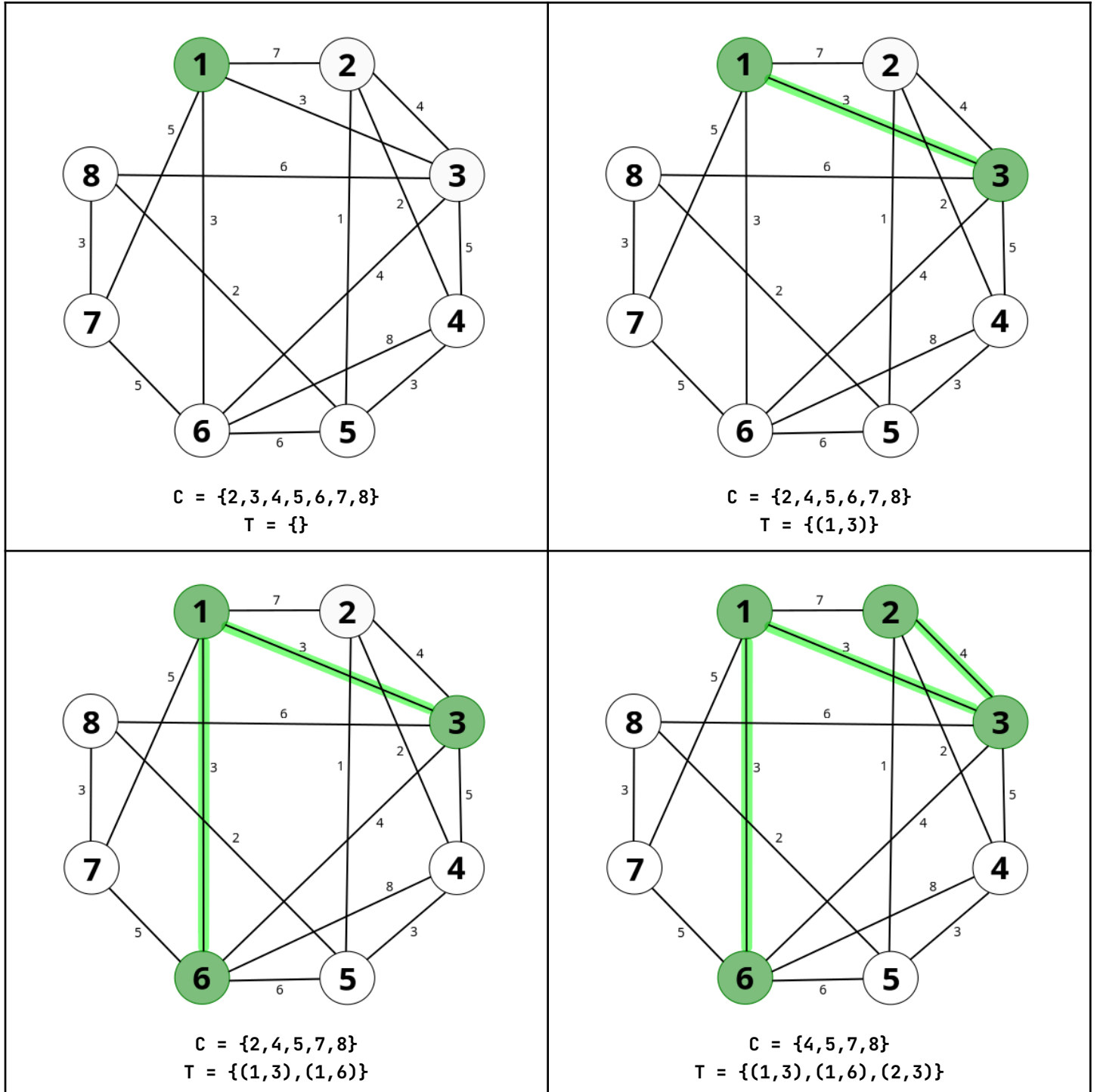
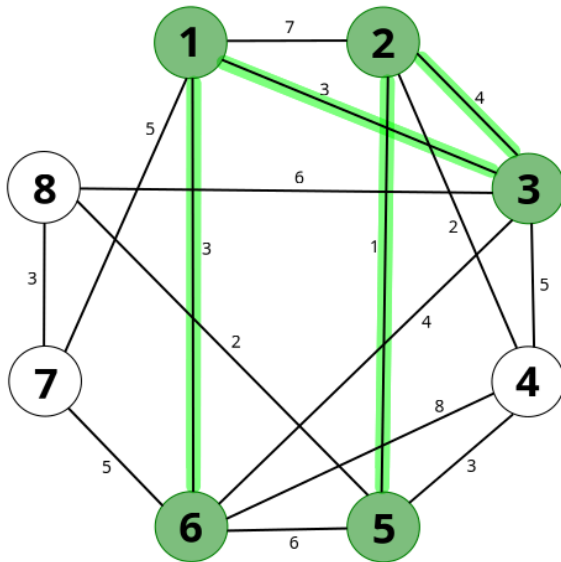


