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Basics (and advanced stuff) of questionnaire development and analysis

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Incredible what is possible with latent variable models

Motivation

Combining research goal, design, and analysis

		Research Goal				
		Description	Prediction	Causation		
'n	Cross-sectional	E.g. proportion or correlation, PCA				
Research Design	Longitudinal	E.g., latent growth curve modeling	E.g., forecasting, cross-validation	ক		
Re	Experimental	E.g., differences between existing groups	E.g., including a covariate	E.g., comparing means across conditions		

Adapted from Hamaker, Mulder and Van IJzendoorn (under review, DCN).

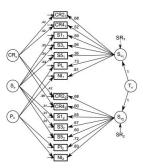


Educational research and experimental psychology: mutual research interests

Motivation

Which cognitive processes underlie differences in cognitive abilities?

Prof. Anna-Lena Schubert (Heidelberg) and others: estimating person parameters by means of cognitive models (e.g. drift-diffusion models) and subsequently applying latent variable models (e.g. latent state-trait models):



Schubert et al. (2016): Frischkorn und Schubert (2018)



Data generation process

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statistical models

common factor models item response models Data generation process: "When [...] data set has been created, a good model has to be constructed for the data generation process (DGP). This is the stage at which the actual [...] analysis begins... When an [...] model has been constructed for the DGP, it should only be used for the analysis if it reflects the ongoings in the system of interest properly" - Lütkepohl und Krätzig (2004), pp. 1-7

- \rightarrow a model should make a parsimonious, plausible and substantially meaningful contribution to the data generation process $_{\rm Hoyle~(2012),~p.~126}$
- ightarrow in statistics, we assume that we can represent the DGP by discrete and continuous distributions

Literatur



Distributions I

DGP

a random variable is defined by assigning numbers to an event of a random process (realisation), for this purpose distributions are necessary:

- Random processes can only be described by functional relations f(X), types of representation:
 - ullet for discrete random variables o probability function
 - ullet for continuous random variables o density function
- → distributions are determined by functions and their parameters

A random variable f(X) is a function that assigns a real number to each possible outcome of a random experiment / process.

furter information see: Wikipedia random variables; Fahrmeir et al. (2016); Zucchini et al. (2009)



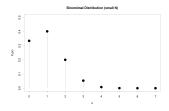
Distributions II: example

DGP

Random variables can only take on finitely many values or countably infinitely many values

 \rightarrow each possible event can be assigned a natural number

Example: rolling 6 or 30 fair dices several times at once and we want to know $A = \{\text{result is } 1\} = \{1\} \rightarrow P(\{1\}) = 1/6 \text{ (binomial distributed)}:$



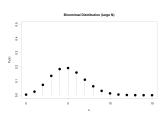


Abbildung: left rolling 6 cubes, right 30 cubes

Is rolling a dice a Gauss distribution?



Distributions III: example 2

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analysis plans exploratory mode common factor models item response models single items can be binomial distributed (! however the real distribution is never known)

Imagine that participants should answer the following two items on a 6 point Likert Scale:

- Should something be done about climate change for future generations?
- Would you be willing to accept personal restrictions for the fight against climate change?

Strongly Disagree	Disagree	Slightly Disagree	Slightly Agree	Agree	Strongly Agree
1	2	3	4	5	6
50% Negative			50% Positive		

 \rightarrow What would you expect?



Take-Home-Message

DGP

• individual items of a Likert scale result from a binomially distributed process $(Y_1 \sim Bin(n, p), ...)$

- → we want to achieve a high variance in the items (all response options are used)
- → variance or covariance (if multiple items) is the most important building block for the statistical models
- → the answering of items should be independent from other people or the ordering of the items
- our statistical models should reflect the ongoings in the system of interest properly / sufficiently and should be theoretically derived

Remember that all models are wrong; the practical question is how wrong do they have to be to not be useful

George Box (1987)

