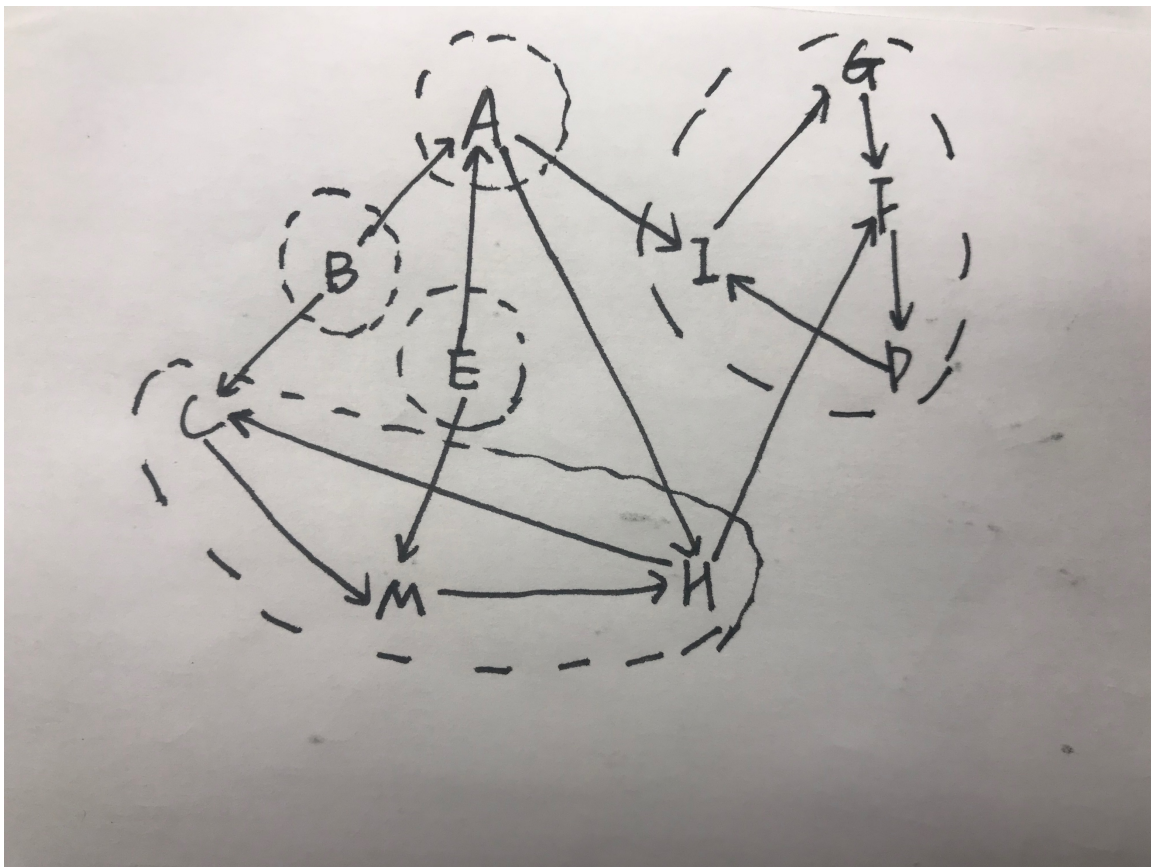


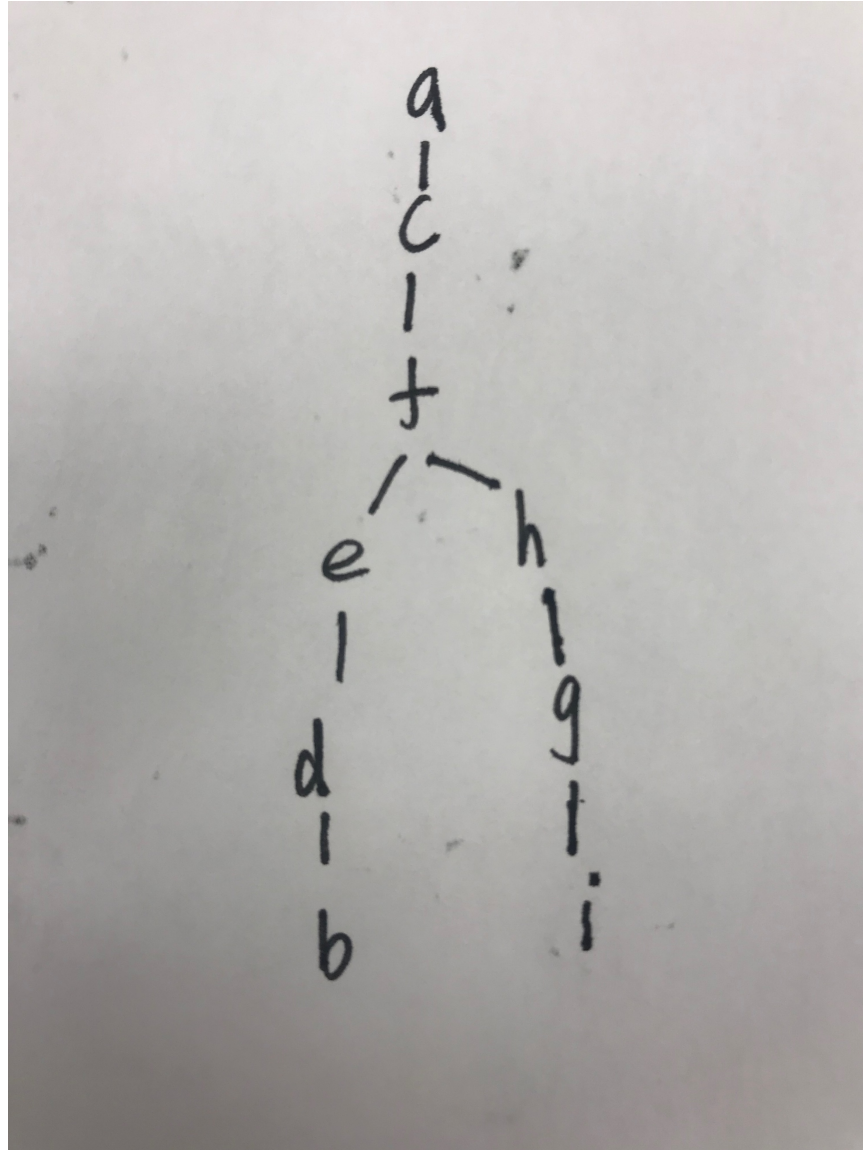
1.

