

Digital Electronics

EEEN 20050

HOMEWORK 2

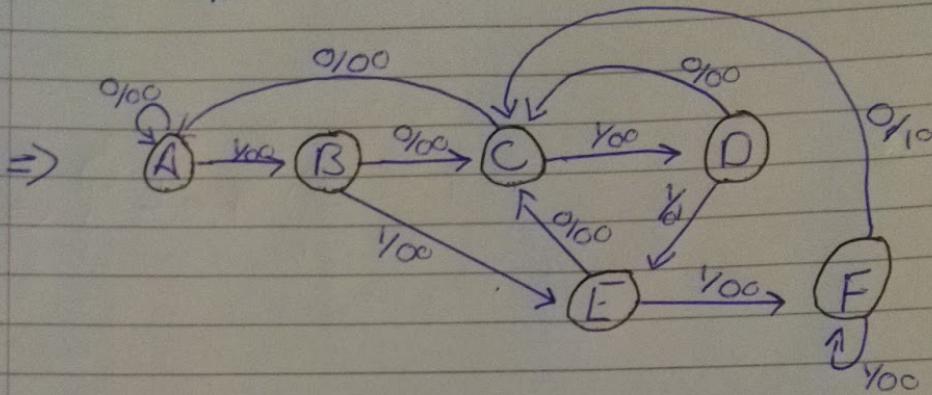
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## Mealy Machine

Sequences: 1011 & 1110

Flip Flop Type: JK



A: No digits for either sequence have been seen.

B: We have seen a (1) beginning of both sequences.

C: We have seen the first two digits of the first sequence (10)

D: We have seen the first three digits of the first sequence (101)

E: We have seen the first two digits of the second sequence (11)

F: We have seen the first three digits of the second sequence.

C: Is also where we return to if we have detected all of sequence two (1110)

E: Is also where we return to if we have detected all of sequence one (1011)

Present State	Input	Next State	Output
A	0	A	00
A	1	B	00
B	0	C	00
B	1	E	00
C	0	A	00
C	1	D	00
D	0	C	00
D	1	E	DI
E	0	C	00
E	1	F	00
F	0	C	10
F	1	F	00

Present State	Input	Next State	Output
A	0	000	00
	1	001	00
B	0	010	00
	1	100	00
C	0	000	00
	1	011	00
D	0	010	00
	1	100	01
E	0	010	00
	1	101	00
F	0	010	10
	1	101	00

PRESENT STATE		INPUT		NEXT STATE		FLIP-FLOP INPUTS				OUTPUT			
$Q_1^2$	$Q_1^1$	$Q_0^0$	$Q_0^1$	$Q_1^2$	$Q_1^1$	$Q_0^0$	$J_1$	$K_1$	$J_0$	$K_0$	$Z_1$	$Z_0$	
0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	1	0	0	0	0	1	0
0	0	0	0	0	0	0	1	0	0	0	0	1	0
0	0	0	0	0	0	0	1	1	0	0	0	0	0
0	0	0	0	0	0	0	0	1	1	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1	1	1

$$\bar{J}_0 = \bar{K}_1 = 0$$

$$J_0 = K_1 = 1$$

$$Q_0 = Q_1 = 0$$

$$Q_1 = Q_0 = 1$$

$J_0$

$Q_2\ Q_1\ \cancel{Q_0}\ X$	00	01	11	10
0 0	0	1	X	X
0 1	0	1	X	X
1 1	X	X	X	X
1 0	0	1	X	X

$$J_0 = X$$

$K_0$

$Q_2\ Q_1\ \cancel{Q_0}\ X$	00	01	11	10
0 0	X	X	1	1
0 1	X	X	1	1
1 1	X	X	X	X
1 0	X	X	0	1

$$K_0 = \overline{Q}_2 + \bar{X}$$

$Z_1$

$Q_2\ Q_1\ \cancel{Q_0}\ X$	00	01	11	10
0 0	0	0	0	0
0 1	0	0	0	0
1 1	X	X	X	X
1 0	0	0	1	0

$$Z_1 = Q_2 Q_0 X$$

$Z_0$

$Q_2\ Q_1\ \cancel{Q_0}\ X$	00	01	11	10
0 0	0	0	0	0
0 1	0	0	1	0
1 1	X	X	X	X
1 0	0	0	0	0

$$Z_0 = Q_1 Q_0 X$$

$J_2$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0	0 0	1 0
0 1	0 0	1 0
1 1	x x	x x
1 0	x x	x x

$$J_2 = Q_0 X$$

$K_2$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0	x x x x	x
0 1	x x x x	x
1 1	x x x x	x
1 0	1 0 0 1	1

$$K_2 = \bar{X}$$

$J_1$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0	0 0	1 0
0 1	x x	x x
1 1	x x x x	x
1 0	1 0 0 1	1

