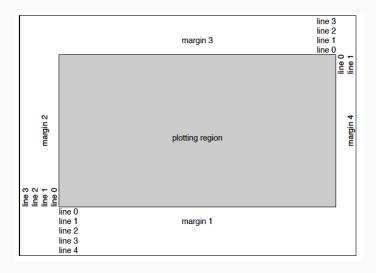
bg	background color
cex	size of a point or a letter
las	should labels be placed parallel wrt the axes
lty, lwd	line type (dashed,) and line width
mar	size of the margins
mfcol, mfrow	multiple plots in one device in rows/columns
mfg	which plot in a device should be chosen?
oma	size of the outer margins
usr	current extrema of the user coordinates
xaxt, yaxt	x-/y-axis scaling

```
# example 1
opar \leftarrow par(mfrow = c(1, 1))
par(mfrow = c(2, 2))
boxplot(trees, col = "blue")
hist(trees$Volume, las = 1)
qqnorm(trees$Volume, cex.axis = 2, pch = (trees$Girth > 14) + 8)
plot(trees$Girth,trees$Height,cex = scale(trees$Volume,center=FALSE))
par(opar)
# example 2
set.seed(123)
x <- rnorm(100)
opar <- par(bg = "lightgreen")</pre>
hist(x, freq = FALSE, col = "red", las = 1,
     xlim = c(-5, 5), ylim = c(0, 0.6),
     main = "100 Draws from N(0,1)-distributed random variables")
curve(dnorm, from = -5, to = 5, add = TRUE, col = "blue", lwd = 3)
par(opar)
                                                                       38
```

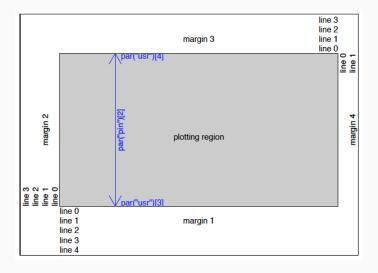
#### **Device Control**



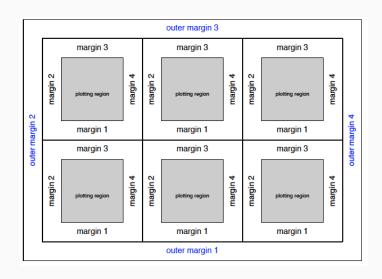
#### **Device Control**



#### **Device Control**



#### par(mfrow=c(2,3))

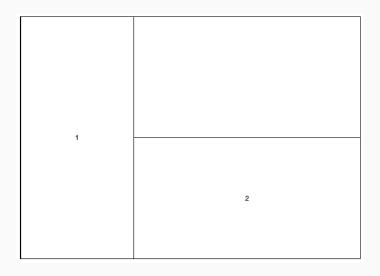


#### layout() Function

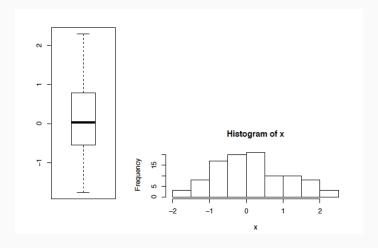
- layout() organizes independent plots on one plotting device, also in irregular grids
- boxes can have different widths
- neighboring boxed can be combined
- boxes can be left empty

```
m <- matrix(c(1,1,0,2), 2, 2)
m
## [,1] [,2]
## [1,] 1 0
## [2,] 1 2
layout(m, widths=c(1,2))
x <- rnorm(100)
boxplot(x)
hist(x)</pre>
```

# layout() Function



# layout() Function

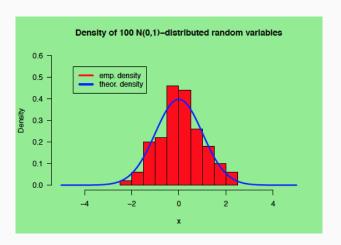


#### **Low-level Graphics**

Low-level functions add elements to a (with high-level function) generated graphic, e.g., additional points, legends, etc.

abline()	"intelligent" lines
arrows()	arrows
axis()	axes
<pre>grid()</pre>	gridlines
legend()	legend
lines()	(stepwise) lines
mtext()	text in margins
<pre>points()</pre>	points
<pre>polygon()</pre>	(filled) polygons
segments()	vector lines
text()	text
title()	title label

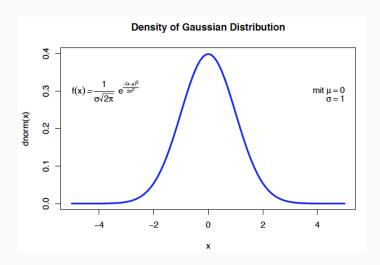
#### **Low-level Graphics**



#### **Mathematical Expressions**

- mathematical notation and symbols formatted similar to LATEXcode can be integrated in functions such as axis(), legend(), mtext(), text(), and title()
- the S expression is not evaluated, but using expression() forwarded and processed internally
- Using bquote() and .() values from variables can be integrated into formulas.
- For help check ?plotmath or run demo(plotmath)

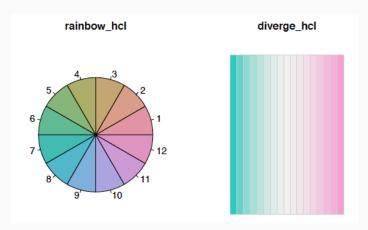
# **Mathematical Expressions**



#### colorspace

The package colorspace provides various functions for perceptually-balanced color palettes

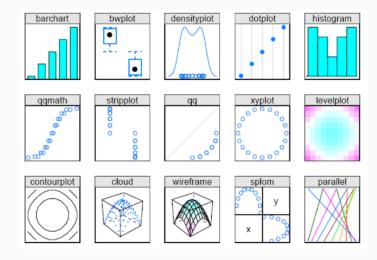
```
rainbow_hcl(12)
diverge_hcl(17, h = c(180, 330), c = 59, l = c(75, 95))
```



- trellis graphics is a family of techniques for viewing complex data sets, that are based on basic concepts of human perception
- everything is possible (using a sufficient number of parameters)
- the trellis graphics system is in the lattice package
- the typical format is

```
graph_type(formula, data= )
```

barchart()	barplot
bwplot()	boxplot
cloud()	3D point clouds
contourplot	3D contour plot
densityplot()	kernel density plot
dotplot()	point plots
histogram()	histogram
levelplot()	levelplots
panel()	functions to add elements
piechart()	pie diagram
<pre>print.trellis()</pre>	plotting trellis object
qq()	QQ-plots
stripplot	strip plots
wireframe()	persp. 3D areas
xyplot()	scatterplot



```
require(lattice)
attach(mtcars)
# create factors with value labels
gear.f<-factor(gear,levels=c(3,4,5),</pre>
   labels=c("3gears","4gears","5gears"))
cyl.f <-factor(cyl,levels=c(4,6,8),</pre>
   labels=c("4cyl","6cyl","8cyl"))
# kernel density plot
densityplot(~mpg,
   main="Density Plot",
   xlab="Miles per Gallon")
# kernel density plots by factor level
densityplot(~mpg|cyl.f,
   main="Density Plot by Number of Cylinders",
   xlab="Miles per Gallon")
# ...
```

#### **Interactive Graphics**

The basic R system does not allow many possibilities for interactive graphics. Some exceptions are:

■ identify() identifies a selected data point, e.g.:

```
x <- rnorm(10)
plot(x)
identify(x)</pre>
```

■ locator() returns the coordinates of a selected point, which can be used for instance for the interactive placing of labels:

```
plot(x)
legend(locator(1), legend = "A legend", pch = 1)
```

