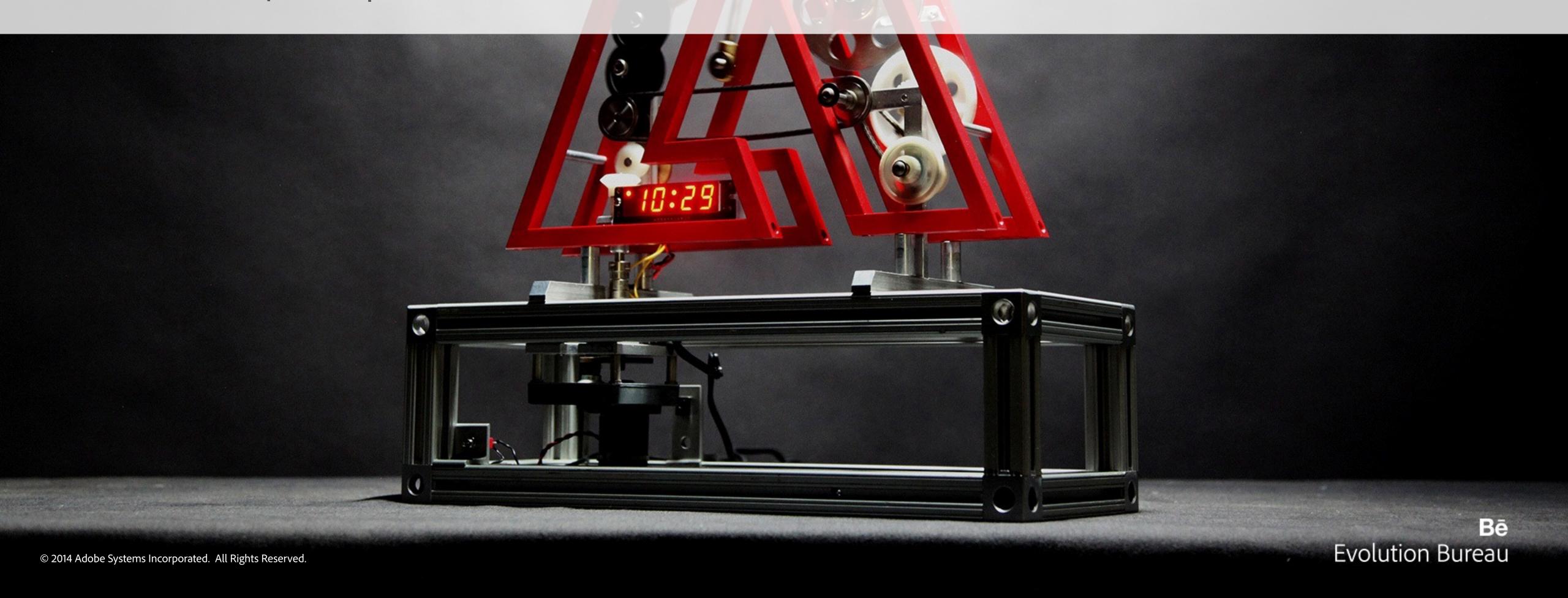


# Better Code: Concurrency

Sean Parent | Principal Scientist



#### Better Code

- Regular Type
  - Goal: Implement Complete and Efficient Types
- Algorithms
  - Goal: No Raw Loops
- Data Structures
  - Goal: No Incidental Data Structures
- Runtime Polymorphism
  - Goal: No Raw Pointers
- Concurrency
  - Goal: No Raw Synchronization Primitives

• • •

#### Common Themes

- Manage Relationships
- Understand the Fundamentals
- Code Simply

# Demo



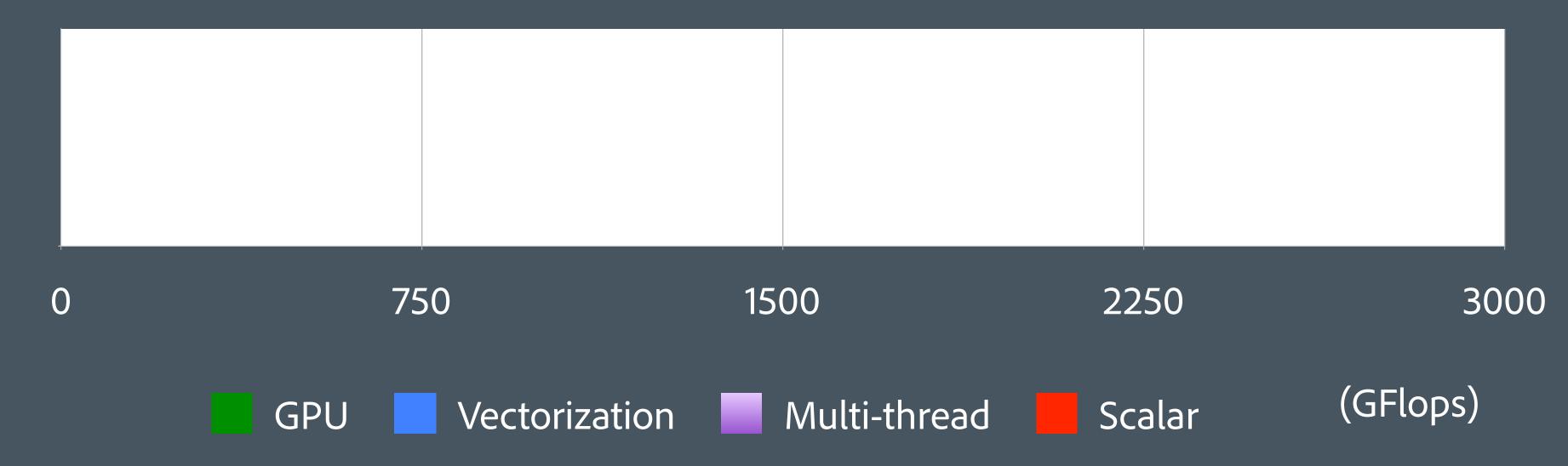
#### Concurrency

- Concurrency: when tasks start, run, and complete in overlapping time periods
- Parallelism: when two or more tasks execute simultaneously
- Why?
- Enable performance through parallelism
- Improve interactivity by handling user actions concurrent with processing and IO

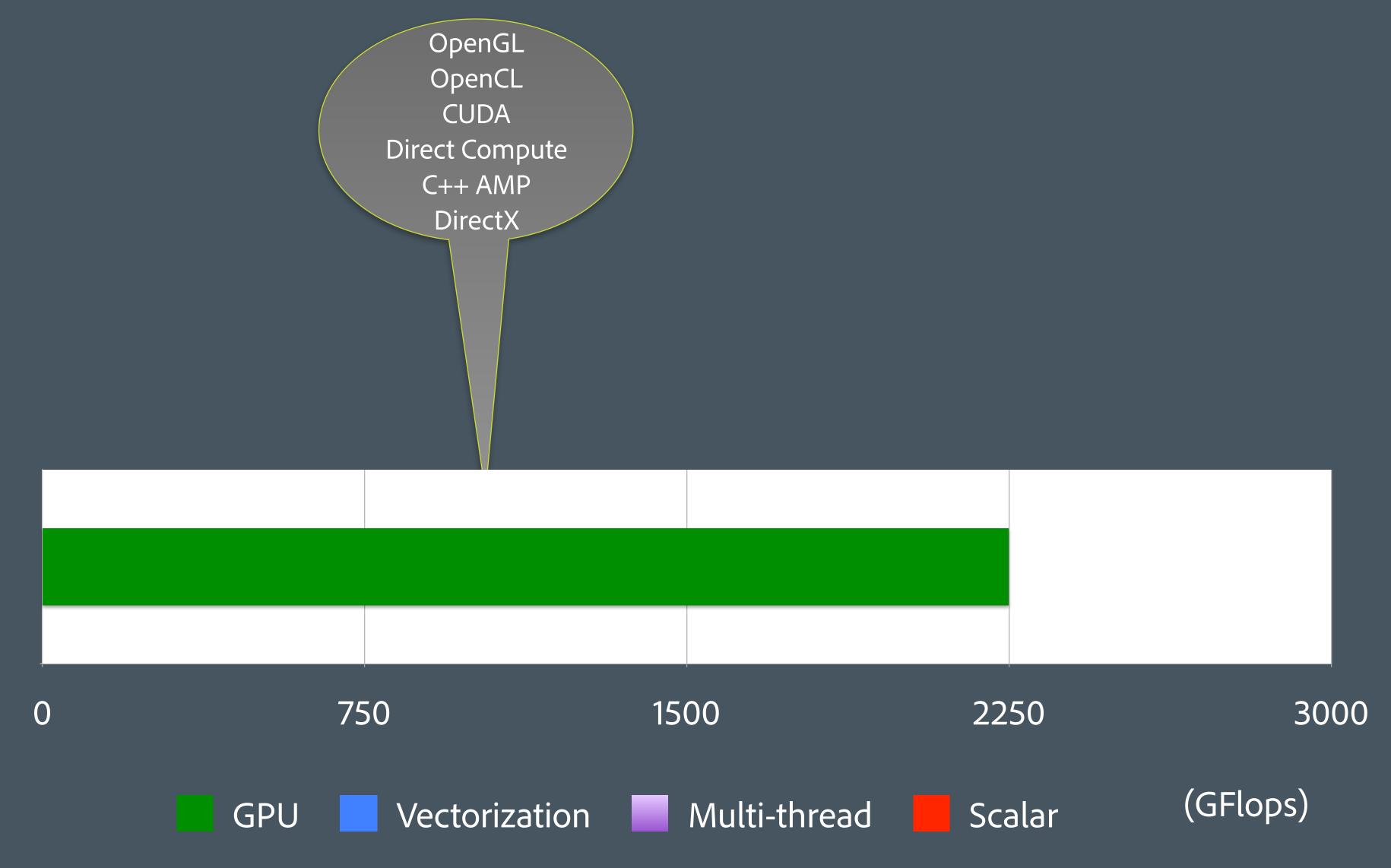
#### What are raw synchronization primitives?

- Synchronization primitives are basic constructs such as:
  - Mutex
  - Atomic
  - Semaphore
  - Memory Fence
  - Condition Variable

