

Generative Models

Discriminative vs Generative

Understanding Machine Learning

Archetype: Naïve Bayes

probabilistic model:

$$P(Y|X_1, \dots, X_p) = \frac{P(Y, X_1, \dots, X_p)}{P(X_1, \dots, X_p)} = \frac{P(Y)P(X_1, \dots, X_p|Y)}{P(X_1, \dots, X_p)} \propto P(Y)P(X_1, \dots, X_p|Y)$$

Bayes' rule constant to be estimated

approach:

1. estimate $P(Y, \mathbf{X}) \rightarrow$ generative model (can be used to generate new samples)
2. calculate $P(Y|\mathbf{X})$ from $P(Y, \mathbf{X}) \rightarrow$ used for discriminative task (classification)

Independence Assumption

(naïve) assumption: conditional independence of features given target

$$P(X_j | Y, X_1, \dots, X_{j-1}, X_{j+1}, \dots, X_p) = P(X_j | Y)$$

$$\Rightarrow P(Y | X_1, \dots, X_p) = \frac{P(Y) \prod_{j=1}^p P(X_j | Y)}{P(X_1, \dots, X_p)}$$

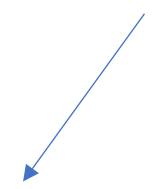
- independent feature contributions (ignoring feature correlations)
- robust against curse of dimensionality

Estimation of Feature Contributions

separate estimations of $P(X_j|Y)$ for each feature

requires assumption of distributions (e.g., Gaussian naïve Bayes) or non-parametric methods (kernel density estimation)

Gaussian feature likelihoods:

$$P(x_{ij}|y) = \frac{1}{\sqrt{2\pi\sigma_{y,j}^2}} \exp\left(-\frac{(x_{ij}-\mu_{y,j})^2}{2\sigma_{y,j}^2}\right)$$


parameter estimation (e.g., mean and variance of Gaussians) can be done with maximum likelihood method (y known in training)

→ no Bayesian methods needed

Maximum a Posteriori Classification

$$\hat{y}_i = \operatorname{argmax}_y P(y) \prod_{j=1}^p P(x_{ij}|y)$$

despite potentially inaccurate probability estimates (due to naïve independence assumption), good identification of correct class via maximum probability

→ bad for regression tasks (if independence assumption is too naïve, i.e., features are correlated)

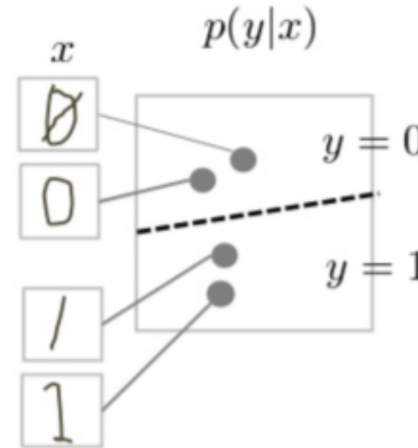
Generative vs Discriminative Models

generative models: predict joint probability $P(Y, \mathbf{X})$ (what allows to create new data samples) or directly generates new data samples

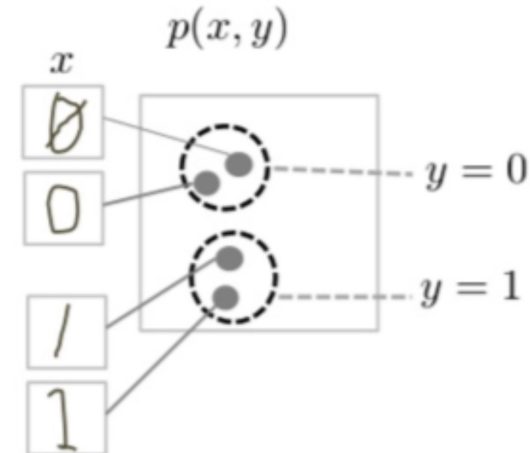
discriminative models: predict conditional probability $P(Y|\mathbf{X})$ or directly output (label for classification, real value for regression)

task of generative models more difficult: model full data distribution rather than merely find patterns in inputs to distinguish outputs

discriminative model



generative model



[source](#)

Naïve Bayes and Logistic Regression

generative-discriminative pair of classification algorithms

- binary case: logit of naïve Bayes' outputs, $\log \left(\frac{P(y_i=1|x_i)}{P(y_i=0|x_i)} \right)$, corresponds to output of logistic regression's linear predictor
- for discrete inputs or Gaussian naïve Bayes: naïve Bayes can be reparametrized as linear classifier

for discriminative task: identical in asymptotic limit (infinite training samples) if independence assumption holds (otherwise naïve Bayes less accurate)

naïve Bayes has greater bias but lower variance than logistic regression → to be preferred for scarce training data (if bias, i.e., independence assumption, correct)