1. Ejecutar paso a paso, graficando las soluciones parciales, el algoritmo de Prim que computa el *árbol generador mínimo* sobre los grafos con nodos  $\{1, 2, \dots, 8\}$  y costos dados por una función  $w$ :

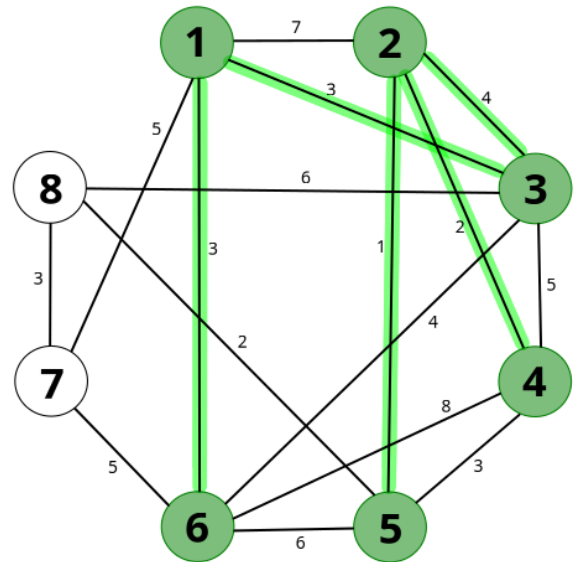
(a)

$$\begin{array}{llll} w((1, 2)) = 7 & w((2, 3)) = 4 & w((3, 6)) = 4 & w((5, 6)) = 6 \\ w((1, 6)) = 3 & w((2, 4)) = 2 & w((3, 8)) = 6 & w((6, 7)) = 5 \\ w((1, 7)) = 5 & w((2, 5)) = 1 & w((4, 6)) = 8 & w((8, 5)) = 2 \\ w((1, 3)) = 3 & w((3, 4)) = 5 & w((5, 4)) = 3 & w((8, 7)) = 3 \end{array}$$

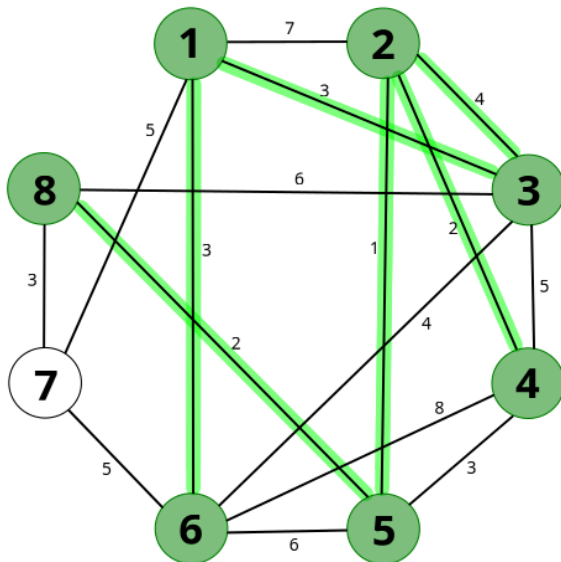




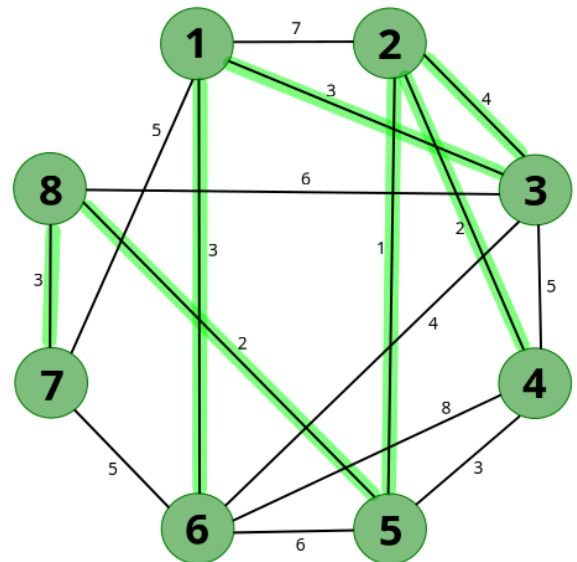
$C = \{4, 7, 8\}$   
 $T = \{(1, 3), (1, 6), (2, 3), (2, 5)\}$



