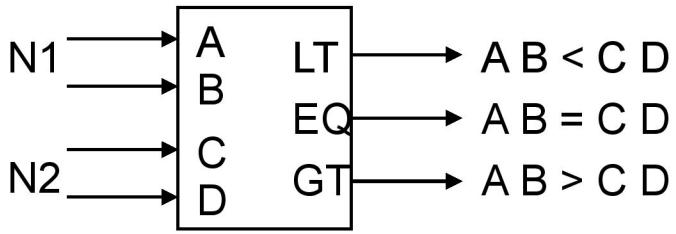
Comparator

Two-Bit Comparator

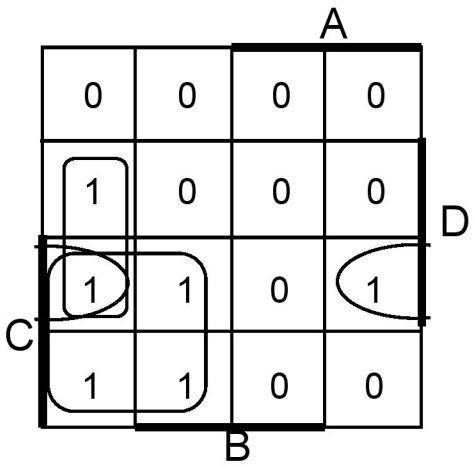


block diagram
and
truth table

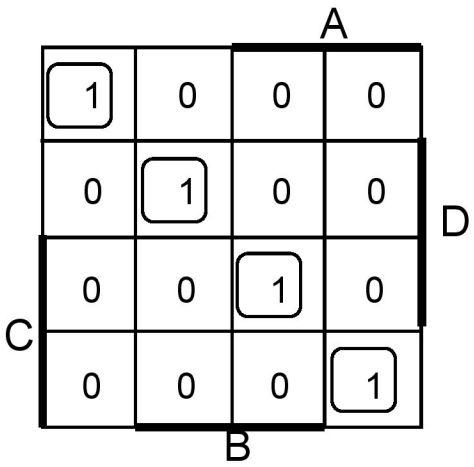
A	B	C	D	LT	EQ	GT
0	0	0	0	0	1	0
		0	1	1	0	0
		1	0	1	0	0
		1	1	1	0	0
0	1	0	0	0	0	1
		0	1	0	1	0
		1	0	1	0	0
		1	1	1	0	0
1	0	0	0	0	0	1
		0	1	0	0	1
		1	0	0	1	0
		1	1	1	0	0
1	1	0	0	0	0	1
		0	1	0	0	1
		1	0	0	0	1
		1	1	0	1	0

we'll need a 4-variable Karnaugh map
for each of the 3 output functions

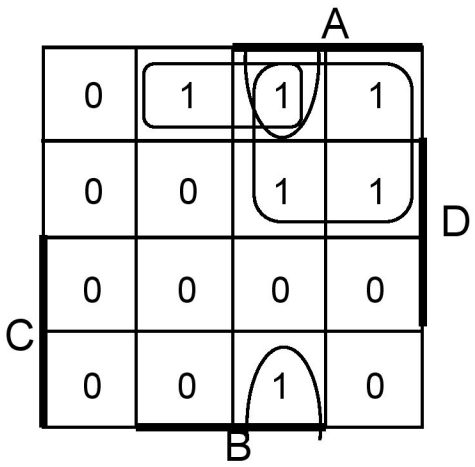
Two-Bit Comparator (cont'd)



K-map for LT



K-map for EQ



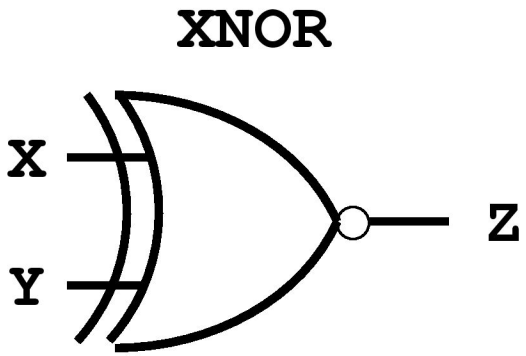
K-map for GT

LT = A' B' D + A' C + B' C D

EQ = A'B'C'D' + A'BC'D + ABCD + AB'CD' = (A xnor C) • (B xnor D)

