

2E1.  $P(\text{rain} | \text{Monday})$  (2) (1)

2E2. (3)

2E3. (1)

2E4. ~~Prope~~  $P=0.7$  would expect it to land

$$P(W) = 0.7 \quad P(W|M) = 1$$

$$P(E) \quad P(E|L) = 0.23$$

$$P(E|L) \propto P(L|E) \cdot P(E)$$

$$\propto 0.3 \times 0.5$$

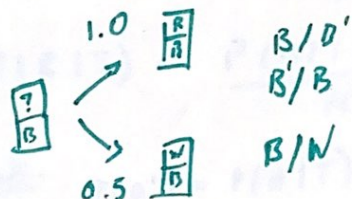
$$\propto 0.15$$

$$P(E|L) = \frac{P(L|E) \cdot P(E)}{P(E)P(L|E) + P(M)P(L|M)}$$

$$= \frac{0.3 \times 0.5}{0.5 \times 0.3 + 0.5}$$

$$= \frac{0.15}{0.65} = 0.23$$

2M4.  $\begin{bmatrix} B \\ B \end{bmatrix} \begin{bmatrix} B \\ W \end{bmatrix} \begin{bmatrix} W \\ W \end{bmatrix}$



$$\therefore \frac{2}{3}$$

2M6.  $B/B, B/W, W/W$

$$BB = 1/6$$

$$BW = 2/6$$

$$WW = 3/6$$

2M5.  $B/B, B/B, W/W, B/W$

$B/B'$   
 $B'/B$   
 $B/B'$   $4/5$   
 $B'/B$   
 $B/W$

$$\frac{2}{6} \times \frac{6}{4} = \frac{12}{24} = \frac{1}{2}$$

$$B/B' \quad 1/6$$

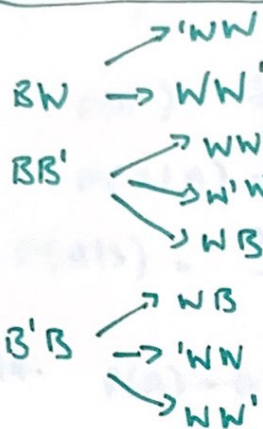
$$B'/B \quad 1/6$$

$$B/W \quad 2/6$$

$$\frac{\left(\frac{2}{6}\right)}{3} = \frac{2}{6} \times \frac{1}{3} = \frac{2}{12}$$

BW BB WW

$B? \rightarrow N? \quad P(?=B) = 0.75 \text{ (y=1)}$



$P(?=B) = \frac{2}{8}$   
 $P(?=W) = 0.75$

2+11  $P(\text{Twins} | B) = 0.2 \quad P(T | A) = 0.1 \quad P(A) = 0.5 \quad P(B) = 0.5$

$P(\text{Twins}) = P(A \text{ Twins}) = ? \quad P(2 \text{ Twins}) = ?$

$P(T) = P(A) \cdot P(T | A) + P(B) \cdot P(T | B)$   
 $= 0.05 + 0.1 = 0.15$

$P(A | T) = \frac{P(T | A) P(A)}{P(T)} = \frac{0.1 \cdot 0.5}{0.15} = \frac{1}{3}$

$P(B | T) = \frac{P(T | B) P(B)}{P(T)} = \frac{0.2 \cdot 0.5}{0.15} = \frac{2}{3}$

Update.  $P(A') = P(A | T) = \frac{1}{3}, \quad P(B') = P(B | T) = \frac{2}{3}$

$P(2 \text{ Twins}) = P(A') P(T | A) + P(B') P(T | B)$

$= \frac{1}{3} \cdot 0.1 + \frac{2}{3} \cdot 0.2$

$= \frac{0.1}{3} + \frac{0.4}{3}$

$= \frac{0.5}{3}$

$= 0.166$



2H2  $\frac{1}{3}$  (prev calculated)

2H3 Data: Twins, Single.

$P(A|T, S)$  given have calculations for Twins event.  
$$P(A|S) = \frac{P(S|A) P(A)}{P(S)} \rightarrow P(S) = 1 - P(T) = 0.85$$

$$P(A) = \frac{1}{3}$$

$$P(S|A) = 0.9 (1 - P(T|A))$$

$$P(A|S) = \frac{0.9 \cdot \frac{1}{3}}{0.85} = 0.35294$$

2H4.  $P(A) = 0.9$   $P(B) = 0.65$

given  $P(A|PA) = 0.9$ ,  $P(B|PB) = 0.65$  ✓

$$P(PA|A) = 0.8, P(PB|B) = 0.65$$

$$P(A|PB) = \frac{P(PB|A) P(A)}{P(PB) P(X)}$$

$$\hookrightarrow P(PB) P(X) = 0.1 \cdot 0.9 + 0.2 \cdot 0.65 = 0.21$$

$$P(A|X) = \frac{0.8 \cdot 0.1}{0.21} = 0.38095$$