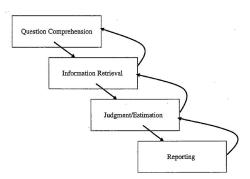


(superficial) model: Cognitive Aspects of Survey Methodology

CASM

also called "Optimizing-Satisficing-Model"

the CASM model tries to explain how people finally arrive at a response:



→ great template for identifying possible sources of error

Tourangeau und Bradburn (2010); Moosbrugger und Kelava (2012), pp. 57-59



test model: linking observable variables to unobservable variables

test model

whatever the exact processes of question answering are (black box), fundamentally we assume that the answer / reporting depends on a score on a latent variable:



 \rightarrow the central task of test theory is to determine the relationship between test behaviour and the (psychological) characteristic to be assessed

Hambleton und R. Jones (1993); Rost (2004)

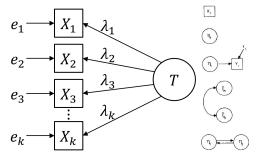


What is a Latent Variable?: depiction

Latent Variables

dev.





rectangular or square box signifies an observed or manifest variable

circle or ellipse signifies an unobserved or latent variable

unenclosed variable signifies a disturbance term (error in either equation or measurement) straight arrow signifies assumption that variable at base of arrow "causes" variable at head of arrow

curved two-headed arrow signifies unanalyzed association between two variables

two straight single-headed arrows connecting two variables signifies feedback relation or reciprocal causation

Abbildung: congeneric measurment model

Abbildung: primary symbols used in path analysis

other possible modes of representation: Matrix notation, system of equations

Bollen (1989); Hoyle (2012)



What is a Latent Variable?: technical aspects

technical aspects:

- definition: Latent variables are random variables whose realized values are hidden
 - → models which are dealing with latent variables are called Latent Variable Models (this kind of models can be used for descriptive analysis, predictive, inferential or causal questions, What is the question?)

An possible operationalisation of a latent variable is a linear measurement model with the equation $Y = \lambda * \eta + \epsilon$.

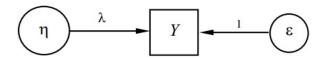


Abbildung: simple linear measurement model - Macho (2016), p. 92

this corresponds to the fundamental equation of Classical Test Theory:

$$Y = T + \epsilon$$

Latent Variables

Bartholomew (2013): Skrondal und Rabe-Hesketh (2007)



What is a Latent Variable?: theoretical aspects

Latent Variables

great dissertation: Schurig (2017): "Latente Variablenmodelle in der empirischen Bildungsforschung - Die Schärfe und Struktur der Schatten an der Wand"

theoretical aspects:

- the theoretical status of latent variables has not been clarified
 - → regarded this variables as representations of real entities or as useful inventions?
 - → Advantage: use of latent variables allow more generalisable reasoning than manifest variables
- latent variables need a substantive scientific foundation, whereby the bridging problem between observed and latent variable must be solved by theoretical assumptions and statistical modelling
- \rightarrow even more surprising the statistical models "get rid" of the latent variable by assuming local independence: $Pr(y_i \mid \eta_i) = \prod_{i=1}^n Pr(y_{ii} \mid \eta_i)$

Schurig (2017): Skrondal und Rabe-Hesketh (2007)



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- we assume that some kind of undefined latent variable "causes" the test behaviour
 - $\rightarrow\,$ since the exact mechanisms are unclear, I would never speak of causality
- each measurement consists of a true value (latent variable) and an error (unique variance)
- in the context of questionnaire development, the central aim is to reproduce the correlation structure between items with a statistical model

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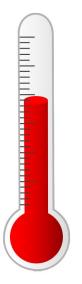


What is measurement?

measurement

How do you measure temperature?

