

1. 向量组 $\alpha_1, \alpha_2, \dots, \alpha_m (m \geq 2)$ 线性相关的充要条件是 ()

(A) $\alpha_1, \alpha_2, \dots, \alpha_m$ 中至少有两个向量成比例

(B) $\alpha_1, \alpha_2, \dots, \alpha_m$ 中至少有一个零向量

(C) $\alpha_1, \alpha_2, \dots, \alpha_m$ 中至少有一个向量可由其余向量线性表示

(D) $\alpha_1, \alpha_2, \dots, \alpha_m$ 中任一部分组线性相关

2. 设 $\alpha_1 = (1, 1, 1)$, $\alpha_2 = (a, 0, b)$, $\alpha_3 = (1, 3, 2)$ 线性相关, 则 a, b 满足_____

3. 设向量组 $\alpha_1, \alpha_2, \alpha_3$ 线性无关, $\beta_1 = \alpha_1 + \alpha_2, \beta_2 = \alpha_2 + \alpha_3, \beta_3 = \alpha_3 + \alpha_1$, 讨论向量组 $\beta_1, \beta_2, \beta_3$ 的相关性

思考题: λ 为何值时, 向量组

$$\alpha_1 = (1, 1, 1, 1, 2), \alpha_2 = (2, 1, 3, 2, 3), \alpha_3 = (2, 3, 2, 2, 5), \alpha_4 = (1, 3, -1, 1, \lambda)$$

线性相关