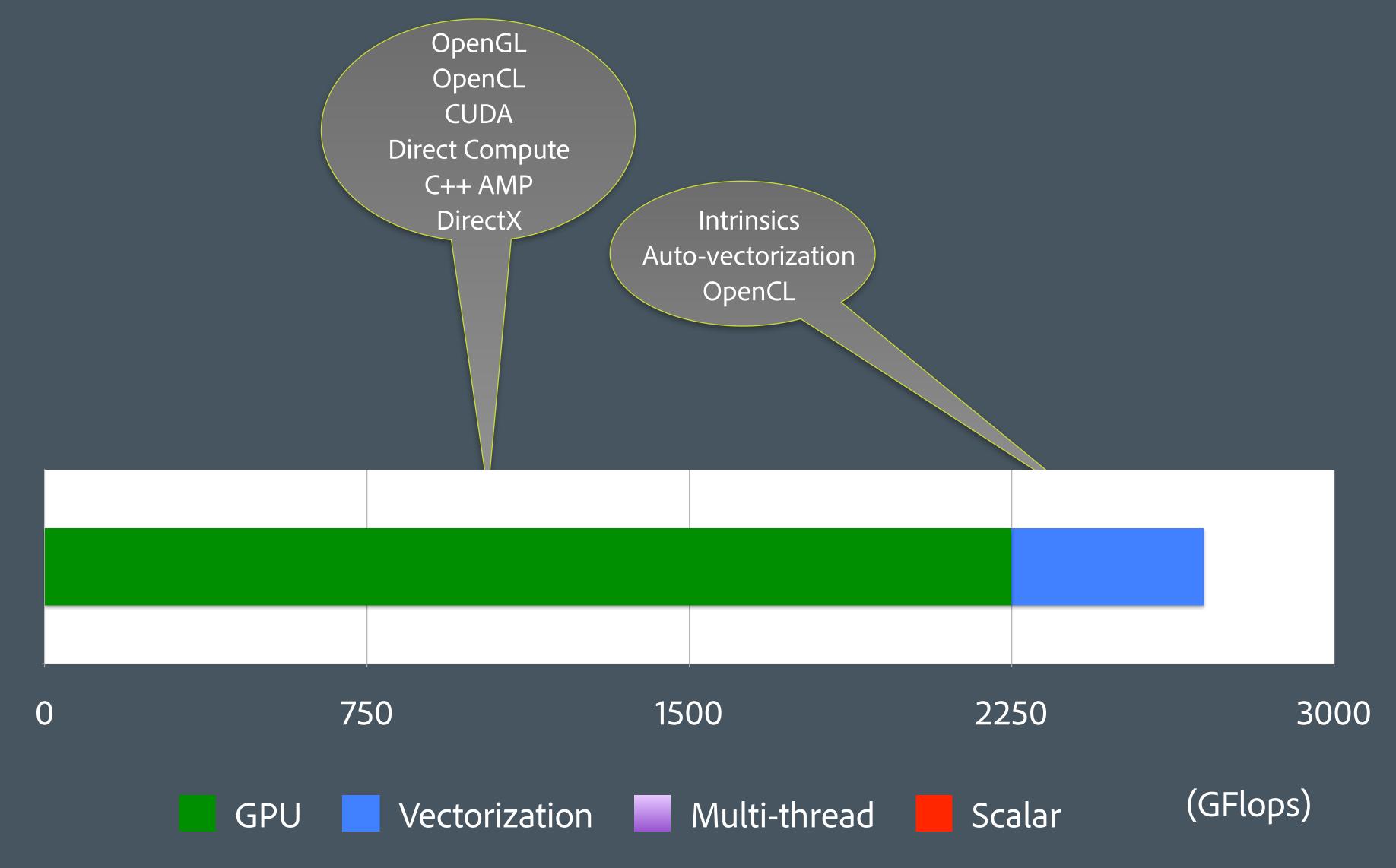




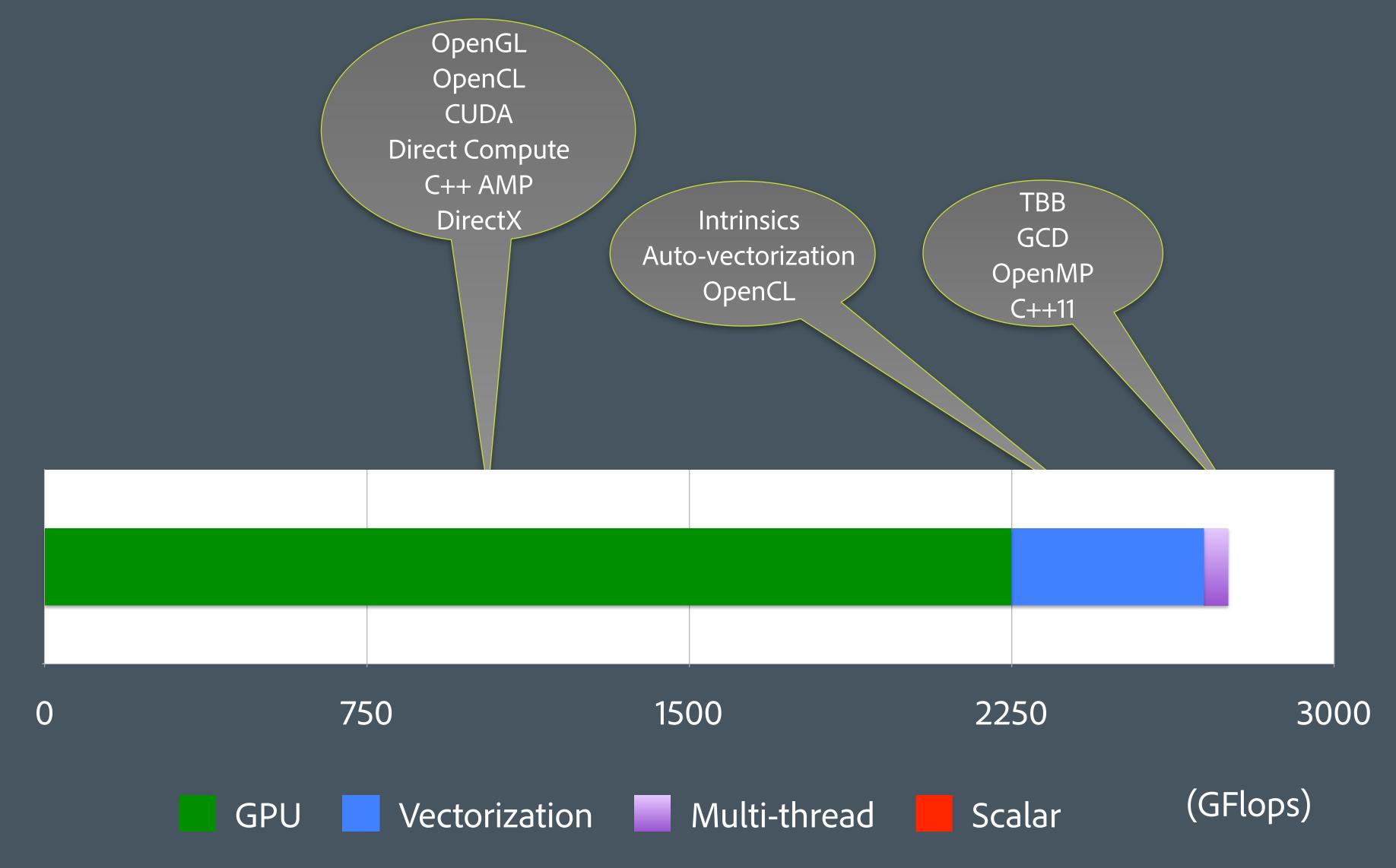




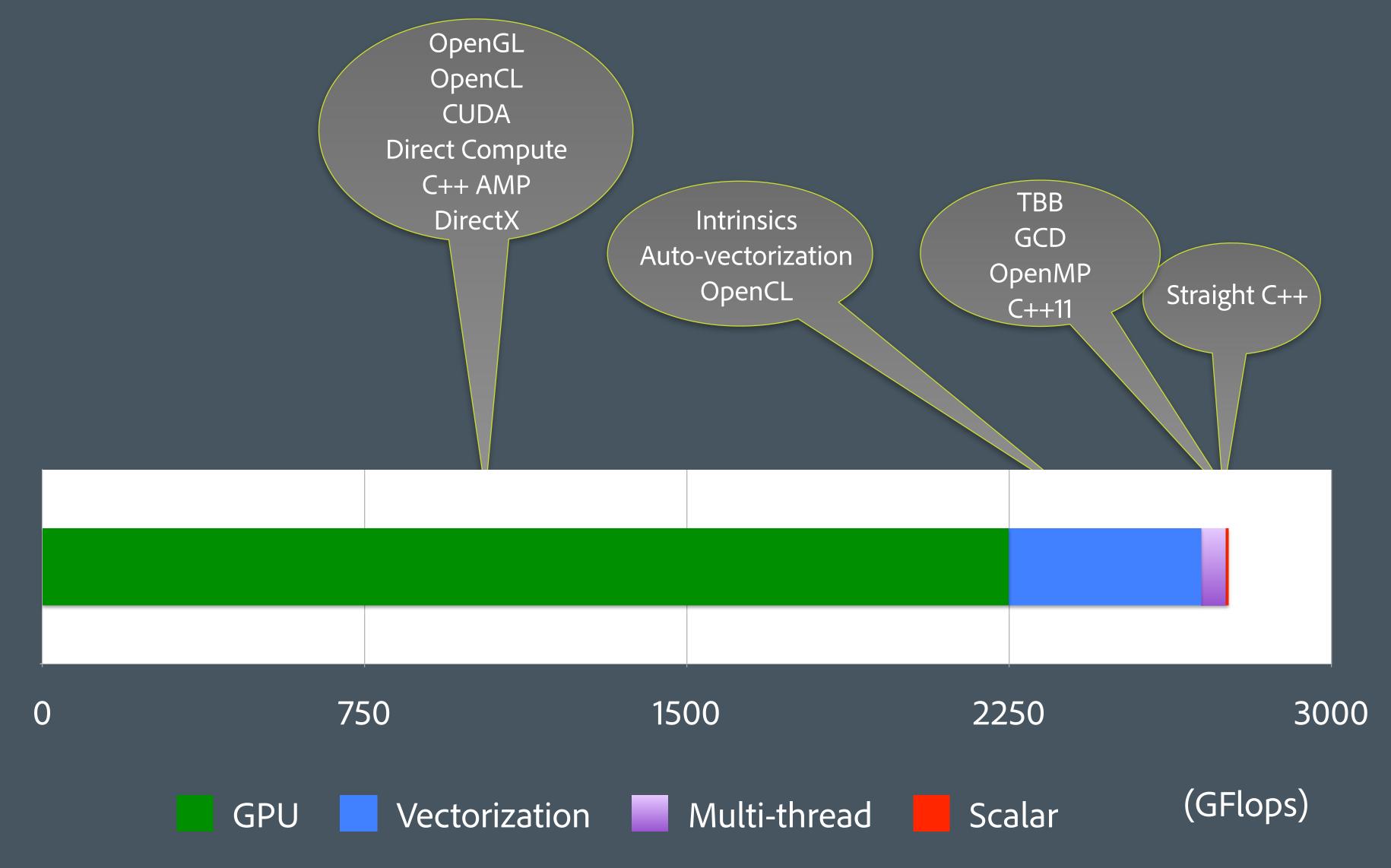














#### Threads and Tasks

- Thread: Execution environment consisting of a stack and processor state running in parallel to other threads
- Task: A unit of work, often a function, to be executed on a thread

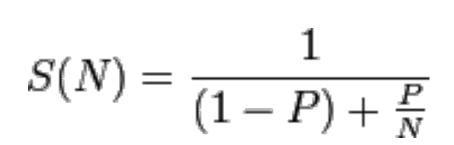
Tasks are scheduled on a thread pool to optimize machine utilization

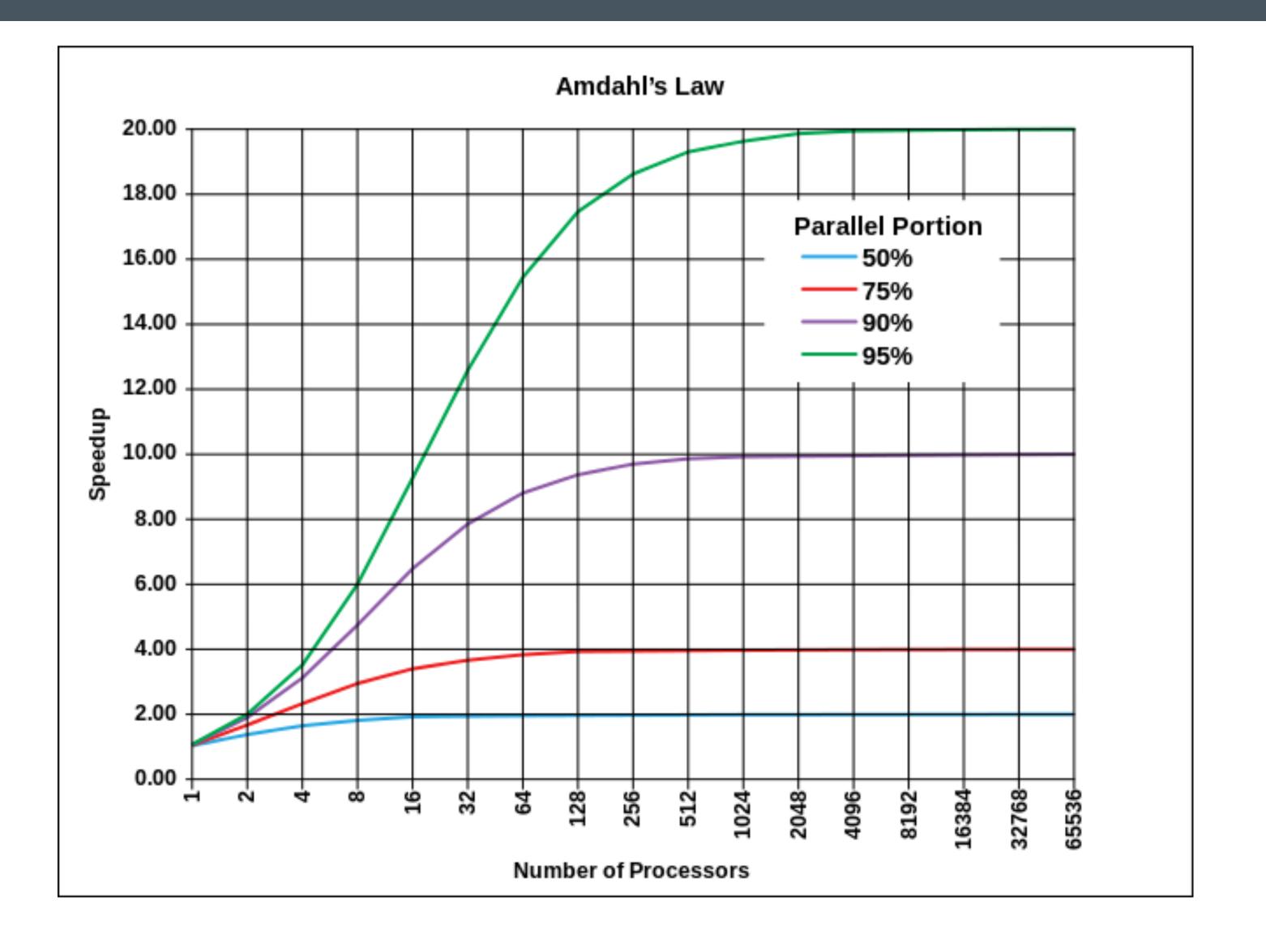
#### C++14 and Tasks

- C++14 does not have a task system
  - Threads
  - Futures (more on this)



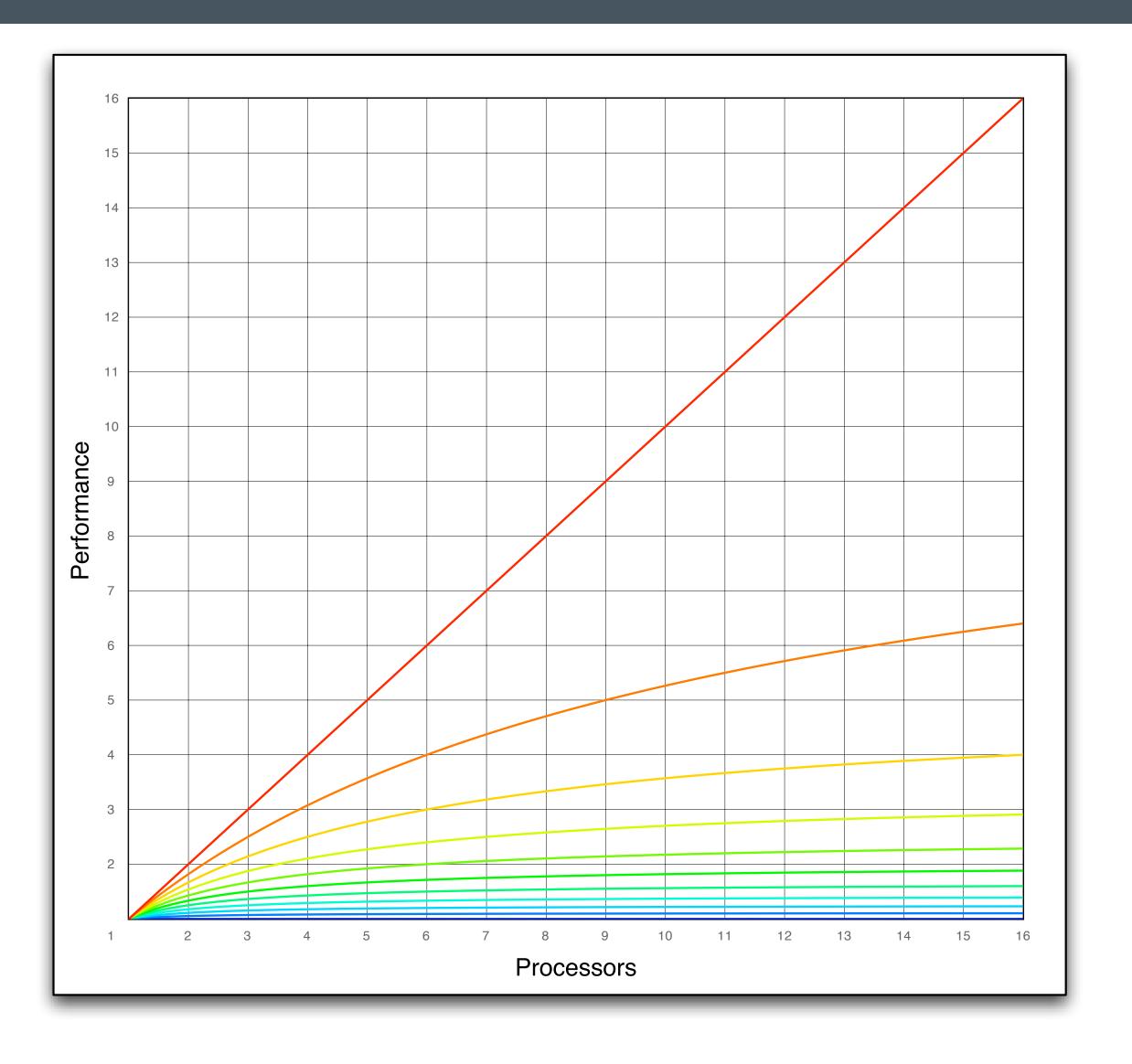
#### Amdahl's Law





http://en.wikipedia.org/wiki/Amdahl%27s\_law

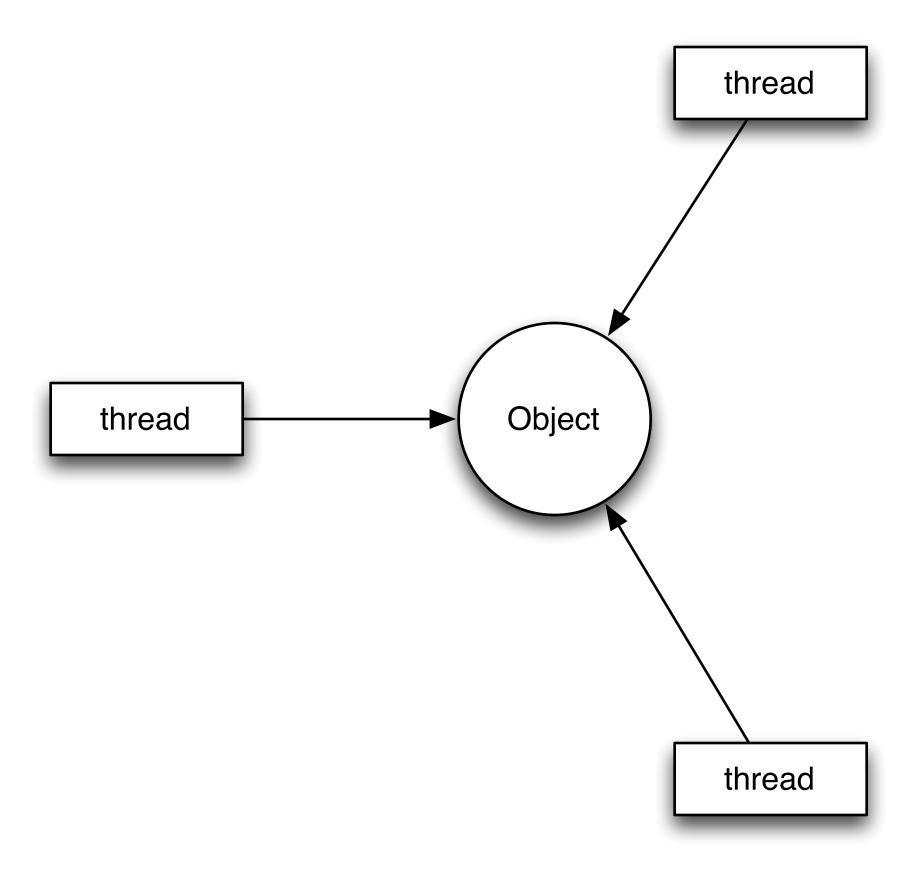
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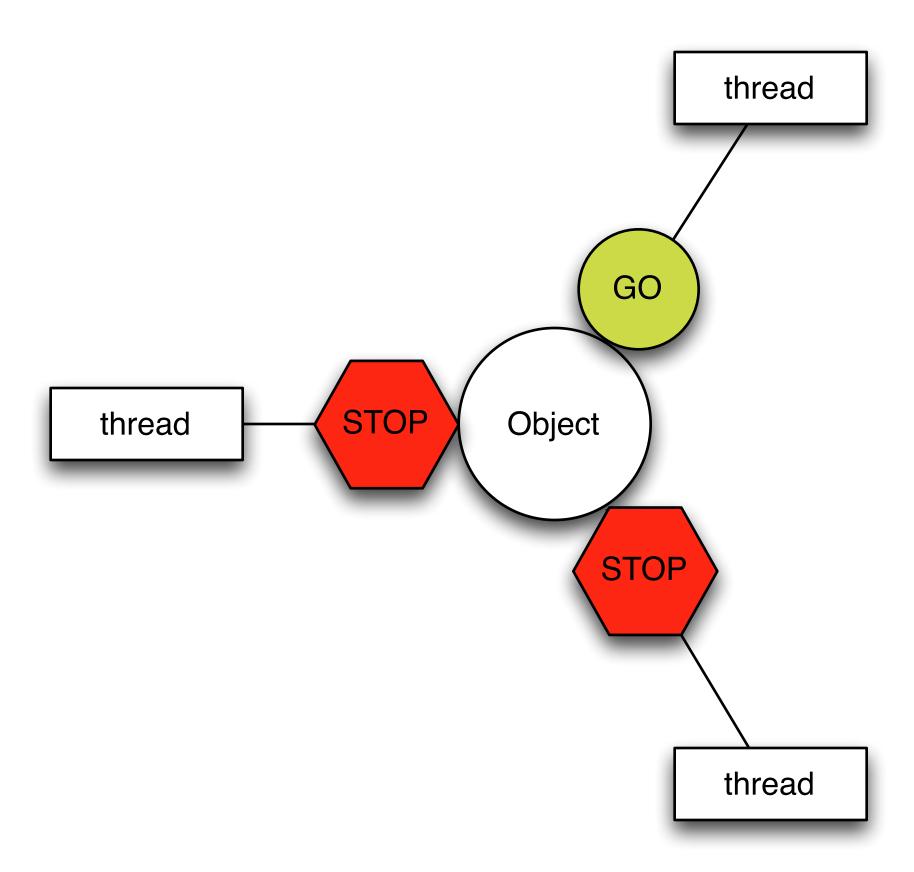


