

Zad. 2. 316055

Rozwinięcie $\cos x$ w szereg Taylora:

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$$

$$\begin{aligned}\cos(3x) - 1 + \frac{9x^2}{2} &= 1 - \frac{3^2 x^2}{2!} + \frac{3^4 x^4}{4!} - \dots \\ &\quad - 1 + \frac{9x^2}{2} \\ &= \frac{3^4 x^4}{4!} - \frac{3^6 x^6}{6!} + \frac{3^8 x^8}{8!} - \dots\end{aligned}$$

$$\begin{aligned}\frac{(\cos(3x) - 1 + \frac{9x^2}{2})}{x^4} &= \frac{3^4}{4!} - \frac{3^6 x^2}{6!} + \frac{3^8 x^4}{8!} - \frac{3^{10} x^6}{10!} + \dots = \\ &= \sum_{i=0}^{\infty} (-1)^i \frac{3^{4+2i} x^{2i}}{(4+2i)!}\end{aligned}$$