

1. Consider the following LSI system with the following transfer function:

$$H(z) = \frac{z^3 - \frac{2}{3}z^2}{z^3 - \frac{21}{20}z^2 + \frac{1}{8}z + \frac{3}{40}}.$$

Draw the filter structures for the implementations of the system in each of the following forms:

- (a) Direct Form I.
  - (b) Direct Form II.
  - (c) Cascade using first- and second-order direct form II sections.
  - (d) Parallel using first- and second-order direct form II sections.
2. The frequency response of a GLP filter can be expressed as  $H_d(\omega) = R(\omega)e^{j(\alpha - M\omega)}$  where  $R(\omega)$  is a real function. For each of the following filters, determine whether it is a GLP filter. If it is, state the Type, find  $R(\omega)$ ,  $M$ , and  $\alpha$ , and indicate whether it is also a linear phase filter.
- (a)  $\{h_n\}_{n=0}^2 = \{2, 1, 1\}$
  - (b)  $\{h_n\}_{n=0}^2 = \{1, 2, 3\}$
  - (c)  $\{h_n\}_{n=0}^2 = \{-1, 3, 1\}$
  - (d)  $\{h_n\}_{n=0}^4 = \{1, 1, 1, -1, -1\}$
  - (e)  $\{h_n\}_{n=0}^2 = \{1, 0, -1\}$
  - (f)  $\{h_n\}_{n=0}^3 = \{2, 1, 1, 2\}$

In each case, the remaining terms of the unit pulse response of the filter are zero.

3. Consider the following systems,

- (i)  $y[n] = \frac{2}{5}x[n] - x[n-1] + x[n-2] - \frac{2}{5}x[n-3]$
- (ii)  $y[n] = \frac{1}{3}x[n] + x[n-1] - x[n-2] - \frac{1}{3}x[n-3]$
- (iii)  $y[n] = x[n] + x[n-2] + x[n-4]$
- (iv)  $y[n] = -x[n] + x[n-1] + \frac{1}{3}x[n-2]$
- (v)  $y[n] = x[n] - 0.76y[n-1]$

For each of the systems,

- (a) Determine whether the system is FIR or IIR? If the system is FIR, sketch its  $h[n]$ .
- (b) If the system is FIR, determine whether  $h[n]$  is of even or odd length.
- (c) If the system is FIR, determine whether  $h[n]$  has even or odd symmetry, or neither.

- (d) Determine whether its  $H_d(\omega)$  has linear phase. If it does not, determine whether it has generalized linear phase (GLP).
- (e) The frequency response of a GLP filter can be expressed as  $H_d(\omega) = R_d(\omega) e^{j(\alpha - M\omega)}$ , where  $R_d(\omega)$  is a real function. For systems that have a GLP or linear phase, find  $R_d(\omega)$ ,  $M$ , and  $\alpha$ .

4. Determine the coefficients of a linear-phase FIR filter

$$y[n] = h_0 x[n] + h_1 x[n-1] + h_2 x[n-2]$$

such that (i) it rejects any frequency component at  $\omega_0 = 5\pi/6$ , and (ii) its frequency response is normalized so that  $H_d(0) = 1$ .