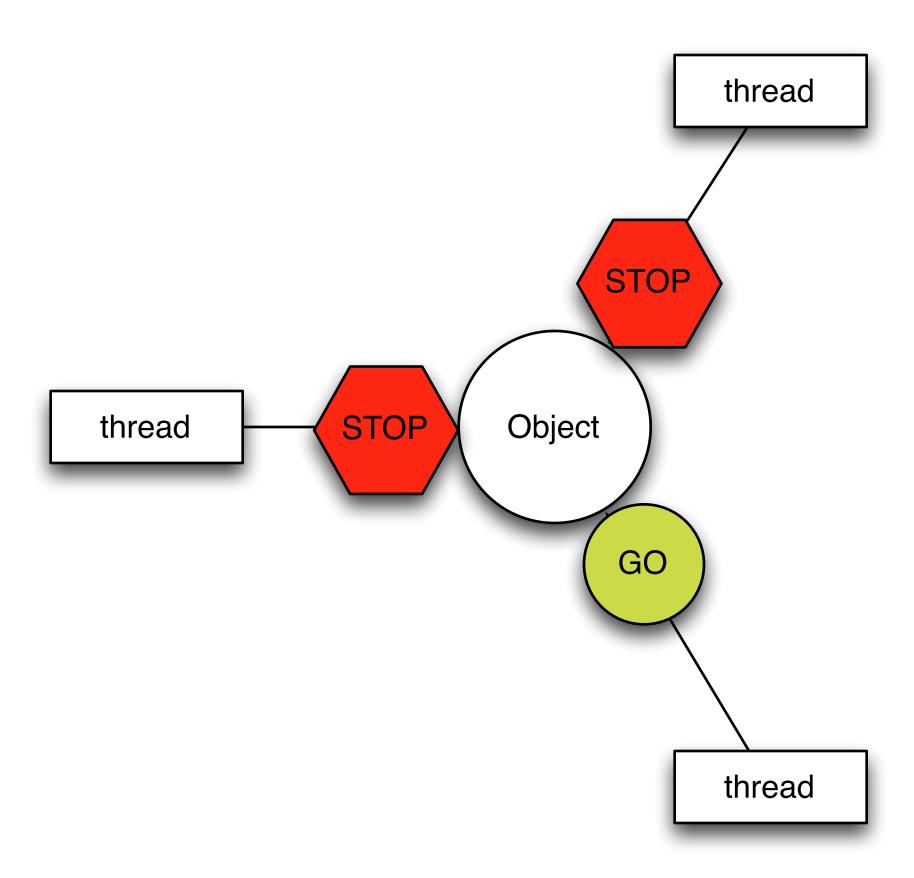
## What Makes It Slow

- Starvation
- Latency
- Overhead
- Wait

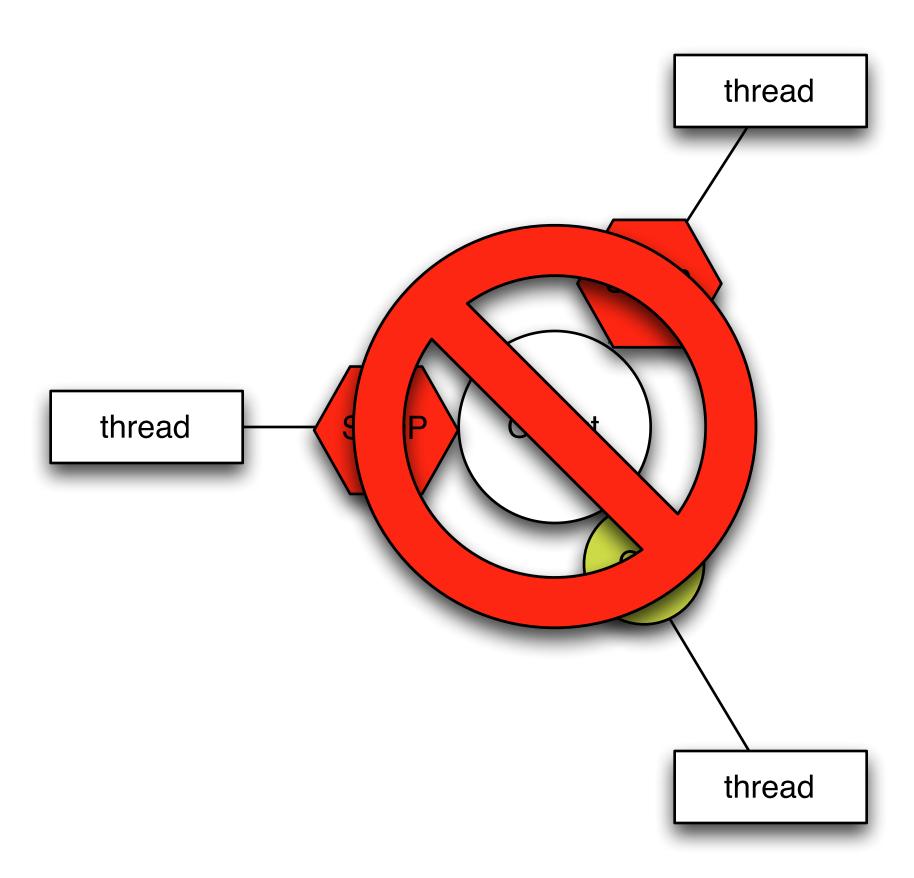
Hartmut Kaiser - HPX













## Minimize Locks



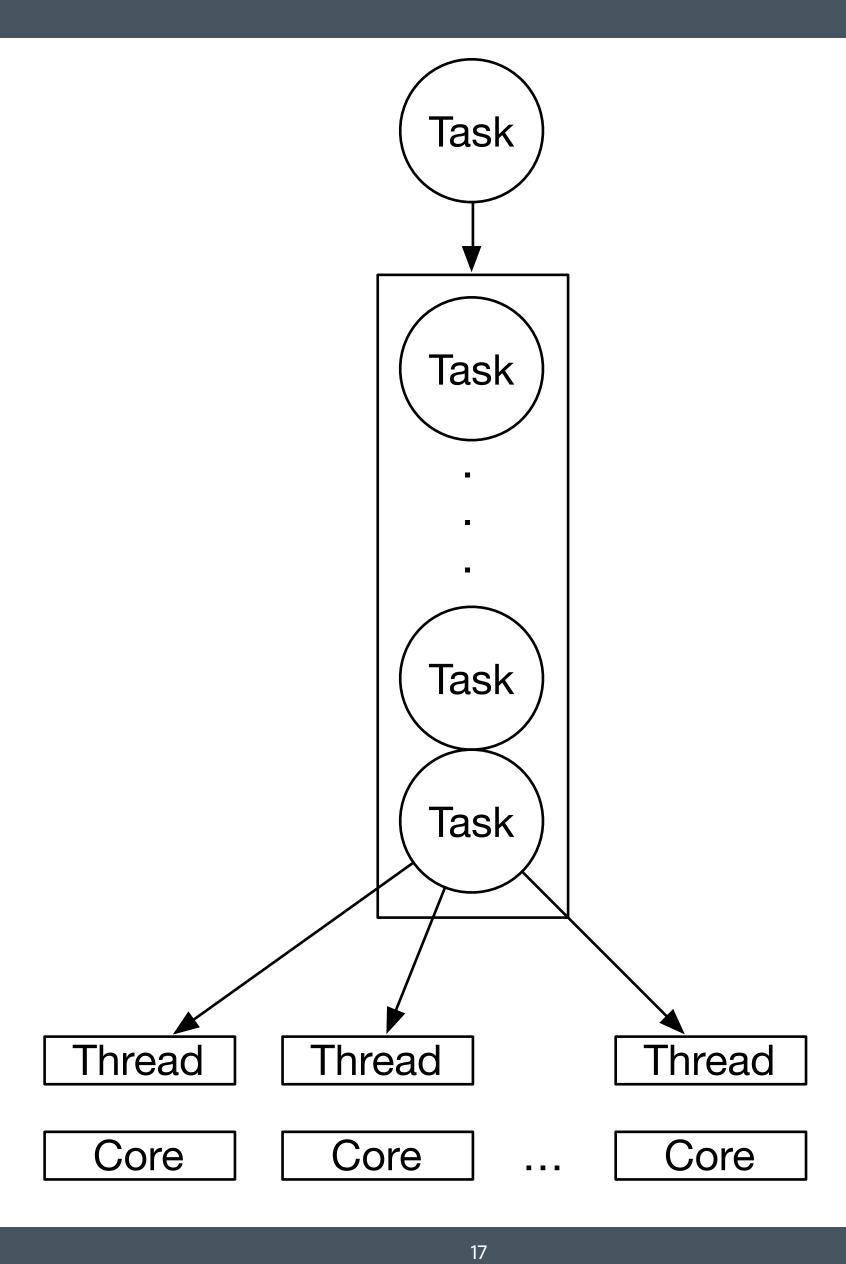


## Minimize Locks





- Portable Reference Implementation in C++14
  - Windows Window Thread Pool and PPL
  - Apple Grand Central Dispatch (libdispatch)
    - open source, runs on Linux and Android
  - Intel TBB many platforms
    - open source
  - HPX many platforms
    - open source



http://docs.oracle.com/cd/E19253-01/816-5137/ggedn/index.html





using lock\_t = unique\_lock<mutex>;







18

```
using lock_t = unique_lock<mutex>;
class notification_queue {
    deque<function<void()>> _q;
    mutex
                            _mutex;
    condition_variable
                            _ready;
  public:
    void pop(function<void()>& x) {
        lock_t lock{_mutex};
         while (_q.empty()) _ready.wait(lock);
         x = move(_q.front());
        _q.pop_front();
    template<typename F>
    void push(F&& f) {
            lock_t lock{_mutex};
            _q.emplace_back(forward<F>(f));
        _ready.notify_one();
```



18



```
class task_system {
    const unsigned
    vector<thread>
    notification_queue
```

```
_count{thread::hardware_concurrency()};
_threads;
_q;
```



```
class task_system {
    const unsigned
    vector<thread>
        notification_queue

    void run(unsigned i) {
        while (true) {
            function<void()> f;
            _q.pop(f);
            f();
        }
}
```



19

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class task_system {
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    vector<thread>
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           _q.pop(f);
           f();
  public:
    task_system() {
        for (unsigned n = 0; n != _count; ++n) {
            _threads.emplace_back([&, n]{ run(n); });
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    ~task_system() {
        for (auto& e : _threads) e.join();
    }
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19

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    }
   template <typename F>
   void async_(F&& f) {
       _q.push(forward<F>(f));
```

19

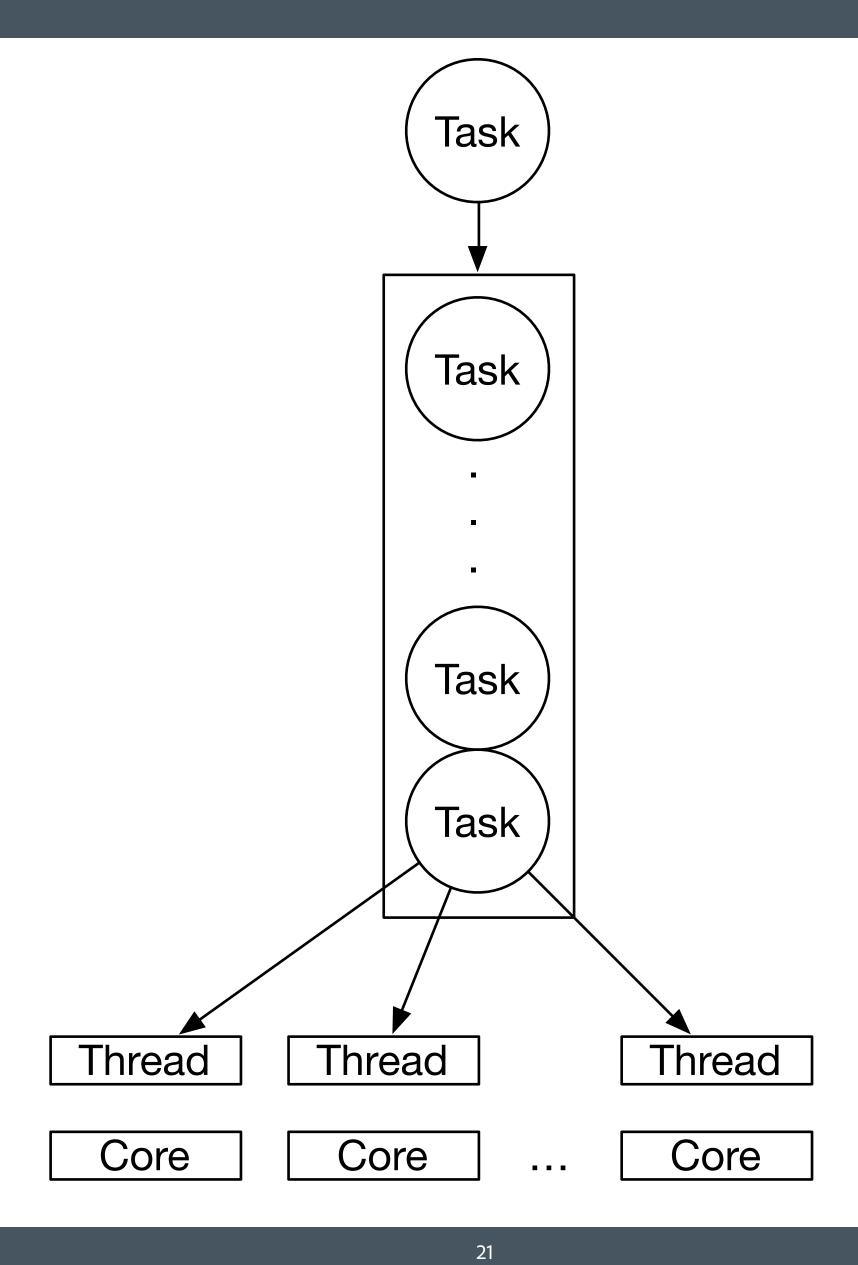
```
class notification_queue {
    deque<function<void()>> _q;
                            _done{false};
    bool
   mutex
                            _mutex;
    condition_variable
                            _ready;
  public:
   void done() {
            unique_lock<mutex> lock{_mutex};
            _done = true;
        _ready.notify_all();
    bool pop(function<void()>& x) {
        lock_t lock{_mutex};
         while (_q.empty() && !_done) _ready.wait(lock);
         if (_q.empty()) return false;
         x = move(_q.front());
        _q.pop_front();
        return true;
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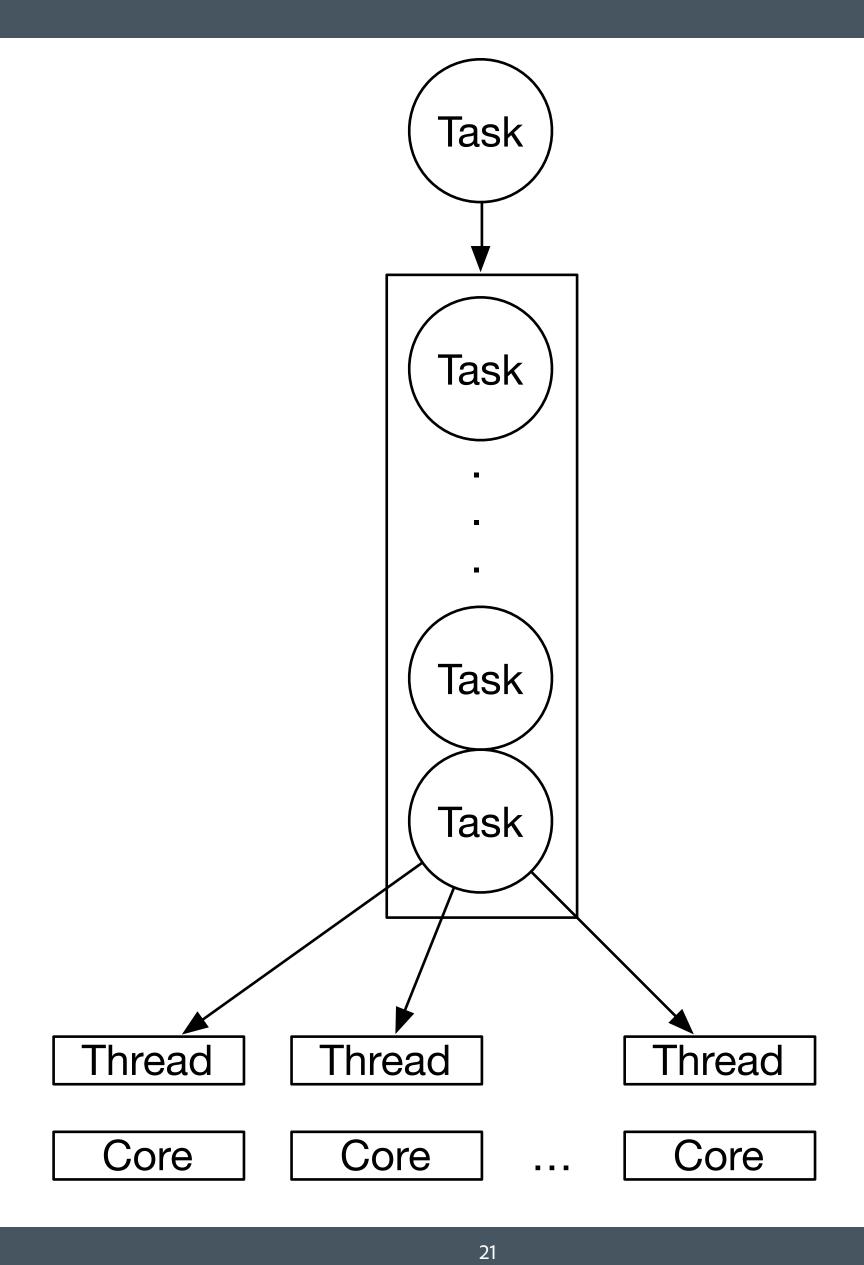
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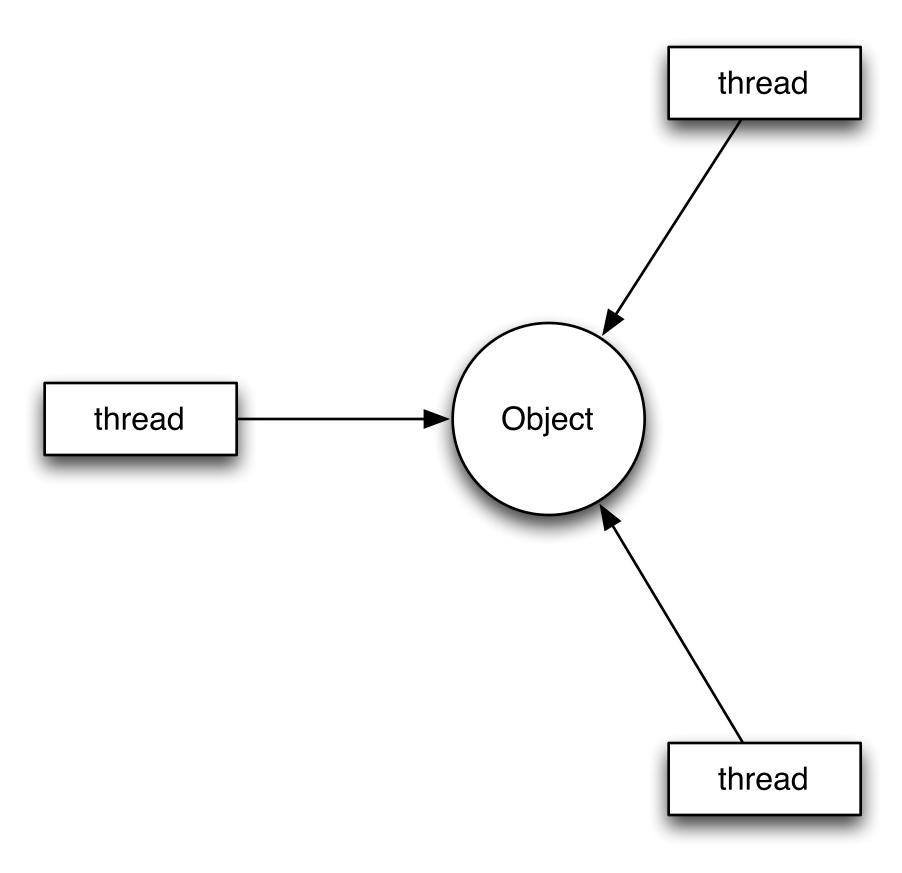