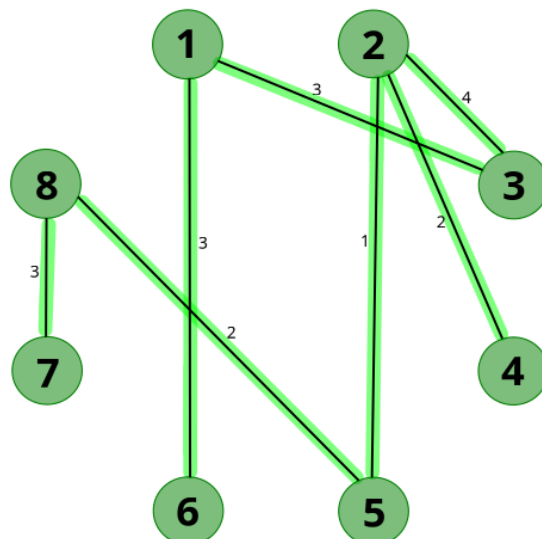
$C = \{7, 8\}$   
 $T = \{(1, 3), (1, 6), (2, 3), (2, 5), (2, 4)\}$



$C = \{7\}$   
 $T = \{(1, 3), (1, 6), (2, 3), (2, 5), (2, 4), (8, 5)\}$



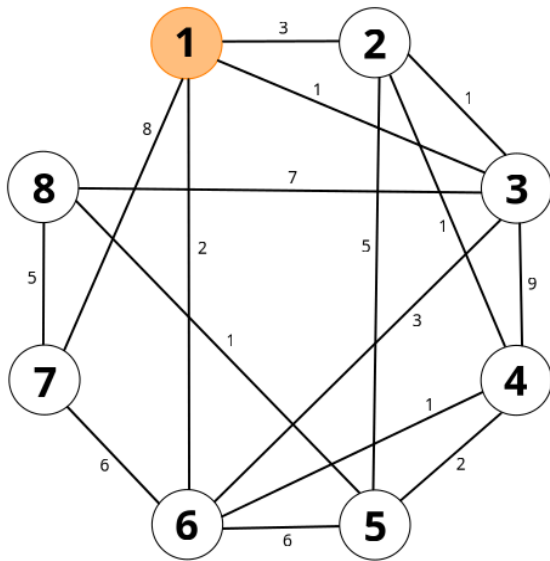
$C = \{\}$   
 $T = \{(1, 3), (1, 6), (2, 3), (2, 5), (2, 4), (8, 5), (8, 7)\}$



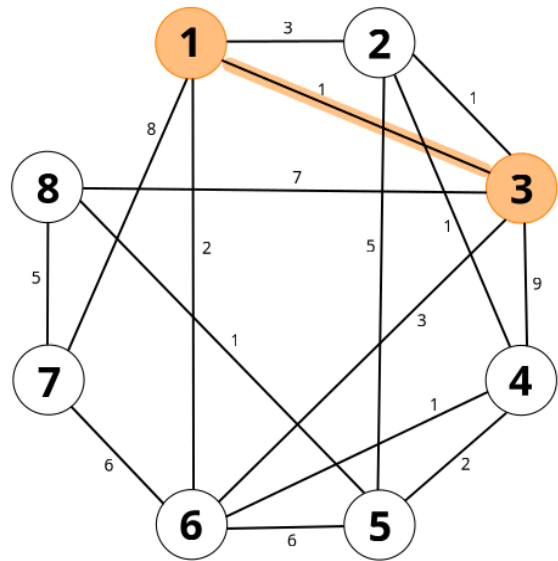
$$\text{Peso} = (1, 3) + (1, 6) + (2, 3) + (2, 5) + (2, 4) + (8, 5) + (8, 7) = 3 + 3 + 4 + 1 + 2 + 2 + 3 = 18$$

(b)

