# Convolutional Neural Networks

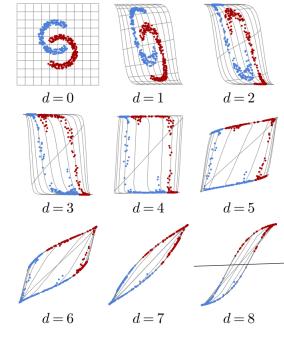
### Recap: Goal of ML

generalization from optimization on training data set (approximation of true data generating probability distribution by empirical risk minimization)

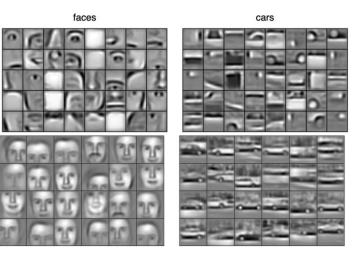
- fitting: complex function approximation
- for generalization: learning of good abstraction/representation of data/concepts
- → deep learning methods (MLP, CNN, ...) optimal candidates

e.g., CNNs can learn hierarchical representation by means of many convolutional and pooling layers

the deeper the better (accuracy, hierarchical representation)



source

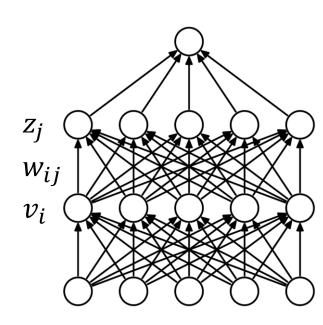


### Recap: Feed-Forward Neural Networks

computation in usual feed-forward network:

scalar input values  $z_j$  to activation function of nodes j in hidden or output layer as matrix multiplication of scalar output values  $v_i$  from activation function of nodes i from previous layer with connecting weights  $w_{i,j}$ 

$$z_j = \sum_i v_i \, w_{i,j}$$



dropping dimension of different training observations in this view → loading full batch or mini-batches

### Grid-Like Data

data with grid-like topology (spatial structures), e.g.:

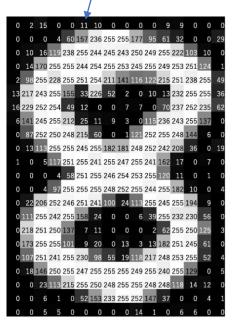
- time-series data: 1-D grid of data taken at regular time intervals (can also be done with recurrent neural networks or transformers)
- image data: 2-D grid of pixels (→ computer vision)

#### convolutional networks:

neural networks using convolutions with kernels (local groups of values, e.g., pixels from an object, highly correlated) in place of general matrix multiplications in at least one of their layers

→ highly regularized feed-forward networks

scalar value (like in usual feed-forward network)



source

### Convolution Operation

to be exact, usually rather cross-correlation instead of convolution operation (what would have — here):

$$Z_{i,j} = (K * V)_{i,j} = \sum_{m,n} V_{i+m,j+n} K_{m,n}$$

feature map

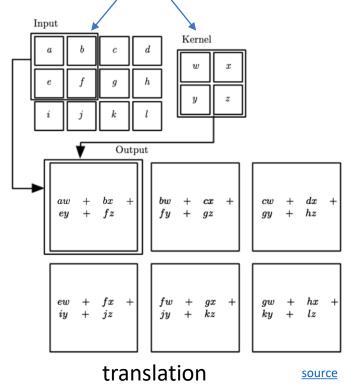
input (matrix) kernel (matrix)

again, dropping dimension of different training observations matrices  $\rightarrow$  tensors: several input channels c (e.g., RGB) and several output channels f (different feature maps, e.g., vertical edge, nose, ear, ...)

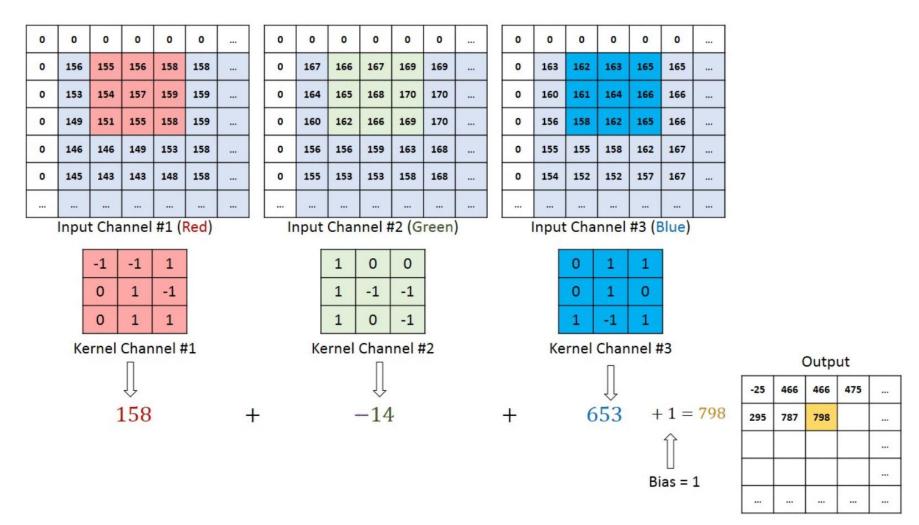
$$Z_{f,i,j} = \sum_{c,m,n} V_{c,i+m,j+n} K_{f,c,m,n}$$