#### **Further References**

- First analysis: Brian Everitt and Torsten Hothorn. A handbook of statistical analyses using R. Chapman & Hall/CRC, 2006
- Trellis: Deepayan Sarkar. Lattice: multivariate data visualization with R. Use R! Springer, 2008
- Colorspace: Achim Zeileis, Kurt Hornik, and Paul Murrell. Escaping RGBland: Selecting colors for statistical graphics. Computational Statistics & Data Analysis, 53:3259?3270, 2009. doi: 10.1016/j.csda.2008.11.033

**Data Management** 

#### **Motivation**

#### Data Import and Export

- can take more time than the statistical analysis itself
- majority of the data is spreadsheet—like data
- Easier to import badly formatted data than explaining what a "good" formatted data is
- R is not good to handle large-scale data
- In practice, you will be often faced with data corrections and updates

#### **Data Import Vocabulary**

#### **Data Import Vocabulary**

```
# Files and directories
setwd, getwd
                # set and get current working directory
                # names of files or directories in a directory
dir
dirname
                # returns the directory name
file.path
                # reads path to a file from components
normalizePath
                # convert file paths to canonical form
file.choose
                # choose a file interactively
download.file
                # download a file from the Internet
# low-level interface to the computer's file system:
file.copy, file.create, file.remove, file.rename, dir.create,
file.exists. file.info
```

#### Import Spreadsheet-like Data

To read spreadsheet-like data you need the function read.table() and variations like read.csv(), ...

fileEncoding: use latin1 for Windows data, and utf-8 for Unix data

header: names of variables (columns) and observations (rows)

sep: field separator vs. record separator

quote: protecting separators appearing in strings

na.strings: which string (or number) represents missing values?

fill=TRUE: are lines with missing trailing fields OK? be careful!

colClasses: which type of variable is contained in which column?

skip: number of lines skipped before beginning to read data

60

#### Importing from other statistical systems

The package require(foreign) provides import facilities for files produced by other statistical systems:

read.epiinfo: reads fixed-width text format .REC files as R data frames

read.mtp: imports 'Minitab Portable Worksheet'

read.xport: reads a file in SAS Transport (XPORT) format

generates a SAS program to convert the ssd contents to

SAS transport format

read.spss: reads files created by SPSS's 'save'/'export' commands

read.dta: imports binary files created by Stata

read.S: reads S's 'data.dump' files

#### Data Export: Basic Vocabulary

```
# Output
print, cat
                       # 'cat' performs much less conversion
                       # than 'print'
dput
                       # Writes an ASCII text representation of
                       # an R object to a file
sink, capture.output
                       # Evaluates its arguments with the output
                       # being returned as a character string or
                       # sent to a file.
# Writing data
                       # The data (usually a matrix) are written
write
                       # to file
write.table, write.csv # converts the object to a data frame and
                       # prints it to a file
                       # writes an external representation of
save
                       # R objects
```

#### Data Export

- exporting from R is easier than importing
- normally exporting a text or csv file with write.table or write.csv is good enough
- MASS:write.matrix provides a specialized interface for writing matrices, with the option of writing them in blocks and thereby reducing memory usage
- sink diverts the standard R output to a file, and thereby captures the output of (possibly implicit) print statements
- foreign::write.foreign writes a code file that will write this text file into another statistical package
- the precision is governed by the current setting of options(digits): Export for report writing or further analysis?

#### Relational Database

#### Why use a database?

- R is not well suited to large data sets. Large data objects can cause R to run out of memory
- provide fast access to selected parts of large databases.
- powerful ways to summarize and cross—tabulate columns in databases.
- store data in more organized ways than the rectangular grid model of spreadsheets and R data frames.
- concurrent access from multiple clients running on multiple hosts while enforcing security constraints on access to the data.
- ability to act as a server to a wide range of clients.

#### R Database Interface Packages

#### R Database Interface Packages:

DBI interface between R and relational DBMS

RJDBC access to databases through the JDBC interface

RMySQL interface to MySQL database

RODBC ODBC database access

ROracle Oracle database interface driver

RpgSQL interface to PostgreSQL database

RSQLite SQLite interface for R

#### Example for SQL queries:

SELECT State, Murder FROM USArrests WHERE Rape > 30 ORDER BY Murder SELECT sex, COUNT(\*) FROM student GROUP BY sex SELECT sch, AVG(sestat) FROM student GROUP BY sch LIMIT 10

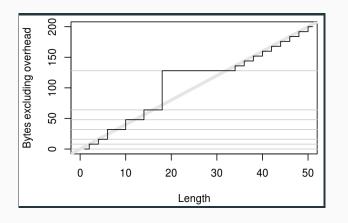
## **Memory Management**

- some understanding of R's memory management will help you predict how much memory you will need
- pryr::object size() tells you how much memory an object occupies (including environments)

```
> require(pryr)
> object_size(1:10)  # 88 B
> object_size(mtcars)  # 6.74 kB
> object_size(numeric())  # 40 B
>
> sizes <- sapply(0:50, function(n) object_size(seq_len(n)))
> plot(0:50, sizes,
+ xlab = "Length", ylab = "Size (bytes)", type = "s")
```

- for memory profiling use the function utils::Rprof() or lineprof::lineprof()
- for more information see also ?Memory

## **Memory Management**



## **Memory Management**

- pryr::mem used() tells you the total size of all objects in memory.
  pryr::mem\_change() tells you how memory changes during code
  execution
- R has automatic garbage collection, but it is lazy, so that it won't ask for memory until it is actually needed, otherwise use gc()
- be aware of possible memory leaks due to deleted objects

```
mem_used()  # 44.6 MB
mem_change(x <- 1:1e6)  # 4.01 MB
mem_change(rm(x))  # -4 MB

mem_change(x <- 1:1e6)  # 4 MB
mem_change(y <- x)  # 1.74 kB
mem_change(rm(x))  # 1.62 kB
mem_change(rm(y))  # -4 MB</pre>
```

### **Project Management**

#### Object Storage

is your current R working environment and includes any user–defined objects (vectors, matrices, data frames, lists, functions). When R is started, a .RData file is loaded, which

can be saved when R is closed

can be saved when R is closed

Binary files: save() allows the explicit saving of functions and data in

binary file, that can be loaded by load()

Source code: source() accepts its input from the named file or URL and

runs the script in the current session

### **Project Management**

### Manage your Workspace

ls() lists the objects in your workspace.
list.files() lists the files located in the folder's workspace
rm() removes objects from your workspace; rm(list = ls())
removes them all.
gives information about your session, i.e., loaded packages,
R version provides information about the R version.

### **Publication Quality Output**

Publication Quality Output and Documentation of Analysis:

enables integration of R code into LaTeX, LyX, HTML, Mark-knitr

down, AsciiDoc, and reStructuredText documents

xtable: converts some R objects into LATEX code.

R2HTML: converts your output text, tables, and graphs in HTML for-

mat

has functions that allow you to imbedd R output in Open

Document Format (ODF)

SWordInstaller: allows you to add R output to Microsoft Word documents

R2PPT provides wrappers for adding R output to Microsoft Power-

Point presentations.