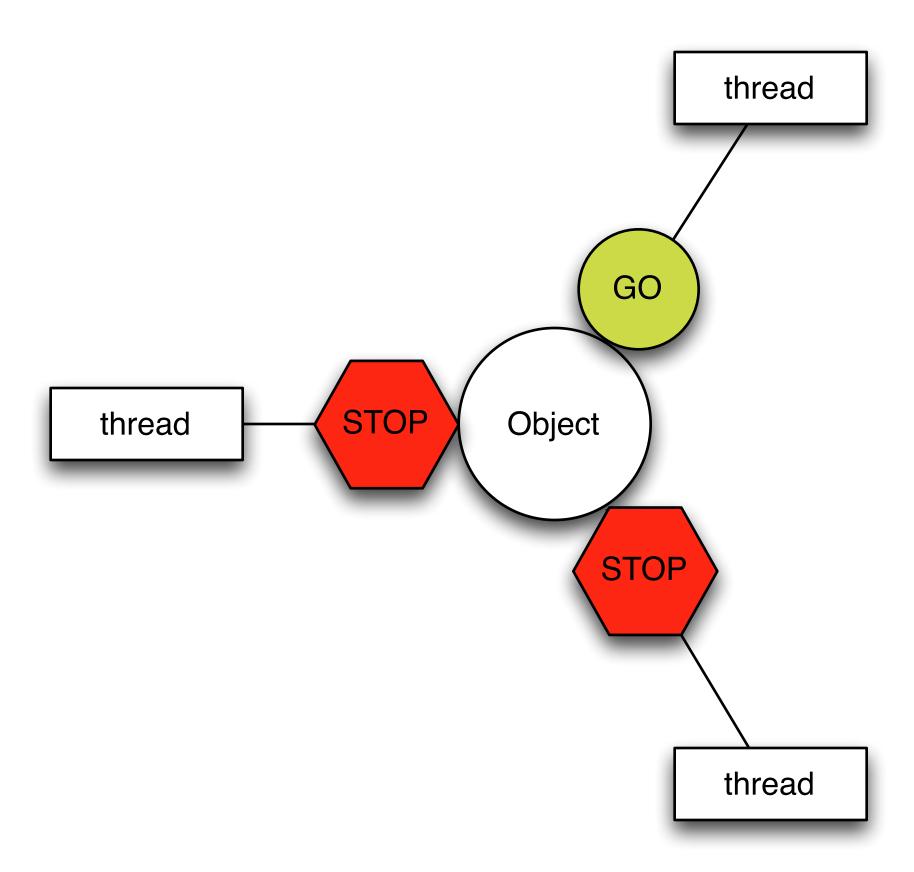




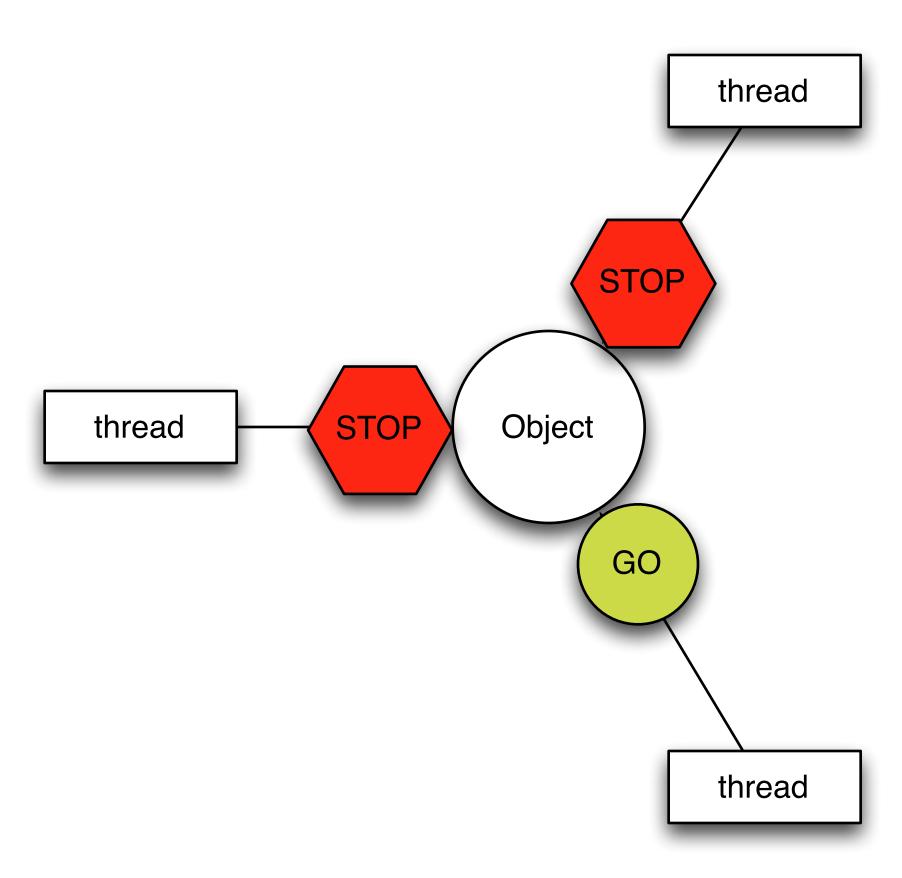




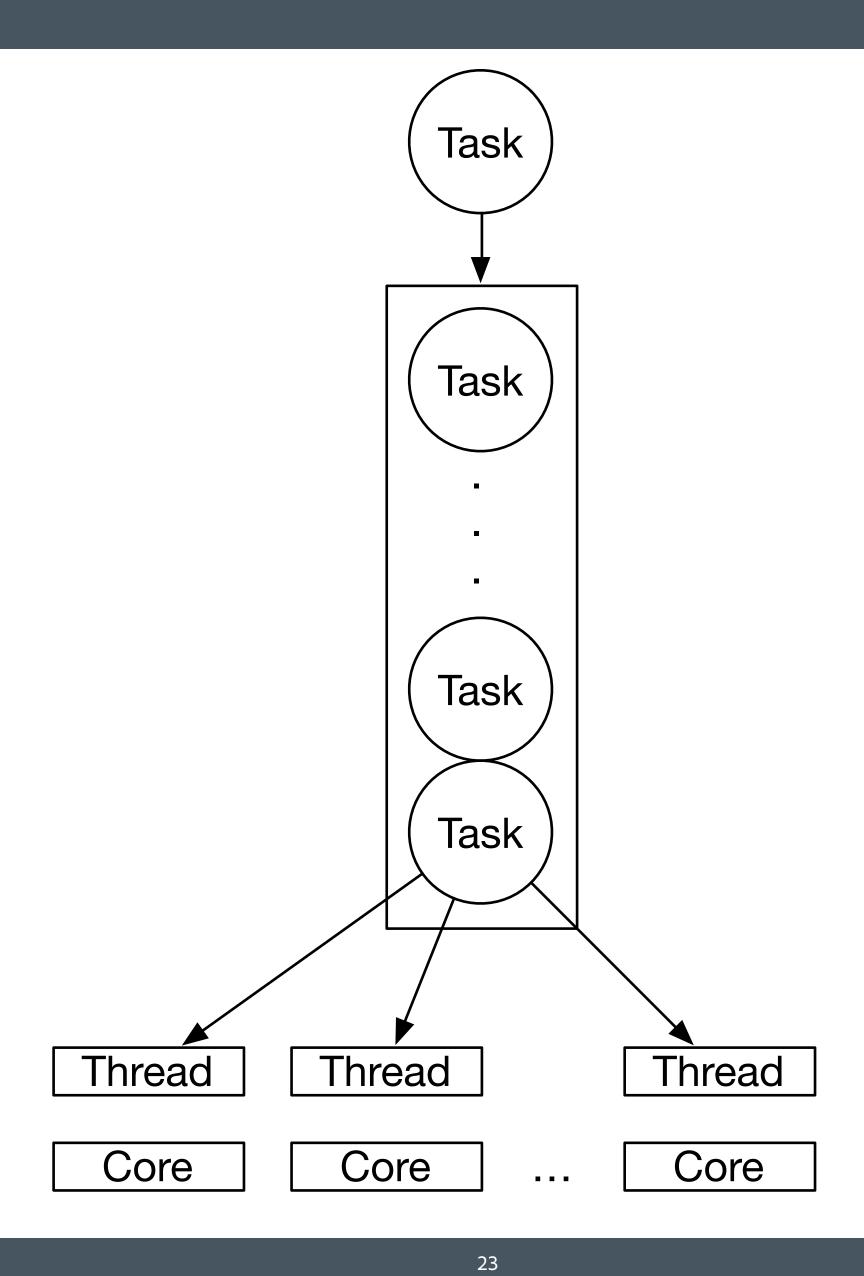
## Why No Raw Synchronization Primitives?



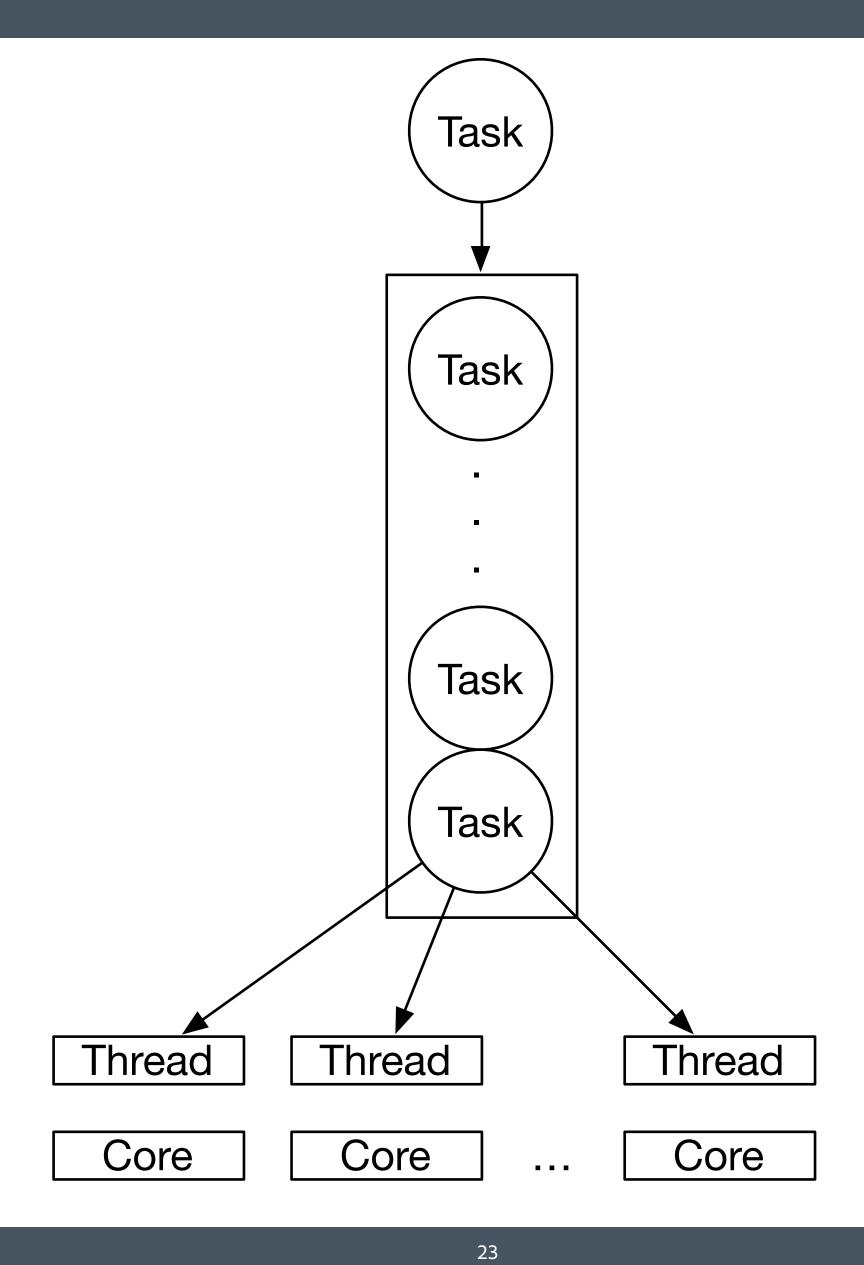
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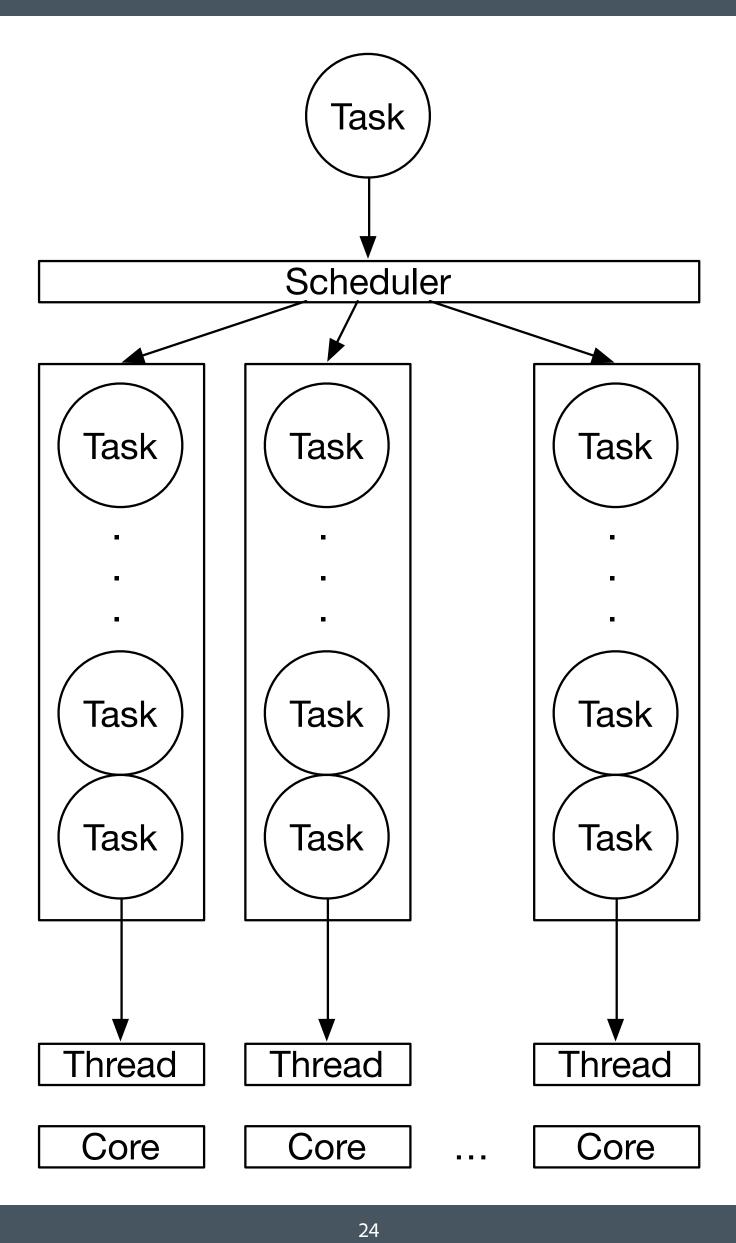












```
class task_system {
    const unsigned
                                _count{thread::hardware_concurrency()};
   vector<thread>
                                _threads;
    vector<notification_queue>
                                _q{_count};
    atomic<unsigned>
                                _index{0};
void run(unsigned i) {
       while (true) {
            function<void()> f;
            if (!_q[i].pop(f)) break;
            f();
  public:
   task_system() { ---}
   ~task_system() {
        for (auto& e : _q) e.done();
        for (auto& e : _threads) e.join();
    template <typename F>
    void async_(F&& f) {
        auto i = _index++;
       _q[i % _count].push(forward<F>(f));
```