Data Generation

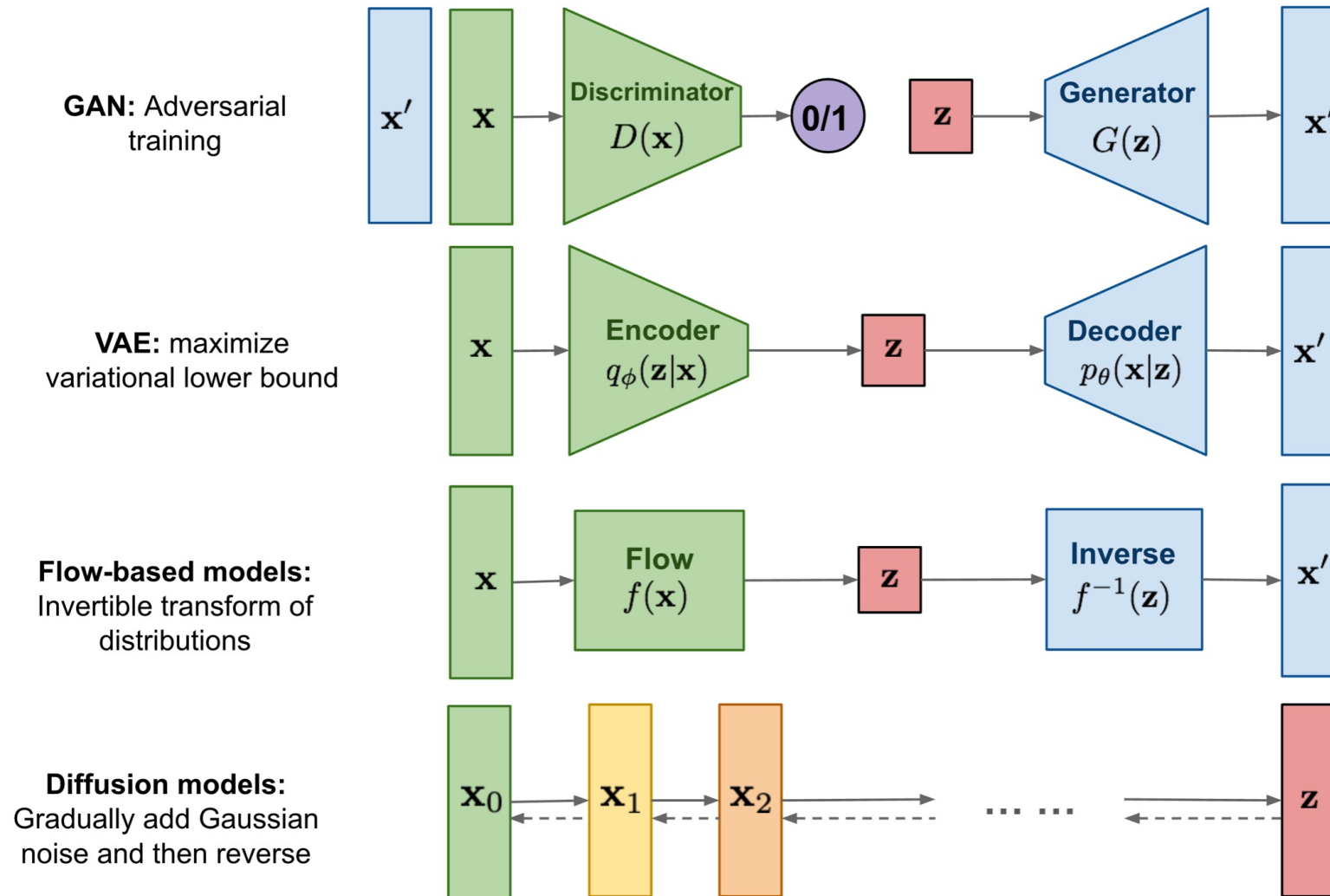
generative models can be used for discriminative tasks (although potentially inferior to direct discriminative methods)

but generative methods do more than discriminative ones: model full data distribution

→ allows generation of new data samples (e.g., images, text, video, ...)