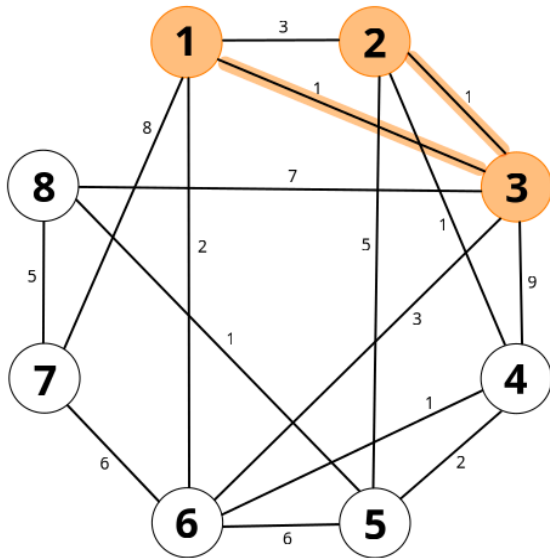
$$\begin{array}{llll}
 w((1,2)) = 3 & w((2,3)) = 1 & w((3,6)) = 3 & w((5,6)) = 6 \\
 w((1,6)) = 2 & w((2,4)) = 1 & w((3,8)) = 7 & w((6,7)) = 6 \\
 w((1,7)) = 8 & w((2,5)) = 5 & w((4,6)) = 1 & w((8,5)) = 1 \\
 w((1,3)) = 1 & w((3,4)) = 9 & w((5,4)) = 2 & w((8,7)) = 5
 \end{array}$$



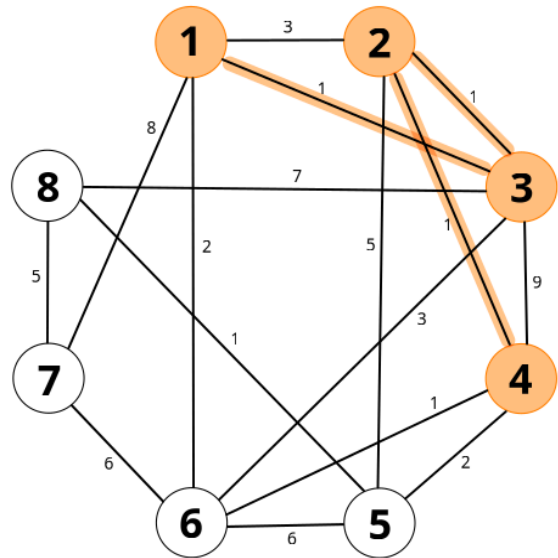
$$\begin{array}{l}
 C = \{2,3,4,5,6,7,8\} \\
 T = \{\}
 \end{array}$$



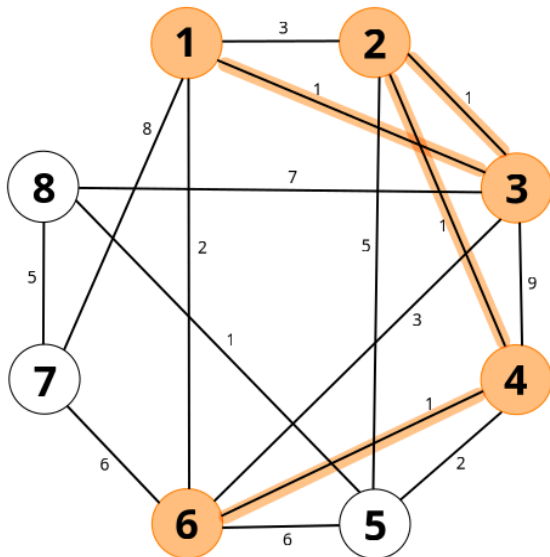
$$\begin{array}{l}
 C = \{2,4,5,6,7,8\} \\
 T = \{(1,3)\}
 \end{array}$$



$$\begin{array}{l}
 C = \{4,5,6,7,8\} \\
 T = \{(1,3), (2,3)\}
 \end{array}$$

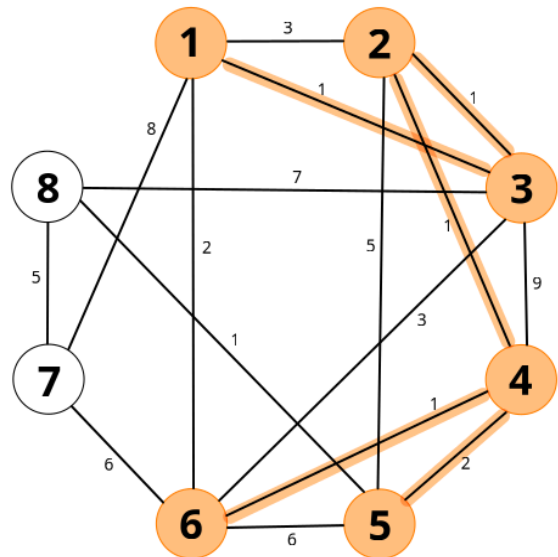


$$\begin{array}{l}
 C = \{5,6,7,8\} \\
 T = \{(1,3), (2,3), (2,4)\}
 \end{array}$$