GT = B C' D' + A C' + A B D'

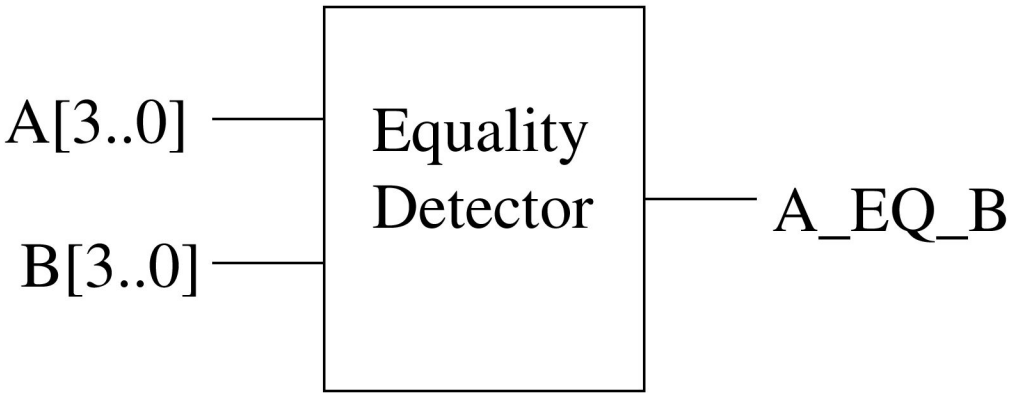
Equality Comparator



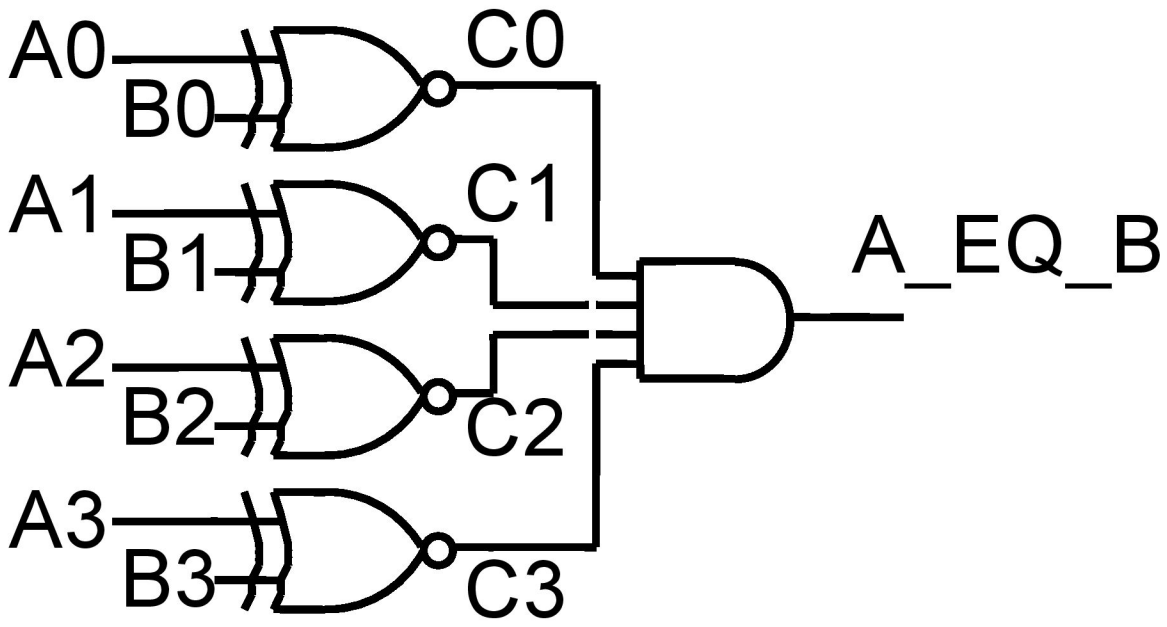
Z = X XNOR Y

X	Y	Z
0	0	1
0	1	0
1	0	0
1	1	1

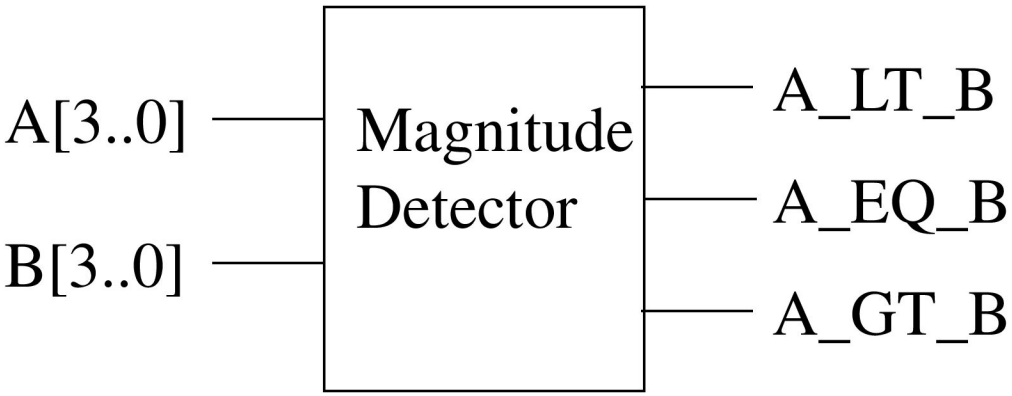