#### learned parameters:

- connection to local patches of previous layer's feature maps
- shared over entire image (common learning across image)

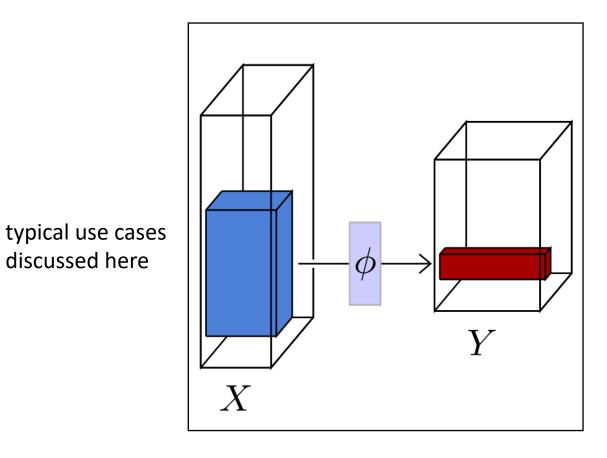


### Channel Mixing



6

### Decrease or Increase Dimensionality



discussed here

e.g., decoder side of autoencoders or U-nets in diffusion models

2D convolution

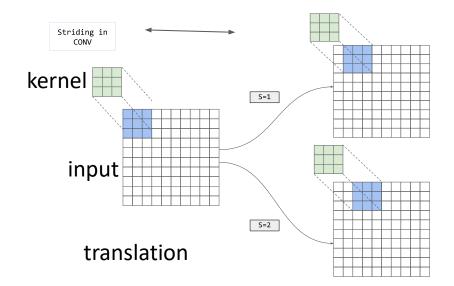
2D transposed convolution

# Important Details: Striding and Padding

need to define how to stride over image

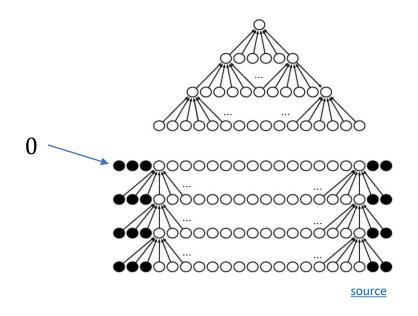
$$Z_{f,i,j} = \sum_{c,m,n} V_{c,i\times s+m,j\times s+n} K_{f,c,m,n}$$

- s > 1 corresponds to down-sampling
- → fewer nodes after convolutional layer



zero-padding of input to make it wider: otherwise shrinking of representation with each layer (depending on kernel

size)  $\rightarrow$  allowing large kernels and slow shrinkage

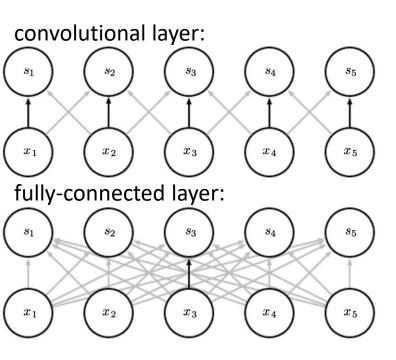


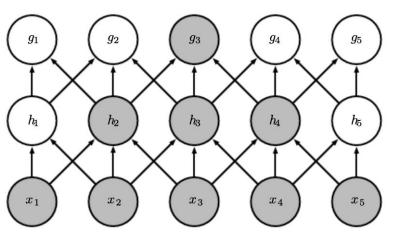
### Regularization Effects

- sparse interactions: much less weights
- parameter sharing: use same weights for different connections

effect of receptive field over several layers:

- consider only locally restricted number of input values from previous layer
- grows for earlier layers (indirect interactions)
- → hierarchical patterns from simple building blocks (many aspects of nature hierarchical)





### Another Ingredient: Pooling

replacing outputs of neighboring nodes with summary statistic (e.g., maximum or average value of nodes)