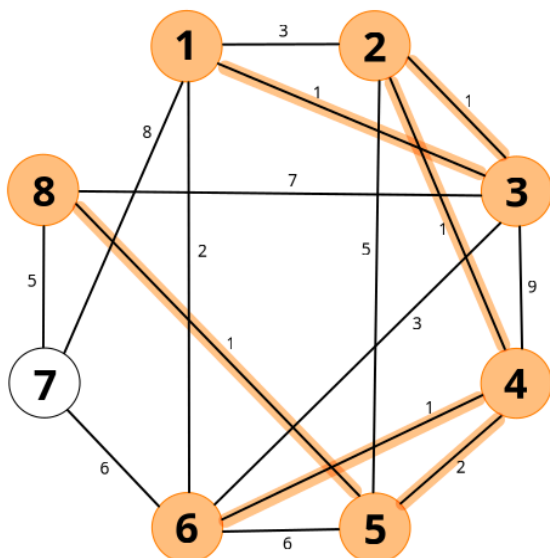
$$C = \{5, 7, 8\}$$

$$T = \{(1, 3), (2, 3), (2, 4), (4, 6)\}$$



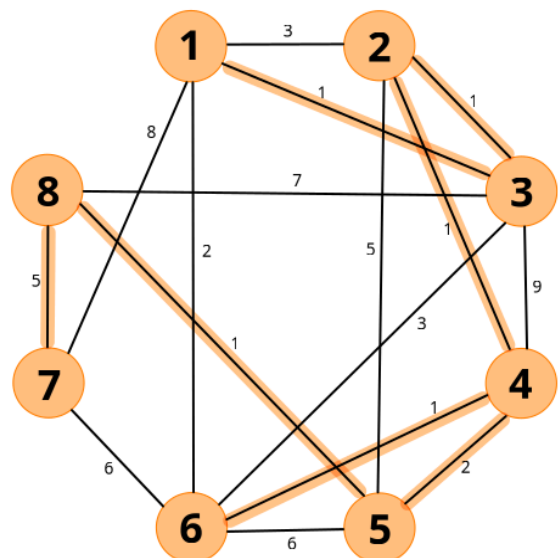
$$C = \{7, 8\}$$

$$T = \{(1, 3), (2, 3), (2, 4), (4, 6), (5, 4)\}$$



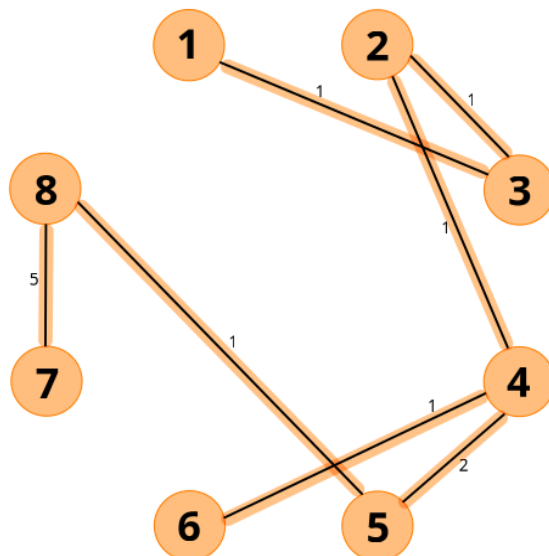
$$C = \{7\}$$

$$T = \{(1, 3), (2, 3), (2, 4), (4, 6), (5, 4), (8, 5)\}$$



$$C = \{\}$$

$$T = \{(1, 3), (2, 3), (2, 4), (4, 6), (5, 4), (8, 5), (8, 7)\}$$



$$\text{Peso} = (1, 3) + (2, 3) + (2, 4) + (4, 6) + (5, 4) + (8, 5) + (8, 7) = 1 + 1 + 1 + 1 + 2 + 1 + 5 = 12$$