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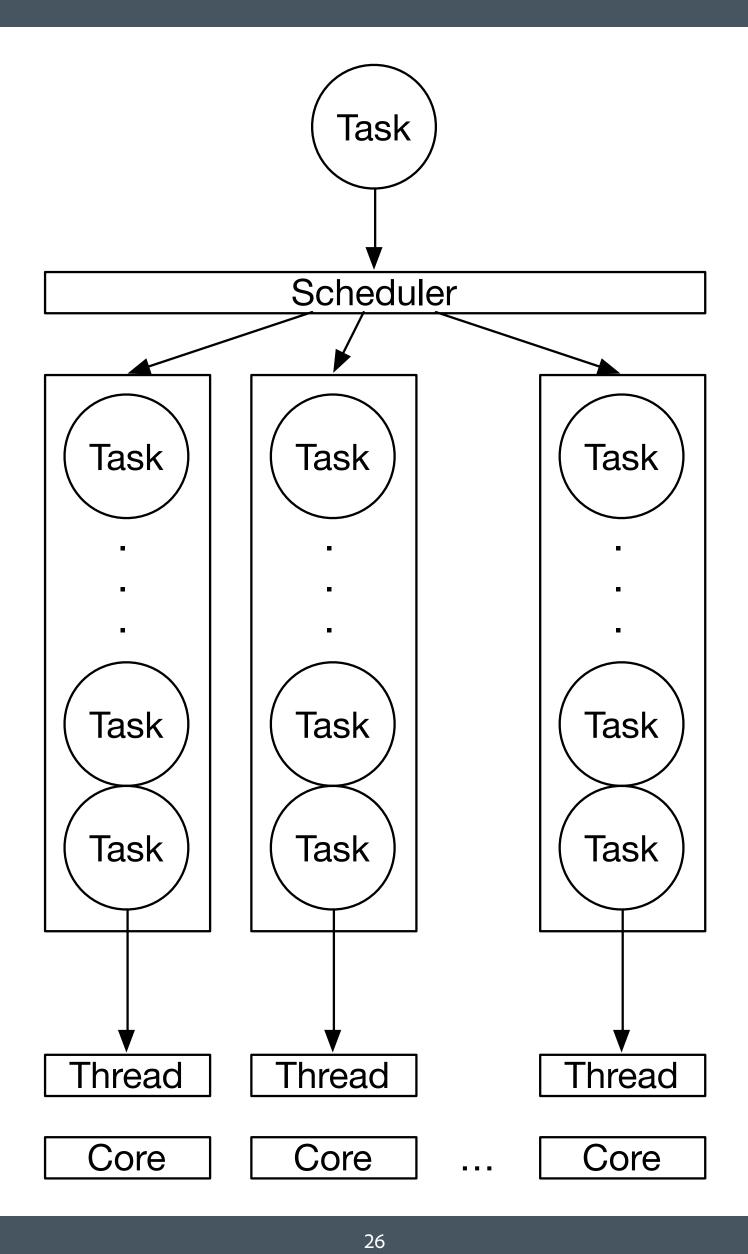
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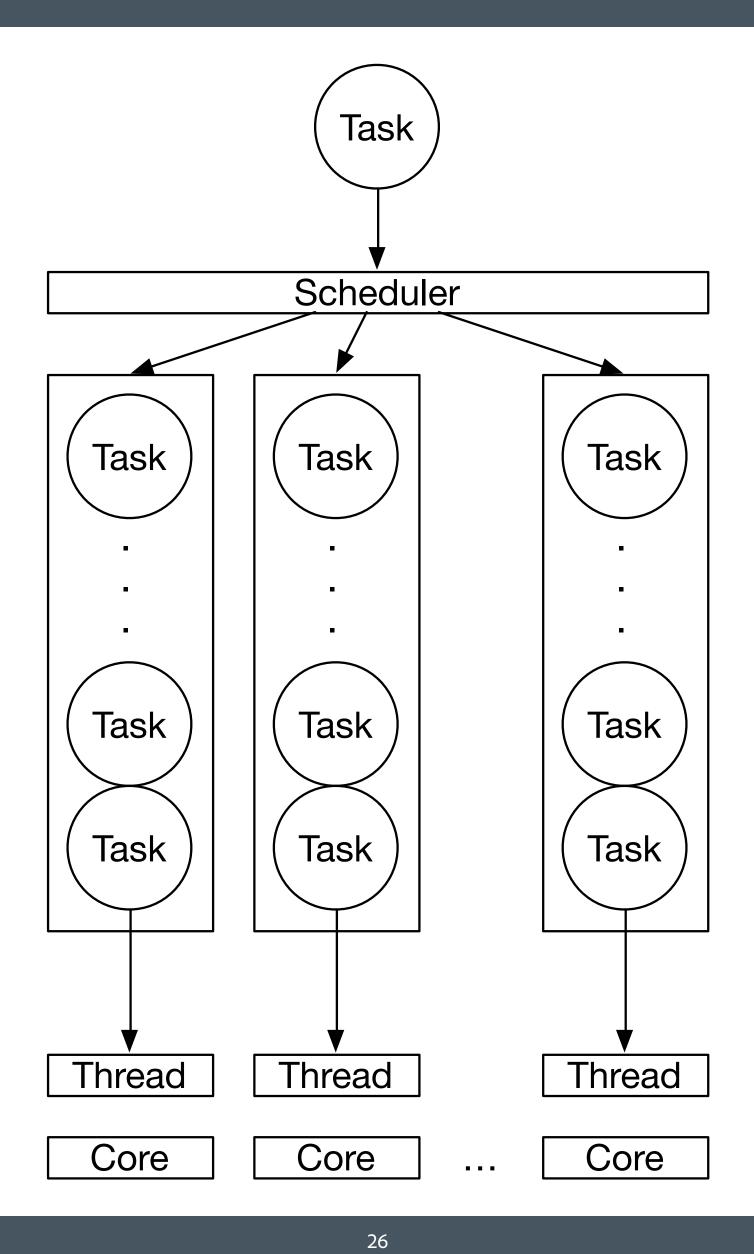
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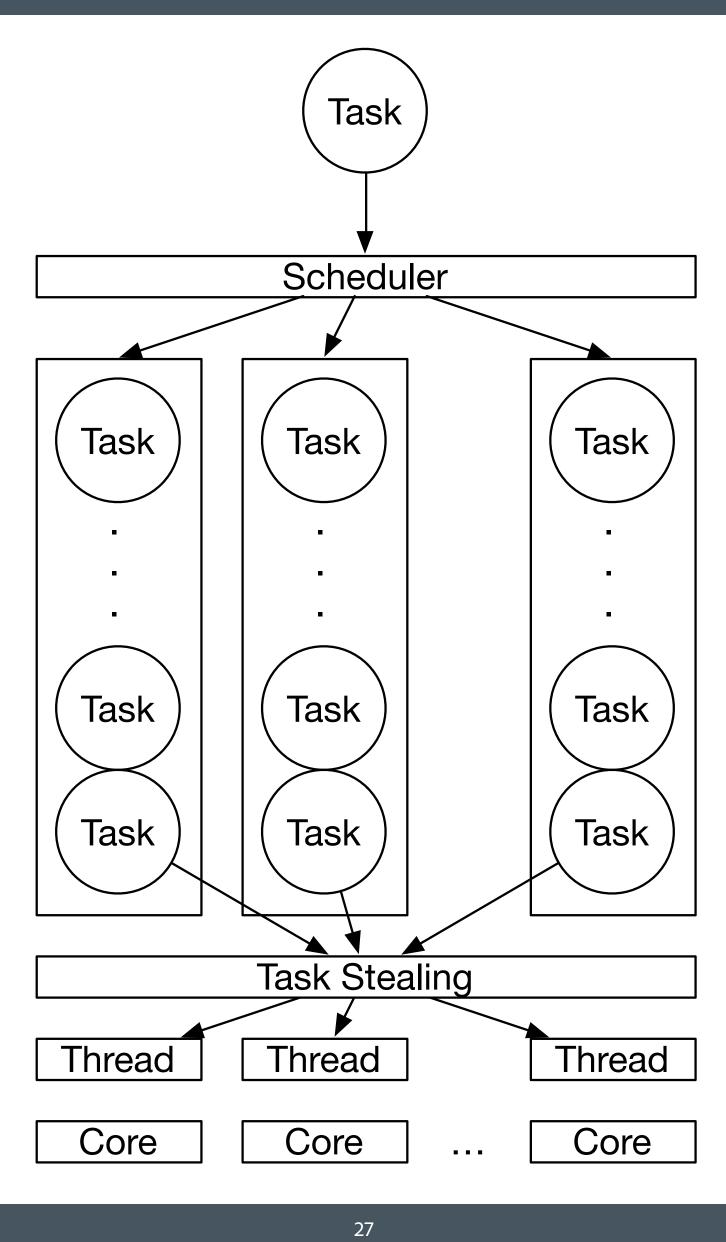












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    condition_variable
                            _ready;
  public:
    bool try_pop(function<void()>& x) {
        lock_t lock{_mutex, try_to_lock};
        if (!lock || _q.empty()) return false;
        x = move(_q.front());
        _q.pop_front();
        return true;
    template<typename F>
    bool try_push(F&& f) {
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        _ready.notify_one();
        return true;
   void done() {
            unique lock<mutex> lock{ mutex};
```



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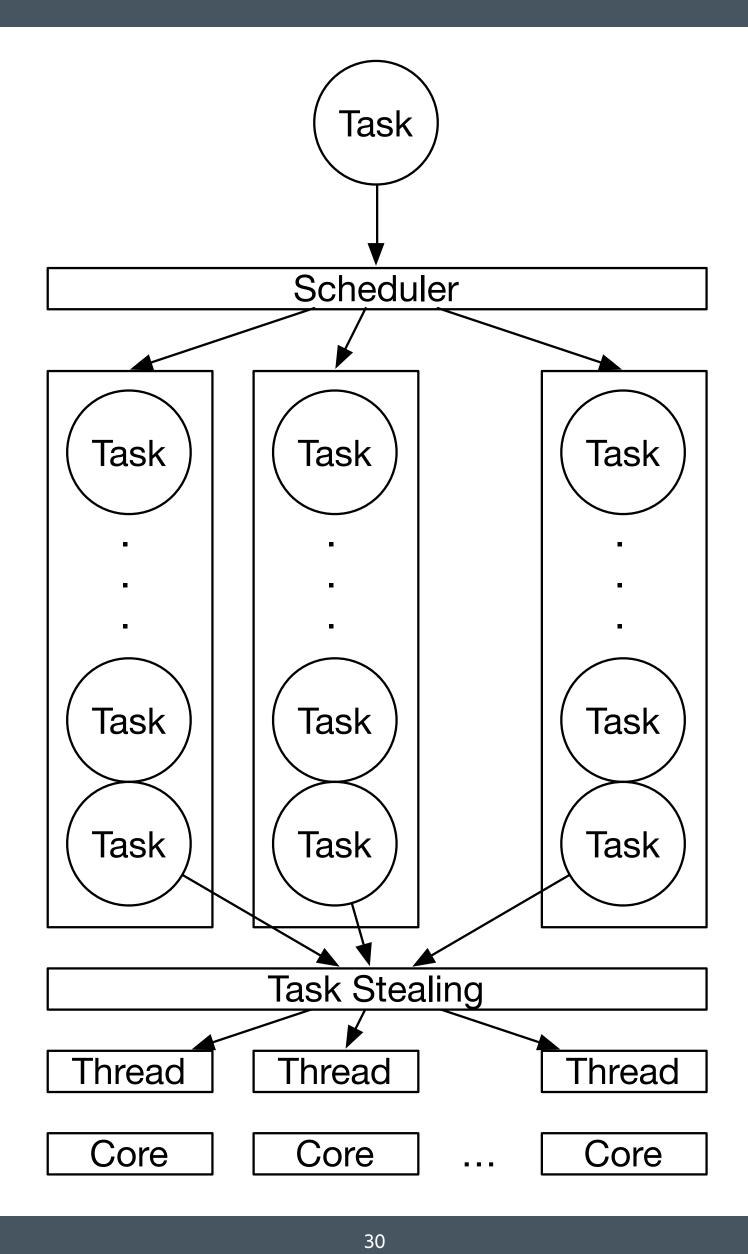
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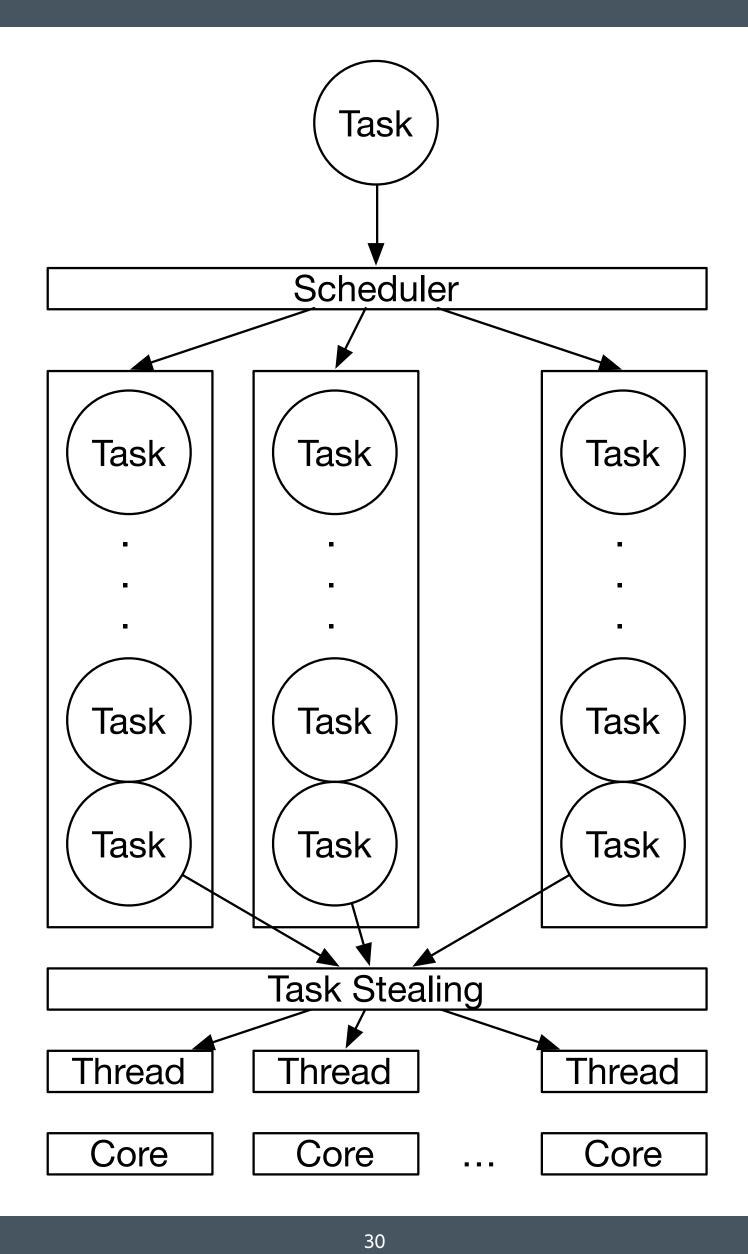
```
***
    void run(unsigned i) {
        while (true) {
            function<void()> f;
            for (unsigned n = 0; n != _count; ++n) {
                if (_q[(i + n) % _count].try_pop(f)) break;
            if (!f && !_q[i].pop(f)) break;
            f();
  public:
   task_system() { •• }
    ~task_system() { • }
    template <typename F>
    void async_(F&& f) {
        auto i = _index++;
        for (unsigned n = 0; n != _count; ++n) {
            if (_q[(i + n) % _count].try_push(forward<F>(f))) return;
        _q[i % _count].push(forward<F>(f));
};
```

```
***
    void run(unsigned i) {
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        _q[i % _count].push(forward<F>(f));
};
```









## Task System

- Within a few percentage points of Apple's GCD (libdispatch) under load
  - Can be improved by spinning more on try\_pop in run



## Futures

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(1'000'000); });

// Do Something

cout << x.get() << endl;</pre>
```



#### Futures

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(1'000'000); });

// Do Something
cout << x.get() << endl;</pre>
```

- Fibonacci is often used as an example for parallel algorithms
  - Please stop...



#### Public Service Announcement - How to Write Fibonacci

```
template <typename T, typename N, typename 0>
T power(T x, N n, 0 op)
{
    if (n == 0) return identity_element(op);

    while ((n & 1) == 0) {
        n >>= 1;
        x = op(x, x);
    }

    T result = x;
    n >>= 1;
    while (n != 0) {
        x = op(x, x);
        if ((n & 1) != 0) result = op(result, x);
        n >>= 1;
    }
    return result;
}
```



#### Public Service Announcement - How to Write Fibonacci

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    T result = x;
    n >>= 1;
    while (n != 0) {
        x = op(x, x);
        if ((n & 1) != 0) result = op(result, x);
        n >>= 1;
    }
    return result;
}
```

Egyptian Multiplication (Russian Peasant Algorithm)
See "From Mathematics to Generic Programming" - Alex Stepanov and Dan Rose



#### Public Service Announcement - How to Write Fibonacci

#### Futures

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0.72s to calculate 208,988 digits

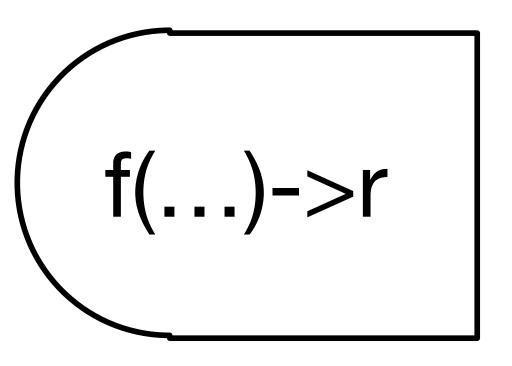


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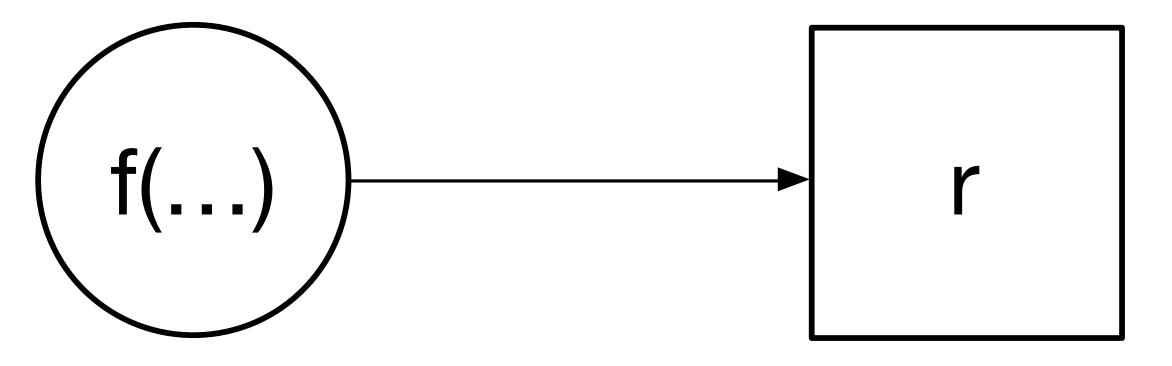
// Do Something