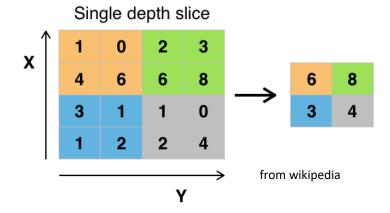
→ non-linear down-sampling (regularization)

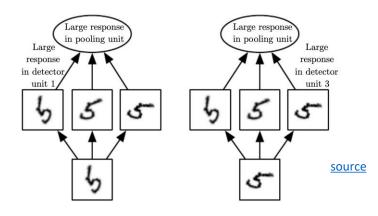
pooling is translation invariant: no interest in exact position of, e.g., maximum value

pooling over features learned by separate kernels (cross-channel pooling) can also learn other transformation invariances, like rotation or scale

(convolutions can detect same translated motif across entire image, but not rotated or scaled versions of it)

#### max pooling:





### Putting It All Together

CNN in short:

potentially with

several channels

local connections, shared weights, pooling, many layers

feature maps

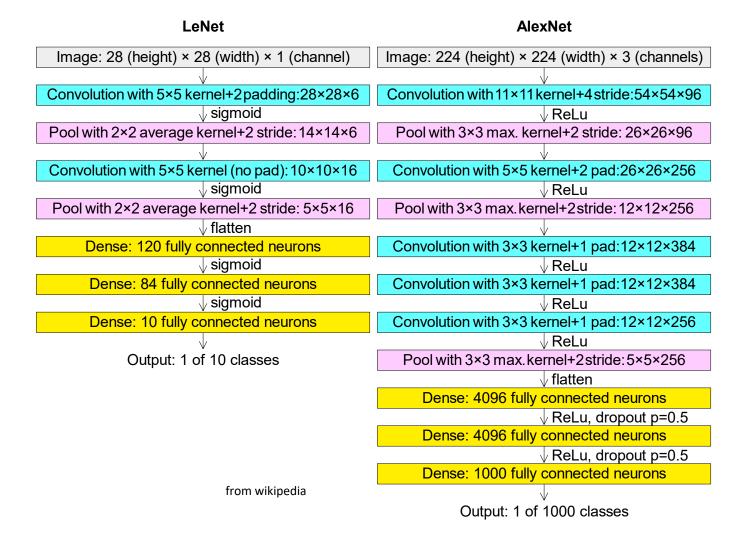
kernels □dog □ cat □lion □ bird Pooling Convolution Pooling Fully-connected Convolution many images down-sampling flatten dimensions several kernels (training examples), by convolutions producing several for final classification

and pooling

or regression

Next layer Convolutional Layer Pooling stage Detector stage: Nonlinearity e.g., rectified linear Convolution stage: Affine transform Input to layer source

### Going Deeper



AlexNet finally started the deep learning hype.

(winning the ImageNet challenge in 2012)

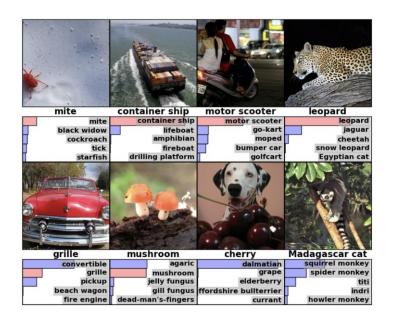
# Rise of Deep Learning

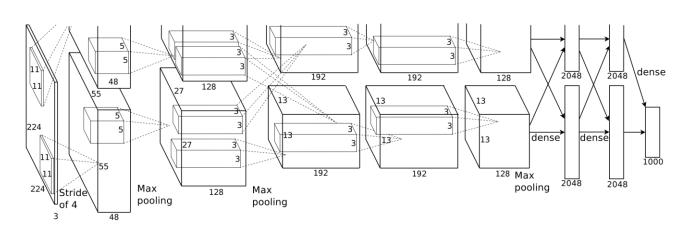
a little bit oversimplified:

deep learning = lots of training data + parallel computation + smart algorithms

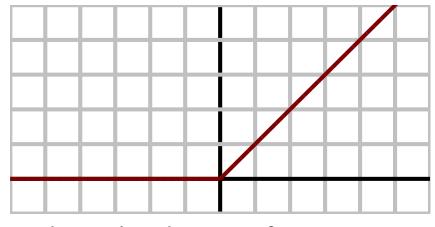
AlexNet: ImageNet (with data augmentation) + GPUs