### Sweave: Integration with LATEX

- Sweave allows you to embed R code in LaTeX, producing attractive reports if you know that markup language.
- R's ability to output results for publication quality reports is somewhat rudimentary
- typewrite the results from R can be laborious, time-consuming and is a potential source for errors
- integration of R code and report allows the reproducibility of the analysis and assures good scientific practice
- the reports are easily updated with corrections and extension of the underlying data

### Sweave Example

```
\documentclass[a4paper]{article}
\title{Sweave Example 1}
\author{Friedrich Leisch}
\begin{document}
\maketitle
In this example we embed parts of the examples from the
\texttt{kruskal.test} help page into a \LaTeX{} document:
<<>>=
data(airquality)
kruskal.test(Ozone ~ Month, data = airquality)
0
which shows that the location parameter of the Ozone
distribution varies significantly from month to month.
\begin{center}
<<fig=TRUE,echo=FALSE>>=
boxplot(Ozone ~ Month, data = airquality)
0
\end{center}
\end{document}
```

### **Sweave Chunk Options**

In recent versions of R the way to run Sweave from the command line:

```
R CMD Sweave example-1.Snw
pdflatex example-1
pdflatex example-1
```

The most important options for Sweave code chunks are:

echo: logical (TRUE). Show code in output file?

eval: logical (TRUE). Evaluate code?

results: character string: verbatim, tex, or hide.

fig: logical (FALSE). Graphics?

eps, pdf: logical (TRUE), EPS/PDF-Datei?

width, height: numerical (6), width and height of graphics

Defaults can be adapted using SweaveOpts()

### **Further Reading**

- R Data Import/Export manual. Available online: http: //cran.r-project.org/doc/manuals/r-release/R-data.pdf
- Hadley Wickham. Advanced R. The R series. CRC Press, 2015; Chapter 18: Memory.
- Sweave webpage by Friedrich Leisch http://www.statistik.lmu.de/~leisch/Sweave/

Functions, Debugging &

**Condition Handling** 

#### **Motivation: Functions in R**

- R is a functional programming language. This means that it provides many tools for the creation and manipulation of functions.
- The structure of a function is given by function ( <arglist> ) { <body> }
  - the keyword function indicates the beginning of a function
  - arguments <arglist> are defined by comma-separated key-value-pairs
  - <body> is a block of R commands which are executed by the function

### **Function Components**

All R functions are objects and consist of three parts:

```
body() code inside the function.

formals() arguments that controls how you can call the function.

environment() the "map" of the location of the function's variables. Global environment is the default.
```

```
f <- function(x) x^2
f  # > function(x) x^2
formals(f) # > $x
body(f) # > x^2
environment(f) # > <environment: R_GlobalEnv>
```

### **Function Arguments**

- When calling a function you can specify arguments by position, by complete name, or by partial name.
- Arguments are matched first by exact name (perfect matching), then by prefix matching, and finally by position.
- Avoid using positional matching for less commonly used arguments, and only use readable abbreviations with partial matching.

```
f <- function(abcdef, bcde1, bcde2) {
   list(a = abcdef, b1 = bcde1, b2 = bcde2)
}
str(f(1, 2, 3))  # ok
str(f(2, 3, abcdef = 1)) # ok
str(f(2, 3, a = 1))  # ok
str(f(1, 3, b = 1)) # Error</pre>
```

### **Default and Missing Arguments**

- Function arguments in R can have default values.
- They can be also defined in terms of other arguments.
- You can determine if an argument was supplied or not with the missing() function.

```
myplot <- function(x, y, mycol = 'red') {
   if(missing(y)) {
      y <- x
      x <- 1:length(y)
   }
   plot(x, y, col = mycol)
}
myplot(1:20)
myplot(1:20, rnorm(20), mycol='darkgreen')</pre>
```

### match.arg()

match.arg matches arguments against a table of candidate values specified by choices

```
match.arg(arg, choices, several.ok = FALSE)
```

missing argument will be replaced with the first candidate

```
talk_about_sex <- function(sex = c("Male", "Female")) {
  match.arg(sex)
}
talk_about_sex("F")  # [1] "Female"
talk_about_sex()  # [1] "Male"
talk_about_sex("W")
# Error in match.arg(sex) (from #2) :
# 'arg' should be one of \Male", \Female"</pre>
```

### Lazy Evaluation

■ By default, R function arguments are lazy – they're only evaluated if they're actually used.

- If you want to ensure that an argument is evaluated you can use force()
- More technically, an unevaluated argument is called a 'promise".
- Laziness is useful in if statements the second statement below will be evaluated only if the first is true.

### The Argument ...

- Functions can have any number of arguments using the special argument "..."
- The argument "..." will match any arguments not otherwise matched, and can be easily passed on to other functions.
- Using "..." comes at a price any misspelled arguments will not raise an error, and any arguments after "..." must be fully named.

```
myplot <- function(x, y, myarg, ...){
    ## optional calculation with x, y and myarg
    ## call standard plot function with additional unspecified
    ## arguments from ...
    plot(x, y, ...)
}</pre>
```

### Connecting the "..."

- "..." can be passed to any number of functions, but the arguments are the same
- Different argument lists can be passed to different functions by using do.call():

```
myfun <- function(x, fun2.args=NULL, fun3.args=NULL, ...)</pre>
  ## calculations
  fun1(x, ...)
  do.call(fun2, fun2.args)
                                 # first arg is either function
  do.call("fun3", fun3.args) # or character
  ## further calculations
myfun(x, fun2.args=list(arg1=value))
```

#### **Return Values**

- The last expression evaluated in a function becomes the return value, the result of invoking the function.
- Functions can return only a single object, so that you have to combine a number of objects in a list.
- Functions can return invisible values, which are not printed out by default when you call the function.
- The code in on.exit() is run regardless of how the function exits.

```
hist_2by2 <- function(data, args, ...) {
  opar <- par(no.readonly = TRUE)
  on.exit(par(opar))
  par(mfrow = c(2, 2))
  # do histrogram plots for all variables in the data frame
  invisible(apply(data, MARGIN = 2, hist, ...))
}
hist_2by2(trees)</pre>
```

### **Basic Debugging Vocabulary**

- While it's true that with a good technique, you can productively debug a problem with just print(), there are times when additional help would be welcome.
- Wickham [2015] provides an outline for a general procedure for debugging:
  - realise that you have a bug: implement testing procedures!
  - 2 make it repeatable: create a minimal example
  - 3 figure out where it is: identify the line of code that's causing the bug
  - 4 fix it and test it: ensure you fixed the bug and have not introduced new ones

## **Basic Debugging Vocabulary**

Make the bug reproducible:

- make sure your workspace is empty
- set seed for drawing random numbers

options(error = c(NULL, browser, recover))

■ create a minimal example

#### **Bug Identification**

Binary search:

you repeatedly remove half of the code until you find the bug.

determines the sequence of calls that lead up to an error (call stack).

browser(), debug():

starts an interactive console in the environment where the error occurred.

### Bug Identification: traceback()

The first tool is the call stack, the sequence of calls that lead up to an error.

```
f <- function(a) g(a)
g <- function(b) h(b)
h <- function(c) i(c)</pre>
i <- function(d) "a" + d
f(10)
# Error in "a" + d (from #1) : non-numeric argument to binary
# operator
traceback()
# 4: i(c) at #1
# 3: h(b) at #1
# 2: g(a) at #1
# 1: f(10)
```

### Bug Identification: browser()

Go to the next statement if the function is being debugged. Continue execution if the browser was invoked.

Continue execution without single stepping.

Where: Show the call stack.

q: Halt execution and jump to the top-level immediately.

```
browser(mean(1:10))
Browse[2]> where
where 1: mean.default(1:10)
where 2: mean(1:10)
Browse[2]> n
debug: if (na.rm) x \leftarrow x[!is.na(x)]
Browse[2]> x
[1] 1 2 3 4 5 6 7 8 910
```

### **Additional Notes on Debugging**

- prevent bugs: Instead of trying to write one big function all at once, work interactively on small pieces.
- a function may generate an unexpected warning. The easiest way to track down warnings is to convert them into errors with options(warn = 2)
- a function may generate an unexpected message. There is no built-in tool to help solve this problem, but it is possible to create one:

```
message2error <- function(code) {
  withCallingHandlers(code, message = function(e) stop(e))
}</pre>
```

your code might crash R completely, which indicates a bug in the underlying C code.