- By looking at a thermometer
- For this to make sense, we need to assume that:
 - ► Temperature causes the level shown in a thermometer
 - The thermometer features. relatively little measurement error





What is measurement? II

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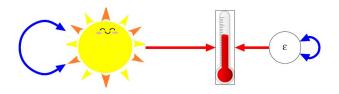
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We can summarize a causal hypothesis in a path diagram:



- Circular nodes (or suns): latent (unobserved) variables
- ► Square nodes: observed variables
 - Also termed indicators of a latent variable
- ▶ Unidirectional links: causal effects
- ► Bidirectional links: (co)variances



our assumptions lead to a path diagram

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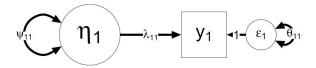
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Assume all observed and latent variables are normally distributed and all causal effects are linear. Without loss of information, we can center data and assume all means are 0 (we don't use means until week 3). Now, the path diagram encodes a causal equation:



$$y_{i1} = \lambda_{11}\eta_{i1} + \varepsilon_{i1}$$
$$\eta_1 \sim N(0, \sqrt{\psi_{11}})$$

$$\varepsilon_1 \sim N(0, \sqrt{\theta_{11}})$$

 λ_{11} is called a factor loading, ε_{i1} the residual variance and ψ_{11} the factor variance.

 \rightarrow remark: reliability is defined as:

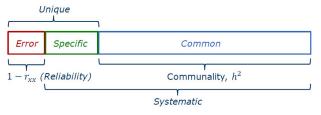
$$\frac{\lambda_{11}^2 \psi_{11}}{\lambda_{11}^2 \psi_{11} + \theta_{11}}$$



Variance splitting

measurement

Within the framework of factor-analytical models (common factor model), the variance of indicators is divided into common and unique variance.



The variance shared between the indicators is the commonality; the remaining variance is the unique variance, which is divided into indicator-specific method variance (specific) and measurement error variance (error).

Kline (2015), p. 190



Take-Home-Message

measurement

• each measurement consists of a true value (latent variable) and an error (unique variance), which is divided in error and specific variance

- → the specific variance can be taken into account via so-called multitrait-multimethod models
- → the acceptable size of the measurement error depends on the consequences of a wrong decision (no statement is possible at the individual level! - Schmidt-Atzert und Amelang (2018), pp. 36-62)
- in the context of questionnaire development, the central aim is to reproduce the correlation structure between items with a statistical model → precondition of communality: high (but not too high) linear correlations between the items



quality criteria

test theory

concrete measurement, than test administration should be carried out taking into account three central quality criteria of tests, which build on each other (no reliable measurement possible without objectivity, etc.):

objectivity \rightarrow reliability \rightarrow validity

Recommendation for reading: Rost (2004); Schmidt-Atzert und Amelang (2018); Moosbrugger und

Kelava (2012); Moosbrugger und Kelava (2020)

great article: Glaesmer et al. (2015): "Kriterienkatalog zur Beurteilung psychodiagnostischer Selbstbeurteilungsinstrumente-Empfehlung des Deutschen Kollegiums für Psychosomatische Medizin (DKPM)" overview of test theoretical terms in German: TU Dresden wissenschaftliches Arbeiten



Quality criterion: objectivity

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common factor models item response models latent class analysis • **objectivity:** Test score is objective if it is independent of any influences outside the tested person (e.g. situational conditions, experimenter - all exogenous variables¹)

- Implementation objectivity (*Durchführungsobjektivität*): standardisation of implementation conditions (writing a test manual, training test leader, standardisation of all other conditions).
- Objectivity of evaluation (Auswertungsobjektivität): the interpretation of the test result is not dependent on the person who evaluates the test (measurable by interrater reliability, such as Kendall's coefficient of concordance).
- Objectivity of interpretation (Interpretationsobjektivität): different test users come to the same conclusions with identical test scores.