cout << x.get() << endl;</pre>
```









• Futures allow minimal code transformations to express dependencies



# Futures: What year is this?

- C++14 futures have:
  - Exception Marshaling
  - Sever Notification (broken promise)

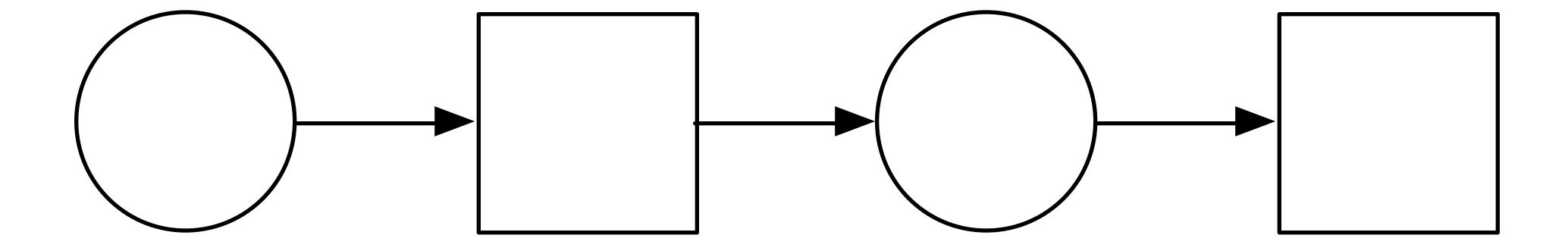


## Futures: What year is this?

- C++14 futures lack:
- Continuations .then()
- Joins when\_all()
- Cancelation
- Progress Monitoring (Except Ready)

• • •

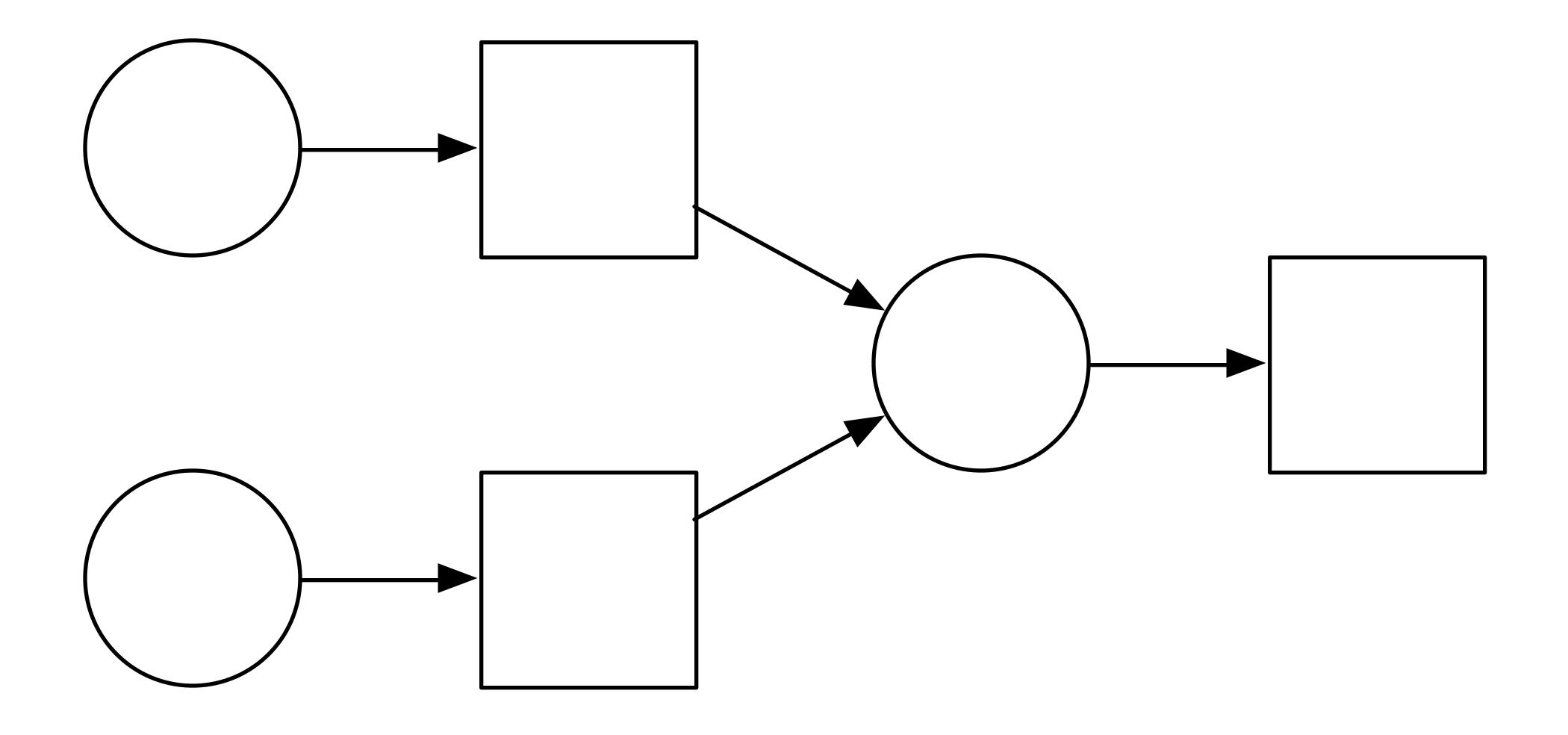
And C++14 futures don't compose (easily) to add these features



- Blocking on std::future.get() has two problems
  - One thread resource is consumed, increasing contention
- Any subsequent non-dependent calculations on the task are also blocked
- C++14 doesn't have continuations
  - GCD has serialized queues and groups
  - PPL has chained tasks
  - TBB has flow graphs
  - TS Concurrency will have them
  - Boost futures have them now

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(1'000'000); });
future<void> y = x.then([](future<cpp_int> x){ cout << x.get() << endl; });
// Do something
y.wait();</pre>
```





```
auto x = async([]{ return fibonacci<cpp_int>(1'000'000); });
auto y = async([]{ return fibonacci<cpp_int>(2'000'000); });

auto z = when_all(std::move(x), std::move(y)).then([](auto f){
    auto t = f.get();
    return cpp_int(get<0>(t).get() * get<1>(t).get());
});

cout << z.get() << endl;</pre>
```

```
auto x = async([]{ return fibonacci<cpp_int>(1'000'000); });
auto y = async([]{ return fibonacci<cpp_int>(2'000'000); });

auto z = when_all(std::move(x), std::move(y)).then([](auto f){
    auto t = f.get();
    return cpp_int(get<0>(t).get() * get<1>(t).get());
});

cout << z.get() << endl;</pre>
```

f is a future tuple of futures

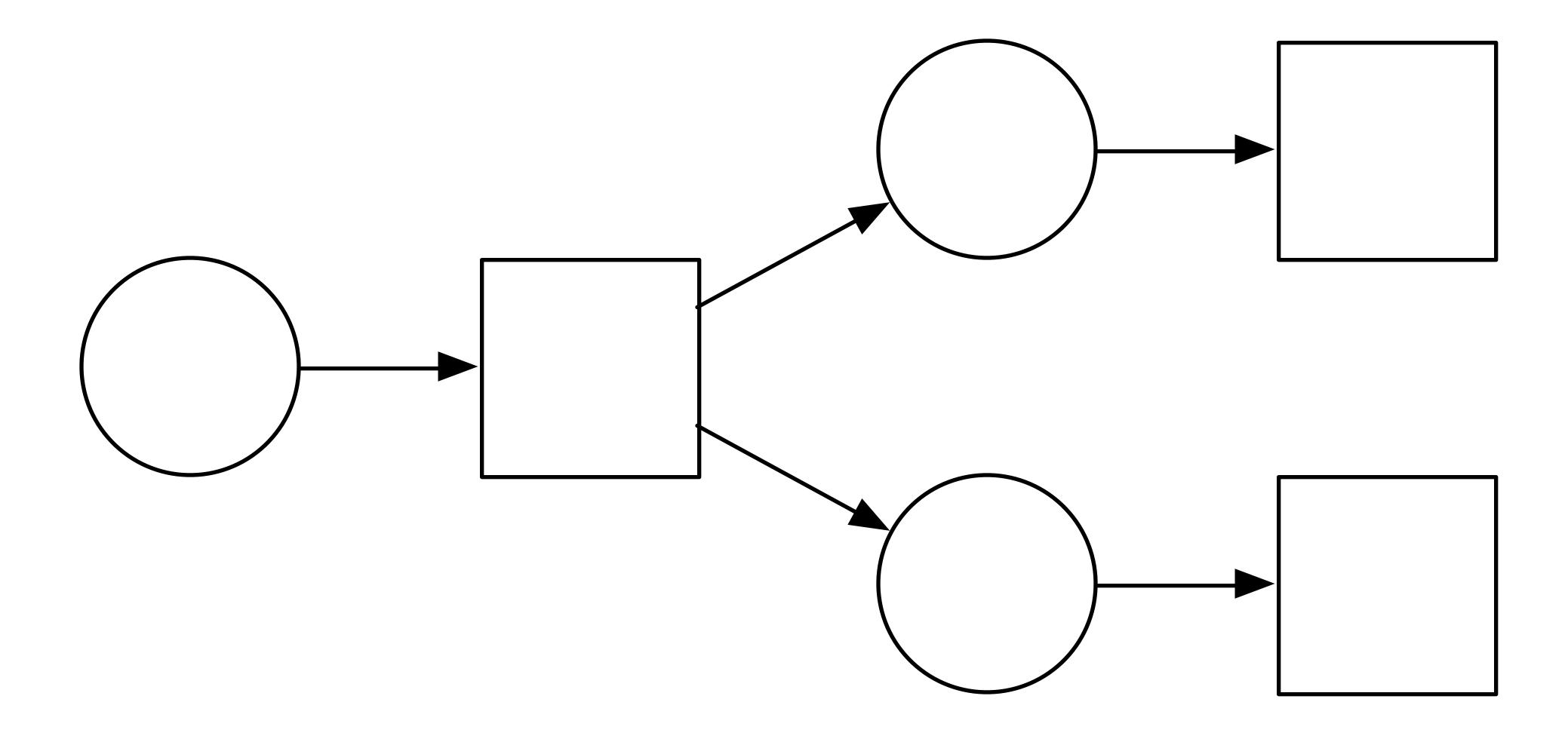
```
auto x = async([]{ return fibonacci<cpp_int>(1'000'000); });
auto y = async([]{ return fibonacci<cpp_int>(2'000'000); });

auto z = when_all(std::move(x), std::move(y)).then([](auto f){
    auto t = f.get();
    return cpp_int(get<0>(t).get() * get<1>(t).get());
});

cout << z.get() << endl;</pre>
```

f is a future tuple of futures

result is 626,964 digits



```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(100); });

future<cpp_int> y = x.then([](future<cpp_int> x){ return cpp_int(x.get() * 2); });

future<cpp_int> z = x.then([](future<cpp_int> x){ return cpp_int(x.get() / 15); });
```

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(100); });

future<cpp_int> y = x.then([](future<cpp_int> x){ return cpp_int(x.get() * 2); });

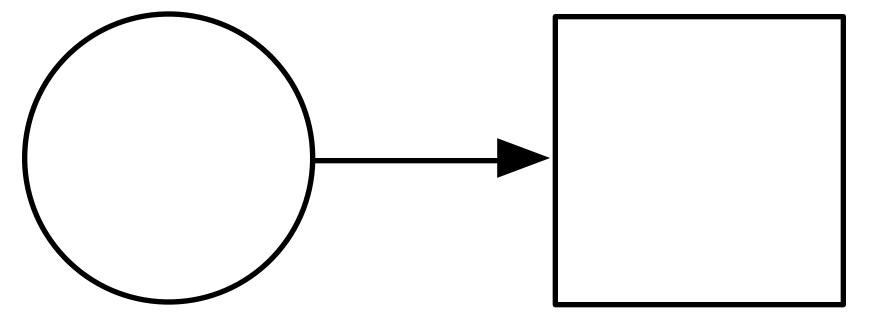
future<cpp_int> z = x.then([](future<cpp_int> x){ return cpp_int(x.get() / 15); });

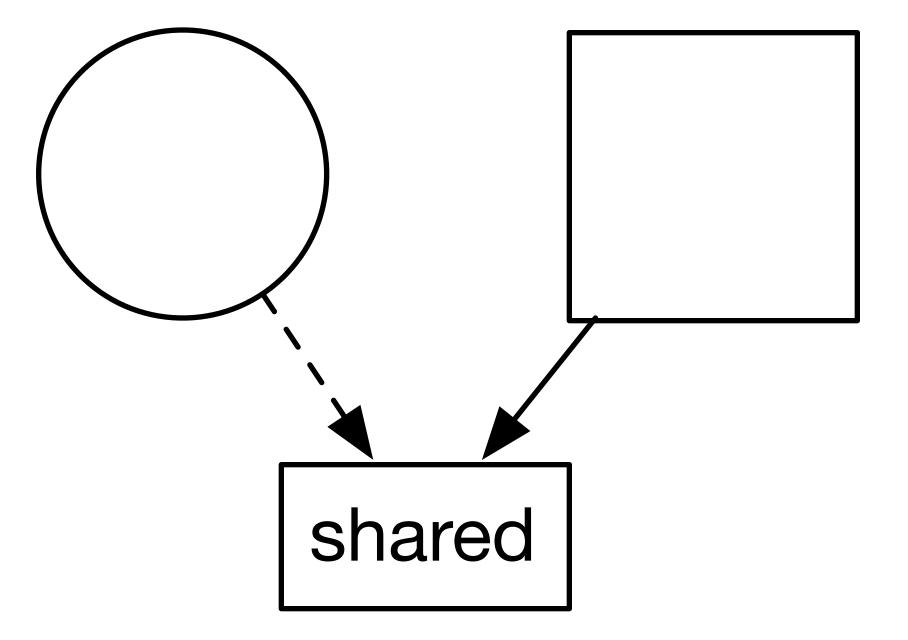
Thread 1: signal SIGABRT
```

Assertion failed: (px != 0), function operator->, file shared\_ptr.hpp, line 648.

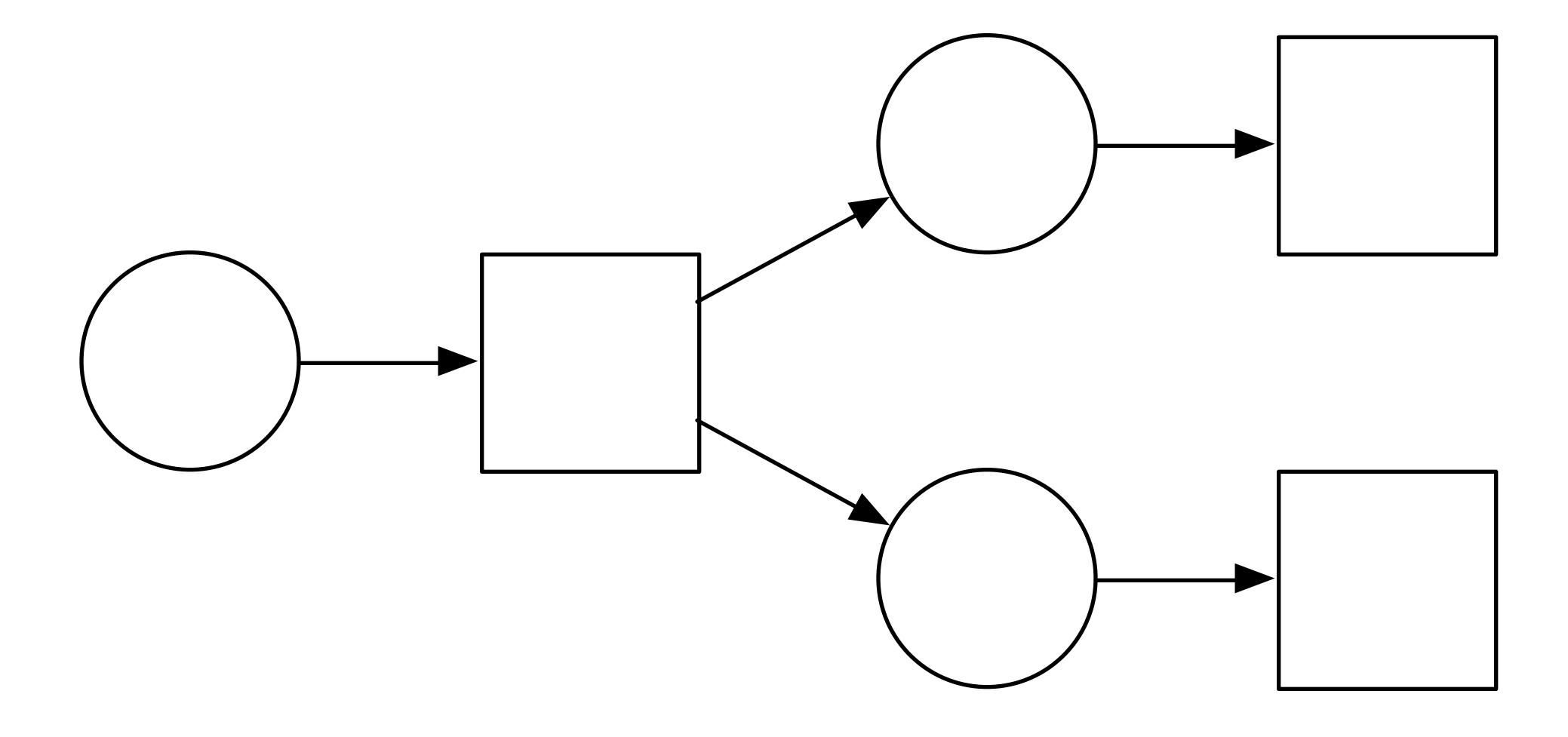
#### Continuations

- Desired behavior
- A future should behave as a regular type a token for the actual value
  - shared\_futures let me pass them around and do multiple get() operations, but don't fix continuations
  - [at least with boost]
- Releasing the last instance of a future should cancel (no-op) any unexecuted, contributing, operations

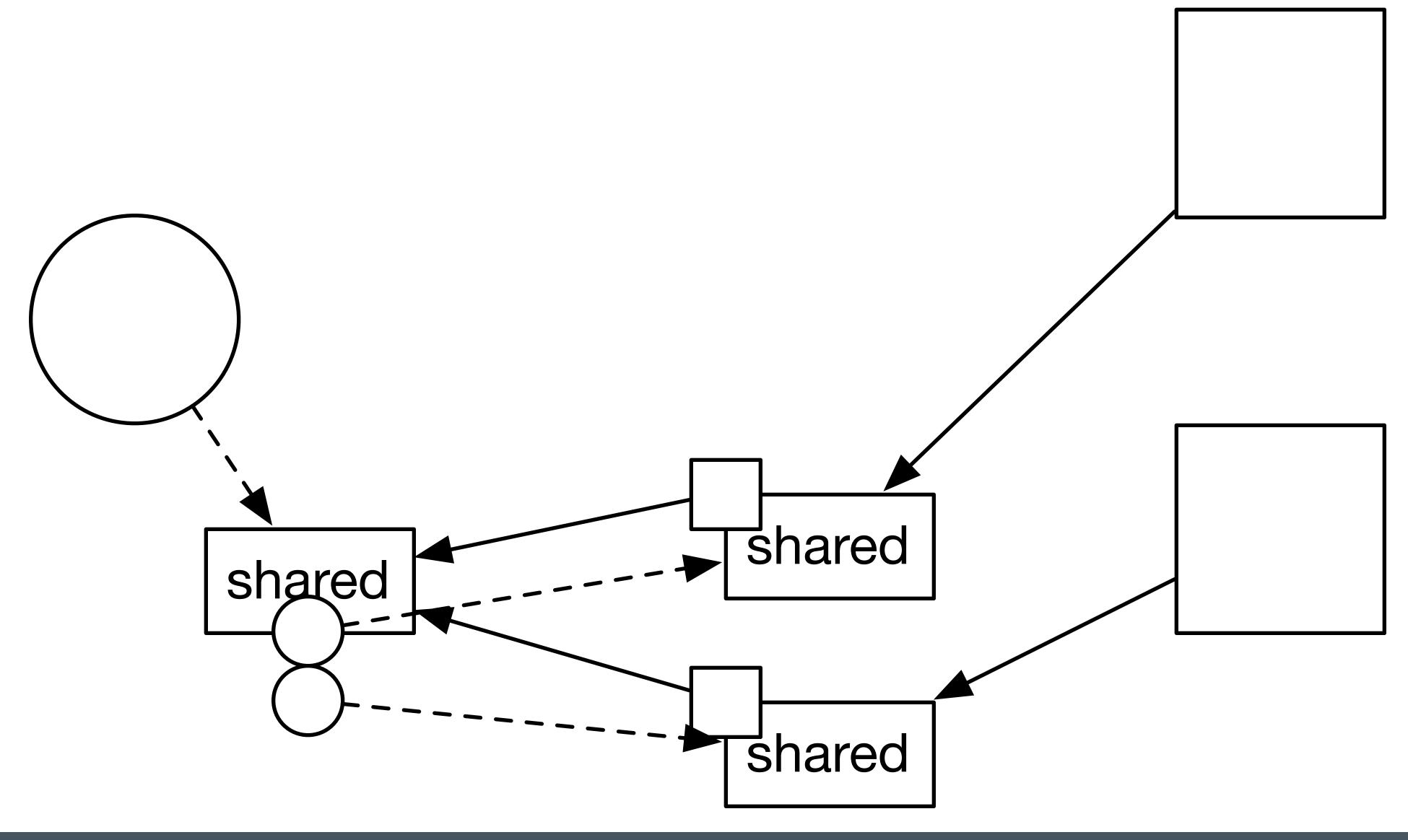