### **Exception Handling**

- some error exceptions are no bugs:
  - numerical problems (over-/underflow)
  - unsuitable (user) inputs
  - convergence failure during iterative algorithms
- successful failure of code: When writing a function, you can often anticipate potential problems and communicate these to the user is the job of conditions:

```
Fatal errors are raised and force all execution to terminate.

warning() Display potential problems

Give informative output in a way that can easily be suppressed by the user (suppressMessages())
```

The behavior of error and warning can be adapted with options()

### stop()

With stop() fatal errors are raised and force all execution to terminate, when there is no way for a function to continue. Typical for testing function arguments follow:

```
f <- function(x) {
  if (!is.numeric(x))
    stop(''supplied x is not numeric.")
  s < - sim(x)
 message("sum = ", s)
f(1:10) #55
sum('nonsense')
# Error: invalid 'type' (character) of argument
f("nonsense")
# Error: supplied x is not numeric.
```

As alternative command, you can also use stopifnot().

### try-error()

- try() allows execution to continue even after an error has occurred.
- if unsuccessful it will return an (invisible) object of class "try-error"
- suppress the message with try(..., silent = TRUE)

```
f <- function(x, silent = TRUE) {
  s <- try(sum(x), silent = silent)
  if (inherits(s, "try-error")) {
    warning("x of wrong type, returning NA.")
   return(NA)
f(1:10)
## [1] 55
f("nonsense")
## Warning: x of wrong type, returning NA.
## [1] NA
```

### tryCatch()

tryCatch() is a general tool for handling conditions: take different actions for errors, warnings, messages, and interrupts.

```
f <- function(x, silent = FALSE) {
  s <- tryCatch(sum(x),
         error = function(e) {
                  warning("x of wrong type, sum is NA.")
                  if (!silent) print(e)
                  return(NA)
               },
               finally = cat("buh bye!\n"))
s }
f(1:10) # buh bye!
        # [1] 55
f("nonsense")
# Warning: x of wrong type, sum is NA.
# <simpleError in sum(x): invalid 'type' (character) of argument>
# buh bye!
# [1] NA
```

#### **Further References**

- Hadley Wickham. Advanced R. The R series. CRC Press, 2015. Chapter 6: Functions & Chapter 9: Exceptions and Debugging.
- Robert Gentleman and Luke Tierney. A prototype of a condition system for R. This describes an early version of R's condition system: http://homepage.stat.uiowa.edu/~luke/R/exceptions/simpcond.html

# **Object Oriented Programming**

#### **Motivation**

- in OOP, computer programs are made out of objects that interact with one another
- a class defines objects via attributes and their relationship to other classes.
- the class is also used when selecting methods, i.e. functions that behave differently depending on the class of their input.
- R has three OO systems: S3, S4, and the system of base types

#### **OOP Essentials**

- fundamental building blocks of a class system
  - definition of classes, generation of class instances
  - specification of inheritance
  - determination of a class and all parental classes of an object
  - access and modification of the class slots
  - class and method management
- generic functions are functions, that run different computations in dependence of the class of their arguments and even return different outputs

### **Base Types**

- base types are the internal C-level types that underlie the other OO systems
- underlying every R object is a C structure that describes how that object is stored in memory
- you can determine an object's base type with typeof()
- the most common base types are atomic vectors and lists, but also encompass functions, environments, other more exotic objects
- functions that behave differently for different base types are almost always written in C

### S3 Object System

- S3 is R's first and simplest OO system
- S3 is informal, ad-hoc, and minimal
- test if an object is an S3 object by using pryr::otype()
- test for a specific class by class()

```
df <- data.frame(x = 1:10, y = letters[1:10])
otype(df)  # [1] "S3"
otype(df$x)  # [1] "base"
otype(df$y)  # [1] "S3"</pre>
```

#### S3 Methods

■ S3 objects at first glance

```
mean
# function (x, ...)
# UseMethod("mean")
# <bytecode: 0x2bc14a0>
# <environment: namespace:base>
```

- pryr::ftype() describes the object system. Default method is generic
  - ftype(mean) # [1] "s3" "generic"
- you can recognise S3 methods by their names, e.g. the Date method for the mean() generic is called mean.Date()
- methods() returns all methods that belong to a generic or lists all generics that have a method for a given class

```
methods("mean")
methods(class = "ts")
```

### **Define S3 Classes and Create Objects**

- can change the class of a base object.
- class names are usually lower case, and you should avoid "."
- S3 has no checks for correctness

#### **Create new Methods and Generics**

- to add a new generic, create a function that calls UseMethod()
- to add a method, you just create a regular function with the correct generic.class name (adding a method to an existing generic works in the same way)

#### S3 Problems

- S3 has no formal definition and therefore no checks for correctness, when construction objects, i.e. every object can get every class
- while you can change the type of an object, but you never should

```
mod <- lm(log(mpg) ~ log(disp), data = mtcars)
class(mod)
print(mod)
class(mod) <- "data.frame"
print(mod)</pre>
```

Not very helpful!

■ the name convention for finding object-specific methods use the dot, which is not a special symbol

```
Does t.test.default() transpose an object from class test.default, or is it the default method for t.test()?
```

# S4 Object System

- S4 works in a similar way to S3, but it adds formality and rigour
- classes have formal definitions which describe their fields and inheritance structures
- identify an S4 object by using isS4(), pryr::otype() or pryr::ftype()

```
require(stats4)
# From example(mle)
y \leftarrow c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
nLL <- function(lambda) - sum(dpois(y, lambda, log = TRUE))
fit <- mle(nLL, start = list(lambda = 5), nobs = length(y))
# An S4 object
isS4(fit) # [1] TRUE
otype(fit) # [1] "S4"
# An S4 generic
isS4(nobs) # [1] TRUE
ftype(nobs) #[1] "s4" "generic"
```

#### **Define S4 Classes and Create Objects**

■ define the representation of a class with setClass() with properties:

```
name S4 class names use UpperCamelCase slots defines field names and permitted classes contains string giving the class it inherits from walidity method that tests if an object is valid prototype object that defines default slot values
```

create a new object with new() or a constructor function with the same name as the class (usually available)

#### **Create new Methods and Generics**

- setGeneric() creates a new generic or converts an existing function into a generic
- setMethod() takes the name of the generic, the classes the method should be associated with, and a function that implements the method
- standardGeneric() is the S4 equivalent to UseMethod() to create
  a new generic from scratch

```
setGeneric("union") # [1] "union"
setMethod("union",
    c(x = "data.frame", y = "data.frame"),
    function(x, y) {
       unique(rbind(x, y))
    }
)
showMethods("union") # x="ANY", y="ANY"
    # x="data.frame", y="data.frame"
```

#### Picking a System

- majority of OO code that I have written in R is S3
- S3 is sufficient for fairly simple objects and methods for pre-existing generic functions like print(), summary(), and plot()
- S4 may be more appropriate for more complicated systems of interrelated objects
- good example for S4 is the Matrix package by Douglas Bates and Martin Maechler

# S3/S4 Object System Comparison

	S3	S4	
defintion	not neccessary	setClass('class	
		name',)	
generation of	class(object)<-	new('class_name')	
instances	'class_name'		
inheritance	vector of class_names (children	contains='parental	
	before parents)	cl' in definition	
test class	<pre>inherits(object, 'class_name')</pre>	<pre>is(object, 'class_name')</pre>	
access slots	depends on base type: for lists \$	new operator: @	
	or [[]].		
list methods	methods()	showMethods()	

#### Conventions

For S3 and S4, there are the following conventions

- constructor functions should be named like the class itself, e.g. lm(),
   with exception if a class is the return value of a number of functions
- standard methods, which are available supplied for many classes:

```
print basic object information, also when using <RET> (S4 show()) summary more detailed description of the objects instance plot graphics
```

 every method should have the arguments of the corresponding generic (same order and defaults) and accept an arbitrary number of additional arguments (use ...)