4-bit Equality Detector



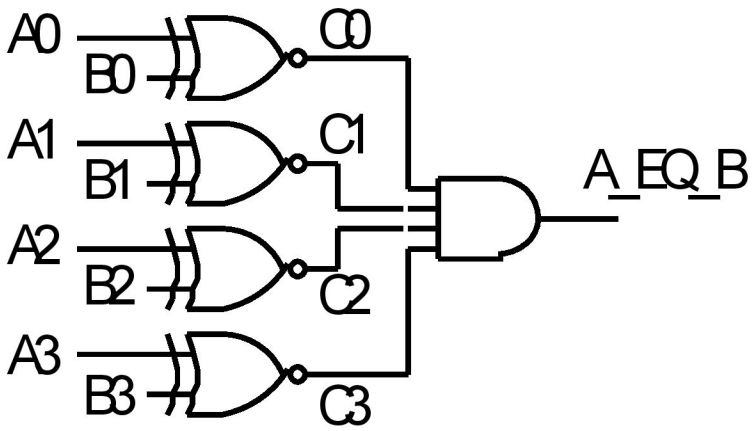
4-Bit Equality Comparator



4-bit Magnitude Comparator



Magnitude Comparator

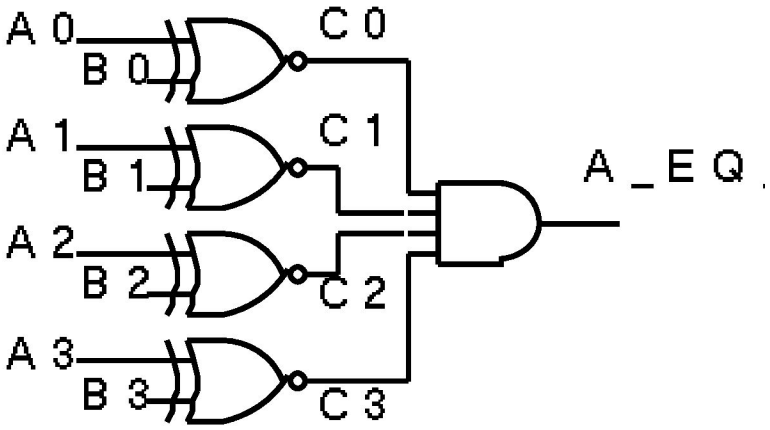


How can we find A_GT_B?