```
template <typename>
struct result_of_; //not defined

template <typename R, typename... Args>
struct result_of_<R(Args...)> { using type = R; };

template <typename F>
using result_of_t_ = typename result_of_<F>::type;
```

```
template <typename>
struct result_of_; //not defined

template <typename R, typename... Args>
struct result_of_<R(Args...)> { using type = R; };

template <typename F>
using result_of_t_ = typename result_of_<F>::type;
```

```
template <typename> class packaged_task; //not defined
template <typename R>
class future {
    shared_ptr</* ... */> _p;
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) { }
    const R& get() const { }
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
 public:
   packaged_task() = default;
   template <typename... A>
    void operator()(A&&... args) const { }
};
```



```
template <typename> class packaged_task; //not defined
template <typename R>
class future {
    shared_ptr</* ... */> _p;
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) { }
    const R& get() const { }
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
 public:
   packaged_task() = default;
   template <typename... A>
    void operator()(A&&... args) const { }
};
```



```
template <typename> class packaged_task; //not defined
template <typename R>
class future {
    shared_ptr</* ... */> _p;
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) { }
    const R& get() const { }
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
 public:
   packaged_task() = default;
   template <typename... A>
    void operator()(A&&... args) const { }
};
```



```
template <typename> class packaged_task; //not defined
template <typename R>
class future {
    shared_ptr</* ... */> _p;
 public:
    future() = default;
    template <typename F>
    auto then(F&& f) { }
    const R& get() const { }
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
    weak_ptr</* ... */> _p;
 public:
    packaged_task() = default;
    template <typename... A>
    void operator()(A&&... args) const { }
};
```



```
template <typename> class packaged_task; //not defined
template <typename R>
class future {
    shared_ptr</* ... */> _p;
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) { }
    const R& get() const { }
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
 public:
   packaged_task() = default;
   template <typename... A>
    void operator()(A&&... args) const { }
};
```



```
template <typename> class packaged_task; //not defined
template <typename> class future;
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
template <typename R>
class future {
    shared_ptr</* ... */> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit future(shared_ptr</* ... */> p) : _p(move(p)) { }
   /* ... */
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
    template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit packaged_task(weak_ptr</* ... */> p) : _p(move(p)) { }
    /* ... */
```

```
template <typename> class packaged_task; //not defined
template <typename> class future;
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
template <typename R>
class future {
    shared_ptr</* ... */> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit future(shared_ptr</* ... */> p) : _p(move(p)) { }
   /* ... */
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
    template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit packaged_task(weak_ptr</* ... */> p) : _p(move(p)) { }
    /* ... */
```

```
template <typename> class packaged_task; //not defined
template <typename> class future;
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
template <typename R>
class future {
    shared_ptr</* ... */> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit future(shared_ptr</* ... */> p) : _p(move(p)) { }
   /* ... */
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
    template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit packaged_task(weak_ptr</* ... */> p) : _p(move(p)) { }
    /* ... */
```

```
template <typename> class packaged_task; //not defined
template <typename> class future;
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
template <typename R>
class future {
    shared_ptr</* ... */> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit future(shared_ptr</* ... */> p) : _p(move(p)) { }
   /* ... */
};
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
   weak_ptr</* ... */> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit packaged_task(weak_ptr</* ... */> p) : _p(move(p)) { }
    /* ... */
```

```
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>> {
    auto p = make_shared<shared<S>>(forward<F>(f));
    return make_pair(packaged_task<S>(p), future<result_of_t_<S>>(p));
}
```

```
template <typename S, typename F>
auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>> {
    auto p = make_shared<shared<S>>(forward<F>(f));
    return make_pair(packaged_task<S>(p), future<result_of_t_<S>>(p));
}
```

```
package<int(double)>(f) -> { void(double), future<int> }
```

```
template <typename R>
struct shared_base {
   vector<R> _r; // optional
   mutex _mutex;
   condition_variable _ready;
   vector<function<void()>> _then;
   virtual ~shared_base() { }
   /* ... */
template <typename> struct shared; // not defined
template <typename R, typename... Args>
struct shared<R(Args...)> : shared_base<R> {
   function<R(Args...)> _f;
   template<typename F>
    shared(F&& f) : _f(forward<F>(f)) { }
   /* ... */
```

```
template <typename R>
struct shared_base {
   vector<R> _r; // optional
   mutex _mutex;
    condition_variable _ready;
   vector<function<void()>> _then;
   virtual ~shared_base() { }
   /* ... */
template <typename> struct shared; // not defined
template <typename R, typename... Args>
struct shared<R(Args...)> : shared_base<R> {
   function<R(Args...)> _f;
   template<typename F>
    shared(F&& f) : _f(forward<F>(f)) { }
   /* ... */
```

```
template <typename R>
struct shared_base {
    vector<R> _r; // optional
    mutex _mutex;
    condition_variable _ready;
    vector<function<void()>> _then;
    virtual ~shared_base() { }
   /* ... */
template <typename> struct shared; // not defined
template <typename R, typename... Args>
struct shared<R(Args...)> : shared_base<R> {
    function<R(Args...)> _f;
    template<typename F>
    shared(F&& f) : _f(forward < F > (f)) { }
   /* ... */
```



```
template<typename R, typename ...Args >
class packaged_task<R (Args...) > {
    weak_ptr<shared<R(Args...) >> _p;

    template <typename S, typename F>
        friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;

    explicit packaged_task(weak_ptr<shared<R(Args...)>> p) : _p(move(p)) { }

public:
    packaged_task() = default;

    template <typename... A>
    void operator()(A&&... args) const {
        auto p = _p.lock();
        if (p) (*p)(forward<A>(args)...);
    }
};
```

```
template<typename R, typename ...Args >
class packaged_task<R (Args...) > {
    weak_ptr<shared<R(Args...) >> _p;

    template <typename S, typename F>
        friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;

    explicit packaged_task(weak_ptr<shared<R(Args...) >> p) : _p(move(p)) { }

public:
    packaged_task() = default;

    template <typename... A>
    void operator()(A&&... args) const {
        auto p = _p.lock();
        if (p) (*p)(forward<A>(args)...);
    }
};
```

```
template<typename R, typename ...Args >
class packaged_task<R (Args...)> {
    weak_ptr<shared<R(Args...)>> _p;

    template <typename S, typename F>
    friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;

    explicit packaged_task(weak_ptr<shared<R(Args...)>> p) : _p(move(p)) { }

public:
    packaged_task() = default;

    template <typename... A>
    void operator()(A&&... args) const {
        auto p = _p.lock();
        if (p) (*p)(forward<A>(args)...);
    }
};
```

```
template <typename R, typename... Args>
struct shared<R(Args...)> : shared_base<R> {
   function<R(Args...)> _f;

   template<typename F>
   shared(F&& f) : _f(forward<F>(f)) { }

   template <typename... A>
   void operator()(A&&... args) {
      this->set(_f(forward<A>(args)...));
      _f = nullptr;
   }
};
```



```
template <typename R, typename... Args>
struct shared<R(Args...)> : shared_base<R> {
   function<R(Args...)> _f;

   template<typename F>
    shared(F&& f) : _f(forward<F>(f)) { }

   template <typename... A>
   void operator()(A&&... args) {
      this->set(_f(forward<A>(args)...));
      _f = nullptr;
   }
}:
```

```
template <typename R>
struct shared_base {
   vector<R> _r; // optional
   mutex _mutex;
   condition_variable _ready;
   vector<function<void()>> _then;
   virtual ~shared_base() { }
   void set(R&& r) {
        vector<function<void()>> then;
            lock_t lock{_mutex};
            _r.push_back(move(r));
            swap(_then, then);
        _ready.notify_all();
        for (const auto& f : then) _system.async_(move(f));
};
```

```
template <typename R>
struct shared_base {
   vector<R> _r; // optional
   mutex _mutex;
   condition_variable _ready;
   vector<function<void()>> _then;
   virtual ~shared_base() { }
   void set(R&& r) {
        vector<function<void()>> then;
            lock_t lock{_mutex};
            _r.push_back(move(r));
            swap(_then, then);
        _ready.notify_all();
        for (const auto& f : then) _system.async_(move(f));
```

```
template <typename R>
class future {
    shared_ptr<shared_base<R>> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
   explicit future(shared_ptr<shared_base<R>> p) : _p(move(p)) { }
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) {
        auto pack = package<result_of_t<F(R)>()>([p = _p, f = forward<F>(f)](){
            return f(p->_r.back());
        });
        _p->then(move(pack.first));
        return pack.second;
    const R& get() const { return _p->get(); }
};
```

```
template <typename R>
class future {
    shared_ptr<shared_base<R>> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
    explicit future(shared_ptr<shared_base<R>> p) : _p(move(p)) { }
public:
   future() = default;
   template <typename F>
    auto then(F&& f) {
        auto pack = package<result_of_t<F(R)>()>([p = _p, f = forward<F>(f)](){
            return f(p->_r.back());
        });
        _p->then(move(pack.first));
        return pack.second;
    const R& get() const { return _p->get(); }
};
```

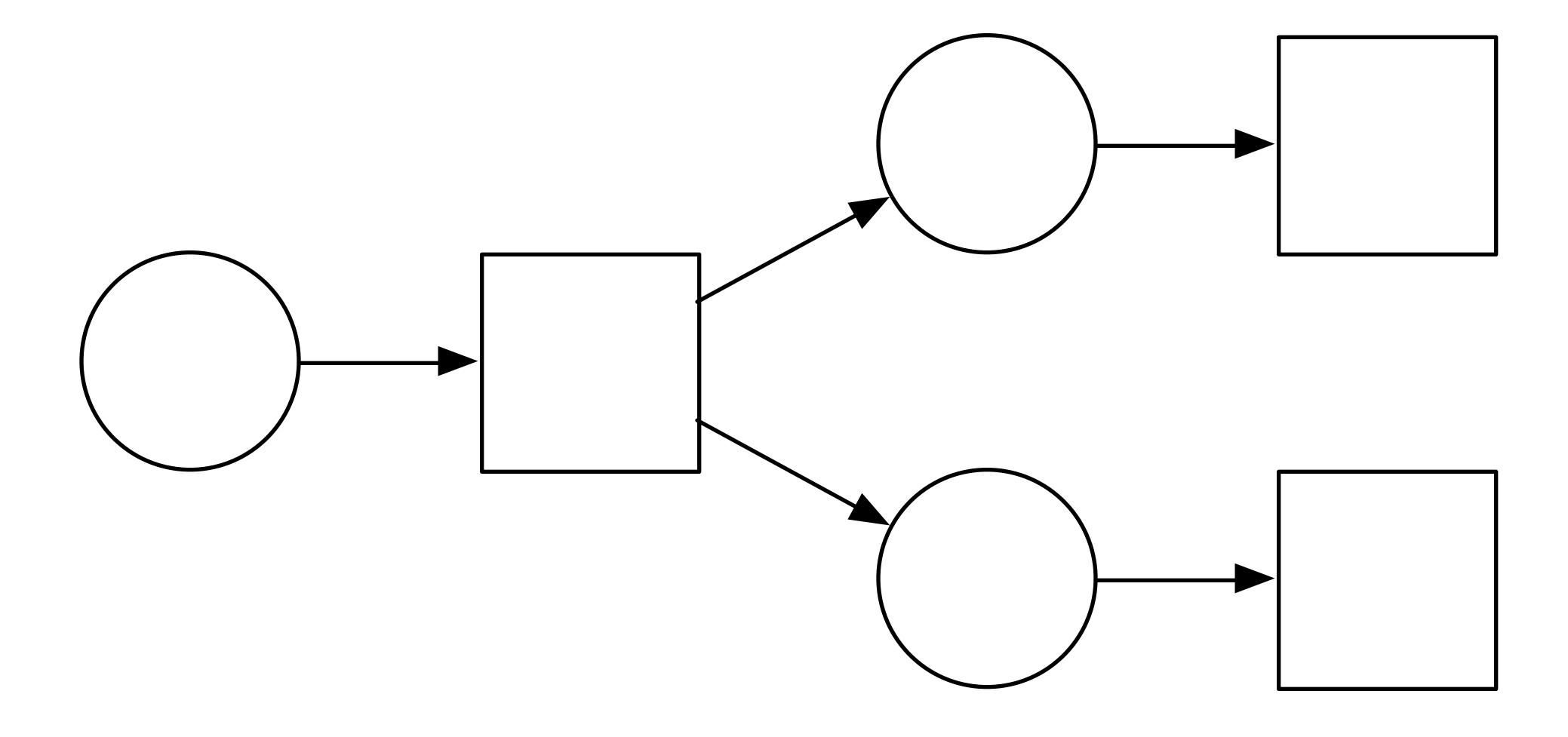
```
template <typename R>
class future {
    shared_ptr<shared_base<R>> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
   explicit future(shared_ptr<shared_base<R>> p) : _p(move(p)) { }
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) {
        auto pack = package<result_of_t<F(R)>()>([p = _p, f = forward<F>(f)](){
            return f(p->_r.back());
        });
        _p->then(move(pack.first));
        return pack.second;
    const R& get() const { return _p->get(); }
};
```