	Discovery time	Finishing time
A	1	16
B	17	18
C	11	14
D	4	9
E	19	20
F	3	10
G	6	7
H	2	15
I	5	8
M	12	13

There are five strongly connected components: $\{E\}$, $\{B\}$, $\{A\}$, $\{H,M,C\}$, $\{F,G,I,D\}$



2. The edges which are added into A (c,f),(g,h),(a,c),(b,d),(e,d),(f,h),(e,f),(g,i).



3.

KRUSKAL(G, w)

$A = \emptyset$

for each vertex $v \in G.V(v)$

MAKE-SET (v)

sort the edges of $G.E$ into nondecreasing order by weight w Sort E : $O(E \lg E)$

for each (u, v) taken from the sorted list Second **for** loop:

if FIND-SET(u) \neq FIND-SET(v)

$A = A \cup \{(u, v)\}$

UNION(u, v)

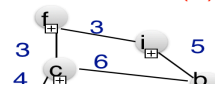
return A

Analysis:

Initialize X : $O(1)$

First **for** loop: $|V|$ MAKE-SET

$O(E)$ FIND-SET and
 $O(V)$ UNION



Because the running time of MAKE_SET is $O(\log|V|)$, FIND_SET is $O(\log|V|)$, UNION is $O(\log|V|)$,

first for loop: $O(|V|\log|V|)$

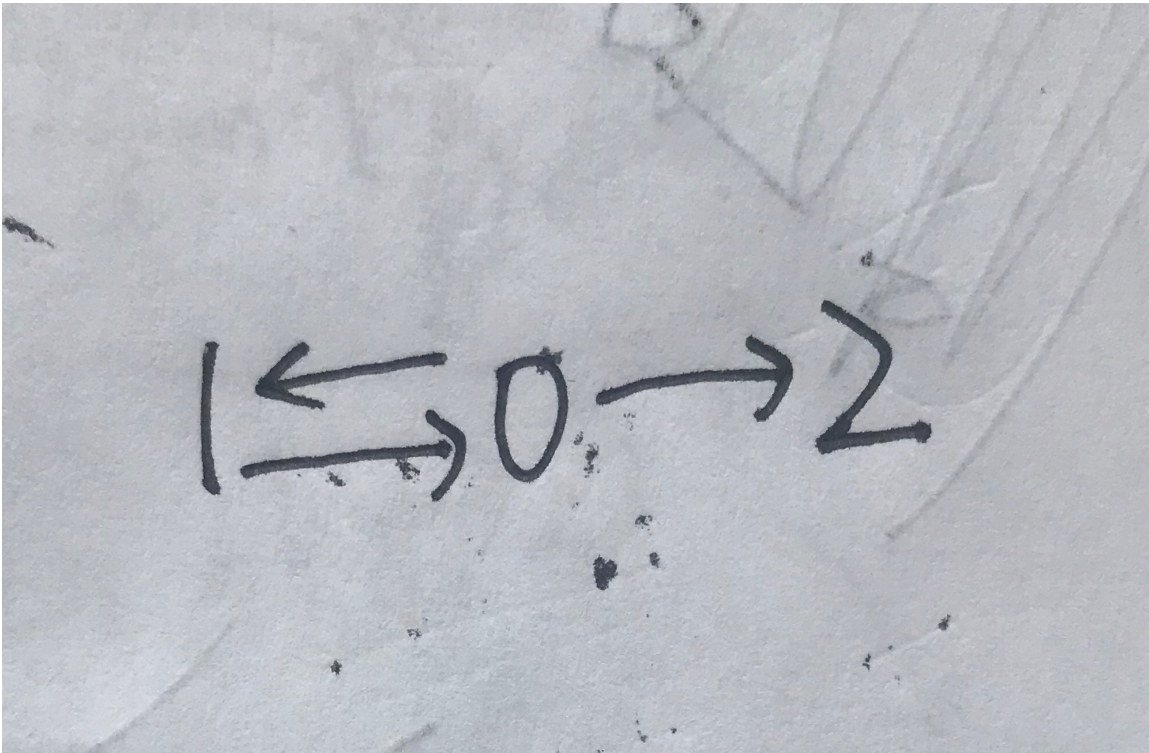
sort E: $O(|E|\log|E|)$

second for loop: $O(E \log|V|) + O(|V|\log|V|)$

Therefore, the running time of the algorithm is $O(|V|\log|V| + |E|\log|E|)$

4. The simpler algorithm does not always produce correct results.

Consider a counter-example like:



The first DFS beginning with 0 will result in the following finishing time order: 1, 2, 0, the second execution of DFS will show all vertices are in the same strongly connected component because 1 is reachable to both 0 and 2, however, this graph definitely has two strongly connected components which are $\{0, 1\}, \{2\}$. So the simpler algorithm is wrong.

5. For each ship, according to the distance between it and the safe polities for it, we make a min_heap, whose running time is $O(n)$, and then we take the minimum from the heap in $O(1)$.