$$J_1 = \bar{Q}_2 Q_0 X + Q_2 \bar{X}$$

$K_1$

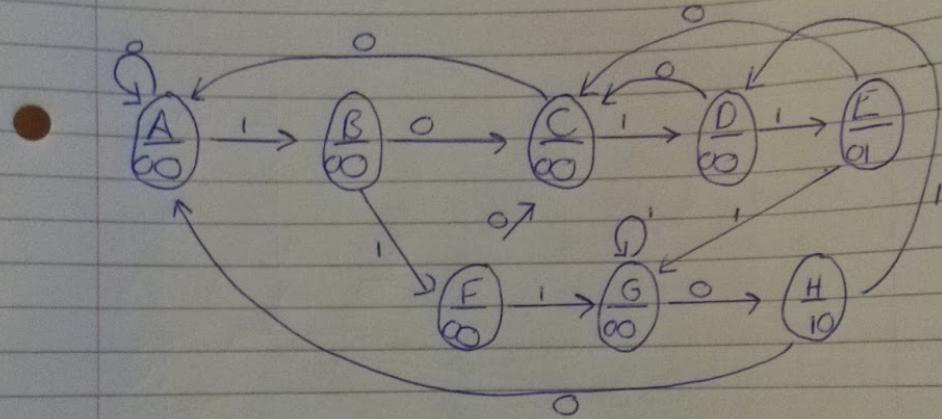
$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0	x x x x	x
0 1	1 0 1 0	0
1 1	x x x x	x
1 0	x x x x	x

$$K_1 = \bar{Q}_0 \bar{X} + \bar{Q}_2 Q_0 X$$

Moore

Sequences: 1011 & 1110

Flip Flop type: JK



- A: None of either of our desired patterns have been read yet
- B: The first bit (1) of both our sequences has been read
- C: The first two bits (10) of our first sequence has been read
- D: The first three bits of our first sequence (101) has been read
- E: We have read all bits (1011) of our first sequence
- F: The first two bits of our second sequence (11) have been read
- G: The first three bits (111) of our second sequence have been read
- H: We have read all the bits for our second sequence (1110)

PRESNT STATE	INPUT	NEXT STATE	OUTPUT
A	0	A	0 0
A	1	B	
B	0	C	0 0
B	1	F	
C	0	A	0 0
C	1	D	
D	0	C	0 0
D	1	E	
E	0	C	0 1
E	1	G	
F	0	C	0 0
F	1	G	
G	0	H	0 0
G	1	G	
H	0	A	1 0
H	1	O	

	PRESENT STATE	INPUT	NEXT STATE	OUTPUT
A	0 0 0	0	0 0 0	0 0
	0 0 0	1	0 0 1	
B	0 0 1	0	0 1 0	0 0
	0 0 1	1	1 0 1	
C	0 1 0	0	0 0 0	0 0
	0 1 0	1	0 1 1	
D	0 1 1	0	0 1 0	0 0
	0 1 1	1	1 0 0	
E	1 0 0	0	0 1 0	0 1
	1 0 0	1	1 1 0	
F	1 0 1	0	0 1 0	0 0
	1 0 1	1	1 1 0	
G	1 1 0	0	1 1 1	0 0
	1 1 0	1	1 1 0	
H	1 1 1	0	0 0 0	1 0
	1 1 1	1	0 1 1	



$J_2$

$Q_2 \ Q_1$	$Q_0 \ X$	$CO \ CI \ II \ IO$
00		00 1 0
01		00 1 0
11		XX XX
10		XX XX

$$J_2 = Q_0 X$$

$K_2$

$Q_2 \ Q_1$	$Q_0 \ X$	$CO \ CI \ II \ IO$
00		XX XX
01		XX XX
11		00 1 1
10		00 0 1

$$K_2 = Q_1 Q_0 + Q_2 \bar{Q}_1 \bar{X}$$

$J_1$

$Q_2 \ Q_1$	$Q_0 \ X$	$CO \ CI \ II \ IO$
00		00 0 1
01		XX XX
11		XX XX
10		11 11

$$J_1 = Q_2 + Q_0 \bar{X}$$

$K_1$

$Q_2 \ Q_1$	$Q_0 \ X$	$CO \ CI \ II \ IO$
00		XX XX
01		10 10
11		00 0 1
10		XX XX

$$K_1 = \bar{Q}_2 Q_0 \bar{X} + \bar{Q}_2 \bar{Q}_0 \bar{X} + \bar{Q}_2 \times Q_0$$

$J_0$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0		0 1 x x
0 1		0 1 x x
1 1		1 0 x x
1 0		0 0 x x

$$J_0 = \bar{Q}_2 X + Q_2 Q_1 \bar{X}$$

$K_0$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0		x x 0 1
0 1		x x 1 1
1 1		x x 1 1
1 0		x x 0 1

$$K_0 = Q_1 + \bar{X}$$

$Z_1$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0		0 0 0 0
0 1		0 0 0 0
1 1		0 0 1 1
1 0		0 0 0 0

$$Z_1 = Q_2 Q_1 \bar{Q}_0$$

$Z_0$

$Q_2 \ Q_1$	$\bar{Q}_0 \ X$	$00 \ 01 \ 11 \ 10$
0 0		0 0 0 0
0 1		0 0 0 0
1 1		0 0 0 0
1 0		1 1 0 0

$$Z_0 = Q_2 \bar{Q}_1 \bar{Q}_0$$

## Difference

In a **Moore Model** State machine the output of a transition is determined by the current state alone whereas in a **Mealy Model** state machine the output is determined by the combination of the current input and the current state.

Due to this a **Moore** machine often needs more hardware to design the circuit however it is more robust as it does not depend on inputs.