¹variables whose covariance structure is not explained by the statistical model, this includes error terms, unobserved influencing variables and exogenous latent constructs (Macho 2016, pp. 62-63)



Quality criterion: reliability

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- reliability: the extent to which a test measures what it measures. The focus here is on measurement accuracy. Reliability is shown theoretically by the fact that repeated measurements under the same conditions produce the same measurement results (the central contribution to the development of reliability measurement is made by the classical test theory, which establishes a theory of measurement error²).
 - Reliability can be estimated by different methods, often internal consistency - Cronbach's Alpha (measure of how items in a scale correlate with one another) is estimated

²The classical test theory assumes that the test performance of a person on the question i is composed of $x_i = \tau_i + \epsilon_i$. Here τ_i corresponds to the person's true score on question i, which is composed of an item response x_i and the error ϵ_i , where the error is unbiased (Moosbrugger und Kelava 2012, pp. 104-105)



Quality criterion: validity

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models latent class anal • validity: A test is considered valid if it actually measures the characteristic it is supposed to measure and not some other characteristic. The measurement of validity is done in two steps:

- (1) via structure-searching (such as exploratory factor analysis) and structure-testing (such as confirmatory factor analysis) procedures, construct validity is determined (see in detail e.g. Messick 1994). This indicates the extent to which conclusions can be drawn from test results for example about psychological personality traits.
- (2) the agreement of the results of the individual constructs should be high with constructs that measure the same or similar characteristics (convergent validity) and the agreement with results from constructs that measure other characteristics should be low (discriminant validity). This can be analysed via correlations

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validation: an argument of accumulating evidence

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argument-based approach to validation: To validate an interpretation or use of measurements is to evaluate the rationale, or argument, for the proposed conclusions and decisions ... Ultimately, the need for validation derives from the scientific and social requirement that public claims and decisions be justified

- interpretive argument: specifies the proposed interpretations and uses of assessment results by laying out a network of inferences and assumptions leading from the observed performances to the conclusions and decisions based on the assessment scores
- validity argument: provides an evaluation of the interpretive argument's coherence and the plausibility of its inferences and assumptions

Kane (2012); Markus und Borsboom (2013)



further quality criteria of scales / single indicators I

A variety of further quality criteria of indicators were developed by the "Key National Indicators Initiative" (2005):

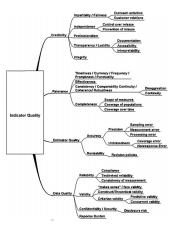


Abbildung: Quality criteria of indicators according to the "Key National Indicators Initiative"; Source: Groves und Lyberg 2010, 856

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further quality criteria of scales / single indicators II

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models item response models → "Key National Indicators Initiative" borrowing from the concept of total survey error (total survey error), which provides a conceptual framework to describe possible sources of survey error (see Groves und Lyberg 2010; for introduction see Faulbaum 2014). Further issues of indicator quality (keyword test economy, usefulness, reasonableness, standards,..) in overview books on test theories (e.g.Moosbrugger und Kelava 2012)

terature 26/5:



Take-Home-Message

it is not trivial to generate items, visible in the concept of generalisability of tests: For the scaling of tests there are theoretically (in)finitely many plausible statistical models and question possibilities (e.g. G. Fischer und Molenaar 1995, pp. 6-7; Robitzsch et al. 2011; Shadish, Cook und Campbell 2002):

$$Var(\hat{d})_{\mathsf{Total}} = Var(\hat{d})_{\mathsf{Persons}} + Var(\hat{d})_{\mathsf{Items}} + Var(\hat{d})_{\mathsf{Models}} + Var(\hat{d})_{\mathsf{Occasions}}$$

Sources of variability of results:

- persons
- selected items (there is a potential universe of possible items for the guery of individual knowledge areas)
- statistical models
- time point of measurement

Generalisability

see: Generalizability Theory: Overview



guidelines questionnaire development

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The following considerations are based on guidelines for questionnaire development, especially Rattray und M. C. Jones 2005; Artino et al. 2014; Boateng et al. **2018**

There are three phases to creating a rigorous scale-item development, scale development, and scale evaluation:

- item development
- scale development
- scale evaluation



item development

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Identification of domain and item generation 2 Content validity

aims:

- To specify the boundaries of the domain and facilitate item generation
- To identify appropriate questions that fit the identified domain
- To evaluate each of the items regarding content relevance, representativeness, and technical quality by experts and target population



Major modes of searching

different modes should be used concurrently and used search strategies should be made explicit

Footnote Chasing

Cooper 1985

References in review papers written by others References in books by others

References in nonreview papers from journals you subscribe to

References in nonreview papers you browsed through

at the library Topical bibliographies compiled by others

Mann 1993

Searches through published bibliographies (including sets of footnotes in relevant subject documents)

Related Records searches

Consultation

Cooper 1985

Communication with people who typically share information with you

Informal conversations at conferences or with students Formal requests of scholars you knew were active in the field (e.g., solicitation letters)

Comments from readers/reviewers of past work General requests to government agencies

Mann 1993

Searches through people sources (whether by verbal contact, E-mail, electronic bulletin board, letters, etc.)

Searches in Subject Indexes

Cooper 1985

Computer search of abstract data bases (e.g., ERIC, Psychological Abstracts)

Manual search of abstract data bases

Mann 1993

Controlled-vocabulary searches in manual or printed sources

Key word searches in manual or printed sources Computer searches-which can be done by subject

heading, classification number, key word. . .

Browsing

Cooper 1985

Browsing through library shelves

Mann 1993

Systematic browsing

Citation Searches

Cooper 1985

Manual search of a citation index

Computer search of a citation index (e.g., SSCI) Mann 1993

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Citation searches in printed sources Computer searches by citation

Cooper, Hedges und Valentine (2009), 58ff.

domain identification



main concern of literature retrieval

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return all of the studies relevant to the review ('recall') without retrieving irrelevant studies ('precision')

Recall:

- expresses (as a percentage) the ratio of relevant documents retrieved to all those in a collection that should be retrieved
- fiction: if we could identify all existing relevant documents in order to count them, we could retrieve them all, and so recall would always be 100 percent

Precision:

- expresses (as a percentage) the ratio of documents retrieved and judged relevant to all those actually retrieved
- measures how many irrelevant documents-false positives-one must go through to find the true positives or hits
- → trade-off: high recall leads to degrading precision



define single items

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common factor models item response models Possible process of item $\ / \$ indicator development proceeds in three steps:

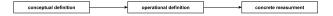


Abbildung: inspired by Planty 2010, pp . 20-38

- **conceptual definition:** describes in the abstract the qualities and concepts that the indicator will purport to describe
- operational definition: developing a concrete, operational (or working) definition for the indicator and identifying the precise measures that will be used to represent the concept described in the conceptual definition
- **concrete measurment:** deciding how the operational concept should be measured (definition of a question)

Planty (2010)



item generation: deductive, inductive, external method

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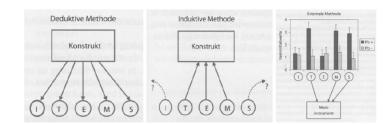


Abbildung: see Schmidt-Atzert und Amelang 2018, p. 111

Schmidt-Atzert und Amelang (2018), pp. 97-112



deductive method: Which items are relevant? CIPO

item generation

Possible process of indicator development proceeds in three steps:

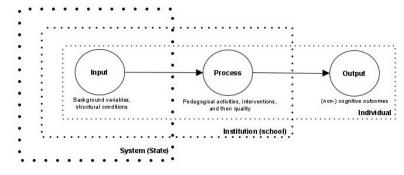


Abbildung: adjusted "CIPO" model

Adjustment according to: N. Fischer et al. (2011); Klieme und Vieluf (2013); Tippelt und Schmidt-Hertha (2018)

Recommendation for reading: Keller (2014); Ditton (2000); primary source: Stufflebeam (1971)