#### **Further Reading**

- Hadley Wickham. Advanced R.The R series. CRC Press, 2015. Chapter 7: OO field guide. Available online: http://adv-r.had.co.nz/00-essentials.html
- Laurent Gatto. A practical tutorial on S4 programming. Available online:

http://www.bioconductor.org/help/course-materials/2013/CSAMA2013/friday/afternoon/S4-tutorial.pdf

Profiling, Performance &

**Parallelization** 

#### **Motivation**

- it is useful to measure the runtime of code
- optimising code to make it run faster is an iterative process:
  - 1 find the biggest bottleneck (the slowest part of your code).
  - 2 try to eliminate it
  - 3 repeat until your code is "fast enough"
- parallelization saves time because you are using more of your computer's resources

#### **Performance Measurment**

- system.time() quick and dirty performance accessment
- microbenchmark:: performance of a very small piece of code
- Rprof() detailled analysis, where how much computing time is required
- lineprof and shine(): interactive profiling with information about memory usage and graphical interface (see memory session)

# system.time()

```
x <- rnorm(100000)
system.time({s <- 0}
            for(i in 1:length(x))
s \leftarrow s + x[i] })
#
  user system elapsed
#
   0.12 0.00
                0.23
system.time({s <- 0}
            for(v in x)
s < -s + v  })
 user system elapsed
# 0.089 0.000 0.076
system.time(sum(x))
  user system elapsed
# 0.000 0.000 0.001
```

# Microbenchmarking

- measurement of the performance of a very small piece of code
- use the microbenchmark package

```
require(microbenchmark)
x <- runif(100)
microbenchmark(
sqrt(x),
x ^ 0.5 )
# Unit: microseconds
# expr min lq mean median uq max neval
# sqrt(x) 1.840 1.9395 2.17828 2.0150 2.076 15.885 100
# x^0.5 11.519 11.7245 12.50866 11.7965 11.902 40.353 100</pre>
```

# Rprof()

■ create a file with your function, e.g. Rprof.r: foo <- function(reps = 20, n = 1e5){ for(r in seq\_len(reps)) {  $x \leftarrow rnorm(n)$ o <- order(x) x < -x[o]invisible(NULL) ■ create a file with your function, e.g. Rprof.r: Rprof("foo-prof.log", line.profiling = TRUE) foo() Rprof(NULL) check results with: summaryRprof("foo-prof.log", lines = 'show')

# lineprof and shine()

```
require(lineprof)
lineprof_example <- lineprof(foo())
shine(lineprof_example)</pre>
```

#### Why is R slow?

- a lot of R code is poorly written, because a few R users have any formal training in programming or software development
- R language is informal and incomplete
- extreme dynamism, so that almost everything can be modified after it is created
- name lookup with mutable environments: due to the combination of lexical scoping and extreme dynamism, it is difficult to find the value associated with a name in the R-language
- lazy evaluation of function arguments: each additional argument to a function decreases its speed a little

# **Optimizing Code**

#### Strategies to achieve better performance:

- look for existing solutions (search online, talk to your colleagues, reverse Rccp dependencies, ...)
- 2 do less work
- 3 vectorize
- 4 parallelize
- avoid copies (whenever you use c(), append(), ... to create a bigger object, R must first allocate space for the new object and then copy the old object to its new home)
- **6** byte-code compile (if code consists of many elemental operations, and is not calling often high-level functions)
- $\mathbf{7}$  rewrite key functions in C++ (next session)

# Optimize code by doing less work

- use a function tailored to a more specific type of input or ouput, or a more specific problem, e.g.
  - rowSums(), colSums(), rowMeans(), and colMeans() are faster than equivalent invocations that use apply() because they are vectorised
- avoid functions which coerce their inputs into a specific type, if your input is not the right type
- functions will do less work if you give them more information about the problem: carefully read the documentation and experiment with different arguments, e.g.
  - read.csv(): specify known column types with colClasses
  - cut(): do not generate labels with labels = FALSE if you do not need them, or, even better, use findInterval()

#### Vectorize

Vectorize means often to use functionals, which is a function that takes a function as an input and returns a vector as output

- the three most frequently used are lapply(), apply(), and tapply()
- as an alternative to for loops
- reduce bugs in your code by better communicating intent
- many are written in C, and use special tricks to enhance performance

```
sqrt2 <- function(x){
   out <- vector(?list?, length(x))
   for(i in seq_along(x)){
      out[[i]] <- sqrt(i)
   }return(out)}
microbenchmark(
   unlist(sqrt2(1:10)),
   unlist(lapply(1:10, sqrt)))</pre>
```

#### **Functionals**

- base functionals is that they have grown organically over time and are not very consistent
- base R only covers a partial set of possible combinations of input and output types:
- the plyr package provides consistently named functions and covers all combinations of input and output data structures:

	list	data frame	array
list	llply()	ldply()	laply
data frame	dlply()	ddply()	daply
array	alply()	adply()	aaply

#### Multicore CPU

- parallelization uses multiple cores to work simultaneously on different parts of a problem
- does not reduce the computing time, but it saves your time because you are using more of your computer's resources
- Unix: simply substitute parallel::mclapply() for lapply()
  system.time(lapply(1:10, pause(0.25)))

  # user system elapsed
  # 0.000 0.004 2.504
  system.time(mclapply(1:10, pause(0.25), mc.cores = 4))
  # user system elapsed
  # 0.011 0.021 0.758
- "Life is a bit harder in Windows" (Wickham): first set up a local cluster and then use parallel::parLapply()
- for platform-independent implementations check for instance source code
   of boot::boot()

#### **Further Reading**

- Hadley Wickham. Advanced R. The R series. CRC Press, 2015.
   Chapter 11: Functionals, Chapter 16: Performance, Chapter 17:
   Optimising Code, Chapter 18 Memory.
- Floreal Morandat, Brandon Hill, Leo Osvald, and Jan Vitek: Evaluating the Design of the R Language. Available online: http://r.cs.purdue.edu/pub/ecoop12.pdf
- Norman Matloff (2011): The Art of R Programming.

# R Interaction with Other Languages

# **Other Languages**

Several programming languages can be included in R:

- C (nlm,optimize,...)
- FORTRAN (subroutines of fields package)
- C++ (Amelia, RcppDE)

# Why R?

C++ can be integrated with the add-on packages Rcpp. Why do we want to integrate C++?

- R is very slow for loops
- Parallelization is nice, but
  - does not reduce the total computational time
  - lacktriangle is not possible for iterative calculations

# **Application**

Determination of the reasons for chronic undernutrition in Peru.

Estimation of the model

stunting = 
$$sex + mEdu + PartnerEdu + householdmembers$$
  
  $+f(breastfeeding) + f(cage) + f(mage) + f(mbmi)$   
  $+f(mheight) + f(wealthscore) + f_{spat}(region)$ 

for  $\tau=5\%$  takes

- 226s with pure R code
- 24s with integration of C++ parts

# Why R?

#### Why R?

- Easy handling of input and output
- No compilation needed
- Good error detection
- Many statistical methods already implemented
- Easy/quick programming

#### **Rcpp**

Rcpp is a easy, nice and fast way to call C++ from R:

- Hadley Wickham. Advanced R. The R series. CRC Press, Boca Raton, 2015. Chapter 19: Rcpp
- Dirk Eddelbuettel. Seamless R and C++ Integration with Rcpp. Springer, New York, 2013
- http://www.rcpp.org
- http://cran.r-project.org/web/packages/Rcpp/index.html
- http://lists.r-forge.r-project.org/mailman/listinfo/ rcpp-devel

#### To learn C++:

- http://www.learncpp.com/
- http://www.cplusplus.com/

#### Compiler

To run Rcpp a C++ compiler is required:

- Windows: Rtools
  http://cran.r-project.org/bin/windows/Rtools/
- Mac: Xcode app store
- Linux: sudo apt-get install r-base-dev

