m231 - quiz#0

Let ACIR' be OPEN. Set Y= 2A. Show 2Y=Y

be I realized later that I forgot to write that
on the board!

1) BYCY: Let nEBY; in particular, Yr>0

B(r,x) \(\partial\) \(\partial\

any B(r, y) in B(r,x).

Since $y \in \partial A$, this small ball contains pts in A & in A^c . Hence $x \in \partial A$ too.

2) Y⊆∂Y: Take any X∈Y=∂A.

Any ball B centered at x contains a point α∈A.

Since A is OPEN, AN∂A=Ø. So α€∂A

Meanwhile B contains x and x∈∂A.

Therefore x∈∂(∂A).

 $\neg B(Cx)$

1) is true regardless of openness of A.

2) is not frue in general. When A is open, 2) is true as I show above.

Lex: A=OCR: DA=R70(A)=Ø

A quick way to prove (1): Show $\partial A = \overline{A} \cap \overline{A}^{c}$.

If you show that, it follows that ∂A is closed because it's the intersection of two closed sets.

Since ∂A is closed, $\partial (\partial A) \subset \partial A$ (shown in dass).