Which items are relevant? CIPO II [german]

item generation

Komponenten	Schüler	Schule	Staat
Input	Alter, Geschlecht, Migra- tionshintergrund; Vorwis- sen; Einstellungen	soziales Einzuggebiet; Ressourcen; Schulform	Demographie, gesell- schaftliche Debatten; Investitionen
Prozess	Lerntempo, Motivation	organisatorische Gestal- tung; Elternkooperation; Lehrerkooperation	Regulierungsinstrumente, wie Maß der Schulautono- mie; Standardsetzung
Output	Lernergebnisse	Anzahl Abbrecher auf Schulebene; durchschnitt- liche Schulleistung; Schulklima	Bildungsstand, Wirt- schaftswachstum, Wohl- stand der Gesellschaft

Tabelle: Einzelne Komponenten des "CIPO"-Modells in Bezug zu den Akteursebenen

Variablen entnommen aus: Klieme und Vieluf (2013), 234; Tippelt und Schmidt-Hertha (2018), 383

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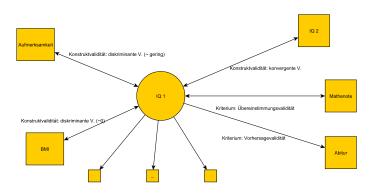
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Why do we need to collect so many items and additional variables? [partly german]

Definition **construct validity**: indicates the extent to which a test or survey procedure measures a characteristic of interest in a way that is consistent with existing construct definitions and theories



see also: blog post

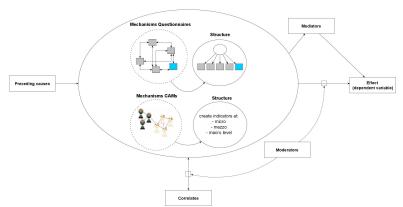
e.g. Moosbrugger und Kelava (2020); Cronbach und Meehl (1955)



construct validity: gradually becoming more complex

confronted by a complex system, we need to "complicate ourselves" and bring together knowledge from different disciplines

Complex System



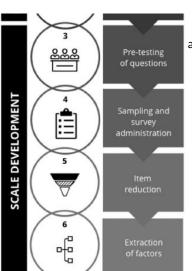
chapter 7 in Jaccard und Jacoby (2020)

item generation



scale development

scale development



aims:

- assess the extent to which questions reflect the domain of interest
- collect data with minimum measurement errors and to ensure the availability of sufficient data
- determine the optimal number of factors or domains that fit a set of items
- → Removal of individual items by means of statistical models



Cognitive interviews

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common factor models item response models latent class analys Cognitive interviews are a qualitative method that examines the question-answer process of the test subjects

- \rightarrow test the comprehensibility of questions and possible difficulty in answering them. Theoretically, cognitive interviews are based on a heuristic question-answer model (see slide 9). This consists of four stages:
 - Understanding the question, this requires the respondent to syntactically relate words and grammar and semantically decode their meaning content
 - recalling information requires recalling information from long-term memory to working memory
 - evaluation and assessment of a question can be made directly in the case of an already reflected topic or only an impression can be given
 - when giving an answer, the assessment made must be reflected in the appropriate answer format of the questionnaire



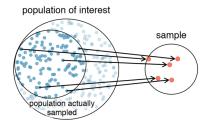
data collection: random sample

sampling

• simple random sample: random selection of statistical units: each object has the same probability of being included in the sample.

Advantage: systematic errors are avoided; can be representative

Example of an biased random sample - Causes e.g. non-response bias, incomplete frame population:



Graphics taken from: OpenIntro Statistics (Diez et al 2019)



data collection: framework

Motivation

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Latent Variable

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Population from which one draws the sample determines the universality of the results and conclusions !