Take care when installing Rtools:

- Path of R must not contain any spaces!
  (C:\R\R-3.x.y)
- Path of Rtools must not contain any spaces!
  (C:\R\Rtools\gcc-4.6.3\bin)
- Some useful tricks: http://lists.r-forge.r-project.org/ pipermail/rcpp-devel/2012-July/003979.html

#### **General Structure**

General Structure: cppFunction( 'variable-type-output function-name(variable-type-input variable-name) ...; ... ; return output; }') Example: library(Rcpp) cppFunction('double meanC(double x, double y, double z) { double m = (x + y + z) / 3; return m; }') meanC(1, 2, 8)

#### C++ Basics

- Specify variable type, e.g. double, int,...
- End each statement with ;
- Use = for assignment not <-
- Return value with return ...;
- Comment with

```
// ... for one line
/* ...
... for multiple lines
... */
```

# C++ Variable Types

R	Rcpp	Values
integer	int	$\mathbb{Z}$
numeric	double	$\mathbb{R}$
logical	bool	TRUE, FALSE, NA (R)
		true, false $(C++)$
character	String	e.g. "a", "text", "Word"
numeric vector	NumericVector	e.g. $(3.1, 3.2, 3.3)^T$
numeric matrix	NumericMatrix	e.g. $\begin{bmatrix} 3.1 & 3.2 & 3.3 \\ 7.1 & 8.2 & 9.3 \end{bmatrix}$

# NumericVector and for-loop

```
cppFunction('double sumC(NumericVector x) {
  int n = x.size();
  double total = 0;
  for(int i = 0; i < n; i++) {
    total += x[i];
  }
  return total;
}')</pre>
```

- Length of a vector with .size()
- Dimensions of a matrix with .ncol() and .nrow()
- Element of a vector/matrix with () or [] (only vector)
- First element of a vector has number 0 and Last element of a vector has number n-1
- i++ is a postfix operator for i=i+1
- total +=  $x[i] \Leftrightarrow total = total + x[i]$ , similar are -=, \*= and /=

#### Sugar

Several methods for elementwise operations of vectors are implemented in RcppSugar:

■ Basic operations:

```
+, *, -, /, pow(,), <, <=, >, >=, ==, !=, !
```

Standard functions:

```
abs(), ceiling(), exp(), log(), log10(), signif(), sin(), sqrt(), . . .
```

Basic statistics:

```
mean(), min(), max(), sum(), sd(), var(), cumsum(),
diff(), pmin(), pmax(), . . .
```

In RcppSugar these methods are only available for vectors and not for matrices!!!

#### Sugar

Elementwise calculation like in R possible with RcppSugar, e.g.

$$12\operatorname{norm}(\boldsymbol{x},\boldsymbol{y}) = \sqrt{\frac{1}{n}\sum_{i=1}^{n}(x_i - y_i)^2}$$

```
cppFunction('List 12norm1(NumericVector x, NumericVector y) {
    NumericVector dist = x - y;
    NumericVector dist2 = pow(dist, 2);
    double meandist = mean(dist2);
    double edist = sqrt(meandist);
    return List::create(Named("dist") = dist,
                        Named("dist2") = dist2,
                        Named("meandist") = meandist.
                        Named("edist") = edist);
}')
cppFunction('double 12norm2(NumericVector x, NumericVector y) {
    return sqrt(mean(pow((x - y), 2)));
    }')
```

#### Inline & Eigen

- With inline additional features like RcppEigen can easily be included
- Eigen is a powerful C++ library for matrix operations and advanced routines

http://eigen.tuxfamily.org/dox/index.html

Alternatively RcppArmadillo can be used http://arma.sourceforge.net/

# Inline & Eigen

$$\hat{\boldsymbol{\beta}} = (\boldsymbol{X}^{\top}\boldsymbol{X})^{-1}\boldsymbol{X}^{\top}\boldsymbol{y}$$

```
library(Rcpp)
library(inline)
LMcpp <- '
using Eigen::MatrixXd;
using Eigen::VectorXd;
VectorXd y(as<VectorXd>(yy));
MatrixXd X(as<MatrixXd>(XX));
VectorXd b = ((X.adjoint() * X).inverse()) * X.adjoint() * y;
return List::create(Named("y")=y,Named("X")=X,Named("b")=b);
,
simpleLM <- cxxfunction(signature(yy = "numeric", XX = "matrix"),</pre>
                        LMcpp, plugin = "RcppEigen")
```

# Inline & Eigen

$$R^{2} = \left(1 - \sum_{i=1}^{n} \hat{\epsilon}_{i}^{2}\right) / \left(\sum_{i=1}^{n} (y_{i} - \bar{y})^{2}\right)$$

For elementwise operations inside Eigen objects use array format

```
LMcpp <- 'using Eigen::MatrixXd;</pre>
          using Eigen::VectorXd;
          VectorXd v(as<VectorXd>(vv));
          MatrixXd X(as<MatrixXd>(XX)):
          VectorXd b = ((X.adjoint() * X).inverse()) * X.adjoint() * y;
          VectorXd resid = v - X * b;
          VectorXd resid2 = pow(resid.array(),2);
          VectorXd diffY = y.array() - y.mean();
          VectorXd diffY2 = pow(diffY.array(),2);
          double R2 = 1 - (resid2.sum()) / (diffY2.sum());
          return List::create(Named("y")=y, Named("X")=X,
          Named("b")=b, Named("R2")=R2);
```

### Pointer to R

Manipulating the C++ object also changes the underlying R object, since the C++ object is a pointer to the R object.

```
manip_bad <- '
    NumericVector invec(vx);
    NumericVector outvec(vx);
    for(int i = 0; i < invec.size(); i++) {</pre>
        outvec[i] = log(invec[i]);
    return outvec;
    ,
fun_bad <- cxxfunction(signature(vx="numeric"), manip_bad, "Rcpp")</pre>
x \leftarrow seq(1.0, 3.0, by=1)
fun_bad(x) ## 0.0000000 0.6931472 1.0986123
              ## 0.0000000 0.6931472 1.0986123
X
```

### Pointer to R

The function clone() produces a hard copy of the input, thus the original input is not manipulated anymore.

```
manip_good <- '
    NumericVector invec(vx);
    NumericVector outvec = clone(vx):
    for(int i = 0; i < invec.size(); i++) {</pre>
        outvec[i] = log(invec[i]);
    return outvec;
    ,
fun_good <- cxxfunction(signature(vx="numeric"), manip_good, "Rcpp")</pre>
x \leftarrow seq(1.0, 3.0, by=1)
fun_good(x) ## 0.0000000 0.6931472 1.0986123
            ## 1 2 3
X
```

# **Further Reading**

- Dirk Eddelbuettel. Seamless R and C++ Integration with Rcpp. Springer, New York, 2013
- Hadley Wickham. Advanced R. The R series. CRC Press, Boca Raton, 2015. Chapter 19: Rcpp
- http://lists.r-forge.r-project.org/mailman/listinfo/ rcpp-devel
- http://eigen.tuxfamily.org/
- http://arma.sourceforge.net/

**Numerics & Simulations** 

### **Basics**

### Representation of numbers

- Computers use indicators to encode information (1 for ON, 0 for OFF)
- One indicator is called a bit, eight bits are one byte, ...
- The way how numbers are represented depends on your computer, R has no influence on that

# Representation of integers

The sign-and-magnitude scheme

- Use one bit for the sign  $(\pm)$  and the rest for the magnitude
- For k bits an integer is represented as

$$\pm b_{k-2} \dots b_2 b_1 b_0$$
,

where each  $b_i$  is 0 or 1. This number is translated to

$$\pm (2^0b_0 + 2^1b_1 + \cdots + 2^{k-2}b_{k-2})$$

### Example 8.1

For k = 8, -1001101 represents the number

$$-(2^{0} \cdot 1 + 2^{1} \cdot 0 + 2^{2} \cdot 1 + 2^{3} \cdot 1 + 2^{4} \cdot 0 + 2^{5} \cdot 0 + 2^{6} \cdot 1) = -77.$$

