

SEMsensitivity: An R Package for Sensitivity Analysis in Structural Equation Modeling

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DOI: [10.xxxxxx/draft](https://doi.org/10.xxxxxx/draft)

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Submitted: 01 January 1970

Published: unpublished

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Summary

The package, SEMsensitivity, addresses the need for robust methods to validate the stability and reliability of SEMs, particularly in light of the replication crisis in psychology and social sciences. Traditional sensitivity analyses often fall short in assessing the impact of individual data points on complex models. SEMsensitivity overcomes these limitations by providing tools to identify influential data points and evaluate their effect on SEM paths. The package integrates with popular R packages like lavaan, dplyr, and semfindr, offering a user-friendly interface and efficient computation. It employs various methods, including Taylor series approximations and the Negamax search algorithm, to iteratively remove data points and assess their influence on model parameters. It is publicly available on GitHub and can be easily installed and utilized by researchers to ensure the robustness and reliability of their SEM models.

Statement of Need

In statistical analysis, ensuring the robustness of models is significant, especially in the context of Structural Equation Modeling (SEM). The replication crisis in psychology and the social sciences highlights the critical need for methodologies that can validate the stability and reliability of statistical findings. Traditional sensitivity analyses often fall short in assessing the impact of individual data points on the overall model conclusions, particularly in complex, multi-dimensional datasets where influential observations may not be readily apparent.

The R package SEMsensitivity addresses this gap by providing a suite of tools specifically designed for performing sensitivity analysis on SEMs. This package allows researchers to determine which specific sample points need to be removed for a particular path in the SEM model to change sign, thus assessing the robustness of the model. By iteratively removing data points and observing changes in model parameters, SEMsensitivity offers a detailed view of how individual observations influence the overall model, facilitating a deeper understanding of model stability.

The importance of this package lies in its ability to streamline and simplify the process of influence analysis for SEMs. Traditionally, such analyses are computationally intensive and challenging to perform, often requiring bespoke solutions that are not readily accessible to all researchers. SEMsensitivity integrates with popular R packages such as lavaan, dplyr, and semfindr, providing a user-friendly interface and leveraging existing computational tools to deliver efficient and accurate results.

By automating the detection of influential data points and providing clear, interpretable outputs, SEMsensitivity empowers researchers to make informed decisions about data dropping and model robustness. This capability is particularly crucial in fields where data integrity and

41 the reproducibility of results are under intense scrutiny. The package not only enhances the
42 methodological rigor of SEM analyses but also contributes to the broader effort of improving
43 transparency and reliability in scientific research.

44 In summary, SEMsensitivity is a vital tool for researchers conducting SEMs, offering a robust
45 framework for sensitivity analysis that is both accessible and computationally efficient. Its
46 development addresses a critical need in the current research landscape, providing a practical
47 solution to ensure the robustness and reliability of statistical models.

48 Method

49 The primary goal of SEMsensitivity is to provide robust methods for sensitivity analysis
50 in SEM. This package includes multiple methods to determine the influence of individual
51 data points on SEM paths and fit indices. Each method iteratively removes data points to
52 identify those that significantly affect the model's parameters. Among these methods, one
53 evaluates when a path coefficient changes its direction, such as from positive to negative.
54 Additionally, another method is designed to monitor the model's fit indices, such as when the
55 Comparative Fit Index (CFI) drops below a threshold like 0.9, indicating a decline in model
56 adequacy. These methods provide a comprehensive assessment of how data points influence
57 both model parameters and fit, making the package suitable for various scenarios and levels of
58 computational complexity.

59 Case Deletions and Approximations in Path Parameters

60 The core functionality of SEMsensitivity revolves around case deletions and approximations,
61 allowing researchers to assess the robustness of their SEM models by systematically removing
62 data points and observing the effects. Following the ideas presented in (Broderick et al., 2020),
63 we employ Taylor series approximations to efficiently compute influence scores. Thus, we
64 implemented various approaches to drop samples, listed in the table below.

Method	Description
Naive Method with Exact Influence	Remove a fixed percentage of samples (determined by the exact influence) at a time and refit the model to observe the change in the parameter of interest.
Naive Method with Approximate Influence	Remove a fixed percentage of samples (determined by the approximate influence, see (Broderick et al., 2020)) at a time and refit the model to observe the change in the parameter of interest.
Specified Approximation Method	Determines when a specific path in a SEM model changes sign by iteratively removing data points.
Simple Depth Method	Determines a specific path in a SEM model value changing by removing samples iteratively, in which influences are determined by naive method and outputs relevant results.
Combined Method	Determines a specific path in a SEM model value changing by removing samples iteratively, in which influences are determined by both naive method and approximate method.

Method	Description
Negamax Search Algorithm	Utilizes a Negamax search algorithm to iteratively drop data points and update the SEM.
Use Depth Method to Try to Switch Sign of Parameter	Uses a depth method to iteratively remove data points in order to switch the sign of a specific path in a SEM.
Use Depth Method to Try to Switch Sign of Parameter	Uses a depth method combined with a Negamax search algorithm to iteratively remove data points in order to switch the sign of a specific path in a SEM.
Simulated Annealing Method	Uses the simulated annealing method to identify a SEM model path value changing by removing samples iteratively.
Particle Swarm Optimization (PSO)	Uses the PSO method to identify a SEM model path value changing by removing samples iteratively.
Brute Search with Cut Method	To identify a SEM model path value changing by removing samples iteratively.