large (auto-regressive) language models examples of generative models

Different Types of Generative Models



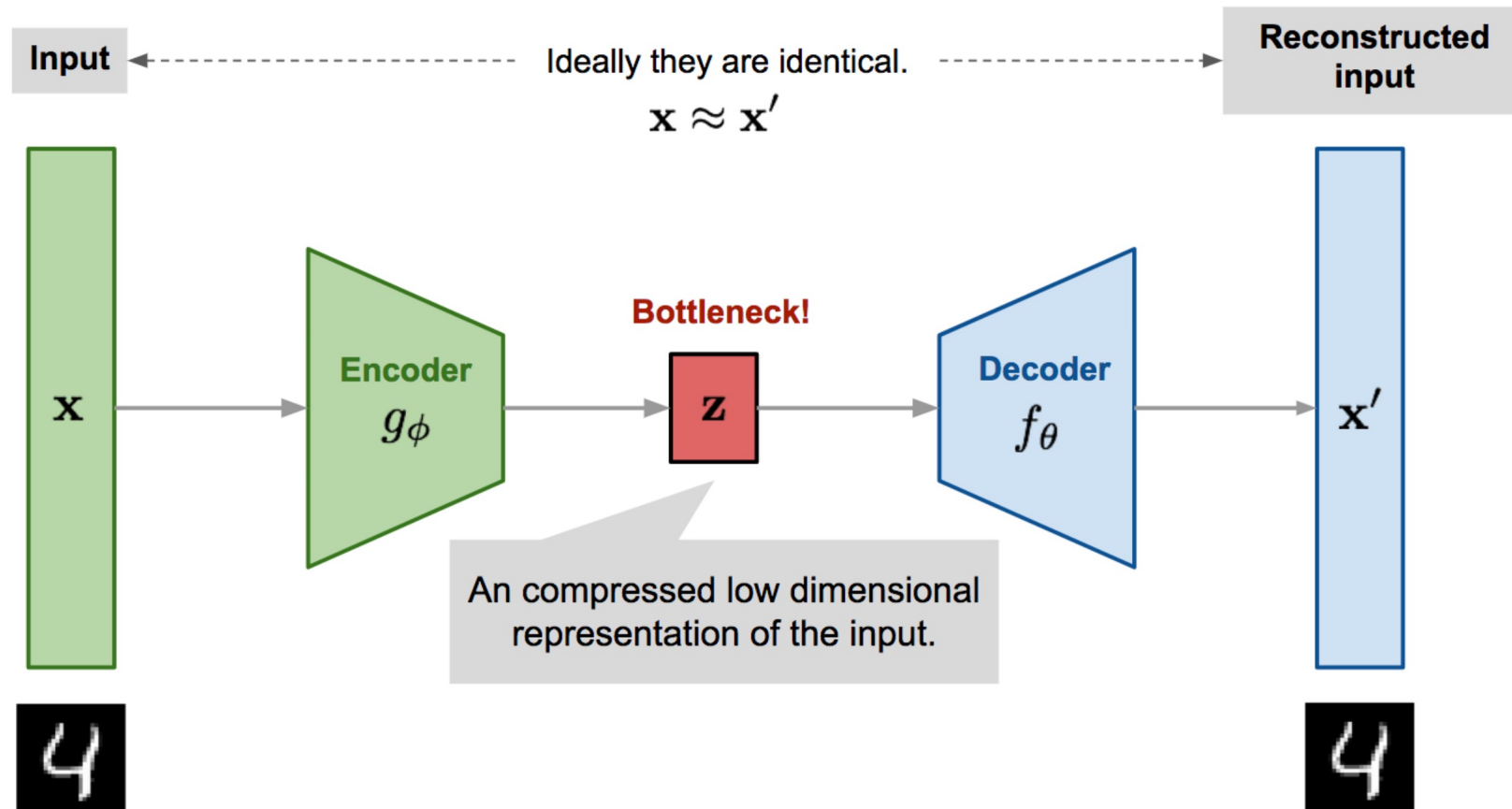
Variational Inference

- Bayesian ...

