

**Assignment – 2**

(Topics covered: Basic Functions, Lists, Recursion)

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The Möbius Function is a simple classifier of positive integers, devised by August Möbius. Given a positive integer  $n$ , the Möbius function  $\mu(n)$  returns:

- 0 if the number is a multiple of a square
- -1 if the number has an odd number of distinct prime factors
- 1 if the number has an even number of distinct prime factors

The  $n = 1$  case is a special case;  $\mu(1)$  is defined to return 1.

You can probably see right away that this function is all about generating and then analyzing the list of prime factors for the input value. A number is a multiple of a square if it has any duplicate prime factors; for example,  $12 = 2 \times 2 \times 3$ , so it is a multiple of a square, and therefore  $\mu(12) = 0$ .

For this section we will focus on one interesting detail about the Möbius Function; runs of square-multiples. We want to **write a program that finds the first run of square-multiples of length N**. For example, the first run of three square-multiples ( $N=3$ ) starts with 48; 48, 49 and 50 are all multiples of squares.

**Note:** I will be testing each sub function with all random test cases ;)

**All of your recursive functions for this section should be tail-recursive!**

**Your Tasks**

1. Create a module named "<your first name>", in the file "<your first name>.erl".

Example: module named "akshay", in the file akshay.erl

**Functions to code:**

**2. Create a function `is_prime` that takes a single argument `N`, and returns true if the number is prime, or false if the number is not prime.**

Your implementation doesn't need to be particularly fast. For example, you can create a helper function that iterates over integers from 2 to  $\sqrt{N}$ , checking whether `N` is evenly divisible by each value. If `N` is not evenly divisible by any value then it is prime; otherwise, it is not prime.

Some Tips from my side to decrease computation time:

- Tip 1:** You can use the remainder operator `rem` to check if `N` is evenly divisible by a particular value. `A rem B` returns the remainder from dividing `A` by `B`.
- Tip 2:** Computing square-roots is computationally costly. A better approach is to take the value, which we will call `Val`, and if  $Val \times Val > N$  then you are done. (You could use guard statements [when etc.] )

Add `is_prime` to your module's export-list, and test it to make sure it works properly.

**3. Create a function `prime_factors` that takes a single argument `N`, and returns a list of all prime factors of `N`.** The result doesn't have to be in any particular order. Add this function to your module's export-list.

**4. Create a function `is_square_multiple` that takes a single argument `N`, and returns true if the argument is a multiple of some square, or false if it is not.**

- Tip 1:** A number is a multiple of a square if it has any prime-factors that appear more than once.
- Tip 2:** You might find some of the functions in the `lists` and/or `sets` modules to be of use! The online erlang documentation is available <http://erlang.org/erldoc>. For example, you might sort the list of prime-factors, then search the sorted list for the same prime-factor appearing twice in sequence.

**5. Finally, create a function `find_square_multiples(Count, MaxN)`.** This function takes a count of how many square-multiples in a row there should be, and also a maximum value of where to stop searching.

- If the function finds a series of Count square-multiples in the range [2, MaxN], it should return the first number in the run.
- If the function doesn't find any series of Count square-multiples in this range, it should return the atom fail.

So, for example, you might have this interaction:

```
1> c(akshay.erl).
{ok,akshay}
2> akshay:find_square_multiples(3, 49).
48
3> akshay:find_square_multiples(3, 20).
fail
```

Note that the start of the run must be no larger than MaxN; the entire run itself may extend beyond MaxN. Example 1 above shows that MaxN=49, so the start of run should be less than or equal to 49 but the run can exceed MaxN=49 ie. The run is 48, 49, 50.

This function should also be exported by your mobius module.

**6.Final task: Once you have finished this function, find the first square-multiple runs of length 4, length 5, and length 6.** You will need to choose a MaxN of 30000. Your program should definitely complete in under 1 minute; if it takes longer then you may have non-tail-recursive code in your implementation, and you need to fix this. (In fact, a good implementation shouldn't take very long to find the answers, but you will have up to a minute to compute the answer.)

Put your results at the end of a <your first name>.txt file.

Example: akshay.txt contains (for example, these are not the answers :P)

```
akshay:find_square_multiples(4,300).
65
akshay:find_square_multiples(5,6000).
1425
```

Best of luck to all the coders!!

Mail your .erl and .txt results to [ieeedpwer@googlegroups.com](mailto:ieeedpwer@googlegroups.com)