# Representation of integers

### Properties and extensions

- Integers range symmetrically from  $-(2^{k-1}-1)$  to  $2^{k-1}-1$
- Two representations of 0 ( $\pm$ )
  - The biased scheme (see references): avoids -0, but addition of integers is complex and slow
  - 2 The *two's complement scheme*: uses the binary representation for positive integers and represents  $-1, -2, \ldots, -2^{k-1}$  via  $2^k 1, 2^k 2, \ldots, 2^k 2^{k-1}$
- Integers have infinite cardinality. In R, there is a "largest" integer
- > .Machine\$integer.max
- [1] 2147483647

### Properties:

Computers need to limit the size of the mantissa and exponent. In double precision

- use 8 bytes (i.e. 64 bits) in total
- 1 bit for the sign
- 52 bits for the mantissa
- 11 bits for the exponent (representation via *biased scheme*, ranges from -1022 to 1024)
- There is also a "largest" real
- > .Machine\$double.xmin
- [1] 2.225074e-308
- > .Machine\$double.xmax
- [1] 1.797693e+308

### Further examples:

■ Underflow/ overflow

```
> 2^1023 + 2^1022 + 2^1021
[1] 1.572981e+308
> 2^1023 + 2^1022 + 2^1022
[1] Inf
```

■ "Asymmetry"

```
> 2^(-1074) == 0

[1] FALSE

> 2^(-1075) == 0

[1] TRUE

> 1 / 2^(-1074)

[1] Inf
```

■ Machine epsilon (smallest x, s.t. 1 + x can be distinguished from 1); round off

#### Numerical errors:

Numerical errors occur all the time. E.g. there is no finite binary representation of 0.1. Denote by  $\tilde{x}$  an approximation of x.

- lacktriangle The absolute error is defined as  $|x-\tilde{x}|$
- The relative error is defined as  $\frac{|x-\tilde{x}|}{x}$

Catastrophic cancellation describes a loss of accuracy with a relative error of  $10^{-8}$  or larger due to error propagation. It can occur when subtracting numbers of similar size.

# Example

Computation of sin(x) - x to 0

Standard computation

$$\lim_{x \to 0} \frac{\sin(x)}{x} = 1 \Rightarrow \sin(x) \approx x \quad \text{near} \quad 0$$

■ Taylor expansion of order 2

$$\sin(x) - x \approx -\frac{x^3}{6} + \frac{x^5}{120} = -\frac{x^3}{6} \left(1 - \frac{x^2}{20}\right)$$

- Relative errors:  $\approx 10^{-11}$ ,  $10^{-4}$ , 1
- Catastrophic cancellation at  $x = 2^{-20}$  and  $x = 2^{-30}$ !

# **Numerical Algorithms**

#### Generalities

- For many mathematical and statistical problems there are no analytical solutions (or they are very hard to find)
- Examples are optimization, integration, solving (systems of) equations, differentiation, eigenvalue problems, . . .
- For most cases, numerical alternatives have been developed and implemented
- Key features of such algorithms are accuracy/precision and convergence (rate)/speed

# **Numerical Algorithms**

Some important functions for numerical mathematics in R:

optimization	derivation	(system of) equations	integration	other
optim(ize)	deriv	solve	integrate	eigen
optimx	grad	polyroot	${\tt adaptIntegrate}$	qr
nlm	hessian	solveLP		

See http://cran.r-project.org/web/views/Optimization.html for more.

Note that also other functions like glm or lme use numerical techniques to optimize the likelihood with respect to the regression parameters.

### **Example**

```
Find the minimum of the function f(x) = x^2. What is the value of
\int_{-2}^{2} x^2 dx?
> my.square = function(x) {
+ x^2
+}
> optimize(f = my.square, interval = c(-2, 2)) $minimum
[1] -5.551115e-17
$objective
[1] 3.081488e-33
> optimize(f = my.square, interval = c(2, 3))
$minimum
[1] 2.000066
$objective
[1] 4.000264
> integrate(f = my.square, lower = -2, upper = 2)
5.333333 with absolute error < 5.9e-14
```

### **Simulations**

### **Definition 8.1**

A (Monte-Carlo)-Simulation is a numerical technique for conducting experiments on a computer. The term Monte-Carlo refers to the involvement of random experiments.

#### Application areas:

Simulation studies are performed when analytical results are hard or impossible to find to

- identify properties of estimators or test statistics (bias, variance, distribution, etc.)
- investigate consequences of violations of model assumptions
- find out about the influence of the sample size
- compare different models or estimators (in terms of bias, precision, computational time, etc.)

### **Simulations**

#### Rationale

- Estimators and test statistics have true sampling distributions (under certain assumptions)
- Knowing the distribution would answer all questions about the properties described above
- Approximate these distributions by conducting according random experiments very often (law of large numbers)

### Usual setup

- lacktriangle Simulate K independent data sets under the conditions of interest
- Calculate the numerical values of the statistic T of interest for each data set, i.e.  $T_1, \ldots, T_K$
- Evaluate the properties of the results under the assumption that the distribution of  $T_1, \ldots, T_K$  approximates the true distribution of the statistic

### Stochastic distributions in R

In R, density (d), distribution (p), quantile (q), and (pseudo) random number generator (r) functions are already implemented.

function	distribution
beta()	beta-
binom()	binomial-
exp()	exponential-
gamma()	gamma-
hyper()	hypergeometric-
logis()	logistic-
<pre>lnorm()</pre>	lognormal-
<pre>nbinom()</pre>	negativ binomial-
norm()	normal-
<pre>pois()</pre>	poisson-
t()	t-
unif()	uniform-

### Stochastic distributions in R

#### Further notes

- The random numbers in R are not really random
- Use set.seed to make your results replicable

```
> set.seed(123)
> rnorm(3)
[1] -0.5604756 -0.2301775  1.5587083
> rnorm(3)
[1] 0.07050839 0.12928774 1.71506499
> set.seed(123)
> rnorm(3)
[1] -0.5604756 -0.2301775  1.5587083
> set.seed(123)
> rnorm(3)
[1] -0.5604756 -0.2301775  1.5587083
```

# Case study

Stochastic Frontier type data:

Stochastic Frontier Analysis (SFA) belongs to the field of productivity analysis

- Aim: quantify inefficiency and determine a production function
- Assumptions: deviations from the production function (the errors) are a combination of stochastic noise and inefficiency, formally  $\epsilon = v u$ .
- Comparison: the model formulation deviates from the classical linear model only in terms of inefficiency

# Case Study

Investigate the behavior of the estimator for the linear regression model without intercept

$$y_i = \beta x_i + \epsilon_i, \quad i = 1, ..., n, \tag{1}$$

when the distributional assumption  $\epsilon_i \stackrel{iid}{\sim} \mathcal{N}(0, \sigma^2)$  is violated.

More precisely, simulate K=50 independent data sets of sample size n=200 with

- $\blacksquare x_i \sim \mathcal{N}(3,2)$
- $lacksquare \epsilon_i = u_i v_i$ , where  $u_i \sim \mathcal{N}(0, 1^2)$  and  $v_i \sim \mathcal{N}_+(0, 1^2)$
- $\beta = 2$
- $y_i$  according to (1).

and estimate the covariate effect for each of the data sets. What are the approximate mean and variance of  $\hat{\beta}$ ?