Recap: Autoencoder

(deep) encoder network
(deep) decoder network
learned together by
minimizing differences
between original input and
reconstructed input
(expressed as losses)

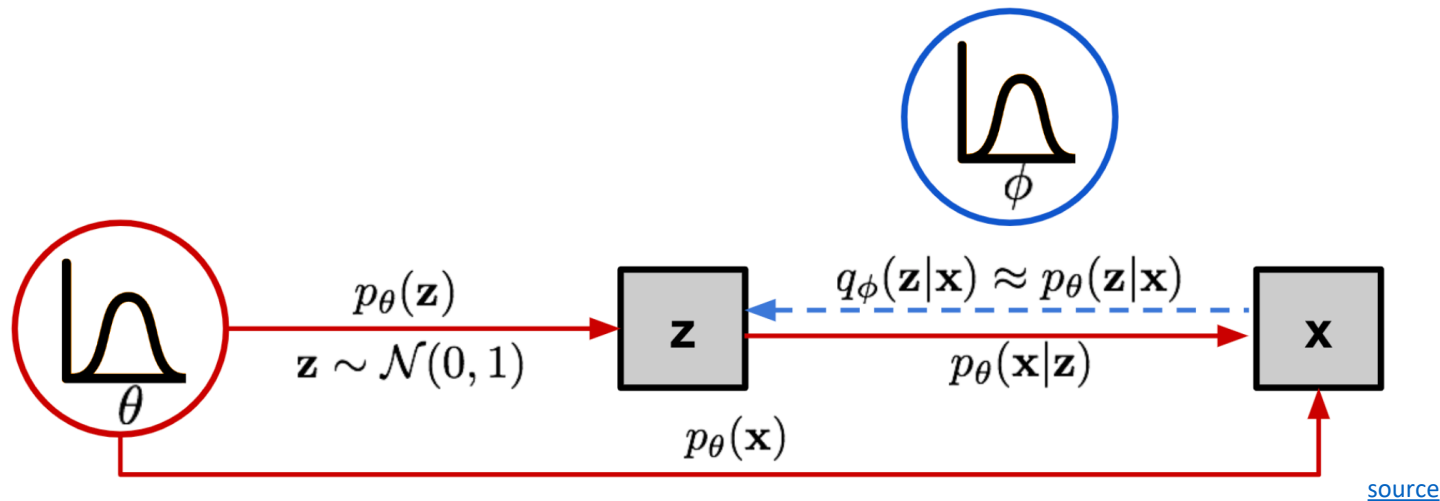
compressed intermediate
representation:
dimensionality reduction



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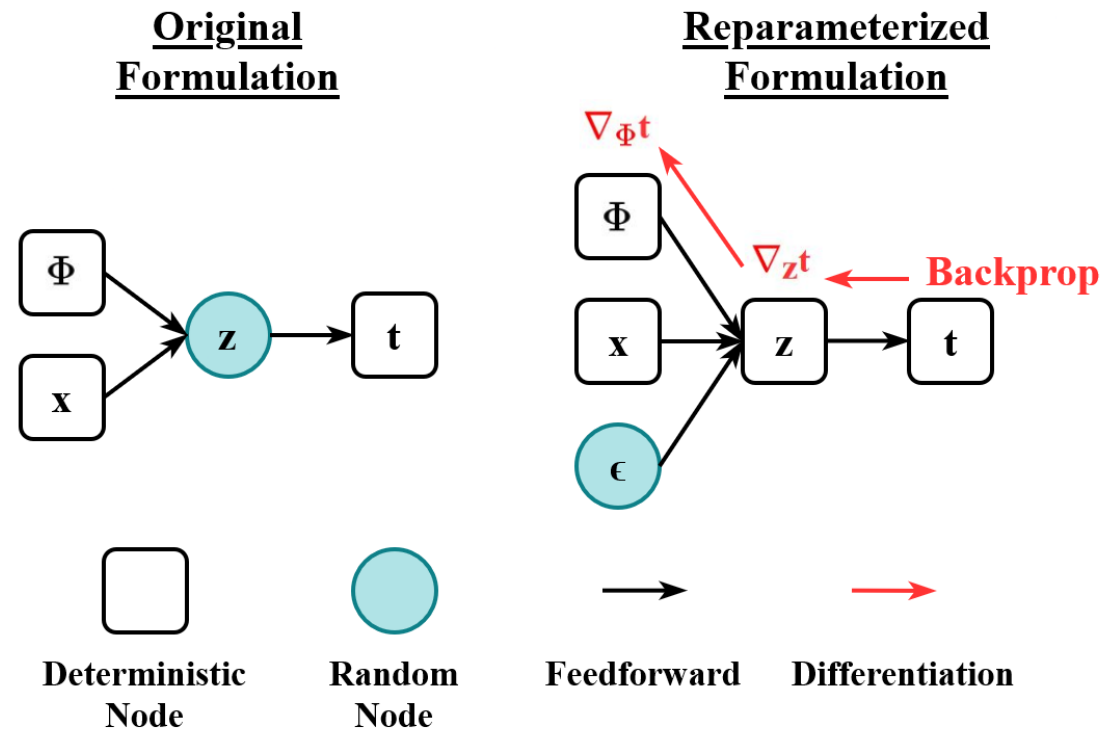
Variational Autoencoder (VAE)