- \rightarrow graph can be rewritten as $T \subseteq F \subseteq R \subseteq S$
 - presence of non-responses (non-response): $S \subset R$
 - List of statistical objects to be drawn (frame population) not fully covering population to be selected (target population): $F \subset T$

Leeuw, Hox und Dillman (2012), 318ff.



scale evaluation

scale evaluation

EVALUATION SCALE

aims:

- testing if latent constructs are as hypothesized (see construct validity slide 36)
- establishing if responses are consistent / reliable (when repeated)
- ensuring you measure the latent dimension you intended (see validation as a process 24)



reliability: recommendation

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exploratory mod common factor models item response models When interpreting Cronbach's alpha, it should be noted that this measure represents a "lower bound to the reliability", as well as "persistently and incorrectly taken to be a measure of the internal structure of the test, and hence as evidence that the items in the test "measure the same thing. "However, alpha does not provide the researcher with this sort of information". (Sijtsma 2009, 107; see also Macho 2016, 87). In the article, Sijtsma (2009) shows that it is necessary to explicitly check the dimensionality of items representing an assumed construct and to test whether a τ -equivalent measurement model exists for the items. The reasons for this are that Cronbach's alpha is neither a measure of internal consistency (correlation of items) nor a measure of unidimensionality (also called homogeneity under the assumption of a general factor) (Sijtsma 2009; Revelle und Zinbarg 2009). In addition, the items should be tested for normal distribution according to Trizano-Hermosilla and Alvarado (2016), since non-normally distributed items lead to a negative bias in Cronbach's alpha regardless of the sample size (Trizano-Hermosilla und Alvarado 2016). Overall, instead of Cronbach's alpha, it is suggested to use other measures such as the "greatest lower bound" (glb) or McDonald's ω_t (see e.g. Siitsma 2009: Revelle und Zinbarg 2009). However, the use of the "correct" reliability measure depends on the data basis (Revelle und Zinbarg 2009; Trizano-Hermosilla und Alvarado 2016).



Latent Variable Models

definition latent variable model: a statistical model that relates a set of observable variables (so-called manifest variables) to a set of latent variables

Traditional latent variable models

Observed variable(s)	Latent variable(s)		
	Continuous	Categorical	
Continuous	Common factor model Structural equation model Linear mixed model Covariate measurement error model	Latent profile model	
Categorical	Latent trait model/IRT	Latent class model	

 \rightarrow we assume that the responses on the indicators or manifest variables are the result of an individual's position on the latent variable(s), and that the manifest variables have nothing in common after controlling for the latent variable (local independence)

Skrondal und Rabe-Hesketh (2007): Skrondal und Rabe-Hesketh (2004)

statistical models



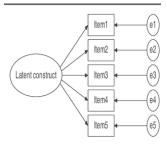
Latent Variable Models II: local independence

statistical models

local independence: latent variable explains why the observed items are related to one another (see example in Wikipedia)

reflective measurement model:

Reflective measurement model



 \rightarrow even more surprising the statistical models "get rid" of the latent variable by assuming local independence: $Pr(y_i \mid \eta_i) = \prod_{i=1}^n Pr(y_{ii} \mid \eta_i)$

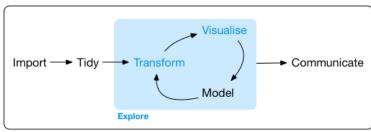
Urbach, Ahlemann et al. (2010)



Data Science Pipeline

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analysis plans



Program

→ collaborate with others: recommendations for data sharing

R for Data Science

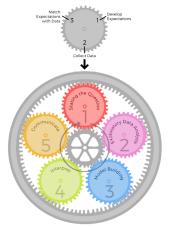
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analysis plans

analysis plans

A data analysis plan is "a detailed document outlining procedures for conducting an analysis on data"



Epicycles of Analysis



overview: exploratory models

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item response models compared to structure-testing (such as confirmatory factor analysis, CFA) procedures, structure-searching (such as exploratory factor analysis, EFA) not assume any a-priori hypothesis, but the boundaries between the approaches are becoming increasingly blurred:

- mathematically, a one-dimensional CFA is identical to an EFA
- there are hybrids between these two procedures, so called Exploratory Structural Equation Modeling (Marsh et al. 2014)
- \rightarrow grouping is based on patterns of variation (correlation)

variable-centred vs. person-centred:

In addition to methods that summarise correlation between variables, it is also useful to identify subgroups in data to test the robustness of the statistical models using for example *Latent class and latent transition analysis* (Collins und Lanza 2010) or *cluster analysis* (Hastie, Tibshirani und Friedman 2009; Kassambara 2017); innovative idea is for example the https://github.com/m-Py/anticlust

ightarrow grouping is based on the distance (proximity)



overview: confirmatory factor analysis (CFA)

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Reflective measurement model Description Formative measurement model Epistemic Item1 relationship Item1 Item2 Item2 Latent construct ▶ Item3 Latent construct Item3 Item4 Item4 Item5 Criteria Flow from measures to latent construct (1) Direction Flow from latent construct to measures of causality Measures define latent construct Construct defines measures Measures should not be Measures should be interchangeably Interchangeinterchangeably ability of the measures Measures need not to have the similar Measures should have the similar content or common theme content or common theme Dropping measures should not change Dropping measures should not change the conceptual meaning of the latent the conceptual meaning of the latent construct construct (3) Not necessary for measures to correlate Measures are expected to correlate Correlation with each other with each other among the measures (4) Nomological net of the measures may Nomological net of the measures Nomological differ should not differ Network

Source: Urbach and Ahlemann (2010)



fundamental principle of confirmatory factor analysis

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item response models The central aim of this procedures is to find parameters for the implied covariance matrix of the model $\Sigma(\theta)$ that most closely match the observed data Σ

$$\Sigma = \Sigma(\theta)$$

Deviation of the covariance matrices is the error

General structure of CFA models

$$Y = \Lambda \eta + \varepsilon$$

$$\begin{bmatrix} Y_1 \\ Y_2 \\ \vdots \\ Y_m \end{bmatrix} = \begin{bmatrix} \lambda_{11} \ \lambda_{12} \ \cdots \ \lambda_{1K} \\ \lambda_{21} \ \lambda_{22} \ \cdots \ \lambda_{2K} \\ \vdots \ \vdots \ \ddots \ \vdots \\ \lambda_{m1} \ \lambda_{m2} \ \cdots \ \lambda_{mK} \end{bmatrix} \cdot \begin{bmatrix} \eta_1 \\ \vdots \\ \eta_K \end{bmatrix} + \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_m \end{bmatrix}$$

Model-implied variance-covariance matrix

$$\Sigma(\theta) = \Lambda \Psi \Lambda' + \Theta_{\varepsilon}$$



overview: item response theory (IRT)

central idea of the IRT: The probability of an item response is determinable by the person ability / attitudes / ... on the measured latent trait, as well as one or more parameters describing the items (G. Fischer und Molenaar 1995, p. 4)

In general, there are three possible applications:

- taxonomy of binary item response models (e.g. Rasch Model, also called One Parameter Logistic Model)
- taxonomy of polytomous item response models (e.g. Graded Response Model) G. Fischer und Molenaar 1995
- "explanatory" item response models (for example to detect ordering effects or differential item functioning, …) - De Boeck und Wilson 2004

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overview: latent class analysis (LCA)

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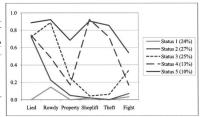
latent class analysis

central idea of LCA: to detect latent (or unobserved) heterogeneity in samples

Table 1.3 Four-Latent-Class Model of Past-Year Delinquency (Add Health Public-Use Data, Wave I; N = 2,087)

	Latent Class				
Assigned label	Non-/Mild Delinquents .49	Verbal Antagonists	3 Shoplifters	General Delinquents	
Probability of membership					
Conditional probability of a Yes' response Lied to parents Publicly loud/rowdy/unruly Damaged property Stolen something from store Stolen something worth < \$50 Taken part in group fight	.33 .20 .01 .03 .00	.81 ⁺ .82 .25 .02 .03 .31	.78 .62 .25 .92 .73 .24	.89 1.00 .89 .88 .88	

Conditional probabilities > .5 in bold to facilitate interpretation.



Collins und Lanza (2010)



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