

Laplace transforms:

- $\mathcal{L}\{f'(t)\} = sF(s) - f(0^-)$
- $\mathcal{L}\{f''(t)\} = s^2F(s) - sf(0^-) - f'(0^-)$

Other Laplace transforms:

- $\mathcal{L}\{\sin(at)\} = \frac{a}{s^2 + a^2}$
- $\mathcal{L}\{\cos(at)\} = \frac{s}{s^2 + a^2}$

General form of inverse Laplace for conjugate roots of R and P:

- $\mathcal{L}^{-1}\left\{\frac{R}{s-P} + \frac{R_{conj}}{s-P_{conj}}\right\} = 2 * \mathbf{abs}(R) * \exp(\mathbf{Re}(P)t) * \cos(\mathbf{Im}(P)t + \mathbf{angle}(R))$

Z Transforms

- $Z\{f(n-1)\} = z^{-1}F(z) + f(-1)$
- $Z\{f(n-2)\} = z^{-2}F(z) + z^{-1}f(-1) + f(-2)$

Other Z transforms:

- $Z\{u(n)\} = \frac{1}{1-z^{-1}}$
- $Z\{\lambda^{-n}u(n)\} = \frac{1}{1-\lambda^{-1}z^{-1}}$
- $Z\{\delta(n)\} = 1$
- $Z\{\sin(\Omega_0 n)\} = \frac{\sin(\Omega_0)z^{-1}}{1-2\cos(\Omega_0)z^{-1}+z^{-2}}$
- $Z\{\cos(\Omega_0 n)\} = \frac{1-\cos(\Omega_0)z^{-1}}{1-2\cos(\Omega_0)z^{-1}+z^{-2}}$

Inverse Z transforms:

- $Z^{-1}\{Az^{-k}\} = A\delta(n-k)$
- $Z^{-1}\left\{\frac{A}{z^{-1}-\lambda}\right\} = \frac{A(-1)^n}{\lambda^{n+1}}u(n)$

General form of inverse Z for conjugate R and P:

- $Z^{-1}\left\{\frac{R}{z^{-1}-P} + \frac{R_{conj}}{z^{-1}-P_{conj}}\right\} = -2 * \frac{\mathbf{abs}(R)}{\mathbf{abs}(P)^{n+1}} * \cos(\mathbf{angle}(P)(n+1) + \mathbf{angle}(R))$

Fourier Transforms

- $\mathcal{F}(A\sin(\omega_0 t)) = \frac{A\pi}{j}(\delta(\omega - \omega_0) - \delta(\omega + \omega_0))$
- $\mathcal{F}(A\cos(\omega_0 t)) = A\pi(\delta(\omega - \omega_0) + \delta(\omega + \omega_0))$
- $\mathcal{F}(A\exp(j\omega_0 t)) = A2\pi\delta(\omega - \omega_0)$
- $\mathcal{F}(1) = 2\pi\delta(\omega)$

Steady state output of a filter with a sinusoidal input and transfer function $H(j\omega)$:

- $A \sin(\omega_n t) \Rightarrow |H(j\omega_n)| * A \sin(\omega_n t + \angle H(j\omega_n))$