- ...
- VAE relies on a surrogate loss



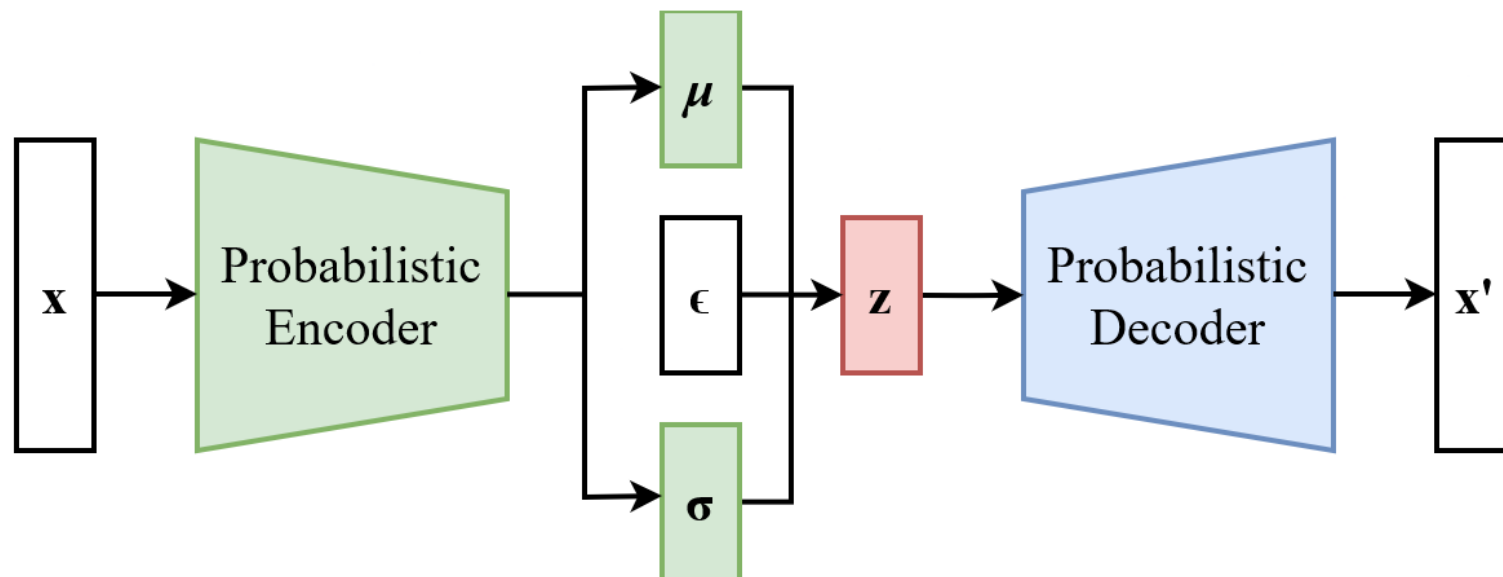
ELBO

- reparameterization trick



from wikipedia

• ...



from wikipedia

Generative Adversarial Networks (GAN)

● ...

- GAN models are known for potentially unstable training and less diversity in generation due to their adversarial training nature.

Flow-Based Methods

● ...

- Flow models have to use specialized architectures to construct reversible transform.

Energy-Based Methods

● ...

Diffusion Models

● ...

- Diffusion models are inspired by non-equilibrium thermodynamics. They define a Markov chain of diffusion steps to slowly add random noise to data and then learn to reverse the diffusion process to construct desired data samples from the noise. Unlike VAE or flow models, diffusion models are learned with a fixed procedure and the latent variable has high dimensionality (same as the original data).

Image Generation

[DALL-E 2](#)

...

Stable Diffusion DreamStudio



A dream of a distant galaxy, by Caspar David Friedrich, matte painting trending on artstation HQ

Literature

papers:

- [variational autoencoder](#)
- [GAN](#)
- [normalizing flows](#)
- [latent diffusion](#)

HWARZENEGGER



Movie-like Intelligence

emergent capabilities of complex systems almost impossible to foresee

mini examples in contemporary ML:

- [large language models](#)
- [multi-agent reinforcement learning](#)

one idea: [reward is enough](#)

philosophical: emotions or consciousness might also occur as emergent capabilities