```
template <typename R>
class future {
    shared_ptr<shared_base<R>> _p;
   template <typename S, typename F>
   friend auto package(F&& f) -> pair<packaged_task<S>, future<result_of_t_<S>>>;
   explicit future(shared_ptr<shared_base<R>> p) : _p(move(p)) { }
 public:
   future() = default;
   template <typename F>
    auto then(F&& f) {
        auto pack = package<result_of_t<F(R)>()>([p = _p, f = forward<F>(f)](){
            return f(p->_r.back());
        });
        _p->then(move(pack.first));
        return pack.second;
    const R& get() const { return _p->get(); }
```

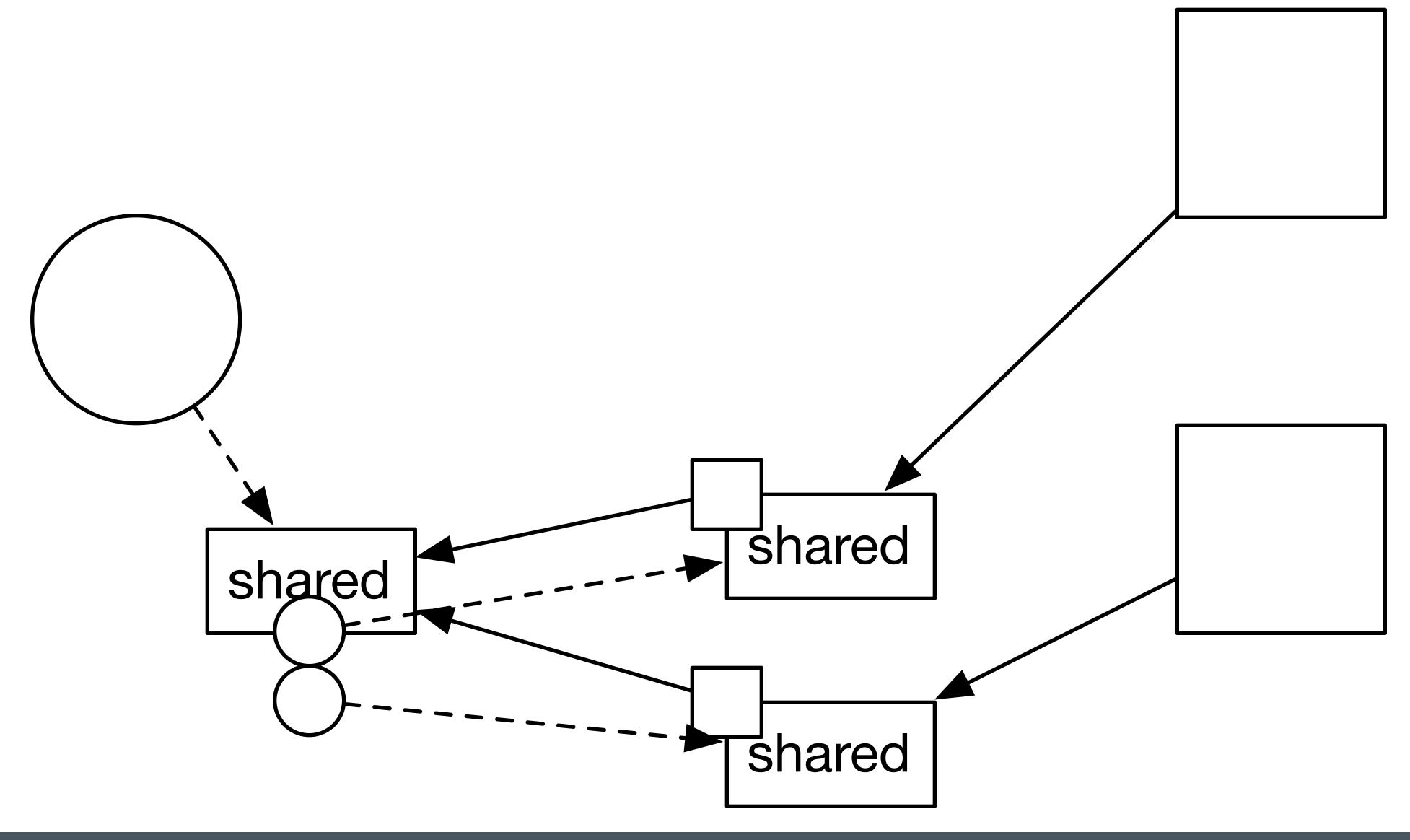
```
template <typename R>
struct shared_base {
    vector<R> _r; // optional
    mutex _mutex;
    condition_variable _ready;
    vector<function<void()>> _then;
    virtual ~shared_base() { }
    void set(R&& r) { ... }
    template <typename F>
    void then(F&& f) {
        bool resolved{false};
            lock_t lock{_mutex};
            if (_r.empty()) _then.push_back(forward<F>(f));
            else resolved = true;
        if (resolved) _system.async_(move(f));
    const R& get() {
        lock_t lock{_mutex};
        while (_r.empty()) _ready.wait(lock);
        return _r.back();
```

```
template <typename R>
struct shared_base {
    vector<R> _r; // optional
    mutex _mutex;
    condition_variable _ready;
    vector<function<void()>> _then;
    virtual ~shared_base() { }
    void set(R&& r) { •• }
    template <typename F>
    void then(F&& f) {
        bool resolved{false};
            lock_t lock{_mutex};
            if (_r.empty()) _then.push_back(forward<F>(f));
            else resolved = true;
        if (resolved) _system.async_(move(f));
    const R& get() {
        lock_t lock{_mutex};
        while (_r.empty()) _ready.wait(lock);
        return _r.back();
```

```
template <typename R>
struct shared_base {
    vector<R> _r; // optional
    mutex _mutex;
    condition_variable _ready;
    vector<function<void()>> _then;
    virtual ~shared_base() { }
    void set(R&& r) { ... }
    template <typename F>
    void then(F&& f) {
        bool resolved{false};
            lock_t lock{_mutex};
            if (_r.empty()) _then.push_back(forward<F>(f));
            else resolved = true;
        if (resolved) _system.async_(move(f));
    const R& get() {
        lock_t lock{_mutex};
        while (_r.empty()) _ready.wait(lock);
        return _r.back();
```







```
template <typename F, typename ...Args>
auto async(F&& f, Args&&... args)
{
    using result_type = result_of_t<F (Args...)>;
    using packaged_type = packaged_task<result_type()>;
    auto pack = package<result_type()>(bind(forward<F>(f), forward<Args>(args)...));
    _system.async_(move(get<0>(pack)));
    return get<1>(pack);
```

#### Futures: Continuations

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(100); });

future<cpp_int> y = x.then([](const cpp_int& x){ return cpp_int(x * 2); });

future<cpp_int> z = x.then([](const cpp_int& x){ return cpp_int(x / 15); });

cout << y.get() << endl;

cout << z.get() << endl;</pre>
```

#### **Futures: Continuations**

```
future<cpp_int> x = async([]{ return fibonacci<cpp_int>(100); });

future<cpp_int> y = x.then([](const cpp_int& x){ return cpp_int(x * 2); });

future<cpp_int> z = x.then([](const cpp_int& x){ return cpp_int(x / 15); });

cout << y.get() << endl;

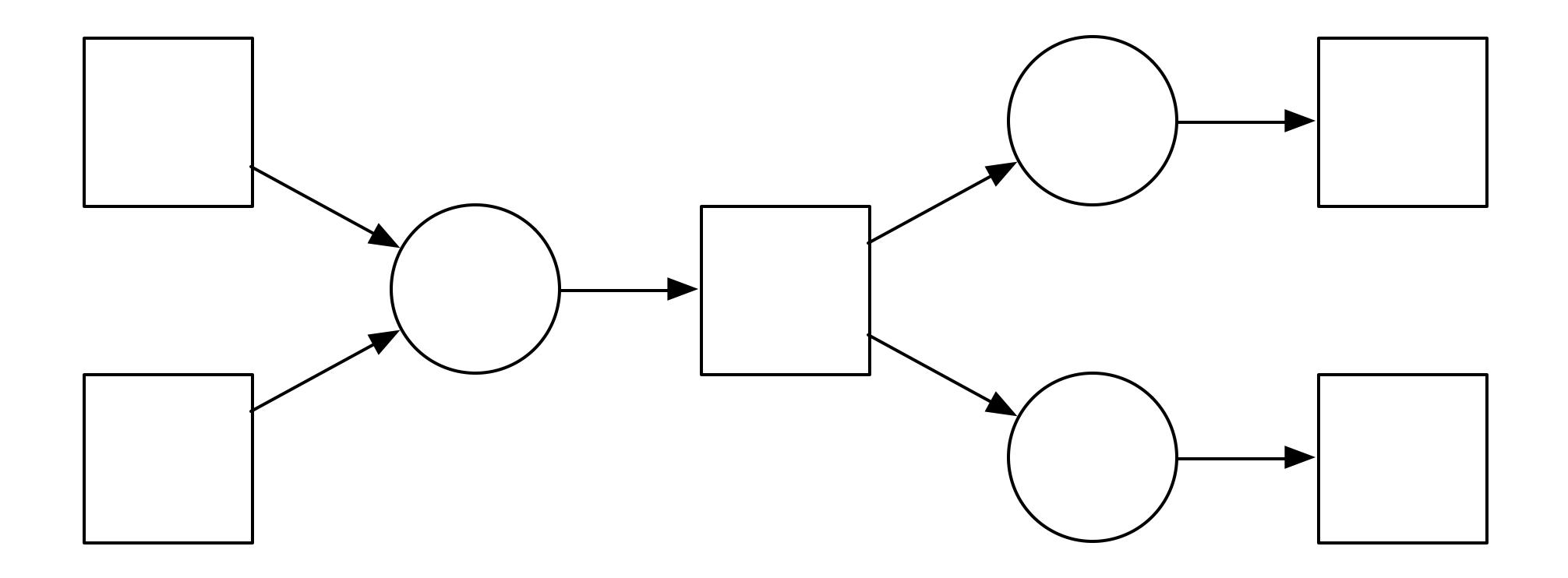
cout << z.get() << endl;</pre>
```

708449696358523830150 23614989878617461005



# Property Models



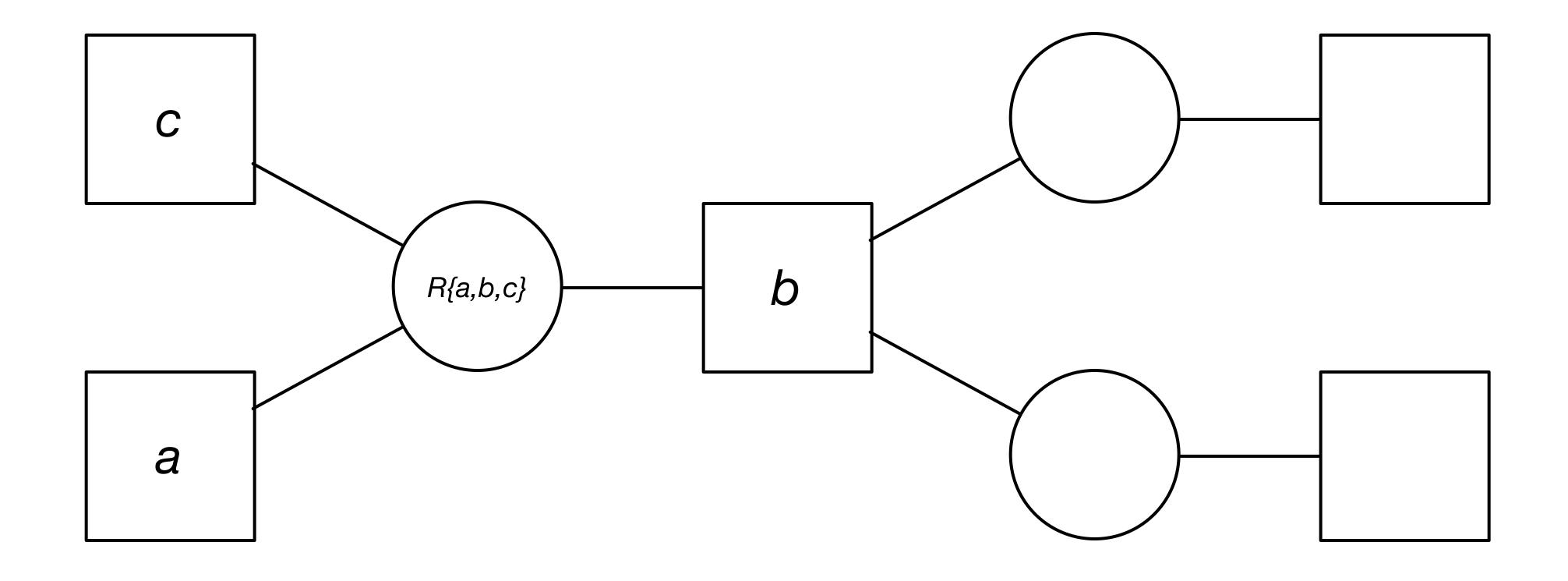


# What if we persist the graph?

- Allow multiple invocations of the tasks by setting the source values
- Each change triggers a notification to the sink values
- This is a reactive programming model and futures are known as behaviors

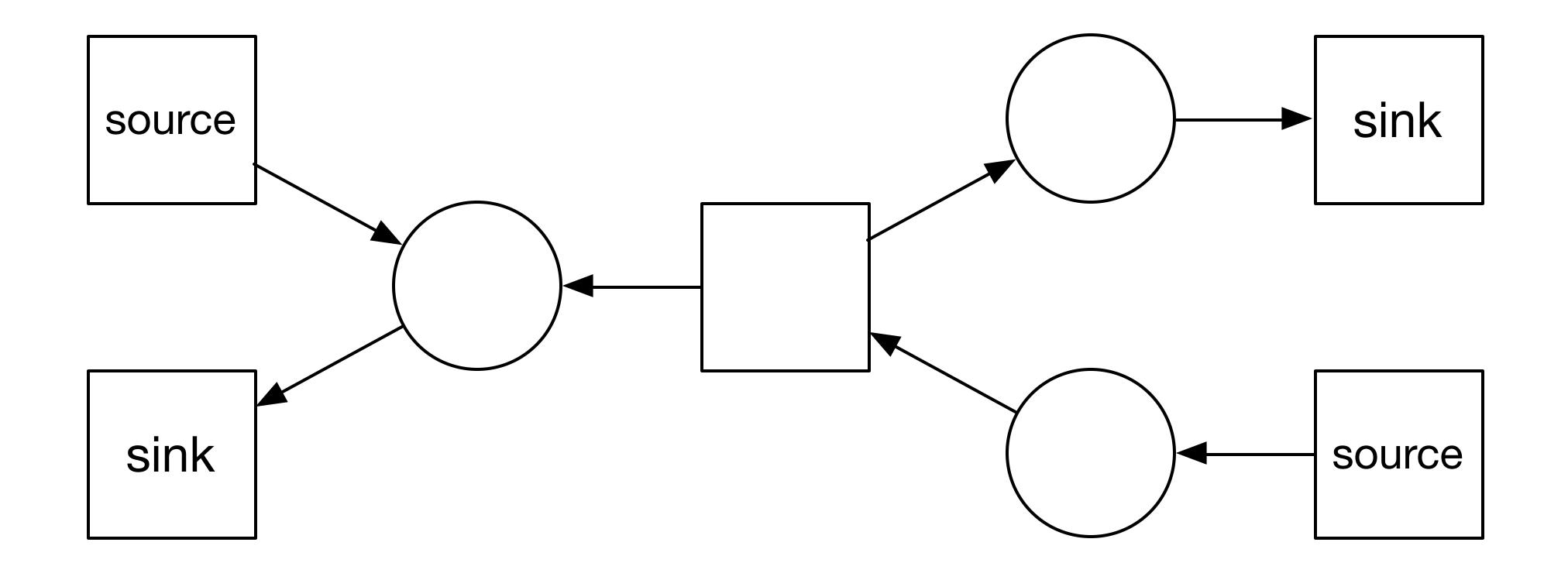
How do the graphs change during execution?





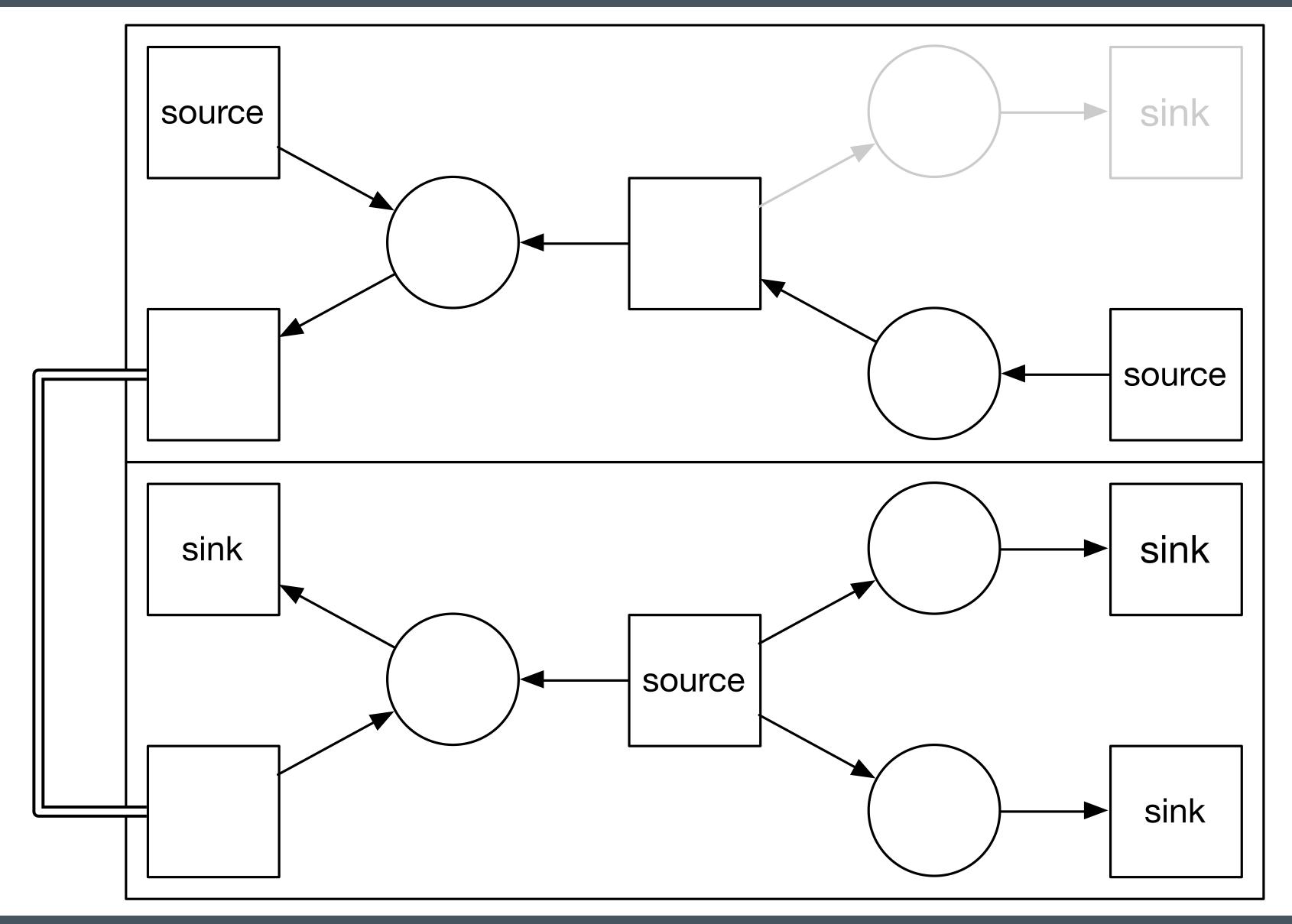
# A function is a directed relationship

- We can remove the arrows by providing a package of functions to represent the relationship
- a = b \* c
   b = a / c
   c = a / b
- This forms a type of constraint system called a property model
- Flow is determined by value, or *cell*, priority
- Cells can only have one in-edge for a given flow or the system is over constrained



#### Property Models

- Reflowing a property model doesn't require all relationships to be resolved
  - The task representing them can still be executing concurrently
- This creates a single dependency graph that is appended to for each new flow and is pruned and unravels as tasks are complete



### Final Thoughts

- Perhaps representing such systems as if it where imperative code is not the correct approach
- Instead the a graph description can be compiled and statically validated