# **Further Reading**

- Jones, Maillardet and Robinson (2009): Scientific Programming and Simulation Using R
- http://cran.r-project.org/web/views/ NumericalMathematics.html
- http://cran.r-project.org/web/views/Optimization.html
- http://cran.r-project.org/web/views/Distributions.html

**Building R Packages** 

# Why Building R Packages?

- platform-independent distribution of R code
  - alpha/beta versions on R-forge or github
  - finished projects on CRAN or Bioconductor
- archiving R code for a specific project and software documentation
- reproducible research: distribute data and software accompanying a paper maintainance of dependencies, and automated loading of required external code
- CRAN uses R CMD check to test package on various platforms; packages are tested daily

## **Basic Structure**

A basic (but good) R package has the following structure:

DESCRIPTION what does the package? who can use it (license)?

who is responsible (maintainer)?

which function should be seen by the user? which

are internal?

R/ R functions

documentation, help files with syntax similar to

man/

data/ example data files

The standard structure can be obtained automatically using

utils::package.skeleton or tools in packages

devtools::create or roxygen2.

### **Basic Structure**

### Naming R Packages:

- can contain letters and numbers, but start with a letter
- avoid self-invented abbreviations, captital letters, ...
- should be identifiable in online search

### R/ directory contains all R code:

- each function in a separate file (good for small packages)
- everything in one file (ok for small packages)
- group related functions in a file with meaningful names (best solution for larger projects)

### **Basic Structure**

## Additional (optional) files in R packages:

```
NEWS describes changings over different package versions demo/ larger demos
src/ C, C++, FORTRAN source code
inst/CITATION how should the user cite the package?
inst/doc/ vignette
test/, inst/tests tests
:
```

#### DESCRIPTION

Package: name of the package

Title: description of the package (one line, ¡ 65 characters)

detailed description (one paragraph, multiple sen-

Description: tences)

Version: version number formatwise

major.minor-patchlevel or
major.minor.patchlevel

name and e-mail of a person who wants to take over Maintainer:

the responsibility

abbreviation of a software licence (GPL-2, BSD,

MIT, ...)

Depends, Suggests,

Imports, Enhances: package dependencies URL: for website of a package

Collate: order R files are loaded (default: alphabetically)

### DESCRIPTION

#### NAMESPACE

- although the file looks like R code, it is not processed as R code
- specifies which variables in the package should be exported to make them available to package users, and which variables should be imported from other packages

```
import(foo, bar)  # all functions from foo and bar import
importFrom(foo, f, g) # selected functions f and g from foo
export(f, g)  # export functions f and g
```

- for packages with many variables to export it may be more convenient to specify the names to export with a regular expression exportPattern("\^{}\\^{}\textbackslash\textbackslash.]")
- assign the DLL reference for the C functions myRoutine, myOtherRoutine from DLL foo:

#### S3 NAMESPACE

- ensure that the generics are imported and register the methods using S3method directives
- the function print.foo does not need to be exported

```
# example samplingbook
export(Smean)
S3method(print, Smean)
export(htestimate)
S3method(print, htestimate)
# example ggplot2
S3method(autoplot, default)
export(autoplot)
import(plyr)
importFrom(MASS,cov.trob)
```

#### **S4** NAMESPACE

- some additional steps are needed for packages which make use of S4 classes and methods
- package should depend on package methods (also DESCRIPTION file)
- you may need to import graphics::plot to make visible a function that can be converted into a implicit generic

```
import("methods")  # S4
import("ff")  # namespaces from dependencies
import("igraph")
importFrom(graphics, "plot")  # S4 plot
exportPattern("^[[:alpha:]]+")  # regular pattern
exportMethods("GeneSNPsize", "plot", "show", "summary")
exportClasses("GWASdata", "kernel", "pathway", "lkmt")
```

### .Rd manual file

■ R documentation format is very LATEX-like output (LATEX installation required)

```
\name{add}
\alias{add}
\title{Add together two numbers}
\usage{ add(x, y) }
\arguments{
  \item{x}{A number}
  \item{y}{A number}
\value{The sum of \code{x} and \code{y}}
\description{ Add together two numbers }
\examples{
add(1, 1)
add(10, 1)
```

# **Building R Packages**

For building a R package pkg run the following commands in your console:

R CMD SHLIB pkg	compiles $C/C++/Fortran$ code in
it one billie pag	pkg/src
R CMD build pkg	generates package bundle
it one build pag	pkg.tar.gz or pkg.zip
R CMD INSTALL pkg.tar.gz	installs package
R CMD check pkg.tar.gz	runs CRAN validity checks (is pkg
1 0 0	valid?)

In windows, installation of Rtools is required:

```
# On windows:
R CMD INSTALL --build pkg
```

## devtools

 $\ensuremath{\mathsf{R}}$  functions from devtools that simplifies  $\ensuremath{\mathsf{R}}$  packaging:

load all()	simulates installing and reloading your package
document()	updates documentation, file collation and NAMESPACE
test()	reloads your code, then runs all testthat tests.
run	examples() will run all examples to make sure they work.
check doc()	runs most of the documentation checking components of R CMD check
check()	updates the documentation, then builds and checks the package
<pre>build(), build win()</pre>	builds a package file from package sources (only one R version) $ \\$

#### testthat

The package testthat provides functions that make it easy to describe what you expect a function to do:

```
describes expected result of your code (value, class,
 expect_that
                        correct error message, computation time, etc.)
                        is grouping a number of expectation?s for one func-
 test_that
                        tions or a feature
                        is grouping a number of content-related tests
 context()
require(testthat)
test_that("trigonometric functions match identities", {
  expect_that(sin(pi / 4), equals(1 / sqrt(2)))
  expect_that(cos(pi / 4), equals(1 / sqrt(2)))
  expect_that(tan(pi / 4), equals(1))
})
```

#### testthat

The package testthat easily integrates in your existing workflow, whether it's informal testing on the command line, building test suites or using R CMD check

within your workflow:

```
testthat::test_file() # test in a file
testthat::test_dir() # all ?test-? files in a directory
```

within a package:

```
library(testthat)
library(yourpackage)
test_check("yourpackage")
test_package("yourpackage")
```

- using R CMD check:
  - DESCRIPTION needs Suggests testthat
  - test files in tests/testthat/ are automatically tested

# Package roxygen2

There are three steps in the transformation from roxygen comments in your source file to human readable documentation:

- add roxygen comments to your source file
- 2 roxygen2::roxygenise() or devtools::document() converts
  roxygen comments to .Rd files
- 3 R CMD check converts . Rd files to human readable documentation

# Package roxygen2

- roxygen comments start with #'
- tags like @param, @return, @author define parts in .Rd file
- tags like @includes, @export, @importFrom generate NAMESPACE und Collate
- tags like @method for OOP documentation

```
#' Add together two numbers
#'
#' @param x A number
#' @param y A number
#' @return The sum of \code{x} and \code{y}
#' @examples
#' add(1, 1)
#' add(10, 1)
add <- function(x, y) { x+y
}</pre>
```

# Package roxygen2

add (rvest) R Documentation Add together two numbers Description Add together two numbers Usage add(x, y) Arguments x A number y A number Value The sum of x and y Examples add(1, 1) add(10, 1)

# **Further Reading**

- Writing R Extensions manual: http://cran.r-project. org/doc/manuals/r-release/R-exts.html
- Hadley Wickham (2015). R packages. O'Reilly Media. Available online: http://r-pkgs.had.co.nz/
- Friedrich Leisch. Creating R Packages: A Tutorial: http://cran.r-project.org/doc/contrib/ Leisch-CreatingPackages.pdf
- testthat: Hadley Wickham (2011). testthat: Get Started with Testing. The R Journal 3(1).
- roxygen2: http://cran.r-project.org/web/packages/ roxygen2/vignettes/rd.html
- Dirk Eddelbuettel & Romain Francois: Writing a package that uses
  Rcpp: http://dirk.eddelbuettel.com/code/rcpp/
  Rcpp-package.pdf