How many rows would a truth table have?

$2^8 = 256!$

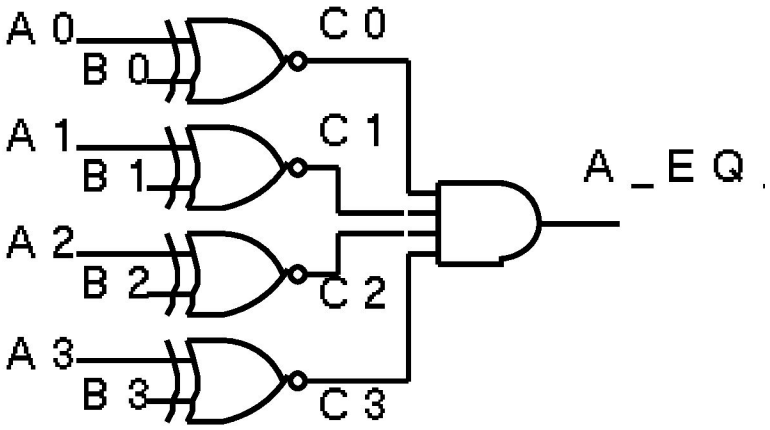
Magnitude Comparator



Find A_GT_B

If A = 1001 and
B = 0111
is A > B?
Why?

Magnitude Comparator



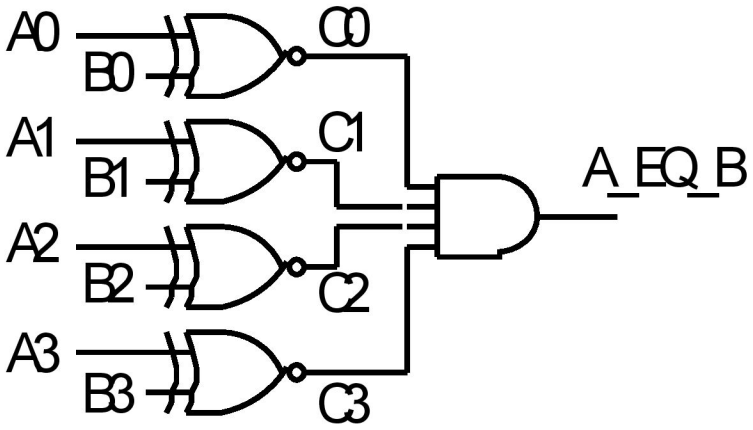
Find A_GT_B

If A = 1001 and
B = 0111
is A > B?
Why?

Because A3 > B3
i.e. A3 . B3' = 1

Therefore, one term in the logic equation for A_GT_B is A3 . B3'

Magnitude Comparator

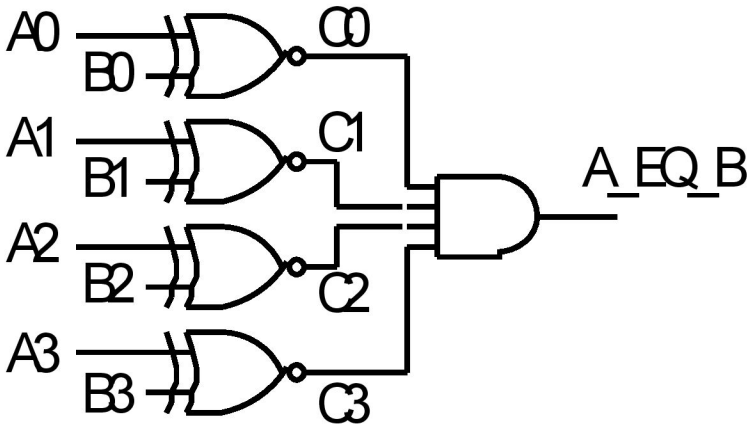


A_GT_B = A3 . B3'
+ …..