Case Deletions in Fit Indices

We use the `semfindr` package to identify data points that exert the most influence on model fit indices. By calculating the impact of individual cases, the package helps detect points that cause significant changes to indices like the CFI or RMSEA. Once the most influential points are identified, they can be deleted in bulk or individually. Bulk deletion allows for the removal of a specified number of cases at once, enabling quick evaluation of whether the model fit becomes inadequate (e.g., CFI dropping below 0.9). Alternatively, cases can be deleted one by one to monitor the incremental impact on fit and determine when the model fails to meet desired thresholds.

Availability

The R package `SEMsensitivity` is publicly available on [Github](#). It could be installed and run by using the following commands:

```
devtools::install_github("Feng-Ji-Lab/SEM-dropping/SEMsensitivity")
library(SEMsensitivity)
```

Example

We take the dataset `PoliticalDemocracy` provided in `lavaan` as an example. First, define a SEM and fit it with `lavaan`. Then, indicate the path of interest and the two variables of interest. Then, run the `SEMsensitivity` function and see the results. The possible method names are shown below:

- Naive Method with Exact Influence
- Naive Method with Approximate Influence
- Specified Approximation Method
- Simple Depth Method
- Combined Method
- Negamax Search Algorithm Function
- Use Depth Method to Try to Switch Sign of Parameter
- Use Depth Method to Try to Switch Sign of Parameter with Negamax

90 Below is a sample code.

91 First, install all needed packages and import dataset.

```
library(lavaan)
library(dplyr)
library(semfindr)
library(R.utils)
library(SEMsensitivity)
```

```
df <- PoliticalDemocracy
```

92 State the model (same as the model in lavaan package).

```
model <- '
  ind60 =~ x1 + x2 + x3
  dem60 =~ y1 + y2 + y3 + y4
  dem65 =~ y5 + y6 + y7 + y8
  dem60 ~ ind60
  dem65 ~ ind60 + dem60
  y1 ~~ y5
  y2 ~~ y4 + y6
  y3 ~~ y7
  y4 ~~ y8
  y6 ~~ y8
'
```

93 State the parameters and path of interest. Use the lavaan package to calculate the initial
94 path parameters and extract them.

```
var_one <- 'dem65'
var_two <- 'ind60'
PAR <- c("dem65~ind60")
threshold <- 10

fit <- sem(model, data = df)
summary(fit)

estimates <- parameterEstimates(fit)

conc <- data.frame(lhs = estimates$lhs, rhs = estimates$rhs, est = estimates$est)
int <- conc %>% filter(lhs == var_one & rhs == var_two)
par_value <- int$est

max_final <- ceiling(threshold * nrow(df) / 100)
N <- nrow(df)
```

```
signFactor <- ifelse(par_value >= 0, TRUE, FALSE)
```

95 Call the function SEMsensitivity to do sensitivity analysis.

```
result_by_name <- SEMsensitivity(df, model, var_one, var_two, PAR, threshold, fit,
  estimates, conc, int, par_value, max_final, N, signFactor,
  "Naive Method with Exact Influence")
summary(result_by_name)

result_by_index <- SEMsensitivity(df, model, var_one, var_two, PAR, threshold, fit,
  estimates, conc, int, par_value, max_final, N, signFactor, 1)
summary(result_by_index)
```

96 After running this, we can see the result as shown below. It shows the path of interest, original
97 value, changed parameter value and the dropped samples indices list.

98 Summary of SEM sensitivity analysis result:
99 Method Name: Naive exact method
100 Path: dem65~ind60
101 Original Value: 0.572336
102 Original Number of Samples: 75
103 Drop Points Percentage: 10
104 Dropped Number of Samples: 8
105 New Parameter Value: 0.076319
106 drop points list:
107 [1] 30 38 2 47 36 14 53 26

108 We also provide an example of fit indices changing from a good-fit model to an inadequate
109 model.

```
fit_result <- SEMsensitivity(df, model, fit = fit, max_final = max_final, N = N, measure = measure,
summary(fit_result)
```

110 The result is shown below:

111 Method Name: Use depth method to try to drop fit measure below threshold
112 Original Fit Value: 0.9954
113 Final Fit Value After Dropping Points: 0.8823
114 Number of Data Points Dropped: 19
115 Difference Between Original Fit and Threshold: 0.0954
116 Cumulative Drop in Fit Value: 0.0963
117 Dropped Points: 74, 41, 12, 69, 63, 45, 66, 36, 18, 56, 53, 2, 59, 53, 4, 12, 53, 16, 5

118 It provides the original fit value, and the changed fit value after dropping points, number of
119 points dropped, and a list of indices of dropped points list.

120 References

121 Broderick, T., Giordano, R., & Meager, R. (2020). An automatic finite-sample robust-
122 ness metric: When can dropping a little data make a big difference? *arXiv Preprint*
123 *arXiv:2011.14999*.