+ ReLU, dropout, SGD





### Rectified Linear Unit (ReLU)



reminder: activation function non-linear transformation of summed weighted input of a node (linear), output to be used as input for nodes of subsequent layer

needs to be differentiable for back-propagation (ReLU at 0 no issue, just set to 0 or 1)

neural network model with <u>ReLU activation</u> can be interpreted as exponential number of linear models that share parameters

main advantages (leading to enablement of deeper networks by better optimization):

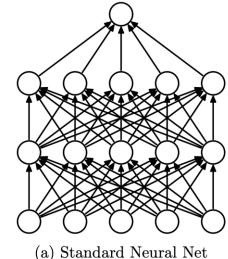
- unlike sigmoid or tanh (predominantly used before) activation, no issue with vanishing gradients from saturation effects
- very efficient computation: constant gradients of 0 and 1 below and above input of zero
- sparse activation: many hidden nodes deactivated (output 0) → information disentangling

### Dropout in Neural Networks

goal: prevent overfitting of large neural networks

idea: randomly drop non-output nodes (along with their connections) during training (not prediction)

→ adaptability: regularizing each hidden node to perform well regardless of which other hidden nodes are in the model





 $\otimes$ 

 $\otimes$ 

source

 $\otimes$ 

- for each mini-batch, randomly sample independent binary masks for the nodes
- much less computation than bagging (training many different neural networks)
- destroying extracted features rather than input values

dropout for 2D structures, such as images, usually drops entire channels instead of individual nodes (because locality nullifies the effect of standard dropout → neighboring nodes step in)

### Inductive Bias (aka Learning Bias)

set of assumptions that a learning algorithm uses to predict outputs of inputs that it has not encountered during training

examples: linear response (linear regression), maximum margin (SVM), nearest neighbors (kNN), spatial structure (CNN)

but also: different regularization and optimization methods

crucial piece of generalization

data in disguise (replacement for missing information on specific situations in limited training data sets)

### No Free Lunch Theorem

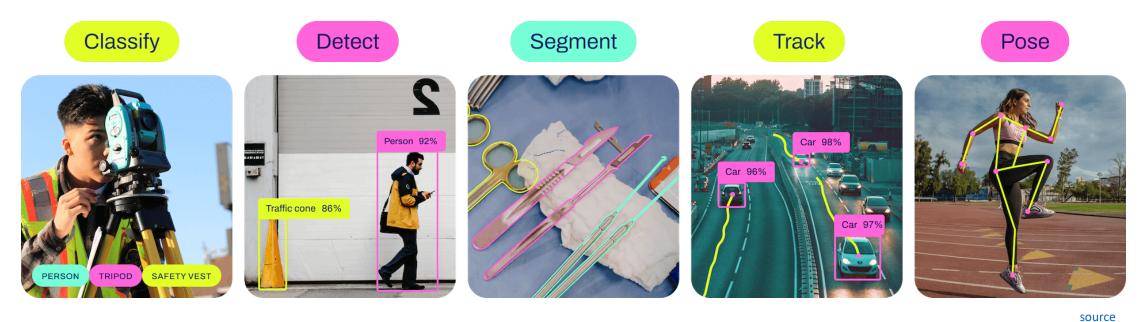
All optimization/ML algorithms (both sophisticated and simple ones) perform equally well when their performance is averaged across all possible problems.

(But deep learning is trying to solve many problems with very general-purpose forms of regularization.)

Particularly, model complexity doesn't reflect if inductive bias is appropriate for problem at hand.

> choose right ML method for learning task at hand

### Object Detection and Image Segmentation



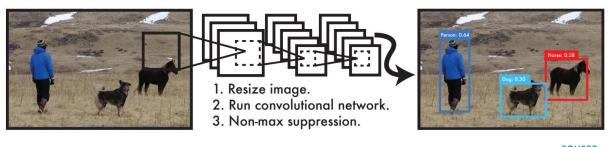
Source

coding example: object detection and image segmentation with **YOLO** 

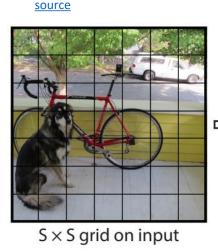
→ homogenous data (like images) and deep learning allow to use one model for different problems

see also image and video segmentation with Segment Anything Model (SAM, SAM 2)

# You Only Look Once (YOLO)



prediction of bounding boxes and class probabilities in one go: partition image into grid and label each



Bounding boxes + confidence Final detections Class probability map

### Assignments

handwritten digit classification: <u>Kaggle Digit Recognizer</u>
(build PyTorch CNN)

• image classification: <u>Kaggle Intel Image Classification</u> (fine-tune a <u>torchvision</u> model, e.g., AlexNet)