Because A3 = B3 and
A2 > B2
i.e. C3 = 1 and
A2 . B2' = 1

If A = 1101 and
B = 1011
is A > B?
Why?

Magnitude Comparator



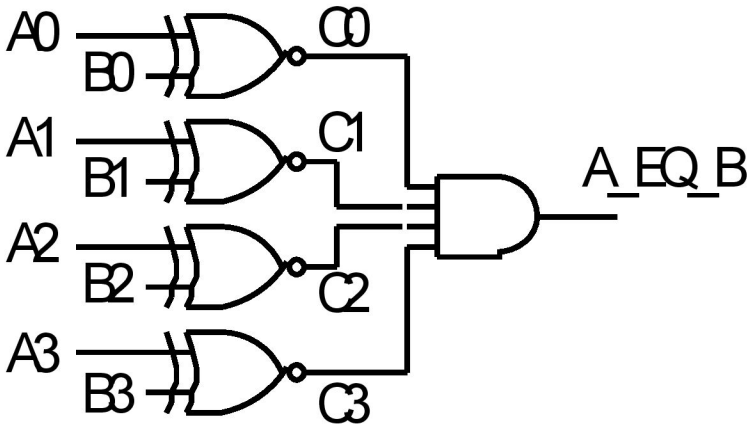
A_GT_B = A3 . B3'
+ …..

Because A3 = B3 and
A2 > B2
i.e. C3 = 1 and
A2 . B2' = 1

If A = 1101 and
B = 1011
is A > B?
Why?

Therefore, the next term in the logic equation for A_GT_B is C3 . A2 . B2'

Magnitude Comparator



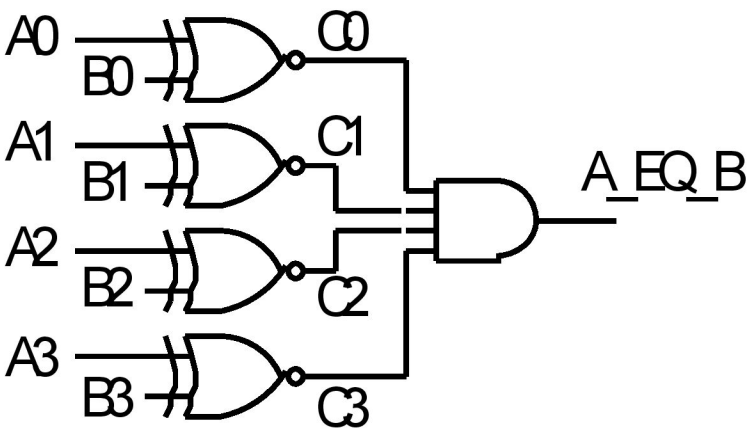
If A = 1010 and
B = 1001
is A > B?
Why?

A_GT_B = A3 . B3'
+ C3 . A2 . B2'
+ .....

Because A3 = B3 and
A2 = B2 and
A1 > B1
i.e. C3 = 1 and C2 = 1 and
A1 . B1' = 1

Therefore, the next term in the logic equation for A_GT_B is C3 . C2 . A1 . B1'

Magnitude Comparator



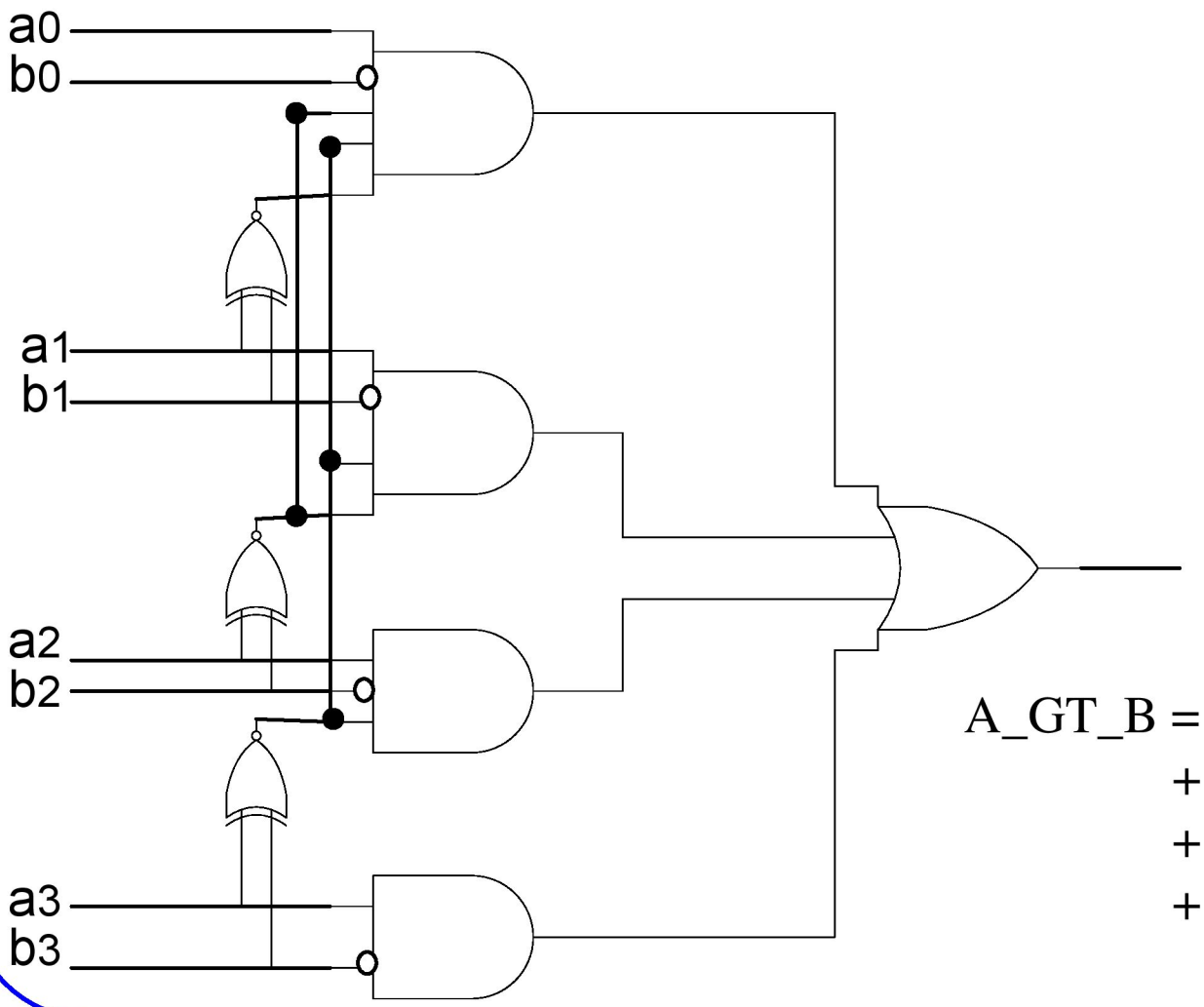
If A = 1011 and
B = 1010
is A > B?
Why?

A_GT_B = A3 . B3'
+ C3 . A2 . B2'
+ C3 . C2 . A1 . B1'
+ .....

Because A3 = B3 and
A2 = B2 and
A1 = B1 and
A0 > B0
i.e. C3 = 1 and C2 = 1 and
C1 = 1 and A0 . B0' = 1

Therefore, the last term in the logic equation for A_GT_B is C3 . C2 . C1 . A0 . B0'

Magnitude Comparator



$$A\_GT\_B = A3 \cdot B3' + C3 \cdot A2 \cdot B2' + C3 \cdot C2 \cdot A1 \cdot B1' + C3 \cdot C2 \cdot C1 \cdot A0 \cdot B0'$$